

Decision entanglement complexity (draft)

Abstract. In this article we propose a quadratic source code complexity measure [Blo19] from the perspective of path testing with the conjecture of independent enclosed scopes, the measure enfolds elementary conditions, nested and cyclic formations.

1 Introduction

A Program consist of a sequences of instructions. The instructions can be categorized into syntax, logic and arithmetic determining the program control flow.

Software complexity is related with modularity, coupling and cohesion hence quality. 40% to 80% of software costs are emerging due to maintenance and approximatly 40% on fixing defects [SG11].

Analysing source code complexity helps to identify risk, finds potential defects to test critical functionality in detail, increase quality, cohesion and decrease maintainance [RB11].

2 Existing measures

Cyclomatic complexity (CC) has been widely discussed by various authors. The most used metric has been formulated by Thomas J. McCabe in 1976 [McC76].

$$m = e - n + 2 \quad (1)$$

Where, e = the amount of edges. n = the amount of nodes.

CC is linear in it's nature and correlation with lines of source code (LOC), which is why Graylin JAY et al. [al.09] are suggesting to implement LOC as complexity measure.

Mir Muhammd Suleman Sarwar et al. [MMSS13] are pointing out that it neither takes into account the difference between combined decisions, elementary conditions nor repeating structures. Their adaptation of CC includes loop iterations

$$V(G)^* = V(G) + \prod_{i=1}^n P_i$$

$$P_i = U_i - L_i + 1$$

Where, P_i = No. of iterations of i th loop. U_i = upper bound of i th loop. L_i = lower bound of i th loop and $V(G)^*$ = adjusted cyclomatic complexity for any control flow graph "G". The measure combines control flow and statements exercised.

Brian A. Nejme. NPATH [Nej88] TODO.

Tevfik et al. [LB15] are providing a reasonable complutable measure: asymptotic path complexity covering nested structures and loops in comparison with CC and NPATH. TODO

2.1 Test Coverage

Test coverage metrics are providing quantitative representation of tested structures. The approach is to maximize coverage while minimizing testing effort. Each condition branches the flow into two control sub-paths, and determines the progression of the programm. The path of an isolated decision d_j thereby is given due to decisions and conditions (MC/DC) [RB11]. Let's define a condition c_j and it's path $\gamma: C \times \Sigma \rightarrow C^*$

$$\Sigma = \{true, false\}$$

$$D \subseteq \{C^*, S, E\}, \quad d_h \in D, \quad d_h \mapsto \Sigma$$

The transition function *alpha*

$$\alpha: D \times \Sigma^* \rightarrow \Sigma \times D$$

The condition

$$C = \{c_0, c_1, c_2, c_3, \dots, c_n\}, c_i \mapsto \Sigma$$

$$\varepsilon: C \rightarrow \Sigma \times C$$

and the transition \vdash

$$\vdash \subseteq (\Sigma^* \times D \times \Sigma) \times (\Sigma^* \times D \times \Sigma)$$

The possible combinations of conditions on γ are arising through c_j 's preceeding and succeeding condition flow. An acyclic transition path through c_j is described due to passing each condition once

$$B_{\lambda j}^T = (v_h, d_h, b_h), \dots \vdash (v_k, d_k, b_k) \vdash^* (v_m, d_m, b_m)$$

$$= (c_i, b_i), \dots \vdash (c_j, b_j) \vdash^* (c_m, b_m)$$

where

$$\alpha(d_m, v_m) \mapsto E$$

with the jacket

$$B_\lambda = (b_h, v_h, d_h) \vdash^* (b_m, v_m, d_m)$$

3 Hypothesis acyclic complexity

Instead of combining arithmetic and logic we propose a metric [Blo19] reflecting the logical test effort of path testing. The concept of basic paths described by [McC76] neglects loops and nesting. 100% sub-path combination coverage q is intricate due to exponential effort (Table 1). Conditions are providing the logical structure of programs (Listing 1-16). Loops and recursions are construed due to their boundary [RB11] and invariant, which is why their quantitative iteration increases probability of condition coverage not condition path length. Let's define the inductive start of independent

