Statistical Methods in Cancer Epidemiology using R

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Lecture 5

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Mar 2, 2020

More than one time scale and SIR & SMR

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- Merging reference rates with the cohort data and performing SIR/SMR computations

Main R functions to be covered

- Lexis.diagram() and other Lexis tools in Epi
- merge()
- sir() and sirspline() in popEpi

Special cohorts of exposed subjects

- Occupational cohorts, exposed to potentially \ hazardous agents
- Cohorts of patients on chronic medication, which may have harmful long-term side-effects

No internal comparison group of unexposed subjects.

Question: Do incidence or mortality rates in the exposed target cohort differ from those of a roughly comparable reference population?

Reference rates obtained from:

- population statistics (mortality rates)
- disease & hospital discharge registers (incidence)

Accounting for age distribution

- Compare rates in a study cohort with a standard set of age-specific rates from the reference population.
- ▶ Reference rates normally based on large numbers of cases, so they are assumed to be "known" without error.
- ► Calculate **expected** number of cases, *E*, if the standard age-specific rates had applied in our study cohort.
- Compare this with the **observed** number of cases, D, by the **standardized incidence ratio** SIR (or standardized mortality ratio SMR)

$$SIR = D/E$$
, $SE[log(SIR)] = 1/\sqrt{D}$

Example: HT and breast ca.

- ► A cohort of 974 women treated with hormone (replacement) therapy were followed up.
- \triangleright D=15 incident cases of breast cancer were observed.
- Person-years (Y_a) and reference rates $(\lambda_a^*, \text{ per } 100000 \text{ y})$ by age group (a) were:

Age	Y_a	$\lambda_{\sf a}^*$	E_a	
40-44	975	113	1.10	
45-49	1079	162	1.75	
50-54	2161	151	3.26	
55–59	2793	183	5.11	
60–64	3096	179	5.54	
$\overline{\Sigma}$			16.77	

Example: HT use and breast ca. (cont'd)

"Expected" number of cases at ages 40–44:

$$975 \times \frac{113}{100\,000} = 1.10$$

- ▶ Total "expected" cases is E = 16.77
- ▶ The SIR is 15/16.77 = 0.89.
- Error factor: $\exp(1.96 \times \sqrt{1/15}) = 1.66$
- ▶ 95% confidence interval is:

$$0.89 \stackrel{\times}{\div} 1.66 = (0.54, 1.48)$$

A statistical model for SIR

▶ The theoretical rates λ_{ap} by age (a) and calendar period (p) in the cohort are assumed to be proportional to the rates λ_{ap}^* in the reference population:

$$\lambda_{\mathit{ap}} = \rho \times \lambda_{\mathit{ap}}^*$$

 $\rho=$ hazard ratio btw the cohort and the reference pop'n.

- ▶ The population rates λ_{ap}^* are assumed to be known.
- ▶ Cohort data: numbers of cases D_{ap} and p-years Y_{ap} by age and period are computed.
- It can be shown that the likelihood of ρ is of Poisson type, and the maximum likelihood estimator of ρ is:

$$\widehat{\rho} = \frac{D}{\sum \lambda_{ap}^* Y_{ap}} = \frac{\text{Observed}}{\text{Expected}} = \text{SIR}$$

Example: The Welsh Nickel Workers' Study

- ► A cohort of 679 men working in nickel smelters in South Wales first employed 1903-25 (for details see **B&D**).
- ▶ Outcomes of interest: deaths from nasal (ICD code 160) and lung cancer (ICD 162 and 163) during follow-up 1934-76.
- Outcome event indicator and basic time variables:

```
icd = code for cause of death, 0 if not yet dead
date.bth = date of birth
date.in = date of starting follow-up
date.out = date when follow-up ended
```

Example (cont'd)

▶ Interesting risk factors in the original data frame:

```
expos = exposure index based on years employed in high-risk areas in the smelter by 1925  \rightarrow \mbox{ categorized version EXP}  date.1st = date when first employed \rightarrow AFE
```

Risk factors to be formed from original variables:

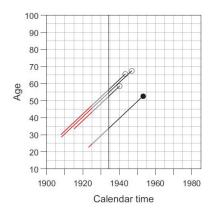
```
age.1st = age when first employed \rightarrow AFE

year.1st = year of first employment \rightarrow YFE

time.1st = time since first exposure \rightarrow TFE
```

Lexis diagram & 4 lifelines from the nickel cohort

Diagram invented by Wilhelm Lexis (1837-1914), German mathematician and demographer, professor in Tartu 1874-76.

