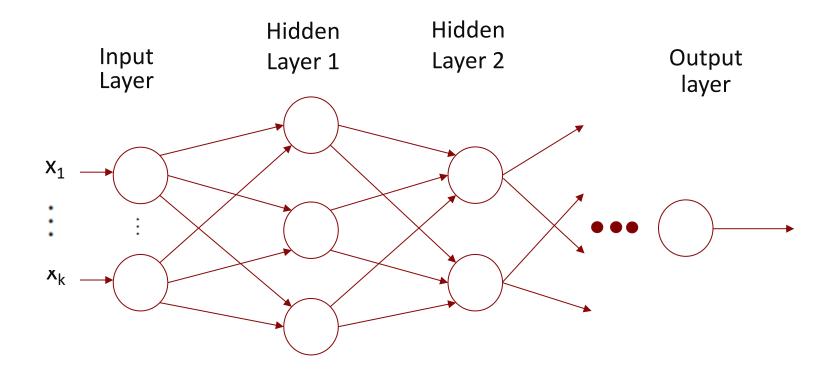
## Lecture 2: Training Deep Neural Networks



15.S04: Hands-on Deep Learning Spring 2024

Farias, Ramakrishnan

## Recap: Designing a DNN



<u>User</u> chooses the # of hidden layers, # units in each layer, the activation function(s) for the hidden layers and for the output layer

### Application: Predicting heart disease

## Predicting Heart Disease

Using a dataset of patients made available by the Cleveland Clinic, we will build our first NN model to predict if a patient has been diagnosed with heart disease from demographics

and bio-markers

Column	Description	Feature Type
Age	Age in years	Numerical
Sex	(1 = male; 0 = female)	Categorical
CP	Chest pain type (0, 1, 2, 3, 4)	Categorical
Trestbpd	Resting blood pressure (in mm Hg on admission)	Numerical
Chol	Serum cholesterol in mg/dl	Numerical
FBS	fasting blood sugar in 120 mg/dl (1 = true; 0 = false)	Categorical
RestECG	Resting electrocardiogram results (0, 1, 2)	Categorical
Thalach	Maximum heart rate achieved	Numerical
Exang	Exercise induced angina (1 = yes; 0 = no)	Categorical
Oldpeak	ST depression induced by exercise relative to rest	Numerical
Slope	Slope of the peak exercise ST segment	Numerical
CA	Number of major vessels (0-3) colored by fluoroscopy	Both numerical & categorical
Thal	3 = normal; 6 = fixed defect; 7 = reversible defect	Categorical
Target	Diagnosis of heart disease (1 = true; 0 = false)	Target

What we want to predict <u></u>

### Let's design our NN

- We design i.e., "lay out" the network
  - Choose the number of hidden layers and the number of 'neurons' in each layer
  - Pick the right output layer based on the type of the output

### Let's design our NN

- We design i.e., "lay out" the network
  - Choose the number of hidden layers and the number of 'neurons' in each layer 1 hidden layer with 16 ReLU neurons
  - Pick the *right output layer* based on the type of the output
     Sigmoid

#### Input Layer







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There are only 13 input variables but some of them are categorical so we one-hot-encode them, resulting in 29 inputs (details in colab).

Input Layer







Hidden layer (16 units)

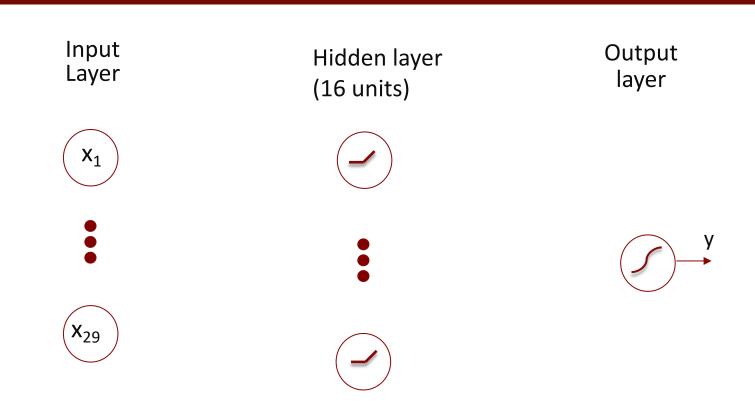




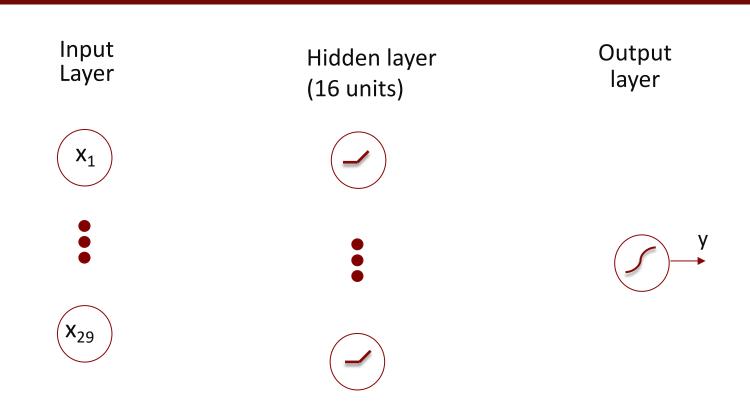


Output layer





How many parameters (i.e., weights and biases) does this network have?



How many parameters (i.e., weights and biases) does this network have? 29 \* 16 + 16 \* 1 + 1 = 497

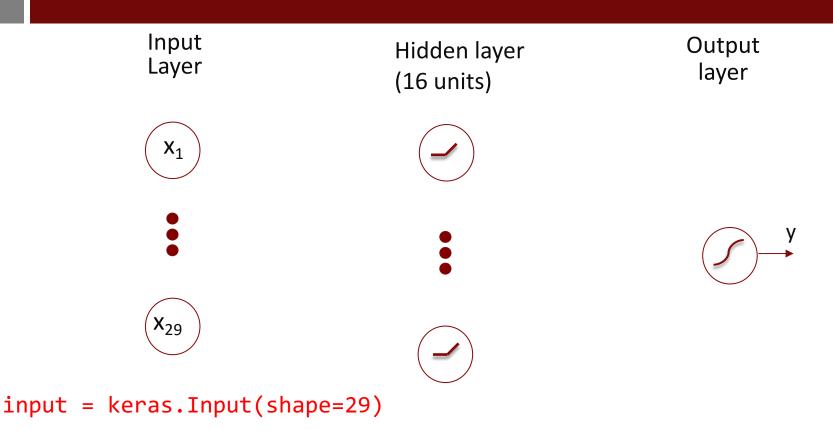
We will now "translate" this network into Keras code to demonstrate how easy it is.