$$\begin{aligned} \alpha_i = & (c_0, true) \rightarrow (c_1), (c_0, false) \rightarrow (c_1), \\ & (c_1, true) \rightarrow (E), (c_1, false) \rightarrow (E) \end{aligned}$$

and dependent branches

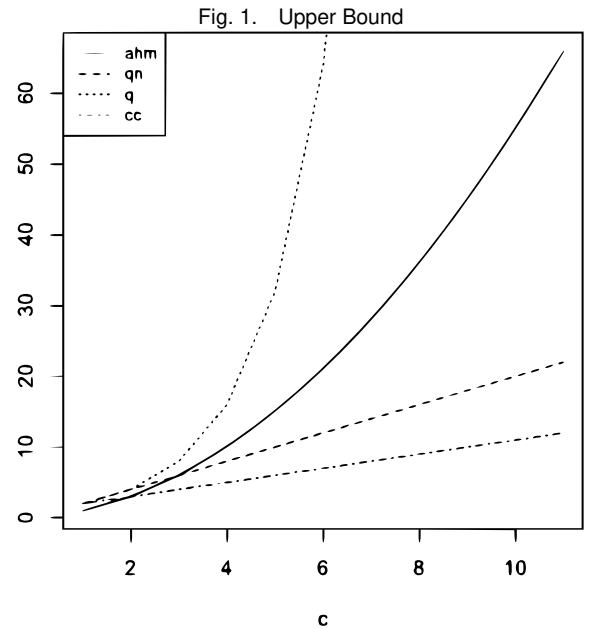
$$\begin{aligned} \alpha_d = & (c_0, true) \rightarrow (E), (c_0, false) \rightarrow (c_1), \\ & (c_1, true) \rightarrow (E), (c_1, false) \rightarrow (E) \end{aligned}$$

Isolated condition paths are $\log(2^n)$ subset of all q paths. The spanning tree of the first branch expands four leaves, the latter three.

Nesting is diminishing the amount of paths, the effort of combinatorial parameter testing is unaffected. The fallacy of subjective perceived complexity increases contrary due to remembering previous conditions (Table 2).

Table 1. Condition formation bound

| $ C $ | $O(n)$ m | $O(2n)$ q_2 | $O(n^2)$ m_{ah} | $O(2^n)$ q | $O(4^{n-1})$ $P(n)$ |
|-------|---------------|------------------|------------------------|--------------------|------------------------|
| 1 | 2 | 2 – 2 | $\frac{1}{2} - 1$ | 2 – 2 | 1 |
| 2 | 3 | 3 – 4 | 1 – 3 | 3 – 4 | 4 |
| 3 | 4 | 4 – 6 | $\frac{3}{2} - 6$ | 4 – 8 | 16 |
| 4 | 5 | 5 – 8 | 2 – 10 | 5 – 16 | 64 |
| 5 | 6 | 6 – 10 | $2\frac{1}{2} - 15$ | 6 – 32 | 256 |
| 6 | 7 | 7 – 12 | 3 – 21 | 7 – 64 | 1024 |
| 7 | 8 | 8 – 14 | $3\frac{1}{2} - 28$ | 8 – 128 | 4096 |
| ... | | | | | |
| 9 | 10 | 10 – 18 | $4\frac{1}{4} - 45$ | 10 – 512 | 65536 |
| ... | | | | | |
| 19 | 20 | 20 – 38 | $9\frac{1}{2} - 190$ | 20 – 524288 | $6.87 * 10^7$ |
| ... | | | | | |
| 49 | 50 | 50 – 98 | $24\frac{1}{2} - 1225$ | $50 - 5 * 10^{14}$ | $7.92 * 10^{27}$ |



