## trecs\_exp-user\_topic\_mapping

#### December 13, 2022

```
[]: import pandas as pd
     import matplotlib.pyplot as plt
     from matplotlib import style
     import numpy as np
     from sklearn.decomposition import NMF
     from importlib import reload
     import wrapper
     import sys
     # caution: path[0] is reserved for script path (or '' in REPL)
     sys.path.insert(1, '../t-recs/')
     import trecs
     import os
     from scipy import sparse
     from trecs.models import ContentFiltering
     from trecs.metrics import MSEMeasurement, InteractionSpread, InteractionSpread,
      InteractionSimilarity, RecSimilarity, RMSEMeasurement, InteractionMeasurement
     from trecs.components import Users
     from wrapper.models.bubble import BubbleBurster
     # from src.utils import get_topic_clusters
     from wrapper.metrics.evaluation_metrics import SerendipityMetric,_
      ⇔DiversityMetric, NoveltyMetric, TopicInteractionMeasurement, ⊔
      →MeanNumberOfTopics, UserMSEMeasurement
     random_state = np.random.seed(42)
     plt.style.use("seaborn-paper")
```

/var/folders/sm/hcy50x855gvf2b1qwkjstnvh0000gn/T/ipykernel\_15680/1425888263.py:2 4: MatplotlibDeprecationWarning: The seaborn styles shipped by Matplotlib are deprecated since 3.6, as they no longer correspond to the styles shipped by seaborn. However, they will remain available as 'seaborn-v0\_8-<style>'. Alternatively, directly use the seaborn API instead. plt.style.use("seaborn-paper")

 $\textbf{Ref:}\ https://towardsdatascience.com/dimensionality-reduction-for-data-visualization-pca-vs-tsnevs-umap-be4aa7b1cb29$ 

```
[]: from sklearn.cluster import KMeans
     def get_topic_clusters(interaction_matrix, n_clusters:int=100, n_attrs:int=100,__
      →max_iter:int=100):
         11 11 11
         Creates clusters of movies based on their genre.
             binary_ratings_matrix: a binary matrix of users and movies
             n_attrs: number of attributes to use in NMF
             nmf_solver: solver to use in NMF
         Outputs:
             clusters: a list of cluster assignments
         # Create topic clusters
         #create co-occurence matrix from binary_interaction_matrix
         print('Calculating clusters...')
         co_occurence_matrix = interaction_matrix.T @ interaction_matrix
         co_occurence_matrix = interaction_matrix.T @ interaction_matrix
         # Matrix factorize co_occurence_matrix to get embeddings
         nmf_cooc = NMF(n_components=n_attrs, max_iter=max_iter, verbose=1)
         W_topics = nmf_cooc.fit_transform(co_occurence_matrix)
         # cluster W_topics
         cluster_ids = KMeans(n_clusters=n_clusters, max_iter=max_iter,__
      →random_state=random_state, verbose=1).fit_predict(W_topics)
         # np.save(file path, cluster ids)
         print('Calculated clusters.')
         return cluster_ids
[]: # import warnings filter
     from warnings import simplefilter
     # ignore all future warnings
     simplefilter(action='ignore', category=FutureWarning)
[]: ratings df = pd.read_csv('data/ml-100k/u.data', sep="\t", names=['UserID', |
      →'MovieID', 'Rating', 'Timestamp'])
[]: from sklearn.decomposition import NMF
     binary_ratings_df = ratings_df.drop(columns=['Timestamp'])
     binary_ratings_df.loc[binary_ratings_df['Rating'] > 0, 'Rating'] = 1
     # turn dataframe into matrix where each movie is a column and each user is a row
```

```
binary_ratings_matrix = binary_ratings_df.pivot(index='UserID',__
 ⇔columns='MovieID', values='Rating').fillna(0).to_numpy()
from lightfm.cross_validation import random_train_test_split
from scipy import sparse
# split data into train and test sets
train interactions, test interactions = random train test split(sparse.
 ⇔csr_matrix(binary_ratings_matrix), test_percentage=0.2, __
 →random_state=random_state)
train_interactions = train_interactions.toarray()
test_interactions = test_interactions.toarray()
n_attrs=100
nmf = NMF(n_components=n_attrs, solver="mu")
user_representation = nmf.fit_transform(binary_ratings_matrix)
item_representation = nmf.components_
print(user_representation.shape, item_representation.shape)
# nmf solver='mu'
n clusters=50
max_iter=500
n_attrs=100
item_topics = get_topic_clusters(binary_ratings_matrix, n_attrs=n_clusters,_
 →max_iter=max_iter)#, nmf_solver=nmf_solver)
users = Users(size=(943,100), repeat_interactions=False)
/Users/madisonthantu/miniforge3/envs/fairRS/lib/python3.8/site-
packages/lightfm/lightfm_fast.py:9: UserWarning: LightFM was compiled without
OpenMP support. Only a single thread will be used.
  warnings.warn(
/Users/madisonthantu/miniforge3/envs/fairRS/lib/python3.8/site-
packages/sklearn/decomposition/_nmf.py:1692: ConvergenceWarning: Maximum number
of iterations 200 reached. Increase it to improve convergence.
  warnings.warn(
(943, 100) (100, 1682)
Calculating clusters...
violation: 1.0
violation: 0.0008111012211140843
violation: 0.0018579971758544973
violation: 0.002348404969455981
violation: 0.001963674297444194
violation: 0.0015236872281129985
violation: 0.0012535307370826517
violation: 0.0010656736015344352
violation: 0.0009157574897872806
```

