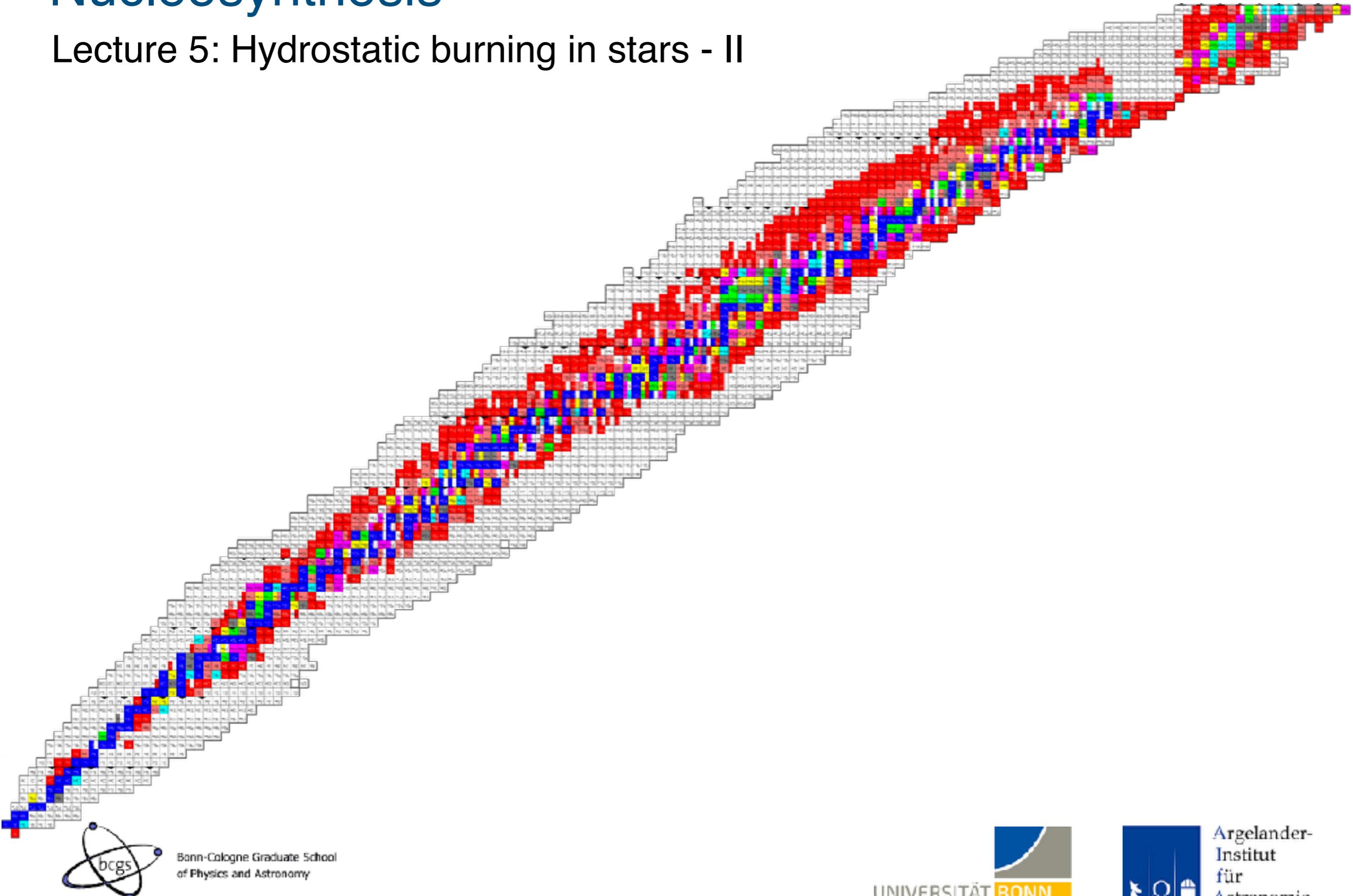


# Nucleosynthesis

## Lecture 5: Hydrostatic burning in stars - II



Bonn-Cologne Graduate School  
of Physics and Astronomy



# Overview

- **Lecture 1:** Introduction & overview
- **Lecture 2:** Thermonuclear reactions
- **Lecture 3:** Big-bang nucleosynthesis
- **Lecture 4:** Thermonuclear reactions inside stars – I (H-burning)
- **Lecture 5:** Thermonuclear reactions inside stars – II (advanced burning)
- **Lecture 6:** Neutron-capture and supernovae – I
- **Lecture 7:** Neutron-capture and supernovae – II
- **Lecture 8:** Thermonuclear supernovae
- **Lecture 9:** Li, Be and B
- **Lecture 10:** Galactic chemical evolution and relation to astrobiology