We will give a fuller intro to Keras/Tensorflow <u>and</u> train this model in Colab soon.

# Typically, we define each layer from left to right

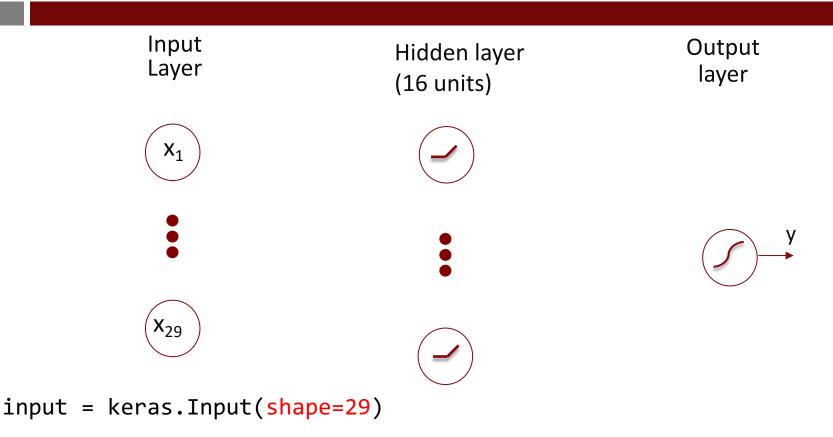
Input Output Hidden layer Layer layer (16 units)  $X_1$ **X**<sub>29</sub>

### Let's start with the input layer



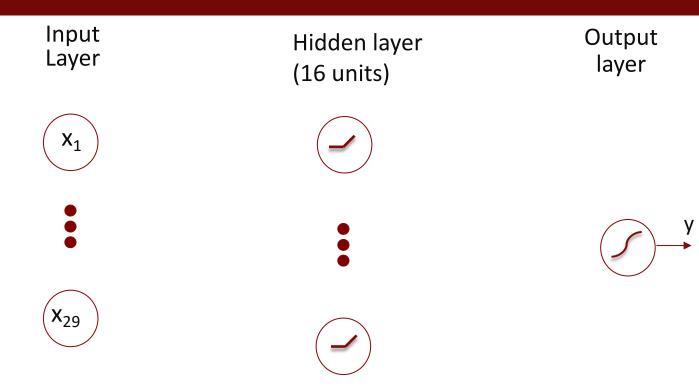
13

### We specify the shape of the input



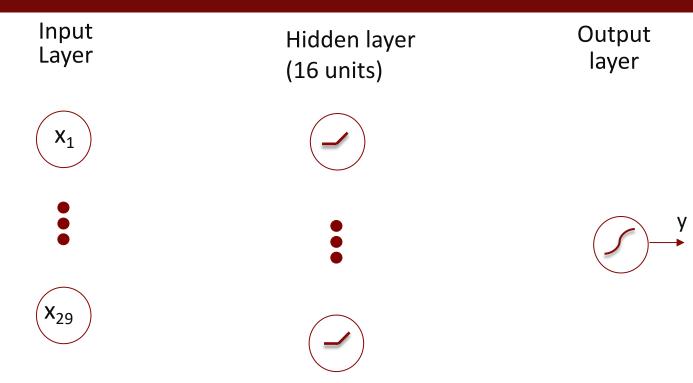
14

### Next, we define the hidden layer



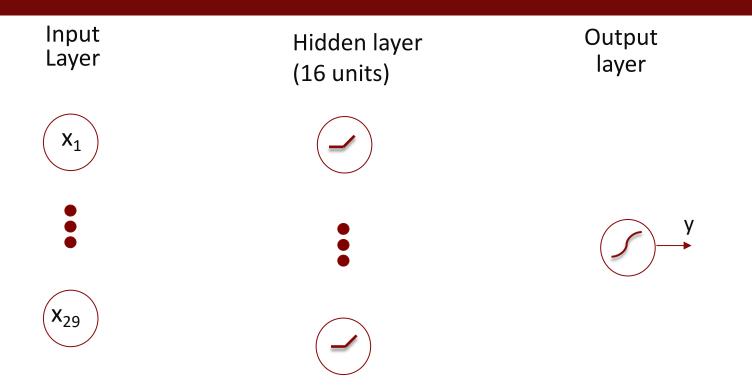
input = keras.Input(shape=29)

# Since this layer is fully connected to the previous and later layers, we use 'Dense'



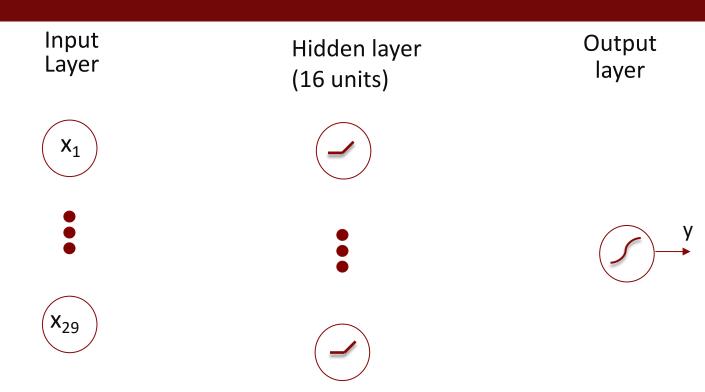
input = keras.Input(shape=29)