violation: 0.0007991225960594281 violation: 0.000714636141551671 violation: 0.0006490381082209844 violation: 0.0005972169726710217 violation: 0.0005549932878832688 violation: 0.0005206685817139828 violation: 0.0004915790573408767 violation: 0.0004652150471906113 violation: 0.00044215158985576287 violation: 0.00042257032842413857 violation: 0.00040465988180981 violation: 0.00038809403110232906 violation: 0.0003732735237999536 violation: 0.00035958751936517996 violation: 0.00034623336152060695 violation: 0.00033458078658895094 violation: 0.0003231686127826073 violation: 0.00031319485990230906 violation: 0.0003040539872361975 violation: 0.000295455944650737 violation: 0.00028767005864218845 violation: 0.0002803228965203025 violation: 0.0002727477995441988 violation: 0.0002659940811304535 violation: 0.0002591283217727306 violation: 0.0002529716205280376 violation: 0.0002472614811032203 violation: 0.0002416809427548128 violation: 0.0002366353774709594 violation: 0.00023188267831263402 violation: 0.0002273211363352962 violation: 0.00022277371693806613 violation: 0.00021874834772473648 violation: 0.0002144331913096802 violation: 0.00021083945802284306 violation: 0.00020720496028834226 violation: 0.00020380619951583227 violation: 0.00020086767557508933 violation: 0.00019787315562147986 violation: 0.00019475156372002648 violation: 0.0001917370730802528 violation: 0.00018886868887122652 violation: 0.0001859912197103872 violation: 0.00018323580093702934 violation: 0.00018062290626195358 violation: 0.00017828193428424952 violation: 0.00017620805406318927 violation: 0.0001742345484770772

violation: 0.00017245644026093025 violation: 0.00017049719087666428 violation: 0.00016852268829433163 violation: 0.00016630931100662804 violation: 0.00016437812817536446 violation: 0.0001624993397099876 violation: 0.00016085606594463538 violation: 0.0001590699135630679 violation: 0.00015748793170812647 violation: 0.000156056768668566 violation: 0.00015461488500869694 violation: 0.00015339804936877617 violation: 0.00015206951623181157 violation: 0.00015057571823102212 violation: 0.0001492616140571389 violation: 0.00014798536436320817 violation: 0.00014667546143148487 violation: 0.00014572591204239528 violation: 0.00014468182427252872 violation: 0.00014373682709311738 violation: 0.0001426940209269569 violation: 0.0001416867766560684 violation: 0.0001406517657688315 violation: 0.0001397758457086101 violation: 0.00013907734142832513 violation: 0.00013849462187389986 violation: 0.00013772753215316225 violation: 0.00013689198994673097 violation: 0.00013609823909708756 violation: 0.00013520129221992656 violation: 0.00013429387141027088 violation: 0.00013355703492046994 violation: 0.00013270918822509817 violation: 0.0001318869785264556 violation: 0.0001309997350818319 violation: 0.0001300957879009074 violation: 0.00012931157491679333 violation: 0.00012846390487191925 violation: 0.00012775505093184374 violation: 0.00012695874676038632 violation: 0.00012626633434095858 violation: 0.00012555779264843494 violation: 0.000124941965222154 violation: 0.00012434488540528533 violation: 0.00012365930006005336 violation: 0.0001231128331119413 violation: 0.0001226249236900704 violation: 0.0001222458218540237

violation: 0.00012183570637850564 violation: 0.00012156473524481501 violation: 0.00012126683561310604 violation: 0.00012091007188147373 violation: 0.00012068220515971065 violation: 0.00012050852157940062 violation: 0.000120280005609624 violation: 0.00012005844604729106 violation: 0.00011980599712798704 violation: 0.00011964615289779544 violation: 0.00011944671580841445 violation: 0.00011916096337377208 violation: 0.00011893054269861008 violation: 0.0001187475781019576 violation: 0.00011839229318121637 violation: 0.00011799960669818226 violation: 0.00011752254126307526 violation: 0.0001171080948196955 violation: 0.00011667759723436887 violation: 0.00011621738822528687 violation: 0.00011578483616821223 violation: 0.00011539233096189993 violation: 0.0001150391914142034 violation: 0.00011469063757728474 violation: 0.00011415785145315042 violation: 0.0001137170754083149 violation: 0.00011324478808189727 violation: 0.00011280984386055837 violation: 0.00011230808047380984 violation: 0.00011170372047301133 violation: 0.00011128154022196592 violation: 0.00011076280424335234 violation: 0.00011032562619120264 violation: 0.00010989595146958646 violation: 0.00010927287165412746 violation: 0.00010863641576810569 violation: 0.00010801692431622748 violation: 0.0001073486761618235 violation: 0.00010661347258346636 violation: 0.00010581302430954739 violation: 0.00010508941133671069 violation: 0.00010435534617830357 violation: 0.00010357589174540546 violation: 0.00010286976853961824 violation: 0.00010225929454772402 violation: 0.0001015852154712779 violation: 0.00010084513096403187 violation: 0.00010011576501942235

```
violation: 9.940881036862153e-05
Converged at iteration 155
Initialization complete
Iteration 0, inertia 48.15432092266328.
Iteration 1, inertia 35.26550347136774.
Iteration 2, inertia 34.437288975092144.
Iteration 3, inertia 34.21929857699359.
Iteration 4, inertia 34.09290293216635.
Iteration 5, inertia 33.98012121826649.
Iteration 6, inertia 33.94793167438911.
Iteration 7, inertia 33.90728602110529.
Iteration 8, inertia 33.888443453013295.
Iteration 9, inertia 33.879798450818974.
Iteration 10, inertia 33.84723002422411.
Iteration 11, inertia 33.84245092302271.
Iteration 12, inertia 33.83652751863964.
Converged at iteration 12: strict convergence.
Initialization complete
Iteration 0, inertia 47.77610769502342.
Iteration 1, inertia 35.46903220989502.
Iteration 2, inertia 34.52495167045987.
Iteration 3, inertia 33.929671393784275.
Iteration 4, inertia 33.7669670689433.
Iteration 5, inertia 33.65685717683232.
Iteration 6, inertia 33.610838454179415.
Iteration 7, inertia 33.60099606512115.
Iteration 8, inertia 33.59455282492198.
Iteration 9, inertia 33.593515755496036.
Iteration 10, inertia 33.59223849332847.
Iteration 11, inertia 33.590234774685456.
Iteration 12, inertia 33.58982793446874.
Iteration 13, inertia 33.5860942699757.
Iteration 14, inertia 33.58459076143862.
Iteration 15, inertia 33.584029075082576.
Iteration 16, inertia 33.58319045906775.
Converged at iteration 16: center shift 1.2489345732429019e-07 within tolerance
1.453389046531099e-06.
Initialization complete
Iteration 0, inertia 49.39264107916929.
Iteration 1, inertia 36.049597750027225.
Iteration 2, inertia 34.97539863591017.
Iteration 3, inertia 34.56974483930776.
Iteration 4, inertia 34.321885921712344.
Iteration 5, inertia 34.22924972638986.
Iteration 6, inertia 34.16320404661296.
Iteration 7, inertia 34.14566016589062.
```

