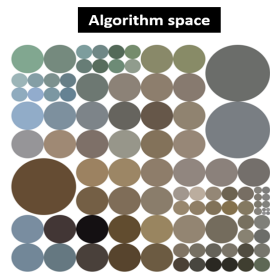
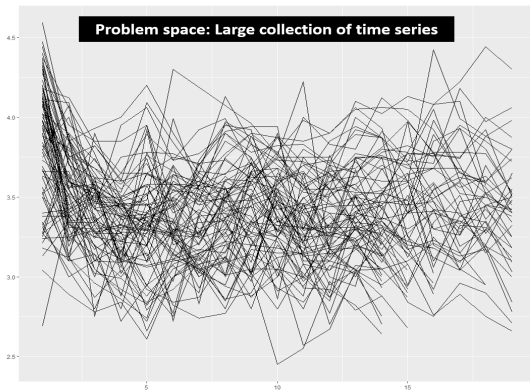


Peeking inside FFORMS: Feature-based FORecast-Model Selection

Thiyanga Talagala,
Rob J Hyndman, George Athanasopoulos

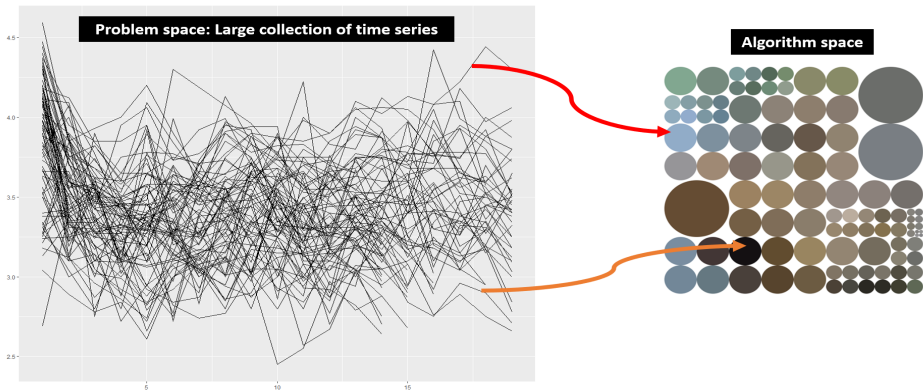
18 June 2019

Big picture



- What algorithm is likely to perform best?

Big picture



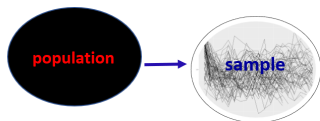
- What algorithm is likely to perform best?
- Algorithm selection problem, John Rice (1976)

FFORMS: Feature-based FOfRecast Model Selection

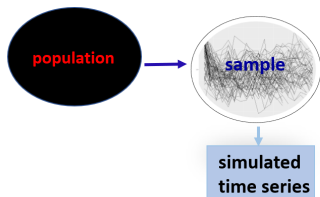


population

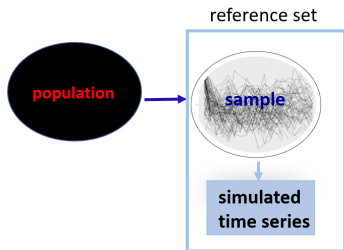
FFORMS: Feature-based FOfecast Model Selection



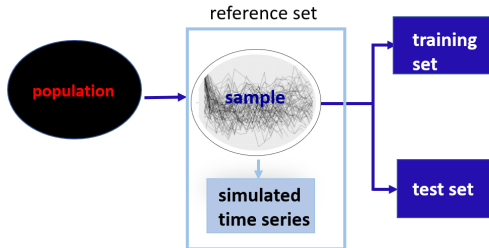
FFORMS: Feature-based FOfRecast Model Selection



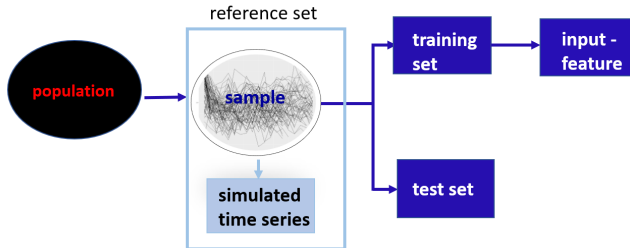
FFORMS: Feature-based FOfRecast Model Selection



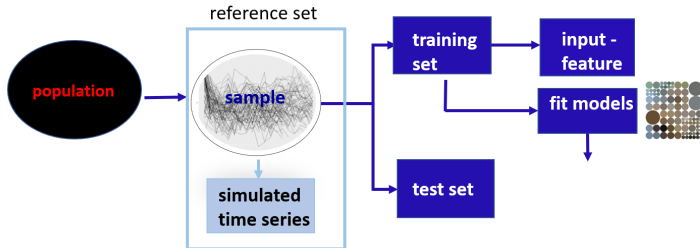
FFORMS: Feature-based FORecast Model Selection