# We specify the number of neurons we want in this layer ...



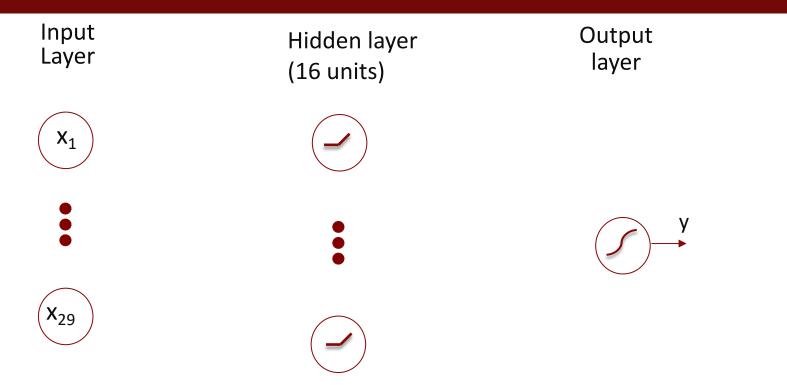
input = keras.Input(shape=29)

#### ... and the activation function



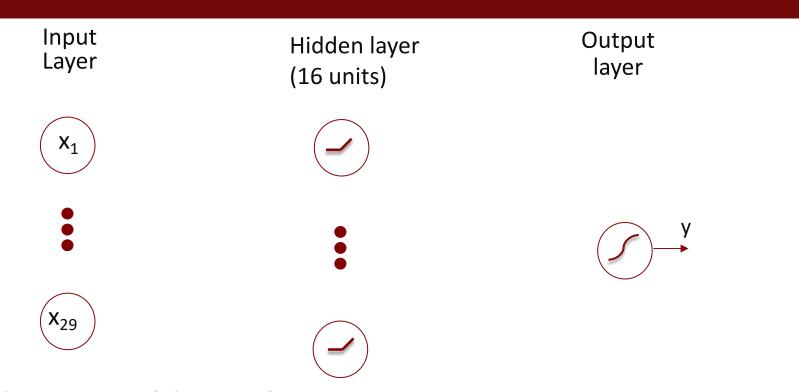
input = keras.Input(shape=29)

### Next, we "feed" the input to this layer ...



input = keras.Input(shape=29)

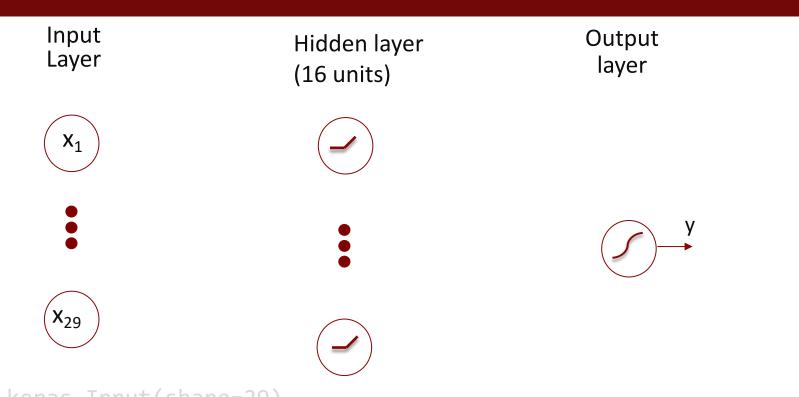
#### ... and give a name to the output of this layer



input = keras.Input(shape=29)

h = keras.layers.Dense(16, activation="relu")(input)

### Finally, we come to the output layer

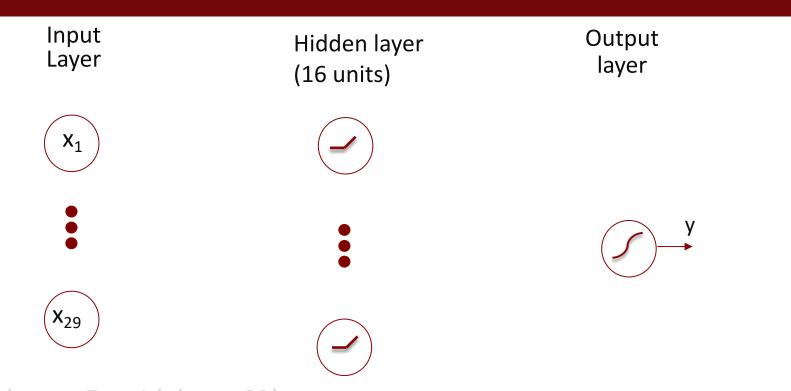


input = keras.Input(shape=29)

h = keras.layers.Dense(16, activation="relu")(input)

keras.layers.Dense(1, activation="sigmoid")

#### We have just one unit in this layer ...

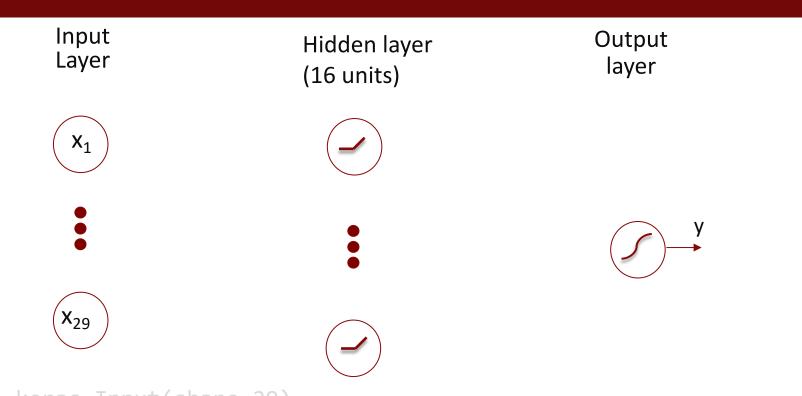


input = keras.Input(shape=29)

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keras.layers.Dense(1, activation="sigmoid")