Iteration 8, inertia 34.12895034659863. Iteration 9, inertia 34.11358925534266.

```
Iteration 10, inertia 34.10373745493676.
Iteration 11, inertia 34.097013178316644.
Iteration 12, inertia 34.07869937899624.
Iteration 13, inertia 34.069955423026805.
Iteration 14, inertia 34.06297065385411.
Iteration 15, inertia 34.06057135190548.
Iteration 16, inertia 34.06007117652773.
Iteration 17, inertia 34.05957346114912.
Iteration 18, inertia 34.059383496374956.
Converged at iteration 18: center shift 1.9702746403215421e-07 within tolerance
1.453389046531099e-06.
Initialization complete
Iteration 0, inertia 48.15707489671477.
Iteration 1, inertia 36.09804562795394.
Iteration 2, inertia 34.97081897990375.
Iteration 3, inertia 34.667956995527256.
Iteration 4, inertia 34.519456599144135.
Iteration 5, inertia 34.428996988027905.
Iteration 6, inertia 34.334163393113386.
Iteration 7, inertia 34.28018099157191.
Iteration 8, inertia 34.26577692468223.
Iteration 9, inertia 34.25018204006152.
Iteration 10, inertia 34.24631735016583.
Iteration 11, inertia 34.24503133789294.
Iteration 12, inertia 34.24482971618422.
Converged at iteration 12: center shift 8.177206990120169e-07 within tolerance
1.453389046531099e-06.
Initialization complete
Iteration 0, inertia 47.88841010462291.
Iteration 1, inertia 35.52704221373162.
Iteration 2, inertia 34.60367650382151.
Iteration 3, inertia 34.36151435348752.
Iteration 4, inertia 34.282846958348394.
Iteration 5, inertia 34.252369783992904.
Iteration 6, inertia 34.2302046245341.
Iteration 7, inertia 34.199282913224394.
Iteration 8, inertia 34.178554194170005.
Iteration 9, inertia 34.13108164583353.
Iteration 10, inertia 34.07464199608229.
Iteration 11, inertia 34.01870074582298.
Iteration 12, inertia 33.93754874127561.
Iteration 13, inertia 33.84242543133578.
Iteration 14, inertia 33.80849621256224.
Iteration 15, inertia 33.78955739444958.
Iteration 16, inertia 33.77715743094834.
Iteration 17, inertia 33.769774545599525.
Converged at iteration 17: strict convergence.
Initialization complete
```

```
Iteration 2, inertia 34.63531442979463.
Iteration 3, inertia 34.355103097936826.
```

Iteration 0, inertia 48.59302782872548. Iteration 1, inertia 35.59681519855493.

Iteration 4, inertia 34.28547309542735.

Iteration 5, inertia 34.28181451428637.

Iteration 6, inertia 34.280847249144756.

Iteration 7, inertia 34.280720281037446.

Converged at iteration 7: strict convergence.

#### Initialization complete

Iteration 0, inertia 48.31913551771591.

Iteration 1, inertia 34.894035422795845.

Iteration 2, inertia 33.952475992020915.

Iteration 3, inertia 33.74336125662098.

Iteration 4, inertia 33.57025839962331.

Iteration 5, inertia 33.49065463214723.

Iteration 6, inertia 33.420631739380354.

Iteration 7, inertia 33.41199563339929.

Iteration 8, inertia 33.40421222606188.

Iteration 9, inertia 33.40026508656289.

Iteration 10, inertia 33.387565391836084.

Iteration 11, inertia 33.37581196133628.

Iteration 12, inertia 33.37235398522871.

Iteration 13, inertia 33.37002678696871.

Converged at iteration 13: strict convergence.

#### Initialization complete

Iteration 0, inertia 47.804014247676434.

Iteration 1, inertia 34.983172785440026.

Iteration 2, inertia 34.253716248611056.

Iteration 3, inertia 34.00490731425433.

Iteration 4, inertia 33.913891518411035.

Iteration 5, inertia 33.870776877665165.

Iteration 6, inertia 33.85201515351134.

Iteration 7, inertia 33.851630123457106.

Converged at iteration 7: center shift 4.5112980118090687e-07 within tolerance 1.453389046531099e-06.

#### Initialization complete

Iteration 0, inertia 47.530164254061624.

Iteration 1, inertia 34.65904628293155.

Iteration 2, inertia 33.545196270677565.

Iteration 3, inertia 33.14165928266153.

Iteration 4, inertia 33.025351013466704.

Iteration 5, inertia 32.91692018596355.

Iteration 6, inertia 32.8612023409233.

Iteration 7, inertia 32.856651531039695.

Iteration 8, inertia 32.828673449962665.

Iteration 9, inertia 32.826707111034494.

Iteration 10, inertia 32.81877318469584.

```
Iteration 11, inertia 32.81665779227108.
Iteration 12, inertia 32.81440589172527.
Iteration 13, inertia 32.813281923594275.
Converged at iteration 13: center shift 1.1317241037209851e-06 within tolerance
1.453389046531099e-06.
Initialization complete
Iteration 0, inertia 48.52701109722608.
Iteration 1, inertia 35.378678769572936.
Iteration 2, inertia 34.54186556532896.
Iteration 3, inertia 34.38200209475497.
Iteration 4, inertia 34.344062699600656.
Iteration 5, inertia 34.32014792548512.
Iteration 6, inertia 34.286042526517264.
Iteration 7, inertia 34.267768115316265.
Iteration 8, inertia 34.23511564448992.
Iteration 9, inertia 34.20369842646498.
Iteration 10, inertia 34.19133109168454.
Iteration 11, inertia 34.18655172785239.
Iteration 12, inertia 34.18355548866075.
Iteration 13, inertia 34.18277223067997.
Iteration 14, inertia 34.182148351182974.
Iteration 15, inertia 34.181869824240415.
Converged at iteration 15: strict convergence.
Calculated clusters.
```