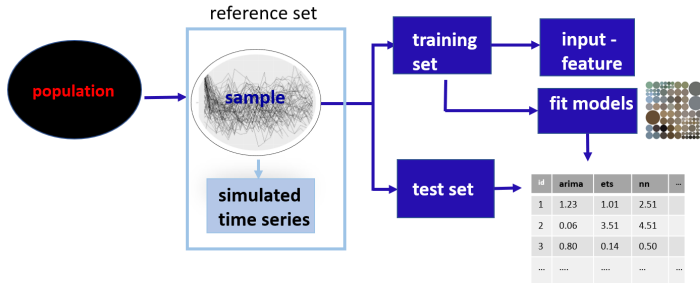
FFORMS: Feature-based FOfecast Model Selection



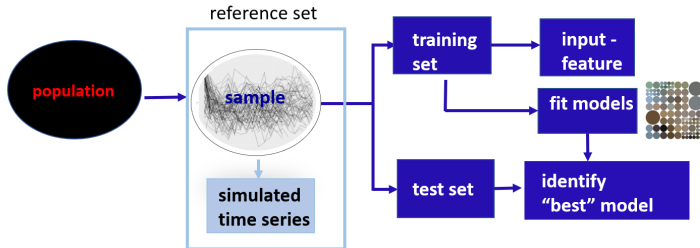
FFORMS: Feature-based FOREcast Model Selection



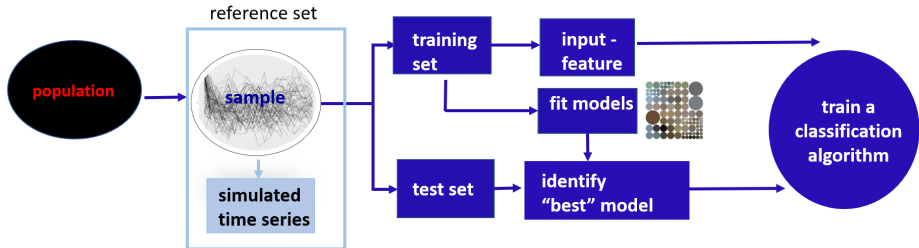
FFORMS: Feature-based FOREcast Model Selection



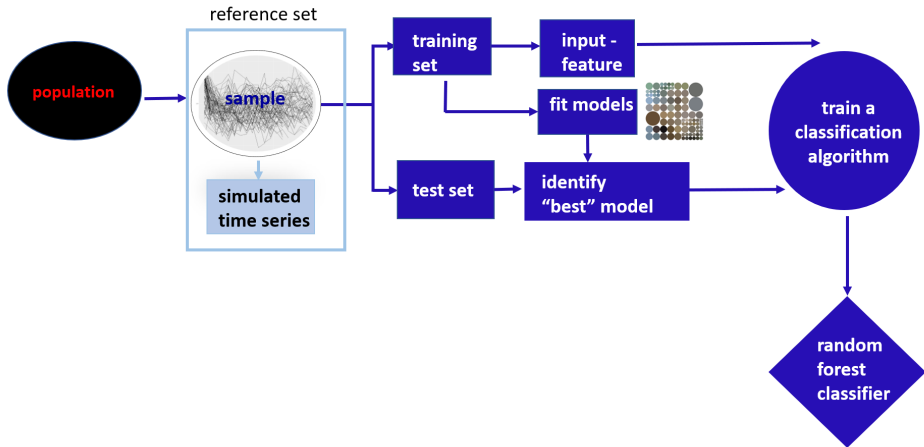
FFORMS: Feature-based FOREcast Model Selection



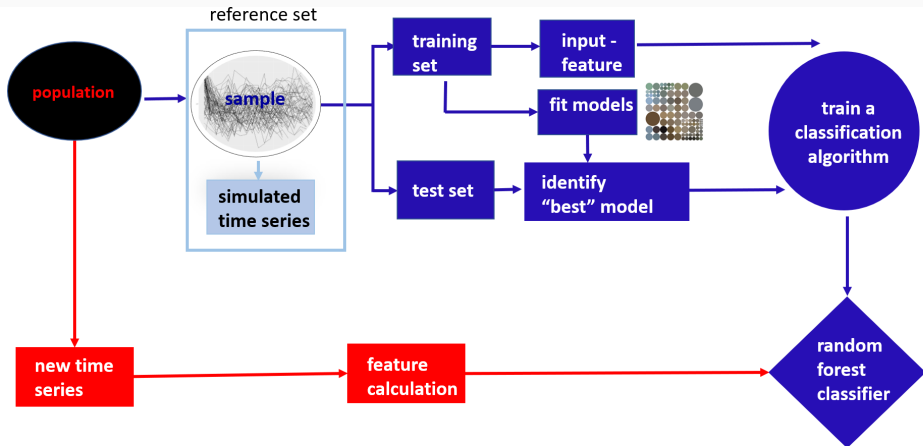
FFORMS: Feature-based FOREcast Model Selection