Listing 1. plain singular
if ($-1 < 1$) { }

$$\hat{u}_0 = 1$$

Listing 2. orthogonal dual
if ($3 > 1 \ \&\& \ 0 < k$) { }

$$\hat{u}_1 = 1\frac{1}{2}$$

Listing 3. tertiary orthogonal
if ($2 > 1 \ \&\& \ 7 > k \ \&\& \ 10 > n$) { }

$$\hat{u}_2 = 1\frac{5}{6}$$

Listing 4. orthogonal dual
if ($2 > 1 \ || \ 0 < k$) { }

$$\hat{u}_1 = 2$$

Listing 5. orthogonal dual nested
if ($0 < 1$) {
 ...
if ($2 > k$) { }
 ...
}

$$\hat{u}_0 = 1$$

$$\hat{u}_1 = 2$$

Listing 6. tertiary orthogonal nested
if ($0 < 1 \ \&\& \ 4 > k$) {
 ...
if ($11 > n$) { }
 ...
}

$$\hat{u}_1 = 1\frac{1}{2}$$

$$\hat{u}_2 = 2\frac{1}{2}$$

Listing 7. tertiary
if ($2 > 1 \ \&\& \ 0 < k \ || \ 4 > n$) { }

$$\hat{u}_2 = 2\frac{1}{2}$$

Listing 8. tertiary parallel
if ($0 < 1 \ || \ 9 > k \ \&\& \ 1 < n$) { }

$$\hat{u}_2 = 2\frac{1}{2}$$

Listing 9. parallel
if ($2 > 1$) { }
 ...
if ($8 > k$) { }

$$\hat{u}_0 = 1$$

$$\hat{u}_1 = 3$$

Listing 10. tertiary parallel identical scope
if ($2 > 1 \ || \ 0 < k \ || \ 4 > n$) { }