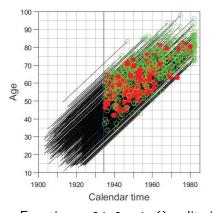


Individual lifelines run diagonally from a given (age, time) starting point to an endpoint.

Here the lines go from start of exposure till the age and time of exit.

Mortality follow-up started in 1934.

Nickel cohort: All lifelines in the Lexis diagram



Follow-up starts not until 1934 for all subjects.

- ▶ dot (red)
 - = lung ca. death,
- circle (green)
 - = censoring

Function splitLexis() splits individual follow-up times into rectangles defined by agebands and calendar periods.

Splitting follow-up by age & calendar time

from the registration of:

- Entry,
- Exit,
- Failure status

of the individuals in the cohort, and the definition of the scale by:

- ► Origin
- ► Scale
- Cutpoints

to the table of:

- ► *D* = events,
- ➤ Y = person time,

by age and period.

Expected numbers in practice

From the records of age-period split & expanded cohort data:

 $y_{i,ap}=$ person-time slot in a record defined by a= ageband of the record p= period of the record

From the file containing the reference rates:

 $\lambda_{ap}^* = {\sf age} \ \& \ {\sf period} \ {\sf specific} \ {\sf rate}$ $a={\sf ageband} \ {\sf of} \ {\sf the} \ {\sf population} \ {\sf rate}$

p =period of the population rate

Expected numbers in practice (cont'd)

Population rates are matched up to the expanded cohort data, and expected numbers individually are computed as:

$$e_{i,ap} = \lambda_{ap}^* \times y_{i,ap}$$

and these are eventually summed: $E = \sum e_{i,ap}$

Always two datasets are needed for SIR:

- 1. the *cohort* data with follow-up information on its individual members. This must be split & expanded to match with
- 2. the *reference rate* data with age & period specific rates in the chosen reference population.

SMR-calculations in R using Lexis tools:

1. Read in the cohort data (Welsh Nickel Workers)

and convert the dates dd/mm/yyyy into "decimal years"

```
library(Epi)
nick <- read.table( "nickel.txt", header=T, as.is=T )
for (j in 4:7) nick[ , j] <-
    cal.yr( nick[ , j], format = "%d/%m/%Y" )</pre>
```

List the records for the 4 men in a previous Lexis diagram

```
round(nick[11:14, ],2)
```

```
id icd expos date.bth date.1st date.in date.out
11 19 160 10.0 1881.73 1915.18 1934.25 1940.21
12 21 14 0.0 1877.80 1908.00 1934.25 1943.37
13 22 177 2.5 1879.50 1908.17 1934.25 1946.98
14 23 162 0.0 1900.50 1923.15 1934.25 1953.20
```

2. Reference rates in E & W read in

```
ewrates <- read.table("ewrates.txt",header=T)</pre>
```

8 first and last rows checked

```
ewrates[c(1:8, 143:150), ]
```

```
year age lung nasal
                          other
1
    1931
          10
                       0
                            1269
    1931
          15
                       0
                           2201
3
    1931
          20
               6
                       0
                           3116
4
    1931
          25
               14
                           3024
5
   1931
          30
                30
                           3188
6
   1931
                68
                       1
                           4165
          35
7
   1931
          40
              149
                       3
                           5651
    1931
              274
                       5
                           8326
8
          45
143 1976
              403
                       3
                           4311
          45
144 1976
          50 1003
                           7687
145 1976
          55 1896
                          12544
146 1976
          60 3342
                      15
                          20787
147 1976
          65 4985
                      17
                          33729
148 1976
          70 6718
                          55480
                      20
149 1976
          75 8068
                      38
                          89199
150 1976
          80 7744
                      33 137360
```

