Maly Projekt nr 4 – Permutacje

Jan Czechowski

zad 1.

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In[*]:= s5 := Permutations[Range[5]]
             lista permutacji
                             zakres
       commutativePairs = Select[Subsets[s5, {2}],
                              wybier... podzbiory
         PermutationProduct[#[1], #[2]] === PermutationProduct[#[2], #[1]] &]
         iloczyn permutacyjny
                                                      iloczyn permutacyjny
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\{\{5, 2, 3, 4, 1\}, \{5, 4, 3, 2, 1\}\}, \{\{5, 3, 4, 2, 1\}, \{5, 4, 2, 3, 1\}\}\}
```

```
In[ • ]:= s4 := Permutations[Range[4]]
              lista permutacji zakres
        NieparzystePermutacje := Select[s4, Signature[#] === -1&]
                                     wybierz wed··· podpis
       NieTranspozycja := Select[NieparzystePermutacje, Length[Cycles[#][1]]] > 1 &]
                             wybierz według kryterium
                                                                  długość cykle
        PermutacjaOdwrotna = {#, InversePermutation[#]} & /@ NieTranspozycja
                                     permutacja odwrotna
Out[•]=
        \{\{\{1, 2, 4, 3\}, \{1, 2, 4, 3\}\}, \{\{1, 3, 2, 4\}, \{1, 3, 2, 4\}\}, \{\{1, 4, 3, 2\}, \{1, 4, 3, 2\}\},
         \{\{2, 1, 3, 4\}, \{2, 1, 3, 4\}\}, \{\{2, 3, 4, 1\}, \{4, 1, 2, 3\}\}, \{\{2, 4, 1, 3\}, \{3, 1, 4, 2\}\},
         \{\{3, 1, 4, 2\}, \{2, 4, 1, 3\}\}, \{\{3, 2, 1, 4\}, \{3, 2, 1, 4\}\}, \{\{3, 4, 2, 1\}, \{4, 3, 1, 2\}\},
         \{\{4, 1, 2, 3\}, \{2, 3, 4, 1\}\}, \{\{4, 2, 3, 1\}, \{4, 2, 3, 1\}\}, \{\{4, 3, 1, 2\}, \{3, 4, 2, 1\}\}\}
```

zad 3.

```
In[15]:= n = 52;
      perm = Table[If[i \le 26, 2i, 2(i-26)-1], {i, 0, n-1}];
             tabela operator warunkowy
In[26]:= cycles = FindPermutationCycles[perm];
In[42]:= znak = Signature[perm];
             podpis
in[19]:= order = LCM@@ (Length /@ cycles);
              najmni… długość
In[20]:= inversions = Select[Subsets[Range[0, n - 1], {2}], perm[[#[1]] + 1]] > perm[[#[2]] + 1]] &];
                    wybier podzbiory zakres
In[24]:= modulo52 = Mod[#, 52] &;
                  modulo
```

In[43]:= {cycles, znak, order, inversions}

Out[43]=

```
{{1}, {2, 3, 5, 9, 17, 33, 12, 23, 45, 36, 18, 35, 16, 31, 8, 15, 29, 4, 7, 13, 25, 49, 44,
          34, 14, 27}, {6, 11, 21, 41, 28}, {10, 19, 37, 20, 39, 24, 47, 40, 26, 51, 48, 42, 30},
       \{22, 43, 32\}, \{38\}, \{46\}, \{50\}, \{52\}\}, 1, 390,
   \{\{1, 27\}, \{2, 27\}, \{2, 28\}, \{3, 27\}, \{3, 28\}, \{3, 29\}, \{4, 27\}, \{4, 28\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, \{4, 29\}, 
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       \{22, 42\}, \{22, 43\}, \{22, 44\}, \{22, 45\}, \{22, 46\}, \{22, 47\}, \{22, 48\}, \{23, 27\},
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       \{23, 44\}, \{23, 45\}, \{23, 46\}, \{23, 47\}, \{23, 48\}, \{23, 49\}, \{24, 27\}, \{24, 28\},
       \{24, 29\}, \{24, 30\}, \{24, 31\}, \{24, 32\}, \{24, 33\}, \{24, 34\}, \{24, 35\}, \{24, 36\},
       \{24, 37\}, \{24, 38\}, \{24, 39\}, \{24, 40\}, \{24, 41\}, \{24, 42\}, \{24, 43\}, \{24, 44\},
       \{24, 45\}, \{24, 46\}, \{24, 47\}, \{24, 48\}, \{24, 49\}, \{24, 50\}, \{25, 27\}, \{25, 28\},
       \{25, 29\}, \{25, 30\}, \{25, 31\}, \{25, 32\}, \{25, 33\}, \{25, 34\}, \{25, 35\}, \{25, 36\},
       \{25, 37\}, \{25, 38\}, \{25, 39\}, \{25, 40\}, \{25, 41\}, \{25, 42\}, \{25, 43\}, \{25, 44\},
       \{25, 45\}, \{25, 46\}, \{25, 47\}, \{25, 48\}, \{25, 49\}, \{25, 50\}, \{25, 51\}, \{26, 27\},
       {26, 28}, {26, 29}, {26, 30}, {26, 31}, {26, 32}, {26, 33}, {26, 34}, {26, 35},
       \{26, 36\}, \{26, 37\}, \{26, 38\}, \{26, 39\}, \{26, 40\}, \{26, 41\}, \{26, 42\}, \{26, 43\},
       \{26, 44\}, \{26, 45\}, \{26, 46\}, \{26, 47\}, \{26, 48\}, \{26, 49\}, \{26, 50\}, \{26, 51\}\}\}
```

zad 4.