## ... and indicate that we need a sigmoid activation function

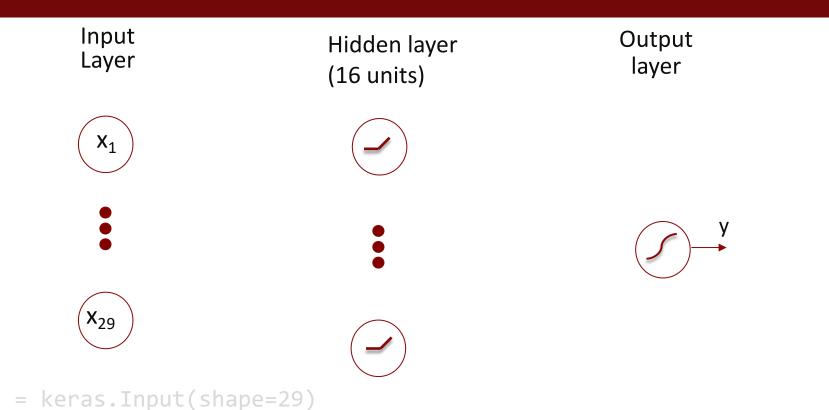


input = keras.Input(shape=29)

h = keras.layers.Dense(16, activation="relu")(input)

keras.layers.Dense(1, activation="sigmoid")

As we did before, we "feed" the output of the hidden layer to this layer ...

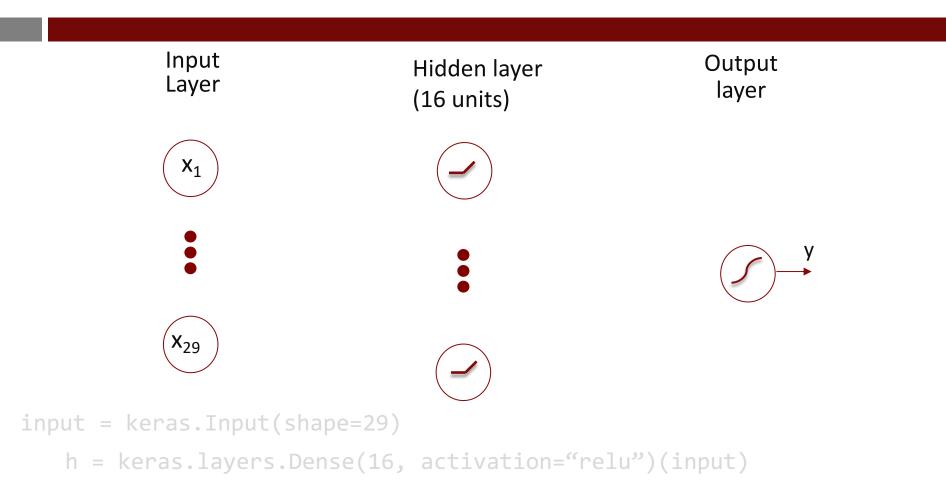


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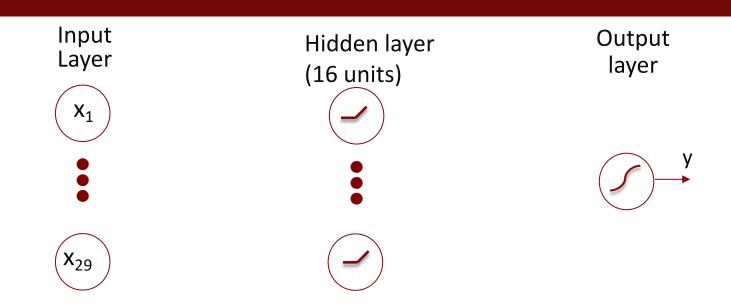
### ... and give the output of this layer a name.



output = keras.layers.Dense(1, activation="sigmoid")(h)

25

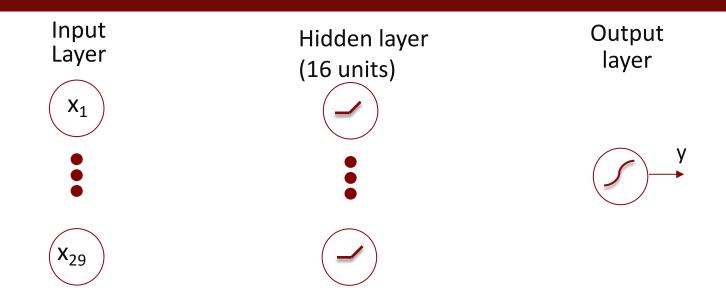
#### We have defined and connected the layers



```
input = keras.Input(shape=29)
h = keras.layers.Dense(16, activation="relu")(input)
output = keras.layers.Dense(1, activation="sigmoid")(h)
```

#### We have defined and connected the layers.

#### The final step is to formally define a model.



```
input = keras.Input(shape=29)
h = keras.layers.Dense(16, activation="relu")(input)
output = keras.layers.Dense(1, activation="sigmoid")(h)
model = keras.Model(input, output)
```

#### That's it!

#### A Neural Model for Heart Disease Prediction

```
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output = keras.layers.Dense(1, activation="sigmoid")(h)
model = keras.Model(input, output)
```

We will show how to train this model with real data and use it for prediction after we cover some *conceptual* building blocks

### Training a Deep Neural Network

## Recap: Training Linear and Logistic Regression Models

#### **Linear Regression**

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + ... + \beta_n x_n$$

+ Data



$$y = 2.8 + 0.89x_1 - 3.9x_2 + \dots + 1.06x_n$$

## Recap: Training Linear and Logistic Regression Models

#### **Linear Regression**

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$$y = 2.8 + 0.89x_1 - 3.9x_2 + \dots + 1.06x_n$$