$$\hat{u}_2 = 3$$

Listing 11. tertiary orthogonal nested
if ($2 > 1$) {

$$\hat{u}_0 = 1$$

...
if ($8 > k$) {
 ...
if ($0 < n$) { }
 ...
}

$$\hat{u}_1 = 2$$

$$\hat{u}_2 = 3$$

Listing 12. singular nested parallel

if ($0 < 1$) {
 ...
if ($4 > k$) { }
 ...
if ($8 > n$) { }
 ...
}

$$\hat{u}_0 = 1$$

$$\hat{u}_1 = 2$$

$$\hat{u}_2 = 4$$

Listing 13. orthogonal singular parallel

if ($0 < 1$) {
 ...
if ($8 > k$) { }
 ...
}

$$\hat{u}_0 = 1$$

$$\hat{u}_1 = 2$$

if ($0 < n$) { }

$$\hat{u}_2 = 4$$

Listing 14. dual parallel

if ($0 < 1$) { }
 ...
if ($9 > k \ \&\& \ 1 < n$) { }

$$\hat{u}_0 = 1$$

$$\hat{u}_2 = 4$$

Listing 15. dual parallel

if ($0 < 1$) { }
 ...
if ($9 > k$) {
 ...
if ($1 < n$) { }
}

$$\hat{u}_0 = 1$$

$$\hat{u}_1 = 3$$

$$\hat{u}_2 = 4$$

Listing 16. tertiary parallel different scope

if ($-4 < 1$) { }
 ...
if ($4 < k$) { }
 ...
if ($8 > n$) { }

$$\hat{u}_0 = 1$$

$$\hat{u}_1 = 3$$

$$\hat{u}_2 = 6$$

| Listing | $ C $ | loc | m | q_2 | m_{ah} | q |
|---------|-------|-----|---|-------|----------------|---|
| 1 | 1 | 1 | 2 | 1 | 1 | 2 |
| 2 | 2 | 1 | 3 | 3 | $1\frac{1}{2}$ | 3 |
| 3 | 3 | 1 | 4 | 5 | $1\frac{5}{6}$ | 4 |
| 4 | 2 | 1 | 3 | 3 | 2 | 3 |
| 5 | 2 | 5 | 3 | 3 | 2 | 3 |
| 6 | 3 | 5 | 4 | 5 | $2\frac{1}{2}$ | 4 |
| 7 | 3 | 1 | 4 | 5 | $2\frac{1}{2}$ | 4 |
| 8 | 4 | 1 | 4 | 5 | $2\frac{1}{2}$ | 4 |
| 9 | 2 | 3 | 3 | 2 | 3 | 4 |
| 10 | 3 | 1 | 4 | 5 | 3 | 4 |
| 11 | 3 | 8 | 4 | 5 | 3 | 4 |
| 12 | 3 | 7 | 4 | 4 | 4 | 5 |
| 13 | 3 | 6 | 4 | 4 | 4 | 6 |
| 14 | 3 | 4 | 4 | 4 | 4 | 6 |
| 15 | 3 | 6 | 4 | 4 | 4 | 6 |
| 16 | 3 | 5 | 4 | 3 | 6 | 8 |

Fig. 3. cc/m_{ah}

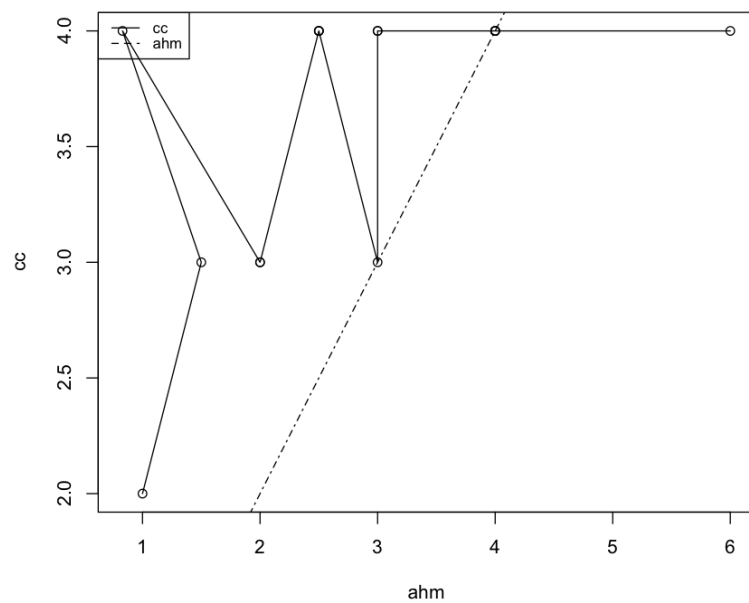


Fig. 4. loc/m_{ah}

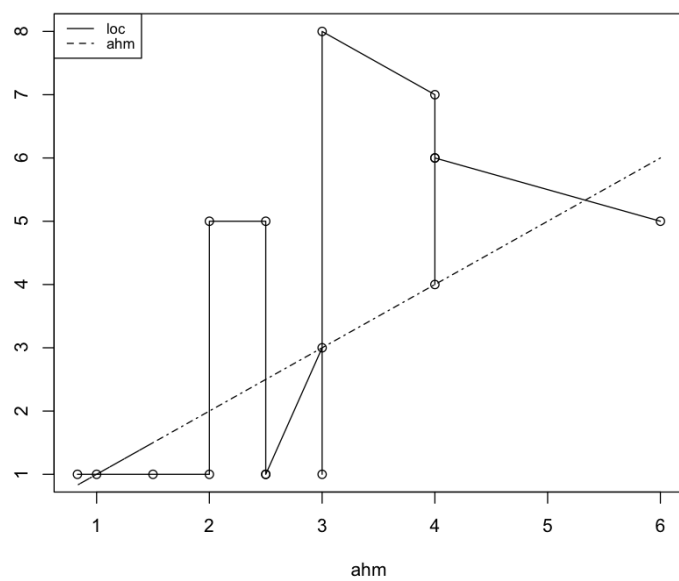
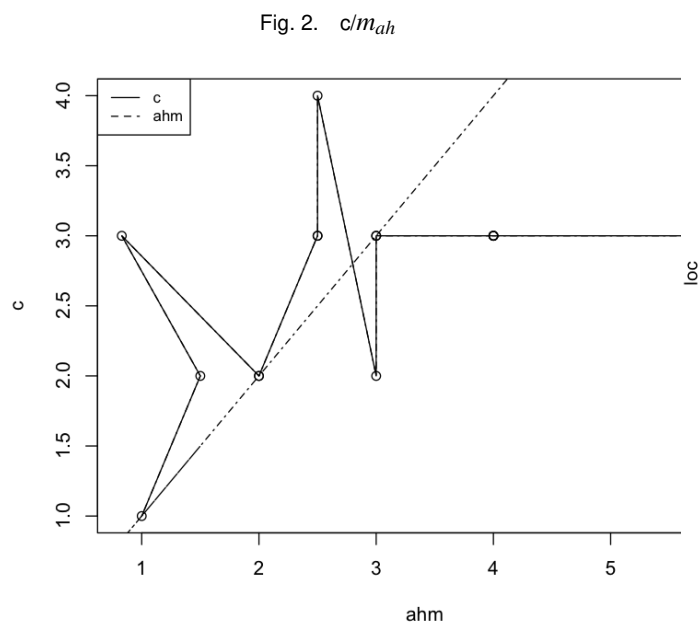