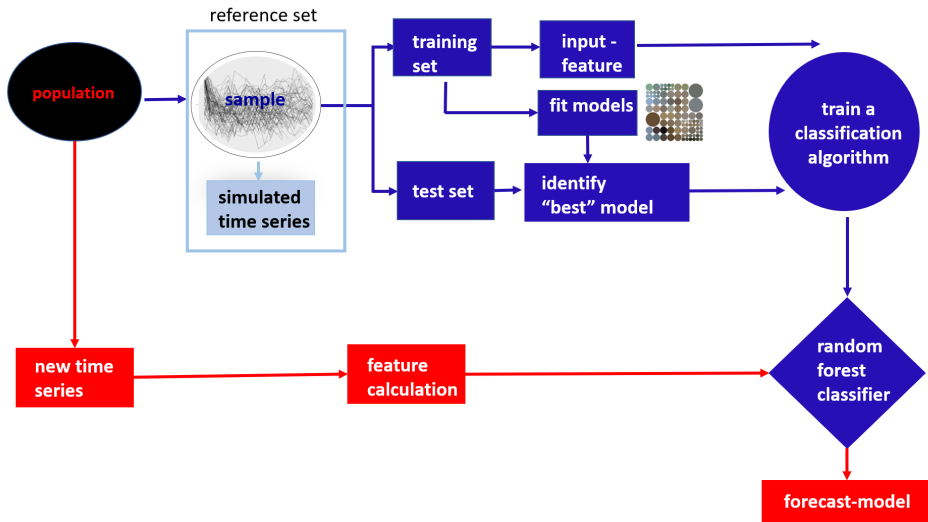
FFORMS: Feature-based FOREcast Model Selection



FFORMS: Feature-based FOREcast Model Selection



FFORMS: Feature-based FOREcast Model Selection



Forecast-models included

- White noise process
- ARMA/AR/MA
- ARIMA
- SARIMA
- Random walk with drift
- Random walk
- Seasonal naive
- TBATS
- neural network forecasts
- Theta method
- STL-AR
- ETS-without trend and seasonal
- ETS-trend
- ETS-damped trend
- ETS-trend and seasonal
- ETS-damped trend and seasonal
- ETS-seasonal
- MSTL-ETS
- MSTL-ARIMA

Time series features

- length
- strength of seasonality
- strength of trend
- linearity
- curvature
- spikiness
- stability
- lumpiness
- spectral entropy
- Hurst exponent
- nonlinearity
- unit root test statistics
- parameter estimates of Holt's linear trend method
- parameter estimates of Holt-Winters' additive method
- ACF and PACF based features - calculated on raw, differenced, seasonally-differenced series and remainder series.

Results: M4 Competition data

| | Yearly | Quarterly | Monthly | Weekly | Daily | Hourly |
|--------------------|--------|-----------|---------|--------|-------|--------|
| FFORMS | 3.17 | 1.20 | 0.98 | 2.31 | 3.57 | 0.84 |
| auto.arima | 3.40 | 1.17 | 0.93 | 2.55 | - | - |
| ets | 3.44 | 1.16 | 0.95 | - | - | - |
| theta | 3.37 | 1.24 | 0.97 | 2.64 | 3.33 | 1.59 |
| rwd | 3.07 | 1.33 | 1.18 | 2.68 | 3.25 | 11.45 |
| rw | 3.97 | 1.48 | 1.21 | 2.78 | 3.27 | 11.60 |
| nn | 4.06 | 1.55 | 1.14 | 4.04 | 3.90 | 1.09 |
| stlar | - | 2.02 | 1.33 | 3.15 | 4.49 | 1.49 |
| snaive | - | 1.66 | 1.26 | 2.78 | 24.46 | 2.86 |
| tbats | - | 1.19 | 1.05 | 2.49 | 3.27 | 1.30 |
| wn | 13.42 | 6.50 | 4.11 | 49.91 | 38.07 | 11.68 |
| mstlarima | - | - | - | - | 3.84 | 1.12 |
| mstlets | - | - | - | - | 3.73 | 1.23 |
| combination (mean) | 4.09 | 1.58 | 1.16 | 6.96 | 7.94 | 3.93 |
| M4-1st | 2.98 | 1.12 | 0.88 | 2.36 | 3.45 | 0.89 |
| M4-2nd | 3.06 | 1.11 | 0.89 | 2.11 | 3.34 | 0.81 |
| M4-3rd | 3.13 | 1.23 | 0.95 | 2.16 | 2.64 | 0.87 |

Results: M4 Competition data

| | Yearly | Quarterly | Monthly | Weekly | Daily | Hourly |
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| M4-3rd | 3.13 | 1.23 | 0.95 | 2.16 | 2.64 | 0.87 |

■ Can we trust ML-algorithms if we don't know how it works?