### 1 Instantiating BubbleBurster

```
[]: sys.path.insert(1, '../')
     from wrapper.models.bubble import BubbleBurster
     from trecs.metrics import MSEMeasurement, InteractionSpread, InteractionSpread,
      InteractionSimilarity, RecSimilarity, RMSEMeasurement, InteractionMeasurement
[]: bubble = BubbleBurster(
         # num_users=number_of_users,
         # num_items=num_items,
         # num attributes=number of attributes,
        item_topics=item_topics,
        user representation=user representation,
         item_representation=item_representation,
        actual user representation=users,
        record_base_state=True,
     )
[]: user_pairs = [(u_idx, v_idx) for u_idx in range(len(user_representation)) for_
      →v_idx in range(len(user_representation))]
```

```
bubble.add_metrics(
        MSEMeasurement(),
         InteractionSpread(),
        InteractionSpread(),
        InteractionSimilarity(pairs=user_pairs),
        RecSimilarity(pairs=user_pairs),
        RMSEMeasurement(),
        InteractionMeasurement()
     print("These are the current metrics:")
     print(bubble.metrics)
    These are the current metrics:
    [<trecs.metrics.measurement.MSEMeasurement object at 0x137e89ee0>,
    <trecs.metrics.measurement.InteractionSpread object at 0x137e0a310>,
    <trecs.metrics.measurement.InteractionSpread object at 0x137e0a610>,
    <trecs.metrics.measurement.InteractionSimilarity object at 0x137e0a940>,
    <trecs.metrics.measurement.RecSimilarity object at 0x137e0a5e0>,
    <trecs.metrics.measurement.RMSEMeasurement object at 0x137e0a160>,
    <trecs.metrics.measurement.InteractionMeasurement object at 0x137e0ac10>]
        Compute user-topic mappings
[]: from src.utils import user_topic_mapping
     actual_user_profiles, actual_item_attributes = bubble.actual_user_profiles, u
      ⇒bubble.actual_item_attributes
     actual_user_topic_mapping = user_topic_mapping(actual_user_profiles,_
      →actual_item_attributes, item_topics)
    /Users/madisonthantu/Desktop/COMS 6998/Project/fair-recommender-
    systems/src/utils.py:135: SyntaxWarning: assertion is always true, perhaps
    remove parentheses?
      assert ((user_profiles.shape[1] == item_attributes.shape[0]),
    /Users/madisonthantu/Desktop/COMS 6998/Project/fair-recommender-
    systems/src/utils.py:137: SyntaxWarning: assertion is always true, perhaps
    remove parentheses?
      assert ((item_topics.shape == (item_attributes.shape[1],)),
[]: actual_user_topic_mapping.shape
[]: (943, 100)
[]: print(actual_user_topic_mapping[1,:])
```

[ 2.56964903e-01 1.25251968e-01 2.63593280e-01 4.79362095e-02

```
5.43423744e-02 1.98480664e-01 2.86978375e-01 2.35920670e-01
      6.29925112e-02 -3.84059410e-04 2.78490848e-01 2.97822356e-01
      2.03296318e-01 1.41966541e-01 5.63235221e-01
                                                     2.02339206e-01
      2.01101158e-01 3.00633318e-01 1.16399742e-02 1.99466265e-02
      7.48324102e-01 7.38473352e-01 1.54858094e-01 2.03099055e-01
      6.12540796e-02 3.35930804e-01 3.03640859e-01
                                                     3.60386094e-02
      2.14261032e-01 1.29881815e-01 4.46951415e-01
                                                     3.01742032e-02
      1.26016683e-01 5.73982085e-01 8.62943310e-02 1.65594644e-02
      1.10557985e-01 7.31949230e-03 7.02577000e-02 6.75177145e-02
      4.17764818e-01 5.99169195e-01 3.29893134e-01 1.67902263e-01
                                                     2.08322268e-02
     -3.12085869e-01 1.48059449e-01 1.97184923e-01
      1.14066086e-01 1.57768681e-01 1.38855192e-01
                                                     3.89795335e-01
      2.22731696e-01 3.70708166e-02 -2.20417165e-01
                                                     6.19282493e-01
      4.03631358e-01 6.60432602e-01 2.17344508e-01 7.29723511e-01
      4.17670047e-01 2.20886894e-01 -1.47363020e-01
                                                     6.56852408e-02
      1.64408807e-01 5.95908914e-01 2.79115740e-02 3.37466043e-01
      1.54310494e-01 4.86966161e-01 3.32688691e-03 -1.04852516e-02
      7.39664328e-01 2.72695453e-01 6.38432344e-02 1.41291446e-02
      1.87203876e-01 3.93263180e-01 5.65938292e-02 3.25403310e-01
      1.19063538e-01 3.52088792e-01 -1.99822832e+00 1.11803875e-01
     -3.17083872e-01 2.84724339e-01 3.41556765e-01 2.53051456e-02
      1.23810432e-02 1.73522985e-01 4.27795036e-02 3.56214673e-02
      9.91566409e-02 3.99785205e-02 8.50098410e-02 -1.42557576e-01
     -9.69143015e-02 6.24352959e-01 -1.62096359e-02 2.97362350e-01]
[]: user_clusters = get_topic_clusters(binary_ratings_matrix.T, n_attrs=n_clusters,_
     max_iter=max_iter)#, nmf_solver=nmf_solver)
    print(user_clusters.shape)
    print(item_topics.shape)
    Calculating clusters...
    violation: 1.0
    violation: 0.00023105663147641192
    violation: 0.0008968555782884329
    violation: 0.002797937212173178
    violation: 0.00319759143004992
    violation: 0.003113167357527142
    violation: 0.0025264247993327677
    violation: 0.002108708820660568
    violation: 0.0017758168790870848
    violation: 0.0015422410030184273
    violation: 0.0013973782795763843
    violation: 0.0013138559707382403
    violation: 0.001232101569542869
    violation: 0.00116297004761247
    violation: 0.0010996678746988044
```

