

# Statistical Methods in Cancer Epidemiology using R

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Lecture 4

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# Time splitting

## Contents:

1. Basic concepts of time to event analysis
2. Piecewise constant hazards model and age-specific incidence rates
3. Splitting follow-up times by age
4. Accounting for current age in rate ratio estimation

Main R functions to be covered, all in Epi package

- ▶ `Lexis()`
- ▶ `splitLexis()`
- ▶ `timeBand()`

# Time to event analysis

Analysis of incidences = analysis of *times to event* or *failure times* or *survival times* (censored).

Mathematical concepts:

$T$  = time to outcome event – random variable,

$S(t) = P(T > t)$  = **survival** function of  $T$ ,

= probability of avoiding the event up to given time  $t$ ,

$\lambda(t) = -S'(t)/S(t)$  = **intensity** or **hazard** function,

$\Lambda(t) = \int_0^t \lambda(u)du = -\log S(t)$  = **cumulative hazard**,

$F(t) = 1 - S(t) = 1 - \exp\{-\Lambda(t)\}$  = **risk** function

= probability of the outcome to occur by  $t$

= cumulative distribution function of  $T$ .

## Hazard rate or intensity function

Can be viewed as *theoretical incidence rate*. Formally

$$\lambda(t) = \lim_{\Delta \rightarrow 0} \frac{P(t < T \leq t + \Delta \mid T > t)}{\Delta}$$

≈ Probability of failure occurring in a short interval  $]t, t + \Delta]$ , given “survival” or avoidance of event up to its start  $t$ , divided by the interval length.

This is equivalent to saying that over this short interval

$$\text{risk} \approx \text{rate} \times \text{length of interval}$$

or 
$$P(t < T \leq t + \Delta \mid T > t) \approx \lambda(t) \times \Delta.$$

## Exponential or constant hazard model

Simplest probability model for time to event:

**Exponential distribution**,  $\text{Exp}(\lambda)$ , in which

$$\lambda(t) = \lambda \text{ (constant)} \quad \Rightarrow \quad \Lambda(t) = -\log S(t) = \lambda t$$

Analysis of failure data of  $n$  individuals. For subject  $i$  let

$y_i$  = time to event or time to censoring,  $Y = \sum y_i$

$d_i$  = indicator for observing the event,  $D = \sum d_i$

$\text{Exp}(\lambda)$  model  $\Rightarrow$  **Likelihood function** of  $\lambda$  is

$$L(\lambda) = \prod_{i=1}^n \lambda(y_i)^{d_i} S(y_i) = \prod_{i=1}^n \lambda^{d_i} e^{-\lambda y_i} = \exp(D \log \lambda - \lambda Y)$$

## Constant rate – Poisson model

This is actually equivalent to the *Poisson-likelihood*, i.e. likelihood of  $\lambda$  assuming that the number of cases  $D$  is distributed according to the **Poisson distribution** with expected value  $\lambda Y$ .

With randomly censored exponential times  $D$  is only approximately Poisson. This is sufficient, though, for likelihood-based (& asymptotic frequentist) inference.

Solving the *score equation*:  $d \log L(\lambda)/d\lambda = 0$

→ **maximum likelihood estimator** (MLE) of  $\lambda$  is

$$\hat{\lambda} = \frac{D}{Y} = \frac{\text{number of cases}}{\text{total person-time}} = \text{empirical incidence rate!}$$

## Time to event – when to start the clock?

Incidence can be studied on various time scales, e.g.

- ▶ age (starting point = birth),
- ▶ exposure time (first exposure),
- ▶ follow-up time (entry to study),
- ▶ duration of disease (diagnosis).

Age is usually the strongest time-dependent determinant of health outcomes.

Age is also often correlated with duration of “chronic” exposure (e.g. years of smoking).

Therefore, adjustment for *current age* is needed rather than for *age at entry* to follow-up (like in clinical survival studies).

## Age to event split into agebands

Let  $T$  = age at which outcome event occurs.