```
In[*]:= permGroup := Permutations[{1, 2, 3, 4}]
                      lista permutacji
       bezPunktowStalychQ[perm_] := AllTrue[Range[4], # # perm[#]] &]
                                         wszystk… zakres
       derangements = Select[permGroup, bezPunktowStalychQ]
                        wybierz według kryterium
Out[0]=
        \{\{2, 1, 4, 3\}, \{2, 3, 4, 1\}, \{2, 4, 1, 3\}, \{3, 1, 4, 2\},
         \{3, 4, 1, 2\}, \{3, 4, 2, 1\}, \{4, 1, 2, 3\}, \{4, 3, 1, 2\}, \{4, 3, 2, 1\}\}
```

zad 5.

```
In[*]:= permGroup := Permutations[{1, 2, 3, 4}]
                      lista permutacji
        czyParzysta[perm_] := EvenQ[Length[PermutationCycles[perm]] - 1]
                                  liczba··· długość permutacje cykliczne
        permParzyste = Select[permGroup, czyParzysta]
                         wybierz według kryterium
Out[•]=
        \{\{1, 2, 3, 4\}, \{1, 2, 4, 3\}, \{1, 3, 2, 4\}, \{1, 3, 4, 2\}, \{1, 4, 2, 3\}, \{1, 4, 3, 2\},
         \{2, 1, 3, 4\}, \{2, 1, 4, 3\}, \{2, 3, 1, 4\}, \{2, 3, 4, 1\}, \{2, 4, 1, 3\}, \{2, 4, 3, 1\},
         \{3, 1, 2, 4\}, \{3, 1, 4, 2\}, \{3, 2, 1, 4\}, \{3, 2, 4, 1\}, \{3, 4, 1, 2\}, \{3, 4, 2, 1\},
         \{4, 1, 2, 3\}, \{4, 1, 3, 2\}, \{4, 2, 1, 3\}, \{4, 2, 3, 1\}, \{4, 3, 1, 2\}, \{4, 3, 2, 1\}\}
```

zad 6.

```
In[@]:= swap[perm_, i_] := Module[{newPerm}, newPerm = perm;
          newPerm[i] = perm[i + 1];
          newPerm[[i + 1]] = perm[[i]];
          newPerm]
       pi := \{1, 2, 3, 4, 5\}
       transpozycje = Table[swap[pi, i], {i, 1, Length[pi] - 1}]
                        tabela
                                                     długość
Out[ • 1=
       \{\{2, 1, 3, 4, 5\}, \{1, 3, 2, 4, 5\}, \{1, 2, 4, 3, 5\}, \{1, 2, 3, 5, 4\}\}
```

zad 7.

```
In[ \circ ] := obrot[k_, n_] := RotateLeft[Range[n], k]
                         cykliczne prz··· zakres
       odbicie[n_{-}] := Table[If[i \le Floor[n/2], n+1-i, i], \{i, 1, n\}]
                       tabela opera··· podłoga
       n1 = 3;
       symetrieTrojkata = Join[{obrot[0, n1], obrot[1, n1], obrot[2, n1]}, {odbicie[n1]}]
       n2 = 4;
       symetrieKwadratu = Join[{obrot[0, n2], obrot[1, n2], obrot[2, n2], obrot[3, n2]},
          {odbicie[n2], odbicie[n2]}]
       n3 = 6;
       symetrieSzescianu = Join[
          {obrot[0, n3], obrot[1, n3], obrot[2, n3], obrot[3, n3], obrot[4, n3], obrot[5, n3]},
          {odbicie[n3], odbicie[n3], odbicie[n3], odbicie[n3], odbicie[n3]}}
Out[•]=
       \{\{1, 2, 3\}, \{2, 3, 1\}, \{3, 1, 2\}, \{3, 2, 3\}\}
Out[ • ]=
       \{\{1, 2, 3, 4\}, \{2, 3, 4, 1\}, \{3, 4, 1, 2\}, \{4, 1, 2, 3\}, \{4, 3, 3, 4\}, \{4, 3, 3, 4\}\}
Out[•]=
       \{\{1, 2, 3, 4, 5, 6\}, \{2, 3, 4, 5, 6, 1\}, \{3, 4, 5, 6, 1, 2\}, \{4, 5, 6, 1, 2, 3\},
        \{5, 6, 1, 2, 3, 4\}, \{6, 1, 2, 3, 4, 5\}, \{6, 5, 4, 4, 5, 6\}, \{6, 5, 4, 4, 5, 6\},
        \{6, 5, 4, 4, 5, 6\}, \{6, 5, 4, 4, 5, 6\}, \{6, 5, 4, 4, 5, 6\}, \{6, 5, 4, 4, 5, 6\}\}\
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