E & W lung ca. death rates by age and period}

```
vear
   1931 1936 1941 1946 1951 1956 1961 1966 1971 1976
10
                      1
                           0
                                                 0
                                                      0
15
                      3
                           2
                          7
                                4
                                      5
20
      6
           6
                6
                      8
                                           4
                                                4
25
     14
          14
                16
                     18
                          13
                                12
                                     11
                                          10
                                                10
30
     30
          30
               34
                     36
                          35
                                35
                                     34
                                          25
                                               24
                                                     17
     68
                          98
                               93
                                          76
                                                     56
35
          68
               81
                     94
                                     90
                                                58
40
    149
         149
               191
                    236
                         248
                              251
                                    223
                                         216
                                               177
                                                    139
45
    274
         274
              384
                    544
                         579
                              590
                                    563
                                         531
                                               503
                                                    403
50
    431
         431
              597
                    954 1224 1248 1221 1160 1070 1003
55
    586
         586
              883 1350 2003 2317 2284 2201 2077 1896
    646
             1021 1717 2555 3315 3663 3695 3546 3342
60
         646
65
    636
         636
              970 1763 2926 3926 4844 5273 5174 4985
70
    533
         533
              748 1400 2624 3878 4977 6210 6820 6718
75
    464
              631 1085 2069 3332 4513 5914 7273 8068
         464
80
    324
         324
              385
                    765 1416 2258 3417 4563 6089 7744
```

3. Creating and expanding the Lexis object}

The data frame converted to a Lexis object in two time scales: year (calendar time) and age:

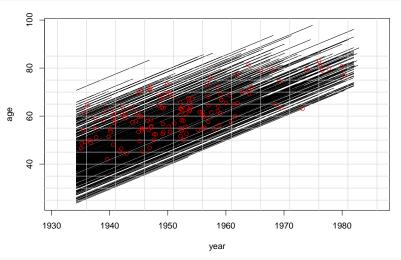
NOTE: entry.status has been set to 0 for all.

The Lexis object jointly split by age and period. Agebands and period bands are named like in the ewrates file — "left" means the lower cutpoint (1st year) of a band.

```
nickL.a <- splitLexis(nickL, "age", br=seq(10,85,5) )
nickL.ap<- splitLexis(nickL.a, "year", br=seq(1931,1986,5))</pre>
```

Splitting follow up time by age and calendar year

```
plot( nickL.ap, c("year", "age"), col=c("black"), xlim=c(1931,1986) )
points( nickL.ap, c("year", "age"), pch=c(NA,1)[nickL.ap$lex.Xst+1], col="red" )
```



```
nickL.ap$year <- timeBand(nickL.ap, "year", "left")
nickL.ap$age <- timeBand(nickL.ap, "age", "left")</pre>
```

The expanded data frame viewed

```
dim(nickL.ap) # 10-fold expansion!
[1] 6949 13
round( subset( nickL.ap, lex.id %in% 13:14)
       [ , c(1:4,6,8,10,12,13)] ,2)
lex.id year age lex.dur lex.Xst icd date.bth date.in date.out
```

```
90
       13 1931
                50
                      0.25
                                0 177
                                        1879.5 1934.25 1946.98
91
       13 1931
               55
                    1.50
                                0 177 1879.5 1934.25 1946.98
92
       13 1936
               55
                   3.50
                                0 177
                                       1879.5 1934.25 1946.98
93
       13 1936
               60
                    1.50
                                0 177
                                        1879.5 1934.25 1946.98
94
       13 1941 60
                      3.50
                                0 177
                                       1879.5 1934.25 1946.98
95
       13 1941
                65
                    1.50
                                0 177
                                        1879.5 1934.25 1946.98
96
       13 1946
                65
                      0.98
                                0 177
                                        1879.5 1934.25 1946.98
97
       14 1931
                30
                    1.25
                                0 162
                                        1900.5 1934.25 1953.20
98
       14 1931
                35
                      0.50
                                0 162
                                        1900.5 1934.25 1953.20
99
       14 1936
                35
                      4.50
                                0 162
                                        1900.5 1934.25 1953.20
100
       14 1936
                      0.50
                                0 162
                                        1900.5 1934.25 1953.20
                40
101
       14 1941
                40
                      4.50
                                0 162
                                        1900.5 1934.25 1953.20
102
       14 1941
                45
                      0.50
                                0 162
                                        1900.5 1934.25 1953.20
103
       14 1946
                45
                      4.50
                                0 162
                                        1900.5 1934.25 1953.20
104
       14 1946
                50
                      0.50
                                0 162
                                        1900.5 1934.25 1953.20
105
       14 1951
                50
                      2.20
                                 1 162
                                        1900.5 1934.25
                                                       1953.20
```