Parametric form of  $\lambda(t)$ , hazard by age – usually unknown.

**Piecewise exponential model** or **piecewise constant hazards' model** – an approximation for  $\lambda(t)$ :

$$\lambda(t) = \lambda_k, \quad t \in ]a_{k-1}, a_k], \quad \Delta_k = a_k - a_{k-1},$$

where cutpoints  $0 = a_0 < a_1 < \dots < a_K$  divide the age range into disjoint **agebands**, each with constant rate.

In chronic disease epidemiology agebands with  $\Delta_k = 5$  years (0-4, 5-9, ..., 80-84) or 10 years are commonly used.



## Age-specific incidence rates

For empirical estimation of rates we calculate in each ageband

$D_k$  = number of cases occurring in ageband  $k$ ,

$Y_k = \sum_{i=1}^n y_{ik}$  = total person-time in ageband  $k$ ,

where  $y_{ik}$  is the time slot that subject  $i$  spends in ageband  $k$  out of his/her whole **follow-up time** (from **entry** to **exit**).

ML estimators of  $\lambda_1, \dots, \lambda_K$ : **age-specific incidence rates**

$$\hat{\lambda}_k = I_k = D_k / Y_k, \quad k = 1, \dots, K$$

based on log-likelihood  $\log L = \sum_k (D_k \log \lambda_k - \lambda_k Y_k)$ .

## Cumulative rates & risks

In this model, the cumulative hazard and risk functions are

$$\Lambda(t) = \sum_{a_j < t} \lambda_j \Delta_j + \lambda_k(t - a_{k-1}), \quad t \in ]a_{k-1}, a_k]$$

$$F(t) = 1 - S(t) = 1 - \exp\{-\Lambda(t)\},$$

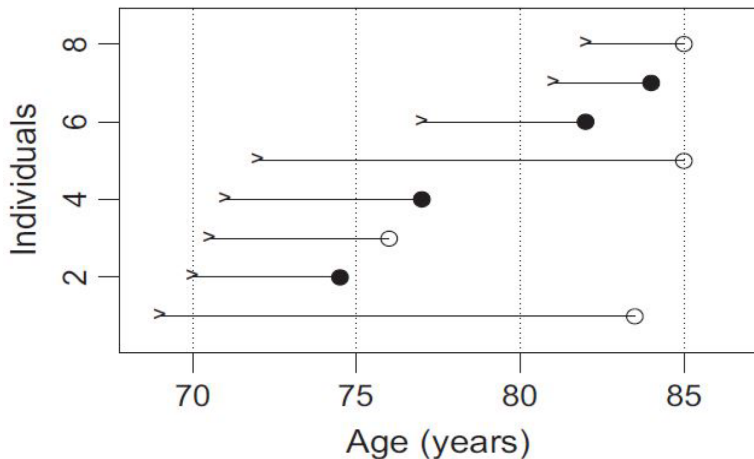
the latter assuming that no **competing risks** are present.

Estimation: Plug in empirical rates  $\hat{\lambda}_j = D_j/Y_j$  to get the cumulative rate  $C$  and incidence proportion  $R$  by  $t$ :

$$C = \hat{\Lambda}(t) = \sum_{a_j < t} \hat{\lambda}_j \Delta_j + \hat{\lambda}_k(t - a_{k-1}), \quad t \in ]a_{k-1}, a_k]$$

$$R = \hat{F}(t) = 1 - \hat{S}(t) = 1 - \exp\{-\hat{\Lambda}(t)\}$$

## Example: Follow-up of a small geriatric cohort



No's of cases/p-years & rates (/100 y) in 5-y agebands:

$$1/21 = 4.8, \quad 1/16 = 6.2, \quad 2/16.5 = 12.1$$

## Splitting follow-up by Lexis() in package Epi

Individual ages at entry and at exit, as well as outcomes are assigned into vectors and stored in a data frame coh:

```
ag.entry <- c(69, 70, 70.5, 71, 72, 76.9, 81, 81.9)
ag.exit <- c(83.5, 74.5, 76, 77, 85, 82, 84, 85)
event <- c(0,1,0,1,0,1,1,0) ; ind <- 1:8
coh <- data.frame( ind, ag.entry, ag.exit, event)
```