violation: 0.0010225828845818446 violation: 0.0009603342206569841 violation: 0.0009052762554306112 violation: 0.0008578066670110475 violation: 0.0008155155380737319 violation: 0.0007934177895929073 violation: 0.0007767893749273988 violation: 0.000751243440723186 violation: 0.0007313453770383489 violation: 0.0007198664975299297 violation: 0.0007083381562689952 violation: 0.0006964311361125571 violation: 0.0006875259660570504 violation: 0.0006786099146629198 violation: 0.0006679631629007681 violation: 0.0006584014898705648 violation: 0.0006484507432968698 violation: 0.0006379619188683355 violation: 0.0006270094492889831 violation: 0.0006147416159439034 violation: 0.0006034339191292861 violation: 0.0005970503552810804 violation: 0.0005912020033861382 violation: 0.0005836785751015997 violation: 0.0005772143633034478 violation: 0.0005712103671903105 violation: 0.0005622982533813432 violation: 0.0005552852043687316 violation: 0.0005501256404276743 violation: 0.0005432499554931478 violation: 0.0005372252743169817 violation: 0.0005285410474037706 violation: 0.0005217023598620187 violation: 0.0005161706517748762 violation: 0.0005071883546391862 violation: 0.0004992470721596444 violation: 0.0004924670143981365 violation: 0.0004835285054936876 violation: 0.00047580407198975154 violation: 0.0004635585926472889 violation: 0.0004549551648482233 violation: 0.00044648249659430463 violation: 0.0004365747106250542 violation: 0.0004262311920258342 violation: 0.0004167765561718009 violation: 0.00040667656566726885 violation: 0.00039667825938806466 violation: 0.0003858842935319456 violation: 0.00037773511514543456 violation: 0.00036926722103784314 violation: 0.00036139377516849455 violation: 0.0003541104215953919 violation: 0.000346875301682097 violation: 0.0003399573430193335 violation: 0.0003336482920386987 violation: 0.0003283308869897798 violation: 0.00032373393031182295 violation: 0.0003189648006183863 violation: 0.0003148067171023186 violation: 0.00030605872659556415 violation: 0.00030086731966276877 violation: 0.00029721510914602824 violation: 0.0002929587578806185 violation: 0.0002902233645633245 violation: 0.0002878523913857171 violation: 0.00028450160118520117 violation: 0.00028144621499566957 violation: 0.00027827151414167907 violation: 0.00027581298865250747 violation: 0.00027315889220076093 violation: 0.00026861963246149187 violation: 0.00026739946951989446 violation: 0.0002660552511345655 violation: 0.0002643516772822293 violation: 0.0002619682942046704 violation: 0.00025991756860185047 violation: 0.0002582001127923777 violation: 0.00025504186692200533 violation: 0.0002519510636934312 violation: 0.00024989317218474444 violation: 0.0002473673635037919 violation: 0.0002455020053750209 violation: 0.00024456537591252255 violation: 0.00024314922358259676 violation: 0.0002416924877553776 violation: 0.00024020293548653282 violation: 0.0002387456441575096 violation: 0.00023668015611098806 violation: 0.00023500098434188463 violation: 0.00023374018033196556 violation: 0.00023269556249144082 violation: 0.00023159034365932682 violation: 0.00023053479018534154 violation: 0.0002284268677119379 violation: 0.0002275258744437841 violation: 0.0002263655300523255 violation: 0.00022534602329691992 violation: 0.00022481091263331393 violation: 0.0002238468414342713 violation: 0.00022204924991835978 violation: 0.00022097204900989429 violation: 0.0002195778813025691 violation: 0.0002183085845205513 violation: 0.00021693166135542996 violation: 0.00021500737791679697 violation: 0.00021383838885194052 violation: 0.00021321828593981587 violation: 0.00021186792248160306 violation: 0.00021101809537301362 violation: 0.00021015433023678393 violation: 0.00020944380913302696 violation: 0.00020754146620214421 violation: 0.00020656716707540164 violation: 0.0002059097563292371 violation: 0.00020526514469925656 violation: 0.00020459936817250846 violation: 0.00020386703832190586 violation: 0.00020344724832499345 violation: 0.0002029299030209613 violation: 0.00020255795323476027 violation: 0.00020237071380110045 violation: 0.00020220915630984835 violation: 0.0002020183092529636 violation: 0.00020197877159925103 violation: 0.00020164909655069285 violation: 0.00020098283617651108 violation: 0.00020057000961555305 violation: 0.00020031697055761114 violation: 0.0002000956188192834 violation: 0.00020017366196597435 violation: 0.0002000404243481933 violation: 0.0001996972988569716 violation: 0.00019961873007258023 violation: 0.00019760754210740804 violation: 0.00019675990292734424 violation: 0.00019604936637580557 violation: 0.00019529326142802856 violation: 0.0001951327814303422 violation: 0.00019503595926075745 violation: 0.00019486140039213324 violation: 0.0001943855234788091 violation: 0.00019430725243369944 violation: 0.0001938048831416383 violation: 0.00019388264817774706 violation: 0.00019393774136990254 violation: 0.00019394475531208936 violation: 0.00019444278985944642 violation: 0.00019473566114418042 violation: 0.000194941171524405 violation: 0.00019492697278148305 violation: 0.00019483312377529993 violation: 0.00019458612250188224 violation: 0.00019433762783132544 violation: 0.00019399211956087553 violation: 0.00019344280198663435 violation: 0.0001927989992206531 violation: 0.00019232659354775325 violation: 0.00019171056459214248 violation: 0.00019090458491266123 violation: 0.00019035568917318834 violation: 0.0001896651072209847 violation: 0.0001890938966505794 violation: 0.0001885632396417336 violation: 0.0001880167432382361 violation: 0.0001874621657097898 violation: 0.00018681470229347933 violation: 0.00018601614229075107 violation: 0.00018533551165468348 violation: 0.00018464004880998605 violation: 0.00018335679872048322 violation: 0.0001822727155298402 violation: 0.0001815738788446468 violation: 0.00018075608853581216 violation: 0.0001796346958119595 violation: 0.00017856733154394058 violation: 0.00017752564932213606 violation: 0.0001765122400093257 violation: 0.00017597095288799397 violation: 0.00017534459070859366 violation: 0.0001743770315538584 violation: 0.00017372349574700763 violation: 0.0001726429171866598 violation: 0.00017152608806192225 violation: 0.00017027363534538806 violation: 0.0001691368985609367 violation: 0.00016806360651771193 violation: 0.00016716379339870322 violation: 0.00016626891974245327 violation: 0.00016535595010234178 violation: 0.00016436060837342757 violation: 0.00016343978052803509 violation: 0.00016233544771072068 violation: 0.00016114151548567659 violation: 0.0001596038562284963