**Paper presentations I**

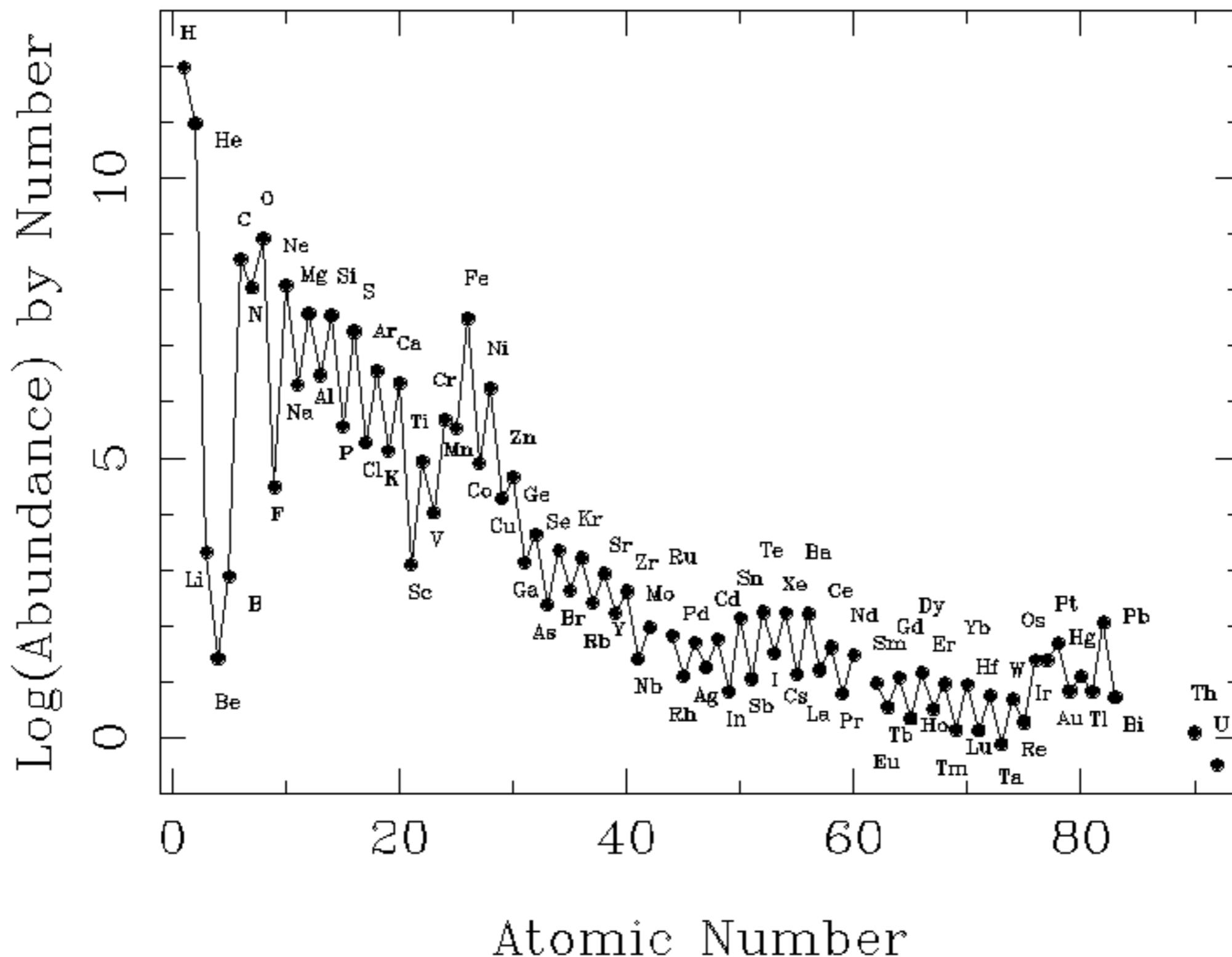
**June 21**

**Paper presentations II**