Function Lexis() specifies the time scale(s) to be considered. It creates an enriched data frame belonging to class Lexis.

```
library(Epi)
coh.L <- Lexis(entry = list(age = ag.entry),
               exit = list(age = ag.exit),
               exit.status = event, data = coh, id = ind)
```

# Data frame of class Lexis

coh.L

|   | age  | lex.dur | lex.Cst | lex.Xst | lex.id | ind | ag.entry | ag.exit | event |
|---|------|---------|---------|---------|--------|-----|----------|---------|-------|
| 1 | 69.0 | 14.5    | 0       | 0       | 1      | 1   | 69.0     | 83.5    | 0     |
| 2 | 70.0 | 4.5     | 0       | 1       | 2      | 2   | 70.0     | 74.5    | 1     |
| 3 | 70.5 | 5.5     | 0       | 0       | 3      | 3   | 70.5     | 76.0    | 0     |
| 4 | 71.0 | 6.0     | 0       | 1       | 4      | 4   | 71.0     | 77.0    | 1     |
| 5 | 72.0 | 13.0    | 0       | 0       | 5      | 5   | 72.0     | 85.0    | 0     |
| 6 | 76.9 | 5.1     | 0       | 1       | 6      | 6   | 76.9     | 82.0    | 1     |
| 7 | 81.0 | 3.0     | 0       | 1       | 7      | 7   | 81.0     | 84.0    | 1     |
| 8 | 81.9 | 3.1     | 0       | 0       | 8      | 8   | 81.9     | 85.0    | 0     |

Interpretation of new columns

age = age at entry to follow-up,

lex.dur = duration of follow-up,

lex.Cst = current status at entry,

lex.Xst = status at exit from follow-up.

## Splitting follow-up times by agebands

Function `splitLexis()` splits individual follow-up times into given agebands and expands the data frame.

```
coh.A <- splitLexis(coh.L,  
  br = c(70,75,80,85), time.scale="age")
```

```
coh.A[-c(8:12),]
```

|    | lex.id | age  | lex.dur | lex.Cst | lex.Xst | ind | ag.entry | ag.exit | event |
|----|--------|------|---------|---------|---------|-----|----------|---------|-------|
| 1  | 1      | 69.0 | 1.0     | 0       | 0       | 1   | 69.0     | 83.5    | 0     |
| 2  | 1      | 70.0 | 5.0     | 0       | 0       | 1   | 69.0     | 83.5    | 0     |
| 3  | 1      | 75.0 | 5.0     | 0       | 0       | 1   | 69.0     | 83.5    | 0     |
| 4  | 1      | 80.0 | 3.5     | 0       | 0       | 1   | 69.0     | 83.5    | 0     |
| 5  | 2      | 70.0 | 4.5     | 0       | 1       | 2   | 70.0     | 74.5    | 1     |
| 6  | 3      | 70.5 | 4.5     | 0       | 0       | 3   | 70.5     | 76.0    | 0     |
| 7  | 3      | 75.0 | 1.0     | 0       | 0       | 3   | 70.5     | 76.0    | 0     |
| 13 | 6      | 76.9 | 3.1     | 0       | 0       | 6   | 76.9     | 82.0    | 1     |
| 14 | 6      | 80.0 | 2.0     | 0       | 1       | 6   | 76.9     | 82.0    | 1     |
| 15 | 7      | 81.0 | 3.0     | 0       | 1       | 7   | 81.0     | 84.0    | 1     |
| 16 | 8      | 81.9 | 3.1     | 0       | 0       | 8   | 81.9     | 85.0    | 0     |