Peeking inside FFORMS!!!

- Which features are the most important?
- Where are they important?
- How are they important?
- When and how are features linked with the prediction outcome?
- When and how strongly do features interact with other features?

Global explanation of feature contribution

Overall role of features in the choice of different forecast-model selection.


- Permutation-based variable importance
- Mean decrease in Gini coefficient
- Partial dependence plots (Jerome H. Friedman, 2001)
- Individual Conditional Expectation (ICE) curves (Goldstein et al., 2015; Zhao and Hastie, 2017)

Partial dependence plots and ICE curves

| x1 | x2 | x3 |
|----|----|----|
| 11 | 4 | 5 |
| 12 | 6 | 7 |

Partial dependence plots and ICE curves

| x1 | x2 | x3 |
|----|----|----|
| 11 | 4 | 5 |
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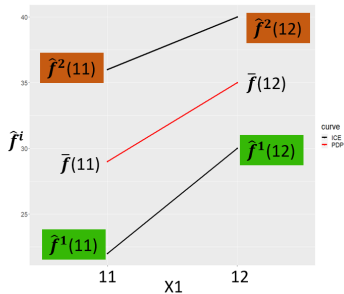
| x1 | x2 | x3 |
|----|----|----|
| 11 | 4 | 5 |
| 11 | 6 | 7 |
| 12 | 4 | 5 |
| 12 | 6 | 7 |

Partial dependence plots and ICE curves

| x1 | x2 | x3 | | x1 | x2 | x3 | | x1 | x2 | x3 | $\hat{f}^i(\mathbf{x1})$ | $\overline{\hat{f}(\mathbf{x1})}$ |
|----|----|----|---|----|----|----|---|----|----|----|--------------------------|-----------------------------------|
| 11 | 4 | 5 | → | 11 | 4 | 5 | → | 11 | 4 | 5 | $\hat{f}^1(11)$ | $\frac{\sum \hat{f}^i(11)}{2}$ |
| 12 | 6 | 7 | | 11 | 6 | 7 | | 11 | 6 | 7 | $\hat{f}^2(11)$ | |
| | | | | 12 | 4 | 5 | | 12 | 4 | 5 | $\hat{f}^1(12)$ | $\frac{\sum \hat{f}^i(12)}{2}$ |
| | | | | 12 | 6 | 7 | | 12 | 6 | 7 | $\hat{f}^2(12)$ | |

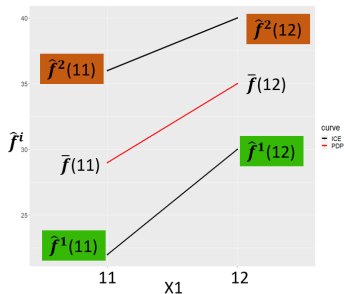
Partial dependence plots and ICE curves

| x1 | x2 | x3 | | x1 | x2 | x3 | | x1 | x2 | x3 | $\hat{f}^i(\mathbf{x1})$ | $\overline{\hat{f}(\mathbf{x1})}$ |
|----|----|----|---|----|----|----|---|----|----|----|--------------------------|-----------------------------------|
| 11 | 4 | 5 | → | 11 | 4 | 5 | → | 11 | 4 | 5 | $\hat{f}^1(11)$ | $\frac{\sum \hat{f}^i(11)}{2}$ |
| 12 | 6 | 7 | | 11 | 6 | 7 | | 11 | 6 | 7 | $\hat{f}^2(11)$ | |
| | | | | 12 | 4 | 5 | | 12 | 4 | 5 | $\hat{f}^1(12)$ | $\frac{\sum \hat{f}^i(12)}{2}$ |
| | | | | 12 | 6 | 7 | | 12 | 6 | 7 | $\hat{f}^2(12)$ | |

