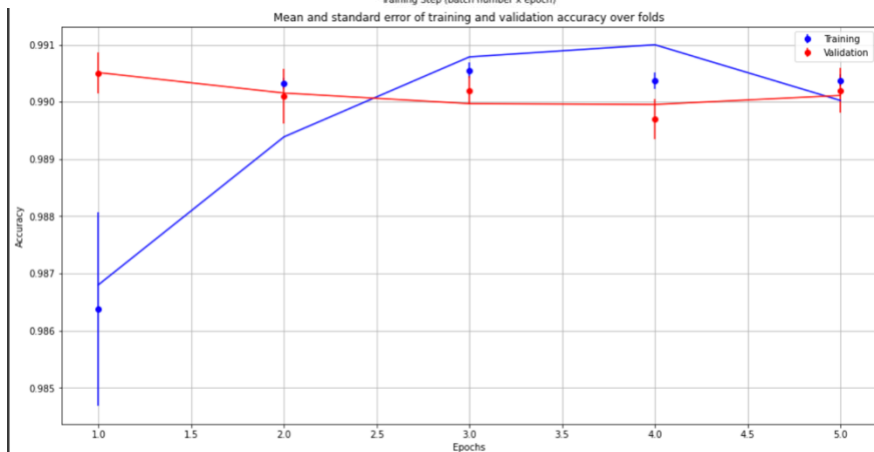
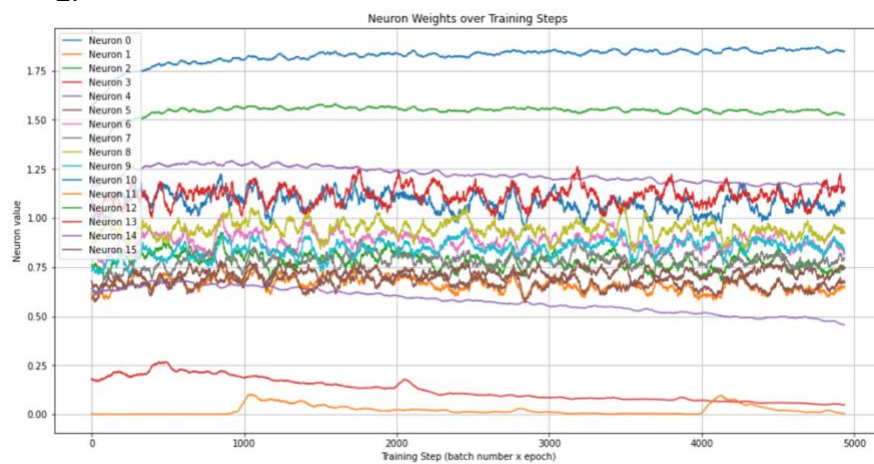


1.

2.



3.

$$J(z) = -\log\left(\frac{1}{1 + \exp(z(1 - 2y))}\right) = \log(1 + \exp(z(1 - 2y)))$$

$$\begin{aligned}\frac{\partial J}{\partial z} &= \frac{1}{1 + \exp(z(1 - 2y))} \cdot \exp(z(1 - 2y)) \cdot (1 - 2y) \\ &= (1 - 2y) \frac{e^{z(1-2y)}}{e^{z(1-2y)} + 1}\end{aligned}$$

i.

$$(1 - 2y) \frac{e^{z(1-2y)}}{e^{z(1-2y)} + 1} \rightarrow -\frac{e^{-z}}{e^{-z} + 1} \approx 0$$

ii.

$$(1 - 2y) \frac{e^{z(1-2y)}}{e^{z(1-2y)} + 1} \rightarrow \frac{e^z}{e^z + 1} \approx 1$$

iii.

$$(1 - 2y) \frac{e^{z(1-2y)}}{e^{z(1-2y)} + 1} \rightarrow -\frac{e^{-z}}{e^{-z} + 1} \approx 1$$

iv.

$$(1 - 2y) \frac{e^{z(1-2y)}}{e^{z(1-2y)} + 1} \rightarrow \frac{e^z}{e^z + 1} \approx 0$$

The derivative of the loss function vanishes when  $z$  is large and positive while  $y=1$  and when  $z$  is large and negative while  $y=0$ . This means that the vanishing gradient may occur for large values of  $z$  which could prevent the effectiveness of gradient decent techniques by stopping changes in model parameters. Since we know that  $z = w^T h + b$ , a possible countermeasure to this problem could be to enforce some regularization penalty to discourage large weights, keeping  $z$  small in magnitude.