Control Lab
ECSE 403 Fall 2020
Lab assignment1
Instructore: Prof. Caines
Due 25th September 2020

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1 Objective

The main goal of this assignment is to review some concepts from the linear control course (ECSE 307), and to become familiar with some useful tools in MATLAB which helps us in designing and implementing controllers.

2 Your duty

Your duty is to answer all questions which have been asked throughout this assignment and submit all your answers in addition to MATLAB codes in MyCourses website. You should submit one single PDF or MATLAB executable notebook file.

3 Model Description

The final goal of this lab is to model and control an inverted pendulum system. In that system the input is applied to a DC motor connected to a cart-pole. The first step to model the whole system is to model the DC motor. The equation of motion of a DC motor can be described by:

$$J_m \ddot{\theta} + (b + \frac{K_t K_e}{R_a})\dot{\theta} = \frac{K_t}{R_a} v_a$$

where θ is the shaft angle (in radians) of the motor and v_a is the applied voltage. System's parameters are as following:

- $J_m = 0.01 kgm^2$ be the inertia of the rotor and the shaft.
- b = 0.001 Nmsec be the viscous friction coefficient
- $K_e = 0.02 Vsec$ be the back emf constant
- $K_t = 0.02Nm/A$ be the motor torque constant.
- $R_a = 10\Omega$ be the armsture resistance

Note that using SI units $K_e = K_t$.

4 Questions

- 1. Find the transfer function between the input voltage and the speed of the motor shaft $(\frac{w(s)}{v_a(s)}, \frac{w(s)}{v_a(s)}, \frac{w(s)}{v_a(s)},$
- 2. Using transfer function derived above and matlab, find the steady-state and time constant of the response of the motor to a step function.[10 marks]

Hint: You can use following matlab commands for defining a transfer function: (random coefficient)

$$s = tf('s')$$

 $G = s/(s^2 + 4*s+1)$

Or instead, you can just use polynomial coefficients.

$$G = tf([1 \ 0],[1 \ 4 \ 1])$$

and then use step command:

```
stepplot(G)
```

- 3. Using previous step response find rise time and settling time of the system.[10 marks]
- 4. Using Final Value Theorem, calculate the steady state speed of the motor to step response theoretically. Compare theoretical value and values you found in matlab.[10 marks]
- 5. Find the transfer function between the shaft's angel and input voltage $(\frac{\theta(s)}{v_a(s)})$. (Identify the order of the system with respect to new definition of input-output signals) [10 marks]
- 6. Consider the transfer function in question 1. Apply a unity feedback loop to the system and find the closed loop transfer function[10 marks].
- 7. Suppose a proportional controller is added to the system such that open-loop transfer function has changed from G(s) to K.G(s). Plot the step response of the closed loop unity feedback system choosing $K = \{0.1, 1, 10, 100\}$, in one figure. Describe the effect of proportional gain on step response's behavior [15 marks].

Hint: One way to plot different graphs on one figure is as following:

```
figure (1);
stepplot(h1);
hold on;
stepplot(h2);
.
hold off;
```

8. Consider the transfer function in question 5, repeat steps of question 7 for this system(plot closed loop unity feedback step response). Describe the effect of proportional gain on step response's behavior [15 marks].(In this case you should explain the effect of proportional gain on the overshoot, rise-time, and settling time)