#### **Logistic Regression**

$$y = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)}}$$

+ Data



$$y = \frac{1}{1 + e^{-(2.8 + 0.89x_1 - 3.9x_2 + \dots + 1.06x_n)}}$$

## Recap: Training Linear and Logistic Regression Models

#### **Linear Regression**

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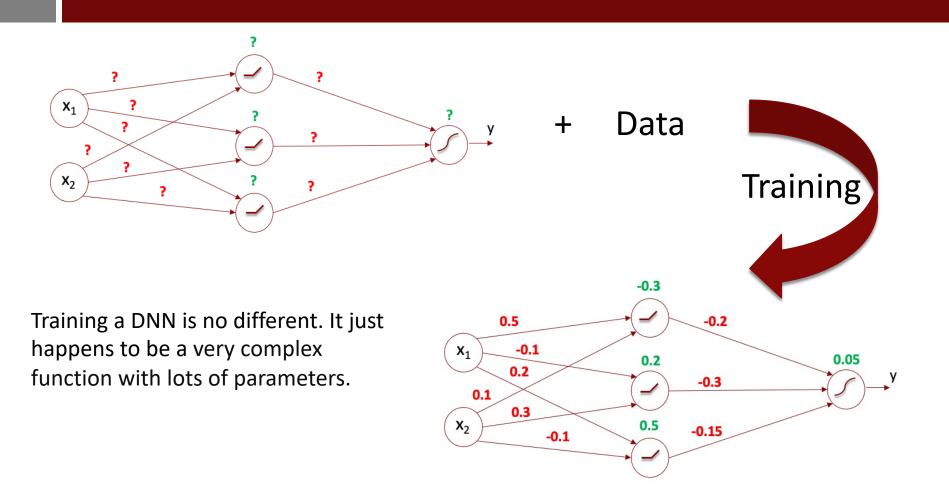


$$y = \frac{1}{1 + e^{-(2.8 + 0.89x_1 - 3.9x_2 + \dots + 1.06x_n)}}$$

#### Recall

- Training is finding values for the weights/coefficients so that the model's predictions come as close to the actual values as possible
- 'lm' and 'glm' use optimization algorithms under the hood to find these "best" values

## Training a DNN



The essence of training is to find the "best" values for the weights and biases i.e., those that minimize a function that measures the discrepancy between the actual and predicted values

These functions are called loss functions in the DL world

#### Loss Functions

#### Loss functions

- A "loss function" is a function that quantifies the error in a model's prediction.
  - If the predictions are close to the actual values, the "loss" would be \_\_\_\_\_.
  - A perfect model would have a loss of \_\_\_\_\_\_.

#### Loss functions

- A "loss function" is a function that quantifies the error in a model's prediction.
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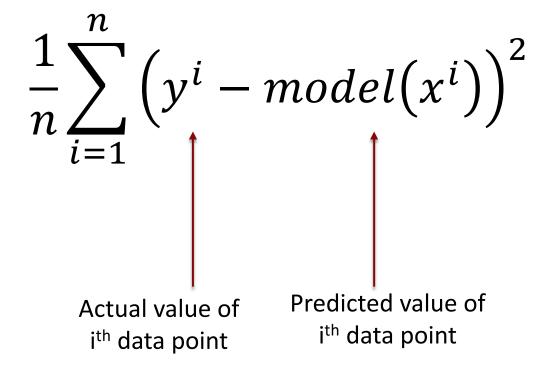
#### Loss functions

- A "loss function" is a function that quantifies the error in a model's prediction.
  - If the predictions are close to the actual values, the "loss" would be small.
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- In linear regression, you will recall that we quantify this error using "sum of squared errors". So, "sum of squared errors" is the loss function used in linear regression

#### Loss functions

- A "loss function" is a function that quantifies the error in a model's prediction.
  - If the predictions are close to the actual values, the "loss" would be small.
  - A perfect model would have a loss of zero.
- In linear regression, you will recall that we quantify this error using "sum of squared errors". So, "sum of squared errors" is the loss function used in linear regression
- The loss function we chose must be matched well with the kind of output that comes out of the model.

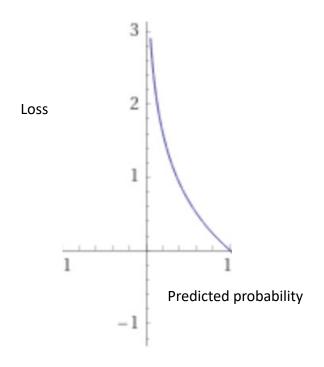
## Mean Squared Error (MSE) Loss is commonly used for general numerical outputs



In the Heart Disease Prediction Model the prediction is a probability number and the actual output is 0-1.

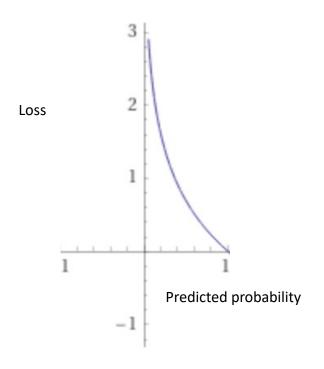
What is a good loss function in this situation?

For data points with y = 1 (i.e., patients with heart disease), lower predicted probabilities should have higher loss



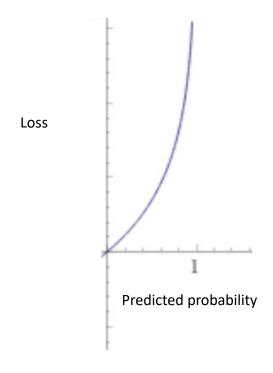
For data points with y = 1

#### We can capture this requirement using the log function



Predicted probability	-log(predicted probability)
1/1000	9.97
1/10	3.32
1/2	1.0
1	0.0

For data points with y = 1, loss = -log(predicted probability) For data points with y = 0 (i.e., patients <u>without</u> heart disease), <u>higher</u> predicted probabilities should have <u>higher</u> loss



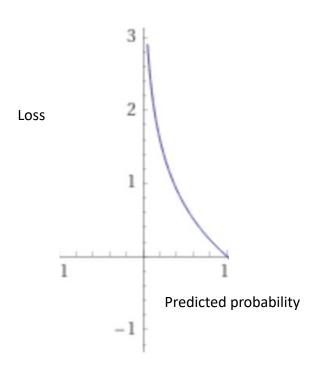
For data points with y = 0

## We can capture this requirement as well using the log function

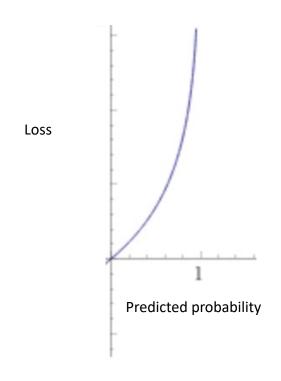
Predicted probability	-log(1 - predicted probability)		
1/1000	0.001	Loss	
1/10	0.15		
1/2	1.0		
0.999999	19.93		/
			Predicted probability