Fig. 5. q/m_{ah}

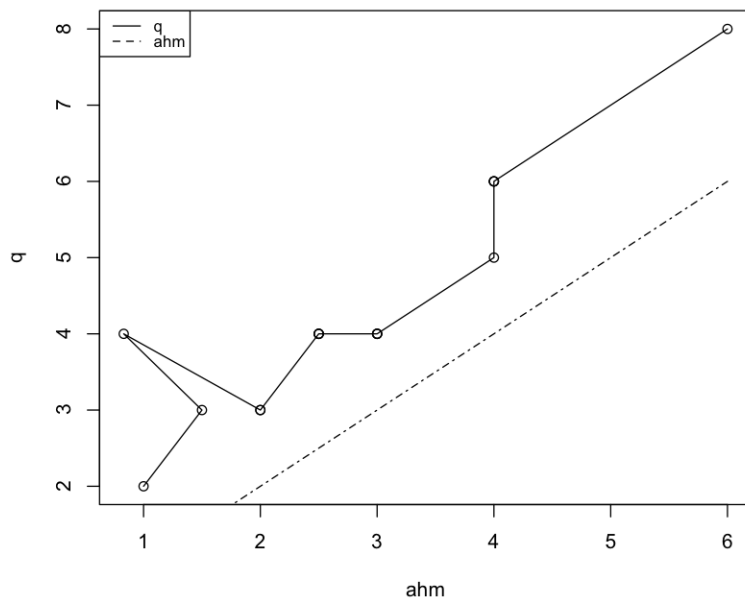


Fig. 6. q_2/m_{ah}

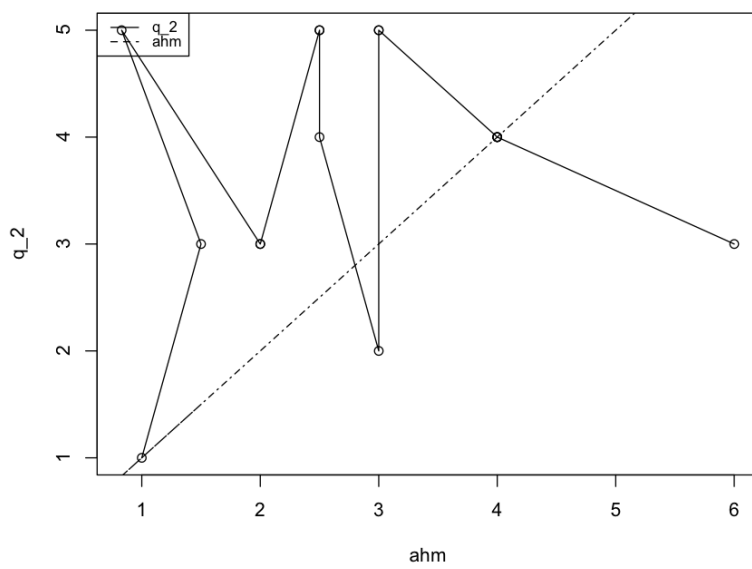


Table 3. α_i flow matrix, $q_2(\alpha_i) = 2$

| | s | c_0 | c_1 | e |
|-------|---|-------|-------|-------|
| s | | t | | |
| c_0 | | | (t,f) | |
| c_1 | | | | (t,f) |
| e | | | | |