## Splitted Lexis object

- ▶ Function `splitLexis()` expanded the original data frame such that for all cohort members one or more rows were created, one for each ageband into which a subject contributes person time.
- ▶ Ex: Subject 1 has been under follow-up in all agebands considered, but subjects 7 and 8 only in 80– < 85 y.
- ▶ Function `timeBand()` converts variable `age` into factor `ageband`. Also, shorthand names for person-time slots and occurrence of outcome event are given.

```
coh.A$ageband <- timeBand(coh.A, "age", "factor")  
coh.A$y_ik <- coh.A$lex.dur # person-time slot  
coh.A$d_ik <- coh.A$lex.Xst # occurrence of outcome
```

## Split Lexis object (cont'd)

```
coh.A[, c(1,10:12)]
```

|    | lex.id | ageband   | y_ik | d_ik |
|----|--------|-----------|------|------|
| 1  | 1      | (-Inf,70] | 1.0  | 0    |
| 2  | 1      | (70,75]   | 5.0  | 0    |
| 3  | 1      | (75,80]   | 5.0  | 0    |
| 4  | 1      | (80,85]   | 3.5  | 0    |
| 5  | 2      | (70,75]   | 4.5  | 1    |
| 6  | 3      | (70,75]   | 4.5  | 0    |
| 7  | 3      | (75,80]   | 1.0  | 0    |
| 8  | 4      | (70,75]   | 4.0  | 0    |
| 9  | 4      | (75,80]   | 2.0  | 1    |
| 10 | 5      | (70,75]   | 3.0  | 0    |
| 11 | 5      | (75,80]   | 5.0  | 0    |
| 12 | 5      | (80,85]   | 5.0  | 0    |
| 13 | 6      | (75,80]   | 3.1  | 0    |
| 14 | 6      | (80,85]   | 2.0  | 1    |
| 15 | 7      | (80,85]   | 3.0  | 1    |
| 16 | 8      | (80,85]   | 3.1  | 0    |

lex.id = subject  
index in original  
data frame,  
ageband = ageband  
and its limits,  
y\_ik = person-time slot  
spent in ageband  
d\_ik = indicator for  
event occurring  
in ageband.

Subject 1's follow-up time (14.5 y = 1 + 5 + 5 + 3.5 y) is split into 4 agebands, ..., subject 8 contributes only to 1 ageband.



## Tabulation of cases, rates etc. by ageband

Event indicators & person-time slots are summed over the rows of the split-expanded data frame in categories of ageband:

```
D <- with(coh.A, tapply(d_ik, ageband, sum))  
Y <- with(coh.A, tapply(y_ik, ageband, sum))
```

Incidence rates ( $I$ ), cumulative rates ( $C$ ) and incidence proportions ( $R$ ), the latter two by the end of each ageband:

```
I <- 100*D/Y; C <- cumsum((D/Y)*5); R <- 1-exp(-C)  
tab <- round(cbind(D,Y,I,C,R),3)[2:4, ]
```

# Age standardised incidence rate

Direct age standardisation

► e.g. to the World Standard population

```
library(popEpi)  
stdpop18
```

|     | agegroup | world | europa | nordic |
|-----|----------|-------|--------|--------|
| 1:  | 0-4      | 12000 | 8000   | 5900   |
| 2:  | 5-9      | 10000 | 7000   | 6600   |
| 3:  | 10-14    | 9000  | 7000   | 6200   |
| 4:  | 15-19    | 9000  | 7000   | 5800   |
| 5:  | 20-24    | 8000  | 7000   | 6100   |
| 6:  | 25-29    | 8000  | 7000   | 6800   |
| 7:  | 30-34    | 6000  | 7000   | 7300   |
| 8:  | 35-39    | 6000  | 7000   | 7300   |
| 9:  | 40-44    | 6000  | 7000   | 7000   |
| 10: | 45-49    | 6000  | 7000   | 6900   |
| 11: | 50-54    | 5000  | 7000   | 7400   |
| 12: | 55-59    | 4000  | 6000   | 6100   |
| 13: | 60-64    | 4000  | 5000   | 4800   |
| 14: | 65-69    | 3000  | 4000   | 4100   |
| 15: | 70-74    | 2000  | 3000   | 3900   |
| 16: | 75-79    | 1000  | 2000   | 3500   |
| 17: | 80-84    | 500   | 1000   | 2400   |
| 18: | 85       | 500   | 1000   | 1900   |