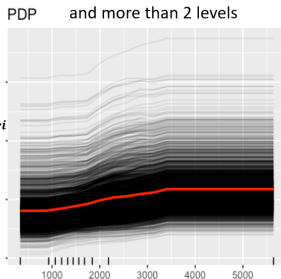


Partial dependence plots and ICE curves

| x1 | x2 | x3 | | x1 | x2 | x3 | | x1 | x2 | x3 | $\hat{f}^i(\mathbf{x1})$ | $\overline{\hat{f}(\mathbf{x1})}$ |
|----|----|----|---|----|----|----|---|----|----|----|--------------------------|-----------------------------------|
| 11 | 4 | 5 | → | 11 | 4 | 5 | → | 11 | 4 | 5 | $\hat{f}^1(11)$ | $\frac{\sum \hat{f}^i(11)}{2}$ |
| 12 | 6 | 7 | | 11 | 6 | 7 | | 11 | 6 | 7 | $\hat{f}^2(11)$ | |
| | | | | 12 | 4 | 5 | | 12 | 4 | 5 | $\hat{f}^1(12)$ | $\frac{\sum \hat{f}^i(12)}{2}$ |
| | | | | 12 | 6 | 7 | | 12 | 6 | 7 | $\hat{f}^2(12)$ | |

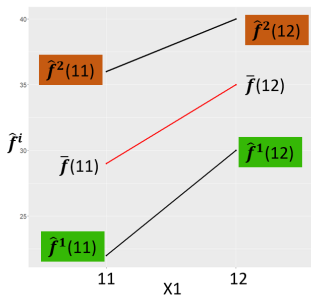


More than 2 observations
and more than 2 levels

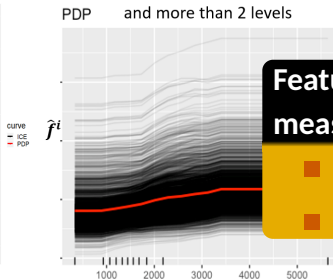


Partial dependence curve and ICE curves

| x1 | x2 | x3 | | x1 | x2 | x3 | | x1 | x2 | x3 | $\hat{f}^i(x1)$ | $\overline{f(x1)}$ |
|----|----|----|---|----|----|----|---|----|----|----|-----------------|--------------------------------|
| 11 | 4 | 5 | → | 11 | 4 | 5 | → | 11 | 4 | 5 | $\hat{f}^1(11)$ | $\frac{\sum \hat{f}^i(11)}{2}$ |
| 12 | 6 | 7 | | 11 | 6 | 7 | | 11 | 6 | 7 | $\hat{f}^2(11)$ | $\frac{\sum \hat{f}^i(11)}{2}$ |
| | | | | 12 | 4 | 5 | | 12 | 4 | 5 | $\hat{f}^1(12)$ | $\frac{\sum \hat{f}^i(12)}{2}$ |
| | | | | 12 | 6 | 7 | | 12 | 6 | 7 | $\hat{f}^2(12)$ | $\frac{\sum \hat{f}^i(12)}{2}$ |



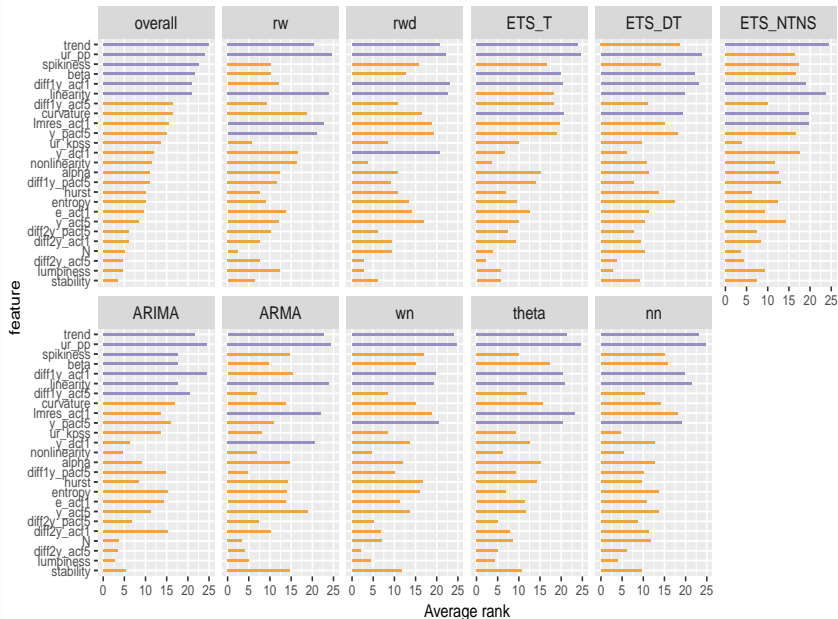
More than 2 observations
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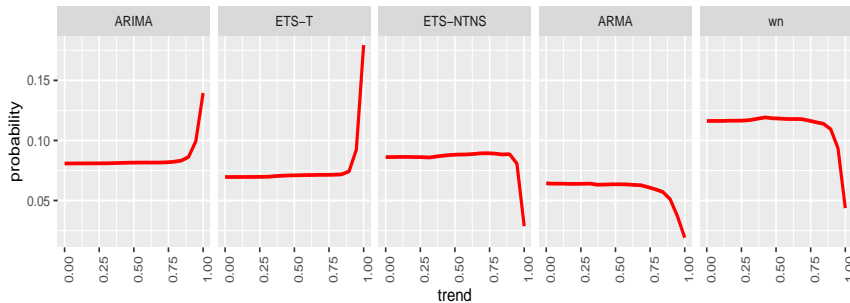
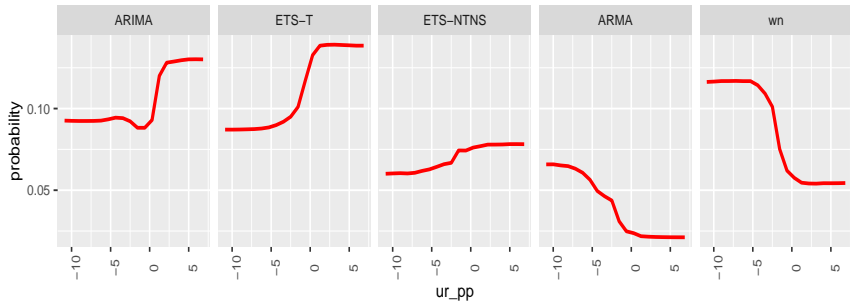
**Feature importance
measures:**