Table 4. α_d flow matrix, $q_2(\alpha_d) = 3$

| | s | c_0 | c_1 | e |
|-------|---|-------|-------|-------|
| s | | t | | |
| c_0 | | | f | t |
| c_1 | | | | (t,f) |
| e | | | | |

The exponential amount of condition path combinations q is parsed into control flow q_2 .

$$\begin{aligned} n &= |C|, \quad n \in N \\ 2^n &\leq q \leq n + 1 \end{aligned} \quad (2)$$

When every condition is isolated the amount of condensed edges (enclosed scope paths) q_2 in the condition flow matrix represents an intuitive measure (Table 2, 1, 3, 4).

The lower and upper bounds of possible isolated condensed condition paths are

$$2 * n \geq q_2 \geq n + 1 \quad (3)$$

$$C_e \subset C; \quad m_u = |C_e| + n$$

with $C_e \subset C$ nested conditions. The metric m_u is undifferentiated regarding condition formation. Subpath combinations caused from parallel decision scope (flat-style) are neglected, as well as the subjective perception of condition memory, therefore we define the nesting function $\varphi(c_i)$

$$\begin{aligned} \frac{n}{2} &< m_{ah} \leq \frac{n(n+1)}{2} \\ m_{ah} &= \sum_{i=0}^n \varphi(c_i) = \sum_{i=0}^n \frac{r_i}{e_i} = \hat{u}_n \end{aligned} \quad (4)$$

Table 5. Complexity Risk [Cha05]

| m_{ah} | risk |
|----------|--------------------------|
| 1-21 | basic program |
| 22-45 | intricate, moderate risk |
| 45- | circuitous, high risk |

References

- [al.09] AL., Graylin J.: Cyclomatic Complexity and Lines of Code: Empirical Evidence of a Stable Linear Relationship. In: . *Software Engineering & Applications 2* (2009), June, S. 137–143
- [Blo19] BLOEMENDAL, Jannis: ahm, decision entanglement complexity. (2019), April, NL Rotterdam. – <http://github.com/jbloemendal/ahm>
- [Cha05] CHARNEY, Reg.: Programming Tools: Code Complexity Metrics. In: *Linux Journal* (2005), January
- [LB15] LUCAS BANG, Tevfik B. Abdalbaki Aydin A. Abdalbaki Aydin: Automatically computing path complexity of programs. In: *ESEC/SIGSOFT FSE 2015* (2015), S. 61–72
- [McC76] MCCABE, Thomas J.: A complexity measure. In: *IEEE* (1976), Dec, Nr. 4, S. 308–320
- [MMSS13] MIR MUHAMMD SULEMAN SARWAR, Ibrar A. Sara Shahzad S. Sara Shahzad: Cyclomatic Complexity. In: *IEEE* 1 (2013), Jan, Nr. 5, S. 274–279
- [Nej88] NEJMEH, Brian A.: NPATH: A Measure of Execution Path Complexity and Its Application. In: *ACM* 31(2) (1988), S. 188–200
- [RB11] REX BLACK, Jamie M.: *Advanced Software Testing Vol. 3*. Santa Barbara, CA : rookynook, 2011
- [SG11] SOUMIN GHOSH, Prof. (Dr.) Ajay R. Sanjay Kumar Dubey D. Sanjay Kumar Dubey: Comparative Study of the Factors that Affect Maintainability. In: *International Journal on Computer Science and Engineering (IJCSSE)* 3 (2011), Dec, Nr. 12, S. 3763–3769