violation: 0.00015848991707879224 violation: 0.00015767968286166642 violation: 0.0001567228941127434 violation: 0.0001557327067357646 violation: 0.00015484407616172093 violation: 0.00015389126720684177 violation: 0.00015299841557831194 violation: 0.000152209944768211 violation: 0.00015126424025098972 violation: 0.00015051980433897504 violation: 0.00014958135289866597 violation: 0.00014873527645262627 violation: 0.00014801414499280115 violation: 0.00014711778941377626 violation: 0.0001464561106564992 violation: 0.00014524284000629688 violation: 0.0001441993096410555 violation: 0.00014317780377953745 violation: 0.00014239111079633336 violation: 0.00014171026660116304 violation: 0.00014113164699706057 violation: 0.00014065261903076914 violation: 0.00014012376517708288 violation: 0.00013947677647549618 violation: 0.00013896547530245205 violation: 0.00013856086096814156 violation: 0.00013808735423045197 violation: 0.00013754957360126438 violation: 0.0001372881482269671 violation: 0.00013693335252153128 violation: 0.0001363426808063565 violation: 0.00013579500697423228 violation: 0.00013541767686159524 violation: 0.00013504177097624885 violation: 0.0001346695868760007 violation: 0.00013425183498090633 violation: 0.00013369849823037245 violation: 0.0001334359364822611 violation: 0.00013321899081252184 violation: 0.00013314028081687444 violation: 0.00013321983240100838 violation: 0.00013257243091620256 violation: 0.00013236952850350335 violation: 0.0001322398959330609 violation: 0.00013204175704052565 violation: 0.00013201413233716804 violation: 0.00013238766664525433 violation: 0.00013221040287134954 violation: 0.00013166937957508667 violation: 0.00013106844966827503 violation: 0.00013060328335704136 violation: 0.00013030166029076652 violation: 0.00013011917338324704 violation: 0.00013000752619452113 violation: 0.00013037660989617038 violation: 0.00013017770096779928 violation: 0.00012992373573108982 violation: 0.0001297390818815286 violation: 0.00012931114910976987 violation: 0.00012896839506065948 violation: 0.00012910496809913108 violation: 0.00012921094986824452 violation: 0.00012921930702443243 violation: 0.00012939542925042343 violation: 0.00012959719411285593 violation: 0.0001296594093977291 violation: 0.00012947683370783454 violation: 0.00012968366985201054 violation: 0.00012972986472100837 violation: 0.00012984050560588484 violation: 0.00012966772885711833 violation: 0.00012964790995819618 violation: 0.00012965356118655466 violation: 0.00012946190026018483 violation: 0.00012935569738637963 violation: 0.00012945510120999327 violation: 0.0001297470250383389 violation: 0.0001303000094355032 violation: 0.00013046105406624016 violation: 0.00013080791687858573 violation: 0.0001315085145860125 violation: 0.00013196868806787069 violation: 0.00013240618436033863 violation: 0.000132794810299209 violation: 0.000133079343293987 violation: 0.0001330410528994564 violation: 0.0001333564795448265 violation: 0.00013358400503839395 violation: 0.0001336146736096596 violation: 0.00013342694472733853 violation: 0.00013336127846074995 violation: 0.00013323007828411237 violation: 0.00013320283856527854 violation: 0.00013294915952880246 violation: 0.0001330457633731801 violation: 0.00013304502259985207 violation: 0.00013275571417004802 violation: 0.0001318858108824086 violation: 0.00013172520702353638 violation: 0.0001316170323268093 violation: 0.00013105563232161007 violation: 0.00013032312772347658 violation: 0.00013003131651412005 violation: 0.00012973720378233806 violation: 0.0001292845357547563 violation: 0.00012891460292933397 violation: 0.00012853040256351973 violation: 0.0001284459256483586 violation: 0.00012807553941161716 violation: 0.00012760919708765153 violation: 0.0001273168621004605 violation: 0.00012700719616897188 violation: 0.00012670330147512057 violation: 0.00012635024744442133 violation: 0.00012602577750548473 violation: 0.00012567619090743447 violation: 0.00012532967981231273 violation: 0.0001250363237401324 violation: 0.00012473430095218905 violation: 0.00012437556370189658 violation: 0.00012408027391922827 violation: 0.00012377308678321205 violation: 0.00012341253583037943 violation: 0.00012297006530582376 violation: 0.00012266886619811954 violation: 0.0001223340060529698 violation: 0.0001220284112972847 violation: 0.00012178366664643479 violation: 0.00012149790759675722 violation: 0.00012128430192361708 violation: 0.00012090926645668062 violation: 0.00012065593557621982 violation: 0.00012038125626971141 violation: 0.0001202094631410268 violation: 0.00011997504657180223 violation: 0.00011965936960432531 violation: 0.0001195817218766747 violation: 0.00011959487722745453 violation: 0.00011937500698397274 violation: 0.00011917936174253856 violation: 0.00011905133289352314 violation: 0.0001189432256143155 violation: 0.00011886247666019603 violation: 0.0001187630745018924