4. Merging the cohort data with E&W rates

```
nickLew.ap <- merge(nickL.ap, ewrates,</pre>
         by = c("age", "year")) # key columns
round(nickLew.ap[1:20, c(1:4,6:8,10,12,13,14)],1)
   year age lex.id lex.dur lex.Xst id icd date.bth date.in date.out lung
   1931
         20
               400
                       0.5
                                 0 574 491
                                             1909.7
                                                     1934.2
                                                               1980.4
                                                                         6
2
   1931
         20
               197
                       0.3
                                 0 273 154
                                            1909.5
                                                     1934.2
                                                              1965.4
                                                                         6
3
  1931
         20
               156
                       0.9
                                 0 213 162 1910.1
                                                     1934.2
                                                              1973.2
                                                                         6
4
  1931
         20
               384
                       0.3
                                 0 546
                                            1909.5
                                                     1934.2
                                                              1982.0
                                                                         6
  1931
               236
                       1.3
                                 0 325 434
                                             1910.5
                                                     1934.2
                                                              1953.5
                                                                         6
         20
6
  1931
         20
              84
                       0.0
                                 0 110
                                        0
                                             1909.2
                                                     1934.2
                                                              1982.0
                                                                         6
  1931
         25
               274
                       1.8
                                 0 380 411
                                             1907.2
                                                     1934.2
                                                              1960.8
                                                                        14
8
  1931
         25
               315
                       1.1
                                 0 443 420
                                             1905.3
                                                     1934.2
                                                              1971.1
                                                                        14
9
  1931
         25
               197
                       1.5
                                 0 273 154
                                             1909.5
                                                     1934.2
                                                              1965.4
                                                                        14
10 1931
         25
               52
                       1.2
                                    75
                                             1905.4
                                                     1934.2
                                                              1982.0
                                                                        14
11 1931
               478
                       1.8
                                   690 420
                                             1906.5
                                                     1934.2
                                                              1961.6
                                                                        14
         25
12 1931
         25
                17
                       1.6
                                    28 420
                                             1905.8
                                                     1934.2
                                                              1967.4
                                                                        14
13 1931
         25
               569
                       1.8
                                   828
                                             1908.7
                                                     1934.2
                                                              1982.0
                                                                        14
                                         0
14 1931
         25
               543
                       1.8
                                 0 792
                                         0
                                             1908.5
                                                     1934.2
                                                              1982.0
                                                                        14
15 1931
         25
               609
                       0.1
                                 0 884
                                             1904.4
                                                     1934.2
                                                              1982.0
                                                                        14
16 1931
         25
               138
                       1.8
                                 0 187 999
                                             1906.5
                                                     1934.2
                                                              1941.0
                                                                        14
17 1931
         25
               368
                       1.8
                                   523
                                             1906.0
                                                     1934.2
                                                              1982.0
                                                                        14
18 1931
         25
               285
                       0.3
                                 0 394 237
                                             1904.6
                                                     1934.2
                                                              1970.4
                                                                        14
19 1931
                       1.3
                                 0 574 491
                                             1909.7
                                                     1934.2
                                                              1980.4
                                                                        14
         25
               400
20 1931
         25
               156
                       0.9
                                   213 162
                                             1910.1
                                                     1934.2
                                                               1973.2
```

5. Calculation of observed and expected

Cases & person-time slots renamed, expectations $\lambda_{ap}^* y_{i,ap}$ of becoming a case computed, and tables by a and p produced.

```
Obs.lung; round(Exp.lung,3)
```

Observed and expected numbers printed

7	year									
age	1931	1936	1941	1946	1951	1956	1961	1966	1971	1976
30	0	0	0	NA						
35	0	0	0	0	NA	NA	NA	NA	NA	NA
40	0	1	1	0	0	NA	NA	NA	NA	NA
45	3	2	4	1	0	0	NA	NA	NA	NA
50	1	5	3	7	6	2	0	NA	NA	NA
55	0	5	6	6	4	5	1	0	NA	NA
60	1	4	5	3	11	6	1	2	1	NA
65	0	0	1	5	4	6	3	0	0	0
70	0	0	1	3	0	2	2	1	0	0
75	NA	0	0	0	0	1	1	2	1	3
80	NA	NA	0	0	0	0	1	0	0	3

