

Course :- Computer Science

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## Assignment :- 1

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## \* Homework 1.1

	Jerry	
	Go to bank	Not go to bank
susan	0.08	0.22
	0.12	0.58
	0.20	0.80
		1

$$P(\text{Jerry} \cap \text{susan}) = 8\%$$

$$\textcircled{a} P(\text{Jerry} | \text{susan}) = \frac{P(\text{Jerry} \cap \text{susan})}{P(\text{susan})} = \frac{8}{30} = 26.66\%$$

$$\textcircled{b} P(\text{Jerry} | \text{susan}) = \frac{P(\text{Jerry} \cap \text{susan})}{P(\text{susan})} = \frac{6}{35} = 0.1714\%$$

$$\textcircled{c} P(\text{Jerry} \cap \text{susan} | \text{Jerry} \cup \text{susan}) =$$

$$= \frac{P(P \cap S) \cap (P \cup S)}{P(P \cup S)}$$



$$= \frac{P(\text{Jerry} \cap \text{susan})}{P(\text{Jerry} \cup \text{susan})}$$

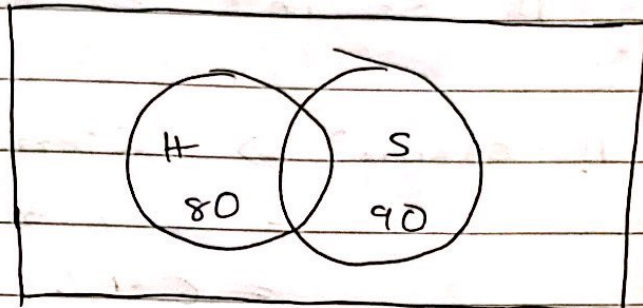
$$= \frac{8}{42} = 19.04\%$$

$$P(\text{Jerry} \cup \text{susan}) = P(J) + P(S) - P(J \cap S)$$

$$= 20 + 30 - 8$$

$$= 42$$

⇒ Homework 1.2.



$$P(H \cup S) = 111.$$

$$\begin{aligned} P(H \cap S) &= P(H) + P(S) - P(H \cup S) \\ &= 80 + 90 - 111 \\ &= 79. \end{aligned}$$

$$\begin{aligned} \text{(a)} \quad P(H - S) &= P(H) - P(H \cap S) \\ &= 80 - 79 \\ &= 1. \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad P(S - H) &= P(S) - P(H \cap S) \\ &= 90 - 79 \\ &= 11. \end{aligned}$$

$$\begin{aligned} \text{(c)} \quad P(H' \cap S') &= 100 - P(H) - P(S) + P(H \cap S) \\ &= 100 - 80 - 90 + 79 \\ &= 9. \end{aligned}$$



\* Homework 1.3

$$P(\text{Jerry} \cap \text{susan}) \Rightarrow 8.1$$

$$\begin{aligned} P(\text{Jerry} \cap \text{susan}) &\Rightarrow P(\text{Jerry}) \times P(\text{susan}) \\ &= 20\% \times 30\% \\ &= 6\% \end{aligned}$$

These events are independent, since both are not same.

\* Homework 1.4 :-

sum	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	10	11	12

$$(a) P(\text{sum is } 5) = \frac{5}{36}$$

$$P(\text{second die shows } 5) = \frac{1}{36}$$

$$= \frac{1}{6}$$

$$P(\text{sum is } 5 \cap \text{second die shows } 5)$$

$$= P(\text{sum is } 5) \times P(\text{second die shows } 5)$$

$$= \frac{5}{36} \times \frac{1}{6} = \frac{5}{216}$$



$$\therefore P(\text{sum is 6} \cap \text{second die shows 5}) = \frac{1}{36}$$

$\therefore$  Both are not equal, so events are dependent.

$$(b) P(\text{sum is 7}) = \frac{6}{36} = \frac{1}{6}$$

$$P(\text{first die shows 5}) = \frac{6}{36} = \frac{1}{6}$$

$$P(\text{sum is 7} \cap \text{first die shows 5}) = P(\text{sum is 7}) \times P(\text{1st die shows 5})$$

$$= \frac{1}{6} \times \frac{1}{6}$$

$$= \frac{1}{36}$$

$\therefore$  Both events are not equal show it is dependent.

## \* Homework I.5 :-

	$T_x$	$A_k$	$N_J$	
oil	18	6	1	25
Necoil	42	24	9	75
	60	30	10	100

$$P(\text{coil} | T_x) = \frac{P(\text{coil} \cap T_x)}{P(T_x)}$$

$$\begin{aligned} P(\text{coil} \cap T_x) &= P(\text{coil} | T_x) \times P(T_x) \\ &= 30 \times 60 \\ &= 18\% \end{aligned}$$

$$\begin{aligned} P(\text{coil} \cap N_J) &= P(\text{coil} | N_J) \times P(N_J) \\ &= 10 \times 10 \\ &= 1\% \end{aligned}$$

$$\begin{aligned} P(\text{coil} \cap A_k) &= P(\text{coil} | A_k) \times P(A_k) \\ &= 20 \times 30 \\ &= 6\% \end{aligned}$$

$$(a) P(\text{coil}) = 25\%$$

$$(b) P(T_x | \text{coil}) = \frac{P(T_x \cap \text{coil})}{P(\text{coil})} = \frac{18}{25} = 72\%$$



\* Homework 1.6

$$(a) P(C \text{ Passenger did not survive}) = \frac{1490}{2201}$$

$$= 0.677$$

$$(b) P(C \text{ passenger stay in first dam}) = \frac{325}{2201}$$

$$= 0.147$$

$$(c) P(C \text{ Passenger in first dam} \mid \text{passenger survive})$$

$$= \frac{203}{711} = 0.2855$$

$$(d) \because P(F \mid C) \neq P(F)$$

$$\therefore (c) \neq (b)$$

$\therefore$  These are dependent

$$(e) P(C \text{ Passenger in first dam and Passenger } \overset{\text{was died}}{\text{survive}})$$

$$= \frac{6}{711} = 0.8438$$

$$P(\text{Passenger is active}) / P(\text{passenger survived})$$

$$= 654 / 711 = 91.98\%$$

$$j) P(A \cap FC | S) = 197 / 711$$

$$P(A) | P(S) = 654 / 711 \quad P(FC | S) = 203 / 711$$

$$P(A \cap FC | S) \neq P(A | S) \times P(FC | S)$$

$$197 / 711 \neq 654 / 711 \times 203 / 711$$

$$0.272707 \neq 0.262 \rightarrow \text{dependent}$$

$\Rightarrow$  Given that passengers survived, active & first class are dependent on each other

$$P(C \cap FC | S) = 6 / 711$$



$$P(C|S) = \frac{57}{711} \quad \text{and} \quad P(F|S) = \frac{203}{711}$$

~~$P(C \cap F)$~~

$$\frac{P(C \cap F)}{5} \neq P(C) \times P(F|S)$$

$$\frac{6}{711} \neq \frac{57}{711} \times \frac{203}{711}$$

$$0.0084 \neq 0.0228 \rightarrow \text{dependent}$$

Therefore, events are dependent