violation: 0.00011863779878138066 violation: 0.0001183246678776806 violation: 0.00011831256067279968 violation: 0.00011831506285814726 violation: 0.0001182661699545628 violation: 0.00011809976271528624 violation: 0.00011802654432681158 violation: 0.00011811066623921699 violation: 0.00011802770842198514 violation: 0.00011793181506194074 violation: 0.00011787749907396532 violation: 0.00011780704207763008 violation: 0.00011763472425502143 violation: 0.00011799223101350968 violation: 0.00011787575701191278 violation: 0.00011751829515210013 violation: 0.00011743520979814978 violation: 0.00011715314132311972 violation: 0.0001169672407684028 violation: 0.00011678302495303588 violation: 0.00011662228016475324 violation: 0.0001164575831922925 violation: 0.00011626370494898773 violation: 0.00011611282208943533 violation: 0.00011601707036869638 violation: 0.00011584123650940679 violation: 0.0001157025447749587 violation: 0.00011564814284117516 violation: 0.00011565373830771702 violation: 0.00011569010645751152 violation: 0.00011560891087149276 violation: 0.00011543728909743764 violation: 0.00011527771893991003 violation: 0.00011501481626344177 violation: 0.00011489004089841334 violation: 0.00011476051257431393 violation: 0.00011459571917321296 violation: 0.00011446156826506874 violation: 0.0001142497328898823 violation: 0.00011400453480961702 violation: 0.00011376220476952039 violation: 0.00011342339686067686 violation: 0.0001131159706766515 violation: 0.00011291647624163866 violation: 0.00011243911690051634 violation: 0.00011221967260460139 violation: 0.00011195531732203191 violation: 0.00011165853400010571 violation: 0.00011144299282344261 violation: 0.00011123792562981561 violation: 0.00011105980730652981 violation: 0.00011092815323453345 violation: 0.00011084912583780216 violation: 0.00011066131303687335 violation: 0.00011045968860964283 violation: 0.00011017725333031826 violation: 0.00010984981384256787 violation: 0.00010962248662127491 violation: 0.00010942155178979839 violation: 0.00010923560958556218 violation: 0.00010908075595858733 violation: 0.00010895781318892518 violation: 0.0001088796043847106 violation: 0.00010878890955811974 violation: 0.00010857174112761494 violation: 0.00010835750351800646 violation: 0.00010822595576165581 violation: 0.00010809492851705961 violation: 0.0001079512452615907 violation: 0.00010767547166359753 violation: 0.00010744078959630728 violation: 0.0001071928457255301 violation: 0.00010691299753713961 violation: 0.00010661953265057088 violation: 0.00010633693827490721 violation: 0.00010605556984429274 violation: 0.00010583023835191906 violation: 0.00010561829646579356 violation: 0.00010533195934997365 violation: 0.00010497053829071802 violation: 0.00010460131428085328 violation: 0.00010425436708161393 violation: 0.00010391435273988114 violation: 0.00010349126300540587 violation: 0.00010313128272605646 violation: 0.00010283122207252228 violation: 0.00010252369483327408 violation: 0.00010222524380559169 violation: 0.00010192794884596724 violation: 0.00010165643006475742 violation: 0.00010143617287753535 violation: 0.00010124685845635797 violation: 0.0001010214837559125 violation: 0.00010073820546631556 violation: 0.00010056556909730763 violation: 0.00010042978430520254 violation: 0.00010024830973945044

violation: 0.00010001695788942446

violation: 9.977317881285299e-05

Converged at iteration 453

Initialization complete

Iteration 0, inertia 15.230433191612041.

Iteration 1, inertia 10.9258315256894.

Iteration 2, inertia 10.639470565383899.

Iteration 3, inertia 10.528642521125548.

Iteration 4, inertia 10.49028335070887.

Iteration 5, inertia 10.477188619846498.

Iteration 6, inertia 10.47458564596802.

Iteration 7, inertia 10.471592019888611.

Iteration 8, inertia 10.470625516653385.

Iteration 9, inertia 10.470470163609779.

Iteration 10, inertia 10.46966106578488.

Converged at iteration 10: strict convergence.

Initialization complete

Iteration 0, inertia 15.009376777337653.

Iteration 1, inertia 11.114539643525653.

Iteration 2, inertia 10.807156561335212.

Iteration 3, inertia 10.732447705374128.

Iteration 4, inertia 10.690543404298705.

Iteration 5, inertia 10.685056330699155.

Iteration 6, inertia 10.680159540909708.

Iteration 7, inertia 10.675850107280791.

Iteration 8, inertia 10.670904462728972.

Iteration 9, inertia 10.670686025168568.

Iteration 10, inertia 10.670592091054885.

Converged at iteration 10: strict convergence.

Initialization complete

Iteration 0, inertia 14.82893371288212.

Iteration 1, inertia 11.095889400341619.

Iteration 2, inertia 10.837225773680263.

Iteration 3, inertia 10.72533714195952.

Iteration 4, inertia 10.695704996499922.

Iteration 5, inertia 10.683764534125093.

Iteration 6, inertia 10.677641133131779.

Iteration 7, inertia 10.673018787027722.

Iteration 8, inertia 10.6678267310072.

Iteration 9, inertia 10.661600059548999.

Iteration 10, inertia 10.647241755416495.

Iteration 11, inertia 10.639391037872437.

Iteration 12, inertia 10.633035999037556.

Iteration 13, inertia 10.62475136760789.

Iteration 14, inertia 10.620813436743001.

Iteration 15, inertia 10.619613694648397.

Converged at iteration 15: strict convergence.

# Initialization complete

Iteration 0, inertia 14.95949764661044.

Iteration 1, inertia 10.98969721183126.

Iteration 2, inertia 10.563722378040026.

Iteration 3, inertia 10.40408102179357.

Iteration 4, inertia 10.339857425313262.

Iteration 5, inertia 10.289604476170322.

Iteration 6, inertia 10.27520232269998.

Iteration 7, inertia 10.267634294723901.

Iteration 8, inertia 10.262889573548652.

Iteration 9, inertia 10.260045837611397.

Iteration 10, inertia 10.259552663113249.

Converged at iteration 10: strict convergence.

#### Initialization complete

Iteration 0, inertia 14.860359549222512.

Iteration 1, inertia 10.91219585474904.

Iteration 2, inertia 10.558240549042553.

Iteration 3, inertia 10.505001725355132.

Iteration 4, inertia 10.476938330746375.

Iteration 5, inertia 10.472157681024022.

Iteration 6, inertia 10.469283066850469.

Iteration 7, inertia 10.467748662348393.

Iteration 8, inertia 10.467531814803465.

Iteration 9, inertia 10.466008999748816.

Iteration 10, inertia 10.464508698658001.

Converged at iteration 10: strict convergence.

#### Initialization complete

Iteration 0, inertia 14.808833593086847.

Iteration 1, inertia 10.983820260862624.

Iteration 2, inertia 10.59569782418625.

Iteration 3, inertia 10.51377043996034.

Iteration 4, inertia 10.474704081679281.

Iteration 5, inertia 10.462952288419686.

Iteration 6, inertia 10.442177960035295.

Iteration 7, inertia 10.43471167756422.

Iteration 8, inertia 10.432569309032122.

Iteration 9, inertia 10.432056151906025.

Converged at iteration 9: strict convergence.

#### Initialization complete

Iteration 0, inertia 14.897559864886855.

Iteration 1, inertia 10.889128488131165.

Iteration 2, inertia 10.593726156645307.

Iteration 3, inertia 10.494076369760258.

Iteration 4, inertia 10.438482780030728.

Iteration 5, inertia 10.418009395133478.

