

exercises:

① $H_2O: c_p^{sp} = 4182 \text{ J K}^{-1} \text{ kg}^{-1} \quad | : 1000 = 4,182 \text{ J K}^{-1} \text{ g}^{-1}$

$\rightarrow c_p = M c_p^{sp} \approx 75,36 \text{ J K}^{-1} \text{ mol}^{-1}$

② Ice: $\Delta_m H^{\circ} = 3,338 \cdot 10^5 \text{ J kg}^{-1} \quad | : 1000 = 3,338 \cdot 10^2 \text{ J g}^{-1}$

$\Delta_m H = M \Delta_m H^{\circ} = 3,338 \cdot 10^2 \cdot 18,02 \approx 6,015 \cdot 10^3 \text{ J mol}^{-1}$

③ $Q = c_p \cdot \Delta T = (c_{p,w} + c_{p,K}) \Delta T = (c_p^{spec,w} \cdot m_w + c_{p,K}) \Delta T =$

$= (4182 \text{ J K}^{-1} \text{ kg}^{-1} \cdot 0,1 \text{ kg} + 120 \text{ J K}^{-1}) \Delta T = 538,2 \text{ J K}^{-1} \Delta T = 500 \text{ J} \rightarrow \Delta T = 0,929 \text{ K}$

if assumption: $c_{p,K} \approx 0 \rightarrow Q = c_{p,w} \cdot \Delta T = c_p^{spec,w} \cdot m_w \cdot \Delta T = 4182 \text{ J K}^{-1} \cdot \Delta T = 500 \text{ J} \rightarrow \Delta T = 1,196 \text{ K}$

④ $Q = \underbrace{m_{ice} \Delta_m H}_{\text{dH man. for melting of 10g ice at } T_E} + \underbrace{m_{ice} c_{p,w}^{spec} (T_f - T_E)}_{\text{dH man for heating of ice water}} + \underbrace{m_w c_{p,w}^{spec} (T_f - T_i)}_{\text{dH man for cooling of (rest) water}} + \underbrace{c_{p,K} (T_f - T_i)}_{\text{dH man for cooling of calorimeter}} = 0$

$\rightarrow T_f = \frac{(m_w c_{p,w}^{spec} + c_{p,K}) T_i + m_{ice} c_{p,w}^{spec} T_E - m_{ice} \Delta_m H}{(m_w + m_{ice}) c_{p,w}^{spec} + c_{p,K}}$

$T_f = 285,95 \text{ K } (12,8^\circ \text{C})$

for $m_w = 100 = 0,1 \text{ kg}$, $c_{p,K} = 120 \text{ J K}^{-1}$,

$T_i = 293,15 \text{ K } (20^\circ \text{C})$, $T_E = 273,15 \text{ K } (0^\circ \text{C})$

$\& m_{ice} = 10 \text{ g} = 0,01 \text{ kg}$ ($c_p^{spec,w} = 2100 \text{ J K}^{-1} \text{ kg}^{-1}$)

if ice water (0°C) is add instead of ice:

$Q = m_{ice,w} c_p^{spec,w} (T_f - T_E) + m_w c_p^{spec,w} (T_f - T_i) + c_{p,K} (T_f - T_i) = 0$

$\rightarrow T_f \cdot (c_p^{spec,w} \cdot m_{ice,w} + c_p^{spec,w} \cdot m_w + c_{p,K}) = m_{ice,w} \cdot T_E \cdot c_p^{spec,w} + T_i \cdot (m_w \cdot c_p^{spec,w} + c_{p,K})$

$\rightarrow T_f = \frac{T_E \cdot m_{ice,w} \cdot c_p^{spec,w} + T_i \cdot (m_w \cdot c_p^{spec,w} + c_{p,K})}{c_p^{spec,w} \cdot (m_{ice,w} + m_w) + c_{p,K}}$

$T_f = 291,95 \text{ K } (18,8^\circ \text{C})$

for $m_w = 0,1 \text{ kg}$, $c_{p,K} = 120 \text{ J K}^{-1}$,

$T_i = 293,15 \text{ K } (20^\circ \text{C})$, $T_E = 273,15 \text{ K } (0^\circ \text{C})$

$\& m_{ice,w} = 0,01 \text{ kg}$ ($c_p^{spec,w} = 2100 \text{ J K}^{-1} \text{ kg}^{-1}$)

⑤ $0 = c_p^{spec,liq} \cdot m_{liq, sol} \cdot \Delta T + n_{liq} \cdot \Delta_{sol} H_{liq}$

$c_p^{spec,liq} = 4,053 \text{ J K}^{-1} \text{ g}^{-1}$

$m_{liq, sol} = 1 \text{ mol} \cdot 42,9 \frac{\text{g}}{\text{mol}} + 100 \text{ mol} \cdot 18,02 \frac{\text{g}}{\text{mol}} = 222,6 \text{ g}$

$\Delta_{sol} H_{liq} = -35,941$

$\Delta T = - \frac{n_{liq} \cdot \Delta_{sol} H_{liq}}{c_p^{spec,liq} \cdot m_{liq, sol}} = \frac{1 \cdot 35,941}{4,053 \cdot 222,6} \approx 0,04 \text{ K} = 0,04^\circ \text{C}$