## Age standardised incidence rate (cont'd)

Weighted average of age-specific incidence rates  $I_k$

$$\sum_k w_k I_k, \text{ where } \sum_k w_k = 1$$

```
tab <- cbind(tab,stdpop18[15:17,1:2])
tab$w <- tab$world/sum(tab$world)
tab
```

|    | D | Y    | I      | C     | R     | agegroup | world | w         |
|----|---|------|--------|-------|-------|----------|-------|-----------|
| 1: | 1 | 21.0 | 4.762  | 0.238 | 0.212 | 70-74    | 2000  | 0.5714286 |
| 2: | 1 | 16.1 | 6.211  | 0.549 | 0.422 | 75-79    | 1000  | 0.2857143 |
| 3: | 2 | 16.6 | 12.048 | 1.151 | 0.684 | 80-84    | 500   | 0.1428571 |

```
#age-standardised incidence per 100 person years
sum(tab$w*tab$I)
```

```
[1] 6.216857
```

```
#non-standardised incidence per 100 person years
100*sum(tab$D)/sum(tab$Y)
```

```
[1] 7.44879
```

## Age standardised incidence rate (cont'd)

$$SE \left[ \log \left( \sum_k w_k I_k \right) \right] \approx \frac{1}{\sum_k w_k I_k} \sqrt{\sum_k \frac{w_k^2 d_k}{y_k^2}}$$

```
std.rate <- sum(tab$w*tab$D/tab$Y)
SE.std.rate <- sqrt( sum(tab$w^2*tab$D/tab$Y^2) )
exp( log(std.rate)+1.96*(1/std.rate)*SE.std.rate*c(-1,1) )
```

```
[1] 0.02082472 0.18559491
```

```
rate(tab,obs="D",pyrs="Y",adjust="agegroup",weights=tab$w)[,c(3,5:6)]
```

Adjusted rates (agegroup; 3) and 95% confidence intervals:

```
      rate.adj rate.adj.lo rate.adj.hi
1: 0.06216882  0.02082472  0.1855949
```

- ▶ Age-standardised incidence in age group 70-84 is:
  - ▶ 6.2 per 100 person years, 95% CI (2.1, 18.6)

## Example: The Diet Study (see C&H)

A cohort of 337 men in three occupational groups in England, aged 30 to 67 y at entry, recruited in '50s and '60s, followed-up until mid '70s for incidence of CHD events.

Risk factors of interest, measured by dietary survey at entry.

energy = total energy intake (kcal/d),  
energy.grp = energy dichotomized:  
1: " $\leq 2750$  KCals", 2: " $> 2750$  KCals",  
fat = fat intake (g/d),  
fibre = dietary fibre intake (g/d),  
height, weight, bmi, etc.

## Important dates and outcome event

The data set diet in Epi contains three dates:

dob = date of **birth**,

doe = date of **entry** into follow-up,

dox = date of **exit**, end of follow-up.

These are given in format yyyy-mm-dd but implicitly stored as *number of days since 1.1.1970*.

In addition, the outcome event is represented by

chd = indicator for **status** at exit:

1 = CHD event occurred, 0 = censored.