- "flatness" of PD curve
- "flatness" of ICE curves

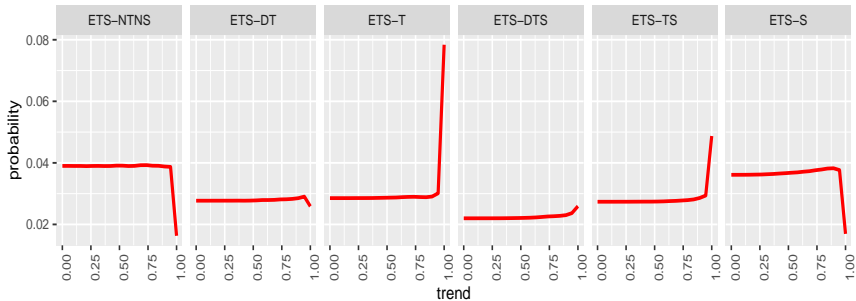
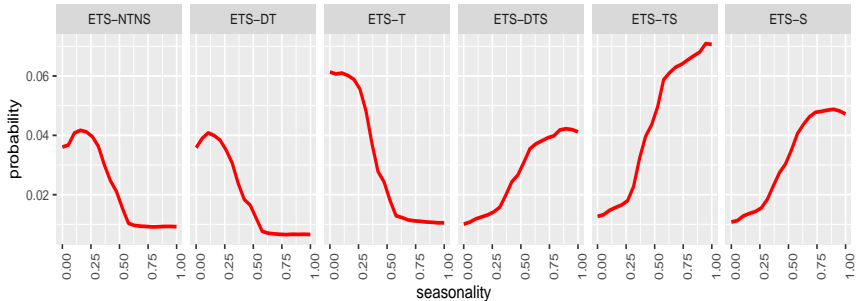
Feature importance plots for yearly data