Iteration 6, inertia 10.409718662059557.

Iteration 7, inertia 10.401633909205117.

Iteration 8, inertia 10.386820928009971.

```
Iteration 9, inertia 10.368835273050383.
Iteration 10, inertia 10.357220627630419.
Iteration 11, inertia 10.35490405198269.
Iteration 12, inertia 10.354026729838246.
Iteration 13, inertia 10.352431047699083.
Iteration 14, inertia 10.351805063139743.
Iteration 15, inertia 10.35165003043074.
Iteration 16, inertia 10.3515589360542.
Converged at iteration 16: strict convergence.
Initialization complete
Iteration 0, inertia 14.839412663296933.
Iteration 1, inertia 10.777320064909642.
Iteration 2, inertia 10.528384851177165.
Iteration 3, inertia 10.395741626951729.
Iteration 4, inertia 10.358186967091925.
Iteration 5, inertia 10.341677786872328.
Iteration 6, inertia 10.337641539436644.
Iteration 7, inertia 10.33713330430263.
Converged at iteration 7: center shift 2.066732268015102e-07 within tolerance
7.003378491781546e-07.
Initialization complete
Iteration 0, inertia 15.294135782968407.
Iteration 1, inertia 10.76025287346923.
Iteration 2, inertia 10.4053572354922.
Iteration 3, inertia 10.3242926392241.
Iteration 4, inertia 10.265629006656292.
Iteration 5, inertia 10.237240611214919.
Iteration 6, inertia 10.220941558503846.
Iteration 7, inertia 10.220843675435697.
Iteration 8, inertia 10.220139449777594.
Iteration 9, inertia 10.219365602519915.
Converged at iteration 9: center shift 1.4452889134366685e-07 within tolerance
7.003378491781546e-07.
Initialization complete
Iteration 0, inertia 15.219164941410767.
Iteration 1, inertia 10.925257269966284.
Iteration 2, inertia 10.583533300151208.
Iteration 3, inertia 10.464389367271789.
Iteration 4, inertia 10.395482811418859.
Iteration 5, inertia 10.372666301479178.
Iteration 6, inertia 10.365475948058915.
Iteration 7, inertia 10.364014655396417.
Iteration 8, inertia 10.360559937464938.
Iteration 9, inertia 10.35733934303313.
Converged at iteration 9: strict convergence.
Calculated clusters.
(943,)
(1682,)
```

## 3 Visualizing user-topic mappings

```
[]: import time
     # For plotting
     import plotly.io as plt_io
     import plotly.graph_objects as go
[]: #PCA
     from sklearn.decomposition import PCA
     #TSNE
     from sklearn.manifold import TSNE
     #UMAP
     import umap
     #LDA
     from sklearn.discriminant_analysis import LinearDiscriminantAnalysis as LDA
    /Users/madisonthantu/miniforge3/envs/fairRS/lib/python3.8/site-
    packages/tqdm/auto.py:22: TqdmWarning: IProgress not found. Please update
    jupyter and ipywidgets. See
    https://ipywidgets.readthedocs.io/en/stable/user_install.html
      from .autonotebook import tqdm as notebook_tqdm
[]: def plot_2d(component1, component2):
         fig = go.Figure(data=go.Scatter(
             x = component1,
             y = component2,
             mode='markers',
             marker=dict(
                 size=20,
                 color=user_clusters, #set color equal to a variable
                 colorscale='Rainbow', # one of plotly colorscales
                 showscale=True,
                 line_width=1
             )
         ))
         fig.update_layout(margin=dict(__
      41=100, r=100, b=100, t=100), width=750, height=450)
         fig.layout.template = 'plotly_dark'
         fig.show()
[]: def plot_3d(component1, component2, component3):
         fig = go.Figure(data=[go.Scatter3d(
             x=component1,
             y=component2,
             z=component3,
```

```
mode='markers',
   marker=dict(
        size=10,
        color=user_clusters,  # set color to an array/list of_u

desired values
        colorscale='Rainbow', # choose a colorscale
        opacity=1,
        line_width=1
    )
)])
# tight layout
fig.update_layout(margin=dict(l=50,r=50,b=50,t=50),width=900,height=500)
fig.layout.template = 'plotly_dark'
fig.show()
```

```
[]: from sklearn.preprocessing import StandardScaler

## Standardizing the data

x = StandardScaler().fit_transform(actual_user_topic_mapping)
```

#### 3.0.1 PCA

Duration: 0.009582996368408203 seconds

```
[]: plot_2d(principalComponents[:, 0],principalComponents[:, 1])
```

#### 3.0.2 t-SNE

```
from sklearn.decomposition import TruncatedSVD

truncated_svd = TruncatedSVD(n_components=50)

X_svd = truncated_svd.fit_transform(x)

tsne = TSNE(random_state = 42, n_components=3, verbose=0, perplexity=40, using the print('Duration: {} seconds'.format(time.time() - start))
```

Duration: 2.1017019748687744 seconds

```
[]: plot_2d(tsne[:, 0],tsne[:, 1])
[]: plot_3d(tsne[:, 0],tsne[:, 1],tsne[:, 2])
    3.0.3 UMAP
[]: start = time.time()
     reducer = umap.UMAP(random_state=42,n_components=3)
     embedding = reducer.fit_transform(x)
     print('Duration: {} seconds'.format(time.time() - start))
    Duration: 3.2564289569854736 seconds
[]: plot_2d(reducer.embedding_[:, 0],reducer.embedding_[:, 1])
[]: plot_3d(reducer.embedding_[:, 0], reducer.embedding_[:, 1], reducer.embedding_[:, u
      ⇒2])
    3.0.4 LDA
[]: start = time.time()
     X_LDA = LDA(n_components=3).fit_transform(x, y=user_clusters)
     print('Duration: {} seconds'.format(time.time() - start))
     # from sklearn.decomposition import LatentDirichletAllocation
     # lda = LatentDirichletAllocation(n_components=3, random_state=0)
     \# lda_x = lda.fit_transform(x)
     # print('Duration: {} seconds'.format(time.time() - start))
    Duration: 0.07077908515930176 seconds
[]: plot_2d(X_LDA[:, 0], X_LDA[:, 1])
```

[]: plot\_3d(X\_LDA[:, 0], X\_LDA[:, 1], X\_LDA[:, 2])