## Data diet: creating a Lexis object

First convert all dates into fractional calendar years using function `cal.yr()` in `Epi`

```
data(diet)
diet <- transform(diet, doe = cal.yr(doe),
                  dox = cal.yr(dox), dob = cal.yr(dob) )
```

Convert the data frame into a Lexis object.

```
dietL <- Lexis( entry = list(age = doe-dob),
                exit = list(age = dox-dob),
                exit.status = chd, data = diet )
```

In the nexty step the Lexis object is splitted according to 3 agebands (y):  $30- < 50$ ,  $50- < 60$ ,  $60- < 70$

## Splitting the Lexis object into agebands

```
dietA <- splitLexis(dietL, br = c(30,50,60,70),
                   time.scale = "age")
dietA$ageband <- timeBand(dietA, "age", "factor")
dietA$y_ik <- dietA$lex.dur ; dietA$d_ik <- dietA$lex.Xst

dietA[1:8,c("id","dob","doe","dox","y","chd","energy.grp","ageband",
            "age","y_ik","d_ik")]
```

|   | id  | dob    | doe    | dox    | y    | chd | energy.grp   | ageband | age  | y_ik | d_ik |
|---|-----|--------|--------|--------|------|-----|--------------|---------|------|------|------|
| 1 | 102 | 1939.2 | 1976.0 | 1986.9 | 10.9 | 0   | <=2750 KCals | (30,50] | 36.9 | 10.9 | 0    |
| 2 | 59  | 1912.5 | 1973.5 | 1982.5 | 9.0  | 0   | <=2750 KCals | (60,70] | 61.0 | 9.0  | 0    |
| 3 | 126 | 1920.0 | 1970.2 | 1984.2 | 14.0 | 1   | <=2750 KCals | (50,60] | 50.2 | 9.8  | 0    |
| 4 | 126 | 1920.0 | 1970.2 | 1984.2 | 14.0 | 1   | <=2750 KCals | (60,70] | 60.0 | 4.2  | 1    |
| 5 | 16  | 1906.7 | 1969.4 | 1970.0 | 0.6  | 1   | <=2750 KCals | (60,70] | 62.7 | 0.6  | 1    |
| 6 | 247 | 1918.5 | 1968.2 | 1979.5 | 11.3 | 1   | <=2750 KCals | (30,50] | 49.7 | 0.3  | 0    |
| 7 | 247 | 1918.5 | 1968.2 | 1979.5 | 11.3 | 1   | <=2750 KCals | (50,60] | 50.0 | 10.0 | 0    |
| 8 | 247 | 1918.5 | 1968.2 | 1979.5 | 11.3 | 1   | <=2750 KCals | (60,70] | 60.0 | 1.0  | 1    |

Properties of the original data frame and the expanded object:

```
> str(diet)
'data.frame':   337 obs. of  17 variables:
> str(dietA)
Classes Lexis and data.frame  729 obs. of  25 variables
```



## Relevelling of energy.grp and some tabulations

The energy.grp variable is relevelled such that “high energy” is taken as the reference or “unexposed” category and “low energy” as the “exposed” one.

```
dietA$eg2 <- Relevel( dietA$energy.grp,  
  ref = ">2750 KCal/s" )
```

Tabulation of cases, person-years and rates:

```
tab.ae <- stat.table( list( ageband, eg2),  
  list( D = sum(d_ik), Y = sum(y_ik),  
        I = ratio(d_ik, y_ik, 1000) ),  
  margin = T, data = dietA )  
print(tab.ae, digits= c(sum=0, ratio=1))
```

# Rates by ageband and energy intake

Crude rate ratio

```
tab.ae[3, 6, 2] /  
  tab.ae[ 3, 6, 1]
```

```
[1] 1.922497
```

Rate ratios by ageband:

```
IRs <- tab.ae[3, 2:4, 2] /  
  tab.ae[3, 2:4, 1]  
round(IRs, 2)
```

| (30,50] | (50,60] | (60,70] |
|---------|---------|---------|
| 0.82    | 2.30    | 1.99    |

- ▶ Low intake risky?
- ▶ No effect in young?