Partial dependency plots for yearly data

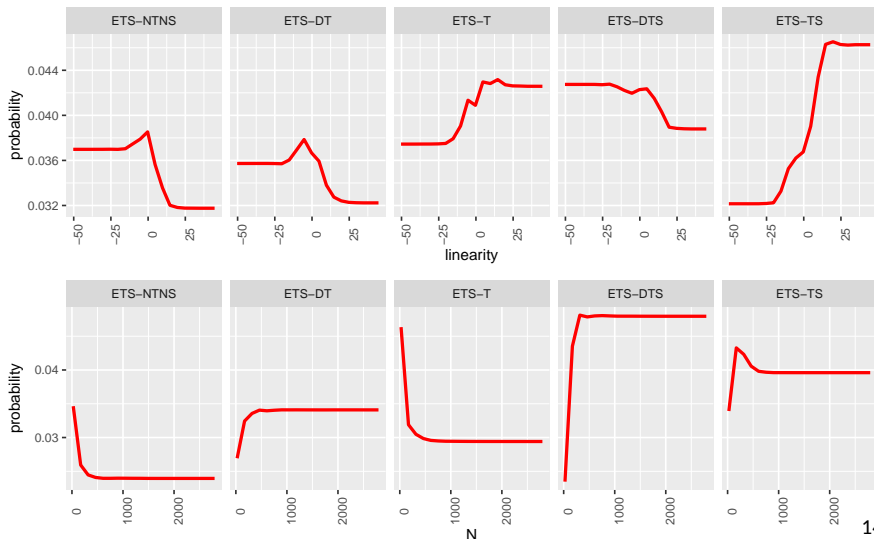


Partial dependency plots for quarterly data



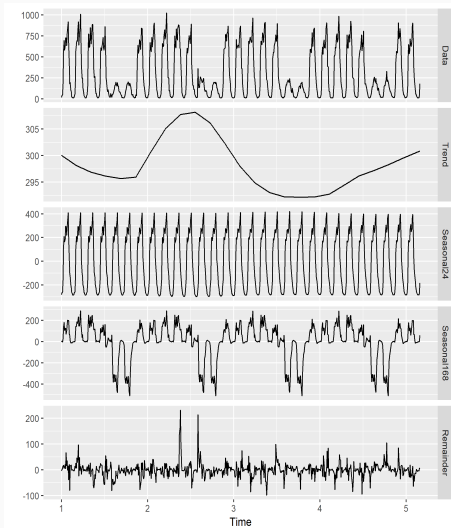
Partial dependency plots for monthly data

linearity: estimated value of β_1 based on $T_t = \beta_0 + \beta_1 \phi_1(t) + \beta_2 \phi_2(t) + \varepsilon_t$



Hourly series

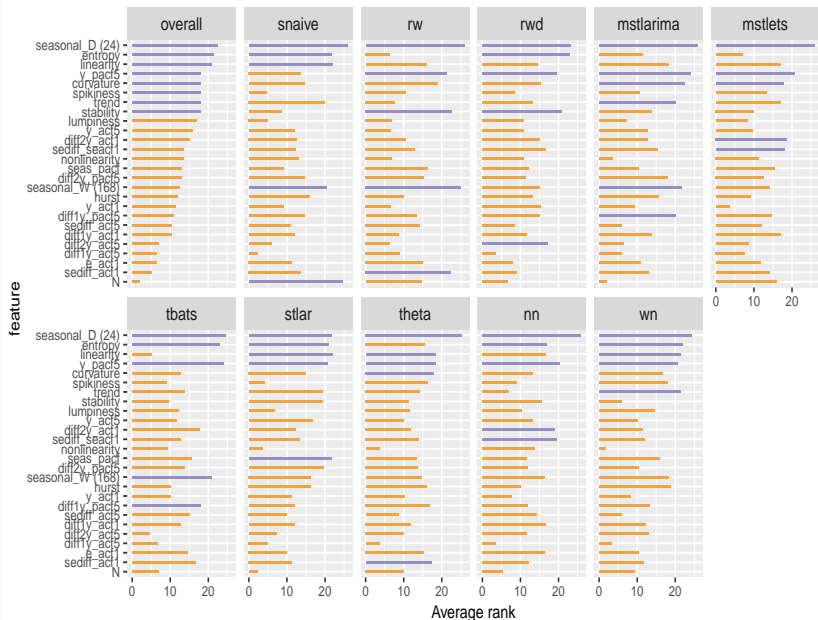
■ multiple seasonality



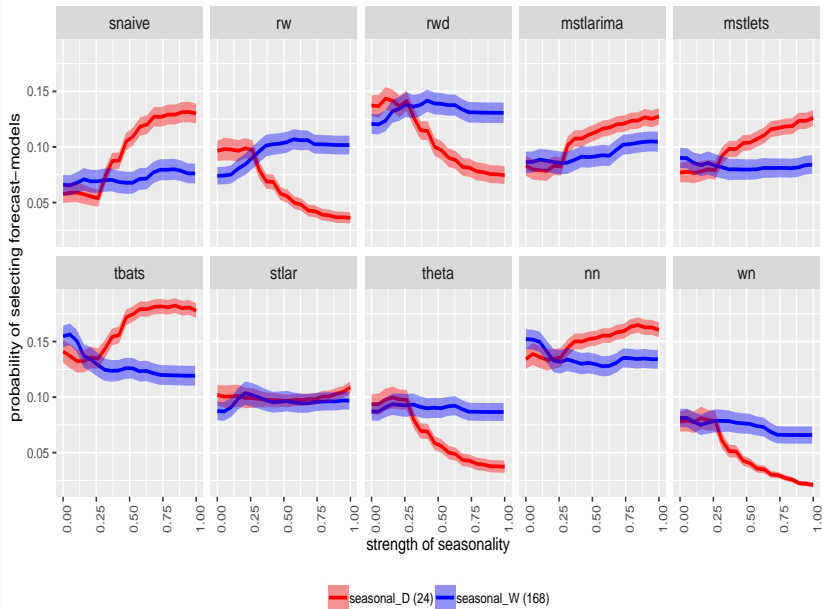
Hourly data

- ▶ daily - 24
- ▶ weekly - 168

Feature importance plots for hourly data



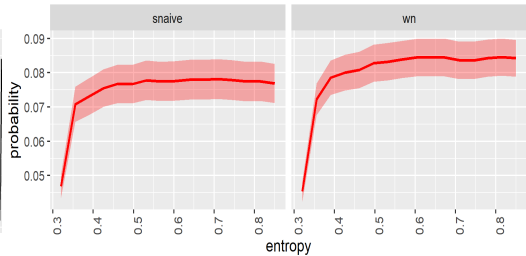
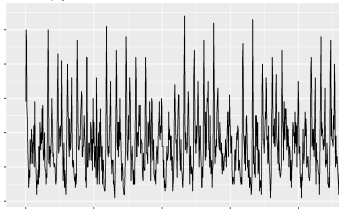
Partial dependency plots for hourly data: Seasonality