For data points with y = 0, loss = -log(1 - predicted probability)

#### Summary

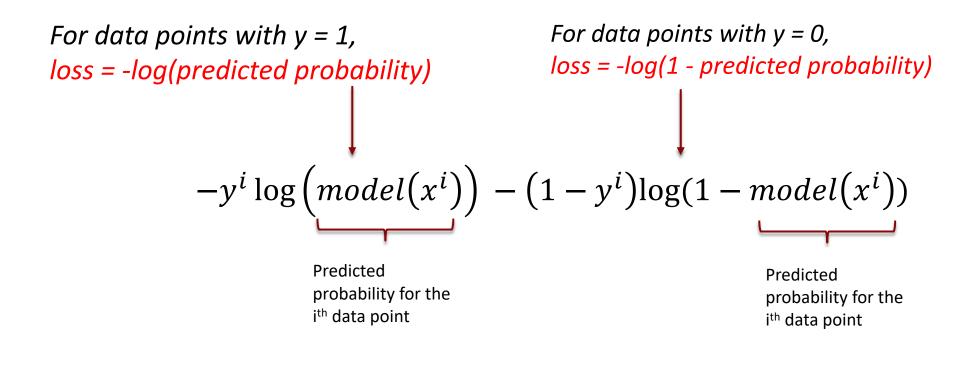


For data points with y = 1, loss = -log(predicted probability)



For data points with y = 0, loss = -log(1 - predicted probability)

## This can be compactly written as a single expression



We can now average this across all *n* data points

$$\frac{1}{n}\sum_{i=1}^{n} -y^{i}\log\left(model(x^{i})\right) - (1-y^{i})\log(1-model(x^{i}))$$

#### This is the Binary Cross-Entropy Loss function!

$$\frac{1}{n}\sum_{i=1}^{n} -y^{i}\log\left(model(x^{i})\right) - (1-y^{i})\log(1-model(x^{i}))$$

### Minimizing loss functions

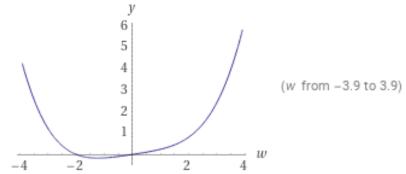
#### Minimizing functions

 Loss functions are just a particular kind of function so we will first consider the general problem of minimizing an arbitrary function

 After we develop some intuition about how to do this, we will return to the specific task of minimizing a loss function

#### Let's say we want to minimize the function:

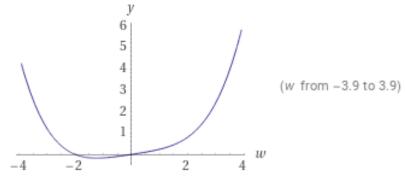
$$g(w) = rac{1}{50}ig(w^4 + w^2 + 10wig)$$



How can we go about this?

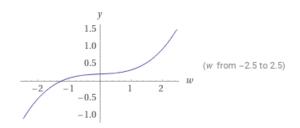
#### Let's say we want to minimize the function:

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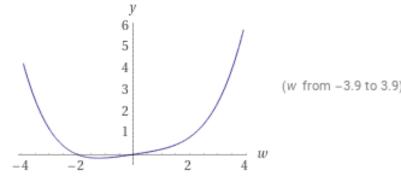
#### Can we use its derivative?

$$rac{\partial}{\partial w}g\left(w
ight)=rac{2}{25}w^{3}+rac{1}{25}w+rac{1}{5}$$



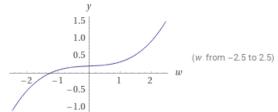
#### Let's say we want to minimize the function:

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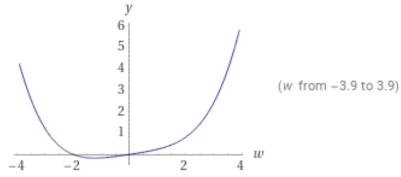
#### What does the derivative at a point tell us?

$$rac{\partial}{\partial w}g\left(w
ight)=rac{2}{25}w^{3}+rac{1}{25}w+rac{1}{5}$$



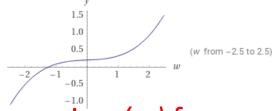
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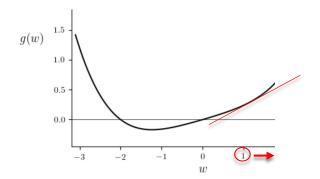
$$\frac{\partial}{\partial w}g\left(w\right)=\frac{2}{25}w^{3}+\frac{1}{25}w+\frac{1}{5}$$



The derivative (or slope) tells us the change in g(w) for a small increase in w

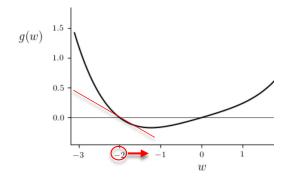
## The value of knowing the derivative

If the derivative at a point w is	What it means
Positive	Increasing w slightly will increase g(w)



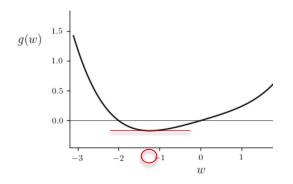
## The value of knowing the derivative

	What it means
Positive	Increasing w slightly will increase g(w)
Negative	Increasing $w$ slightly will decrease $g(w)$



### The value of knowing the derivative

If the derivative at a point w is	What it means
•••	
Positive	Increasing $w$ slightly will increase $g(w)$
Negative	Increasing w slightly will decrease g(w)
~0	Changing $w$ slightly won't change $g(w)$