| ageband   | eg2               |                    | Total              |
|-----------|-------------------|--------------------|--------------------|
|           | >2750<br>KCal/s   | <=2750<br>KCal/s   |                    |
| (-Inf,30] | NA                | NA                 | NA                 |
| ...       |                   |                    |                    |
| (30,50]   | 4<br>622<br>6.4   | 2<br>381<br>5.2    | 6<br>1003<br>6.0   |
| (50,60]   | 6<br>1128<br>5.3  | 12<br>979<br>12.3  | 18<br>2107<br>8.5  |
| (60,70]   | 8<br>794<br>10.1  | 14<br>699<br>20.0  | 22<br>1493<br>14.7 |
| (70,Inf]  | NA                | NA                 | NA                 |
| ...       |                   |                    |                    |
| Total     | 18<br>2544<br>7.1 | 28<br>2059<br>13.6 | 46<br>4604<br>10.0 |

## Poisson model on age and exposure

Let  $D_{kj}$ ,  $Y_{kj}$ , and  $I_{kj}$  be cases, p-years & rate in ageband  $k$  & exposure category  $j$  (1="unexposed", 2="exposed").

Piecewise Exp-model in both exposure categories assumed:

$$\lambda_{kj} = \text{theoretical rate in cell } kj.$$

Theoretical rate ratio  $\rho_k = \lambda_{k2}/\lambda_{k1}$ ,  
comparing exposed vs. unexposed.

- (a) What are the "true" values of  $\rho_k$ ?
- (b) Can we assume  $\rho_k = \rho$ , same rate ratio in all agebands?
- (c) What is the value of the common rate ratio  $\rho$ ?

## Poisson model (cont'd)

Assuming common rate ratio the true rates are modelled

$$\log \lambda_{kj} = \alpha_k + \beta_j = \sum_{k=1}^K \alpha_k A_k + \sum_{j=1}^2 \beta_j X_j,$$

where  $A_k$  and  $X_j$  are indicator (1/0) variables for level  $k$  of ageband and level  $j$  of exposure. In exponential form

$$\lambda_{kj} = \exp(\alpha_k + \beta_j) = e^{\alpha_k} e^{\beta_j}.$$

Set  $\beta_1 = 0$  ("unexposed" as reference)  $\Rightarrow$  Interpretation:

$\alpha_k = \log(\lambda_{k1}) =$  log-rate of unexposed in ageband  $k$

$\beta_2 = \log(\lambda_{k2}/\lambda_{k1}) = \log(\rho) =$  log-common rate ratio

## Fitting the Poisson model

Use function `glm()` on the expanded data frame:

```
m.ea <- glm( d_ik/y_ik ~ ageband + eg2,  
             fam = poisson, w = y_ik, data = dietA )
```

```
round(ci.lin(m.ea, Exp=T)[ , -(3:4)], 4 )
```

|                | Estimate | StdErr | exp(Est.) | 2.5%   | 97.5%  |
|----------------|----------|--------|-----------|--------|--------|
| (Intercept)    | -5.4033  | 0.4390 | 0.0045    | 0.0019 | 0.0106 |
| ageband(50,60] | 0.3027   | 0.4721 | 1.3535    | 0.5366 | 3.4145 |
| ageband(60,70] | 0.8456   | 0.4613 | 2.3294    | 0.9431 | 5.7535 |
| eg2<=2750 KCal | 0.6233   | 0.3027 | 1.8651    | 1.0306 | 3.3753 |

The estimated rate ratio for “low” vs. “high” energy consumption, adjusted for age, is thus 1.87 [1.03 to 3.38], only slightly lower than the unadjusted one 1.92 [1.06 to 3.47].

## Concluding remarks

- ▶ Modelling could continue from this to include other confounders, continuous covariates, interactions, *etc.*
- ▶ Agebands may well be much narrower than in our example. With infinitely narrow bands Poisson regression equals the famous Cox model.
- ▶ Splitting by many time scales (e.g. age, calendar time, time since first exposure, *etc.*) simultaneously and the corresponding data frame expansion is straightforward using these tools. More about this in the next lecture.