year

age	1931	1936	1941	1946	1951	1956	1961	1966	1971	1976
30	0.004	0.005	0.001	NA						
35	0.012	0.032	0.015	0.004	NA	NA	NA	NA	NA	NA
40	0.027	0.075	0.090	0.045	0.011	NA	NA	NA	NA	NA
45	0.054	0.135	0.184	0.246	0.110	0.025	NA	NA	NA	NA
50	0.082	0.231	0.281	0.438	0.511	0.220	0.046	NA	NA	NA
55	0.070	0.263	0.411	0.557	0.789	0.834	0.343	0.069	NA	NA
60	0.035	0.162	0.362	0.644	0.880	1.108	1.155	0.502	0.104	NA
65	0.004	0.045	0.178	0.481	0.775	1.015	1.314	1.240	0.539	0.122
70	0.001	0.004	0.041	0.157	0.486	0.682	0.796	1.172	1.203	0.519
75	NA	0.001	0.003	0.039	0.136	0.342	0.470	0.498	0.954	0.885
80	NA	NA	0.001	0.001	0.037	0.098	0.158	0.218	0.293	0.536

6. Calculation of SMR

We can sum either over individual time slots:

```
D <- sum(nickLew.ap$d_iap)
E <- sum(nickLew.ap$e_iap)
```

or over the newly formed tables:

```
D <- sum(Obs.lung, na.rm=T)
E <- sum(Exp.lung, na.rm=T)</pre>
```

Either way, the calculation proceeds:

```
SMR <- D/E; SE <- 1/sqrt(D); EF <- exp(1.96*SE)
round(c(D, E, SMR, SMR/EF, SMR*EF), 2)</pre>
```

[1] 137.00 26.62 5.15 4.35 6.08

6. Fit model for SMR

```
m <- glm( d_iap ~ 1+offset(log(e_iap)),
  family=poisson, data=nickLew.ap )
round( ci.exp( m ), 2 )</pre>
```

```
exp(Est.) 2.5% 97.5% (Intercept) 5.15 4.35 6.08
```

6. Fit model for SMR by age group

```
nickLew.ap$agegrp <- cut(nickLew.ap$age,c(20,50,65,100),right=F)
m <- glm( d_iap ~ -1+agegrp+offset(log(e_iap)),
  family=poisson, data=nickLew.ap )
round( ci.exp( m ), 2 )</pre>
```

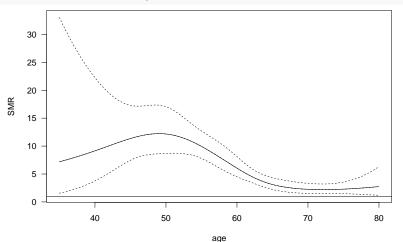
```
exp(Est.) 2.5% 97.5% agegrp[20,50) 11.13 6.32 19.60 agegrp[50,65) 8.42 6.80 10.41 agegrp[65,100) 2.59 1.90 3.53
```

6. Fit model for SMR using popEpi package

```
library(popEpi)
nickLew.ap$ref.rate <- nickLew.ap$e_iap/nickLew.ap$y_iap
m <- sir( coh.data = nickLew.ap, coh.obs = 'd_iap', coh.pyrs = 'y_iap',
          ref.data = nickLew.ap, ref.rate = 'ref.rate',
          adjust = c('age', 'year'), print = 'agegrp', conf.type = "wald")
m
SIR (adjusted by age, year) with 95% confidence intervals (wald)
Test for homogeneity: p < 0.001
Total sir: 5.15 (4.32-6.08)
Total observed: 137
Total expected: 26.62
Total person-years: 15199
    agegrp observed expected pyrs sir sir.lo sir.hi p value
1: [20,50)
                 12 1.08 4576.71 11.13 6.32 19.60
2: [50,65)
              85 10.10 6864.99 8.42 6.80 10.41
                                                            0
3: [65,100)
           40 15.45 3757.27 2.59 1.90 3.53
                                                            0
```

6. Fit model for SMR using popEpi package

```
m <- sirspline(
  coh.data = nickLew.ap, coh.obs = 'd_iap', coh.pyrs = 'y_iap',
  ref.data = nickLew.ap, ref.rate = 'ref.rate',
  adjust = c('age', 'year'), spline = 'age', knots=5, subset = age>30)
plot(m, conf.int = F)
lines(m, conf.int = T, lty=2)
```



Concluding remarks

- ▶ If specific exposure factors exist that have variable values within the target cohort, the estimation of rate ratios associated with them may be efficiently adjusted for age and calendar period by taking the age- and period-specific expected number as the baseline in Poisson-modelling.
- Follow-up time could be split yet by another relevant time axis, like time passed since start of exposure, which may be taken as an explanatory variable when modelling the effects of exposure within a cohort.
- The main challenge is to identify a sufficiently comparable reference population. The "general" population is rarely an ideal one.