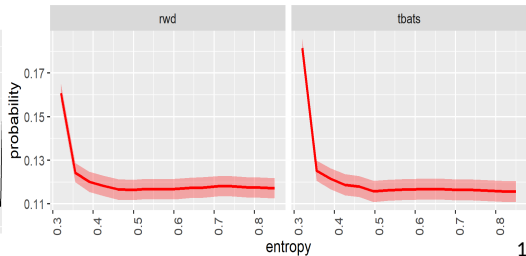
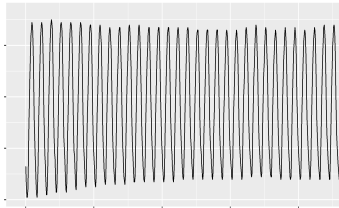
Partial dependency plots for hourly data: entropy

■ forecastability of a time series

entropy: 0.85



entropy: 0.44



- Friedman's H-statistic

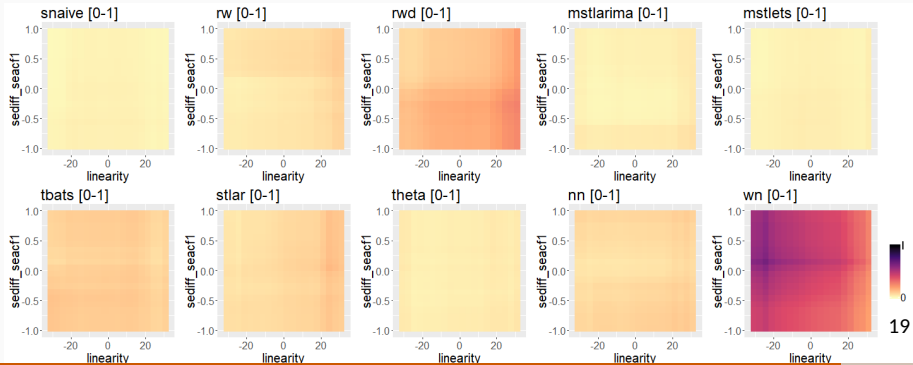
fraction of variance of two-variable partial dependency not captured by sum of the respective individual partial dependencies.

Interaction effect

■ Friedman's H-statistic

fraction of variance of two-variable partial dependency not captured by sum of the respective individual partial dependencies.

Hourly: interaction between linearity and seasonal lag at seasonally-differenced series

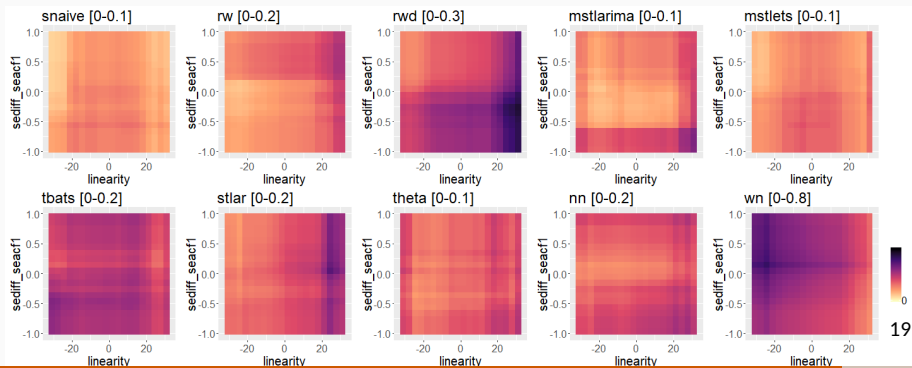


Interaction effect

■ Friedman's H-statistic

fraction of variance of two-variable partial dependency not captured by sum of the respective individual partial dependencies.

Hourly: interaction between linearity and seasonal lag at seasonally-differenced series



- Global perspective of feature contribution: the overall role of features in the choice of different forecast-models.

- Global perspective of feature contribution: the overall role of features in the choice of different forecast-models.
- **What next?** Local perspective of feature contribution: zoom into local regions of the data to identify which features contribute most to classify a specific instance.



available at: <https://github.com/thiyanagt/seer>

```
devtools::install_github("thiyanagt/seer")  
library(seer)
```