1. Start with some point w

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3. If you have reached max iterations or run out of time, stop. Else, go to step 2

#### This is Gradient Descent!

- 1. Start with some point w
- 2. Calculate the derivative (i.e., slope) of g(w) at w

This can be written compactly as

If the derivative is	What it means	Since we want to minimize loss, do this
Positive	Increasing w will increase the loss function	Reduce w slightly
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~0	Changing w won't change the loss function	Stop

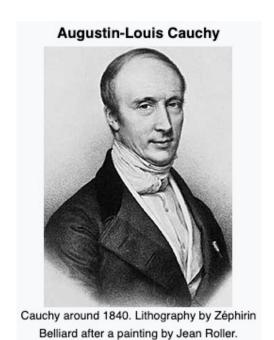
$$w \leftarrow w - \alpha \frac{dg(w)}{dw}$$

3. If you have reached max iterations or run out of time, stop. Else, go to step 2

## Any guesses when Gradient Descent was invented?

# Gradient descent was invented in 1847 by Cauchy!

Cauchy, A. (1847). Methode generale pour la res- olution des systemes d'equations simultanees. Comptes Rendus de l'Académie des Sciences, 25. 91



https://en.wikipedia.org/wiki/Augustin-Louis\_Cauchy

#### Gradient Descent

$$w \leftarrow w - \alpha \ \frac{dg(w)}{dw}$$

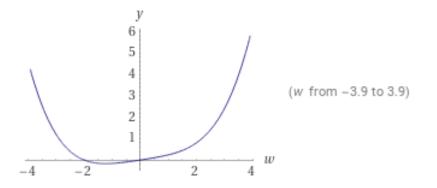
 $\alpha$  is called the "learning rate" and is our way of ensuring that we increase or decrease w slightly

Typically set to small values (e.g., 0.1, 0.001, 0.0001) and determined by trial and error

## Let's apply this algorithm to g(w)

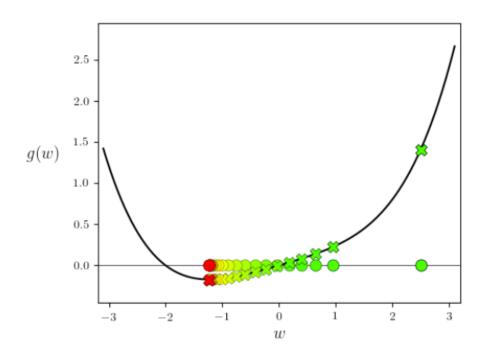
$$g(w) = rac{1}{50}ig(w^4 + w^2 + 10wig)$$

$$rac{\partial}{\partial w}g\left(w
ight)=rac{2}{25}w^3+rac{1}{25}w+rac{1}{5}$$



$$w \leftarrow w - \alpha \, \frac{dg(w)}{dw}$$

#### Gradient Descent in action



We will start at w=2.5, set  $\alpha=1$  and run the algorithm. In a few iterations, it finds the minimum.

### Minimizing a multi-variable function

$$g(w_1, w_2) = w_1^2 + w_2^2 + 2$$

We can calculate the partial derivative of  $g(w_1, w_2)$ 

$$\left[\frac{\partial g}{\partial w_1}, \frac{\partial g}{\partial w_2}\right] = [2w_1, 2w_2]$$

How should we interpret this?

### Minimizing a multi-variable function

$$g(w_1, w_2) = w_1^2 + w_2^2 + 2$$

$$\nabla g = \left[ \frac{\partial g}{\partial w_1}, \frac{\partial g}{\partial w_2} \right] = [2w_1, 2w_2]$$

The first number is the change in g(w) for a small increase in  $w_1$ , with  $w_2$  kept unchanged. The second number is the change in g(w) for a small increase in  $w_2$ , with  $w_1$  kept unchanged

### Minimizing a multi-variable function

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This is called the "gradient" of  $g(w_1, w_2)$  and written as  $\nabla g$ 

#### Minimizing a multi-variable function

$$\nabla g = \left[ \frac{\partial g}{\partial w_1}, \frac{\partial g}{\partial w_2} \right] = [2w_1, 2w_2]$$

We can simply do gradient descent on <u>each</u> coordinate by using the corresponding partial derivative.

$$w_1 \leftarrow w_1 - \alpha \left(\frac{\partial g}{\partial w_1}\right)$$

$$w_2 \leftarrow w_2 - \alpha \left(\frac{\partial g}{\partial w_2}\right)$$

#### Minimizing a multi-variable function

$$\nabla g = [2w_1, 2w_2]$$

$$w_1 \leftarrow w_1 - \alpha \left(\frac{\partial g}{\partial w_1}\right)$$

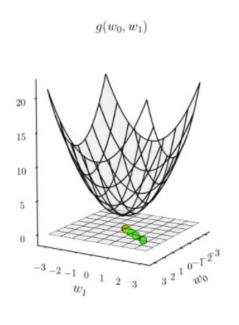
$$w_2 \leftarrow w_2 - \alpha \left(\frac{\partial g}{\partial w_2}\right)$$

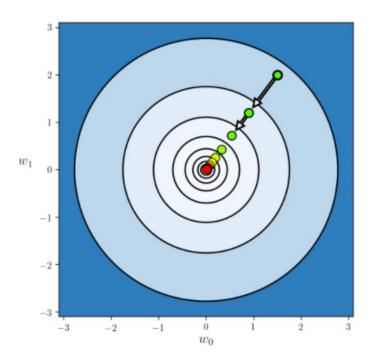
As before, this whole thing can be summarized compactly as:

$$w \leftarrow w - \alpha \nabla g(w)$$

#### Gradient Descent in two dimensions

$$g(w_0, w_1) = w_0^2 + w_1^2 + 2$$





https://kenndanielso.github.io/mlrefined/blog\_posts/6\_First\_order\_methods/6\_4\_Gradient\_descent.html

GD may stop near a local minimum (not necessarily a global minimum) or a saddle point but we don't worry about this in practice.

