SDS 383D Propagating Uncertainty

Jan-Michael Cabrera, JC7858

February 13, 2019

A: Standard Error

$$\hat{\Sigma} \approx \text{cov}(\hat{\theta}) = \text{E}\left[(\hat{\theta} - \bar{\theta})(\hat{\theta} - \bar{\theta})^T \right]$$
(1)

$$f(\theta) = \theta_1 + \theta_2 \tag{2}$$

$$\hat{\Sigma}_f = \text{cov}(\hat{\theta}_1 + \hat{\theta}_2) \tag{3}$$

$$= E\left[(\hat{\theta}_1 + \hat{\theta}_2)(\hat{\theta}_1 + \hat{\theta}_2) \right] \tag{4}$$

$$= \mathrm{E}\left[\hat{\theta}_1^2 + 2\hat{\theta}_1\hat{\theta}_2 + \hat{\theta}_2^2\right] \tag{5}$$

$$= E\left[\hat{\theta}_1^2\right] + 2E\left[\hat{\theta}_1\hat{\theta}_2\right] + E\left[\hat{\theta}_2^2\right]$$
(6)

$$= \operatorname{var}(\hat{\theta}_1) + 2\operatorname{cov}(\hat{\theta}_1\hat{\theta}_2) + \operatorname{var}(\hat{\theta}_2) \tag{7}$$

$$= \hat{\Sigma}_{11} + 2\hat{\Sigma}_{12} + \hat{\Sigma}_{22} \tag{8}$$

$$g(\theta) = \sum_{i=1}^{p} \theta_p \tag{9}$$

$$\hat{\Sigma}_g = \sum_{i=1}^p \sum_{j=1}^p \hat{\Sigma}_{ij} \tag{10}$$