

Discrete Time Systems:

1.

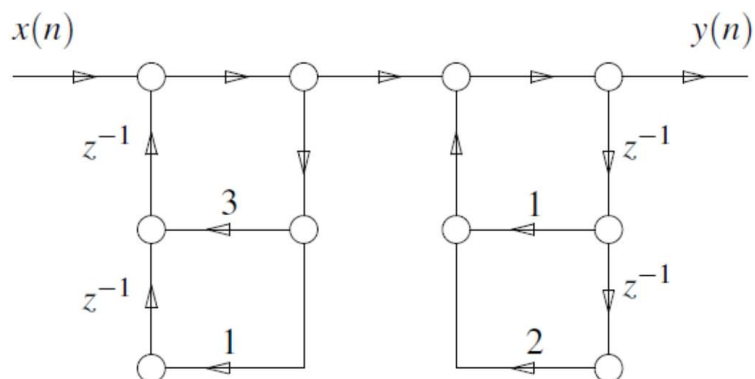
- a. The system function of a causal, LTI system is given by

$$H(z) = \frac{1 + \frac{1}{5}z^{-1}}{\left(1 - \frac{1}{2}z^{-1} + \frac{1}{3}z^{-2}\right)\left(1 + \frac{1}{2}z^{-1}\right)}$$

Draw the signal flow graphs for implementation of the system in

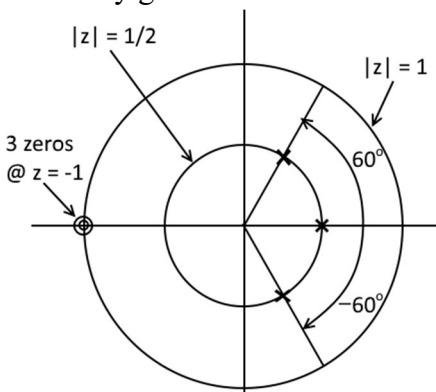
- Direct Form I
- Direct Form II
- Cascade Form

- b. A LTI system is realized by the signal flow graph shown below.



- Determine the system function $H(z)$.
- Is it possible to implement the system with fewer number of unit delays? Give reasons for your answer.

2. A z-plane pole-zero plot for a certain digital filter with three zeros and three poles is shown in the figure below. The filter has unity gain at dc.



- a. Determine the system function in the form

$$H(z) = A \left[\frac{(1 + a_1 z^{-1})(1 + b_1 z^{-1} + b_2 z^{-2})}{(1 + c_1 z^{-1})(1 + d_1 z^{-1} + d_2 z^{-2})} \right]$$

giving numerical values for the parameters $A, a_1, b_1, b_2, c_1, d_1$ and d_2 .

- b. Draw block diagrams showing numerical values for path gains in the following forms:

- a. Direct form II (canonic form)
- b. Cascade form (make each section canonic, with real coefficients)

3. Determine the system function and the impulse response of the system shown in the figure below.