**Minimize** 
$$\frac{1}{n} \sum_{i=1}^{n} -y^{i} \log \left( model(x^{i}) \right) - (1-y^{i}) \log (1 - model(x^{i}))$$

What are the variables we need to change to minimize this function?

**Minimize** 
$$\frac{1}{n} \sum_{i=1}^{n} -y^{i} \log \left( model(x^{i}) \right) - (1-y^{i}) \log (1 - model(x^{i}))$$

What are the variables we need to change to minimize this function?

They are the parameters "hiding" inside  $model(x_i)$ 

$$\begin{aligned} \textit{Minimize} & \frac{1}{n} \sum_{i=1}^{n} -y^{i} \log \left( model(x^{i}) \right) - (1-y^{i}) \log (1-model(x^{i})) \\ model(x^{i}) &= \frac{1}{1+e^{-(w_{1}+w_{2}max(0,w_{3}+w_{4}x_{1}^{i}+w_{5}x_{2}^{i})+w_{6}max(0,w_{7}+w_{8}x_{1}^{i}+w_{9}x_{2}^{i})+w_{10}max(0,w_{11}+w_{12}x_{1}^{i}+w_{13}x_{2}^{i}))} \\ \text{Recall this model} & \text{Input} & \text{Hidden layer} & \text{Output} & \text{Input} & \text{I$$

$$\begin{aligned} & \frac{1}{n} \sum_{i=1}^{n} -y^{i} \log \left( model(x^{i}) \right) - (1-y^{i}) \log (1 - model(x^{i})) \\ & model(x^{i}) = \frac{1}{1 + e^{-(w_{1} + w_{2}max(0, w_{3} + w_{4}x_{1}^{i} + w_{5}x_{2}^{i}) + w_{6}max(0, w_{7} + w_{8}x_{1}^{i} + w_{9}x_{2}^{i}) + w_{10}max(0, w_{11} + w_{12}x_{1}^{i} + w_{13}x_{2}^{i}))} \end{aligned}$$

w<sub>1</sub>, w<sub>2</sub>, ..., w<sub>13</sub> are the variables we can change to minimize the loss function

The values of  $x_{1,}$   $x_{2}$  and y, on the other hand, are just data

$$\begin{aligned} & \frac{1}{n} \sum_{i=1}^{n} -y^{i} \log \left( model(x^{i}) \right) - (1-y^{i}) \log (1 - model(x^{i})) \\ & model(x^{i}) = \frac{1}{1 + e^{-(w_{1} + w_{2} max(0, w_{3} + w_{4}x_{1}^{i} + w_{5}x_{2}^{i}) + w_{6} max(0, w_{7} + w_{8}x_{1}^{i} + w_{9}x_{2}^{i}) + w_{10} max(0, w_{11} + w_{12}x_{1}^{i} + w_{13}x_{2}^{i}))} \end{aligned}$$

Imagine replacing  $model(x^i)$  with the mathematical expression above wherever  $model(x^i)$  appears in the loss function

Now, your loss function is just a "good old" function of  $w_1$ ,  $w_2$ , ...,  $w_{13}$  and you can apply gradient descent to it as we normally would.

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- The efficiency stems from exploiting the layer-by-layer architecture of NNs

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Please see HODL-SP24-Lec-2-Backprop\_Example.pdf for a step-by-step example

#### Gradient Descent -> Stochastic Gradient Descent

 Problem: For large datasets (e.g., n in the millions), computing the gradient of the loss function can be very expensive

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$$w \leftarrow w - \alpha \nabla g(w)$$

- The Solution:
  - At each <u>iteration</u>, instead of using all the n data points in the calculation of the gradient of the loss function, randomly choose just a few of the n observations (called a *minibatch*) and use only these observations to compute the partial derivatives.

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#### • The Solution:

- At each iteration, instead of using all the n data points in the calculation of the gradient of the loss function, randomly choose just a few of the n observations (called a *minibatch*) and use only these observations to compute the partial derivatives.
- This is called Stochastic Gradient Descent (SGD)\*

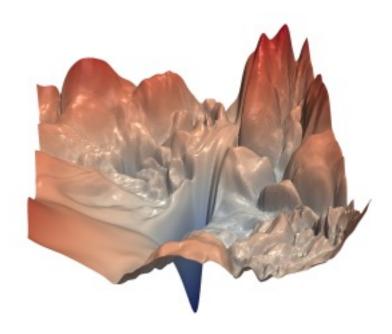
<sup>\*</sup> Strictly speaking, SGD chooses just <u>one</u> observation. What we are describing here is Minibatch Gradient Descent but the term SGD is widely used in the field to describe the latter so we will do the same

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#### • The Solution:

- At each iteration, instead of using all the n data points in the calculation of the gradient of the loss function, randomly choose just a few of the n observations (called a *minibatch*) and use only these observations to compute the partial derivatives.
- This is called Stochastic Gradient Descent (SGD)
- Because not all n data points are used in the calculation, this only approximates the true gradient but nevertheless works well in practice. In fact, because it is only an approximation of the true gradient, it can sometimes escape local minima.
- SGD comes in many "flavors" and we will use a flavor called "Adam" as our default in HODL

# Visualization of an actual DL loss function landscape



https://arxiv.org/pdf/1712.09913.pdf

### Summary of overall training flow

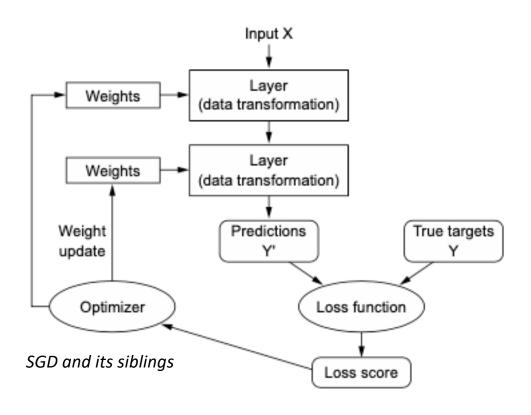


Figure 2.26 Relationship between the network, layers, loss function, and optimizer

Image: Page 61 of textbook