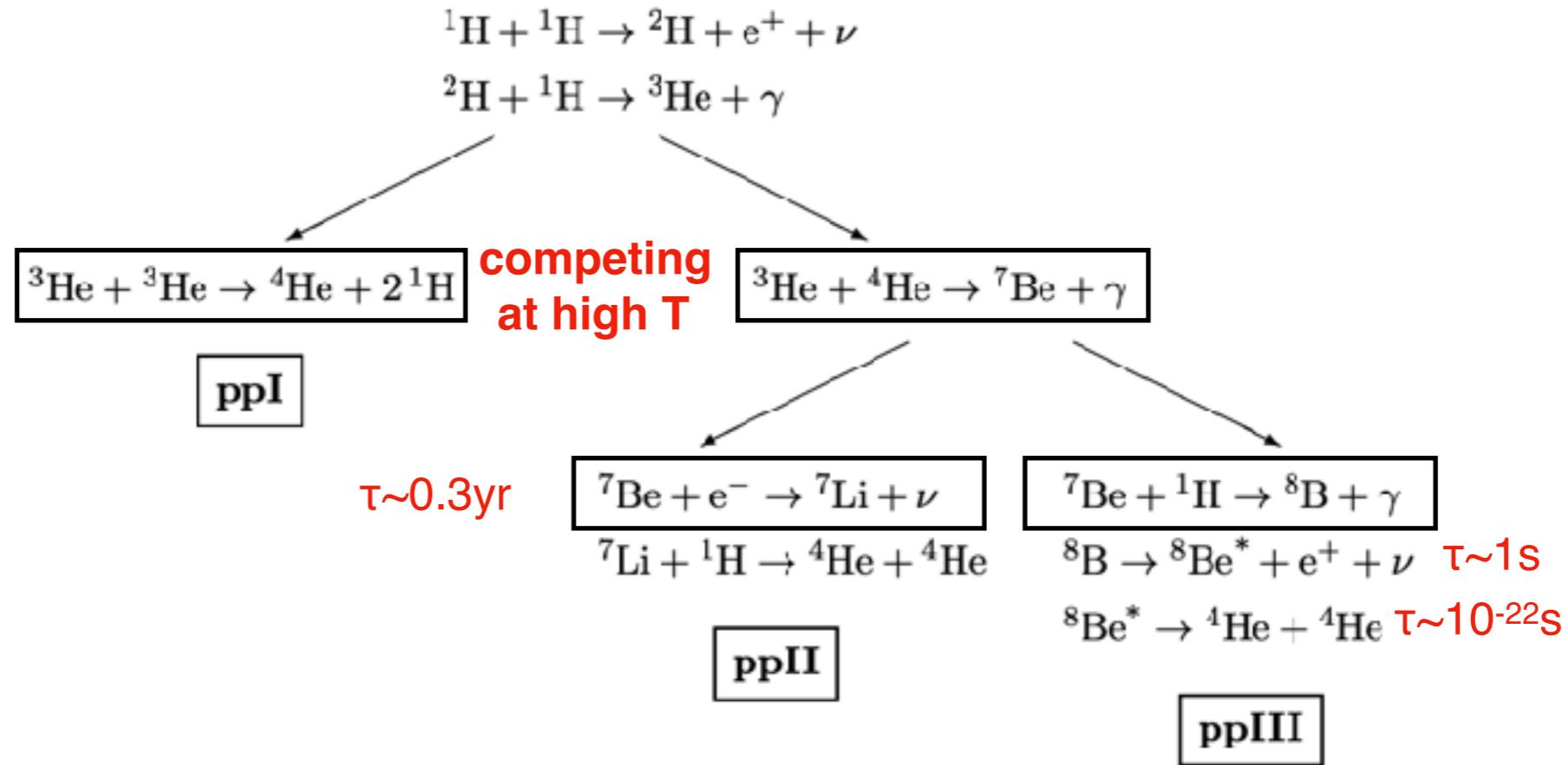
**June 28**

## Overview of previous lectures

Logarithmic SAD Abundances:  $\text{Log}(\text{H}) = 12.0$

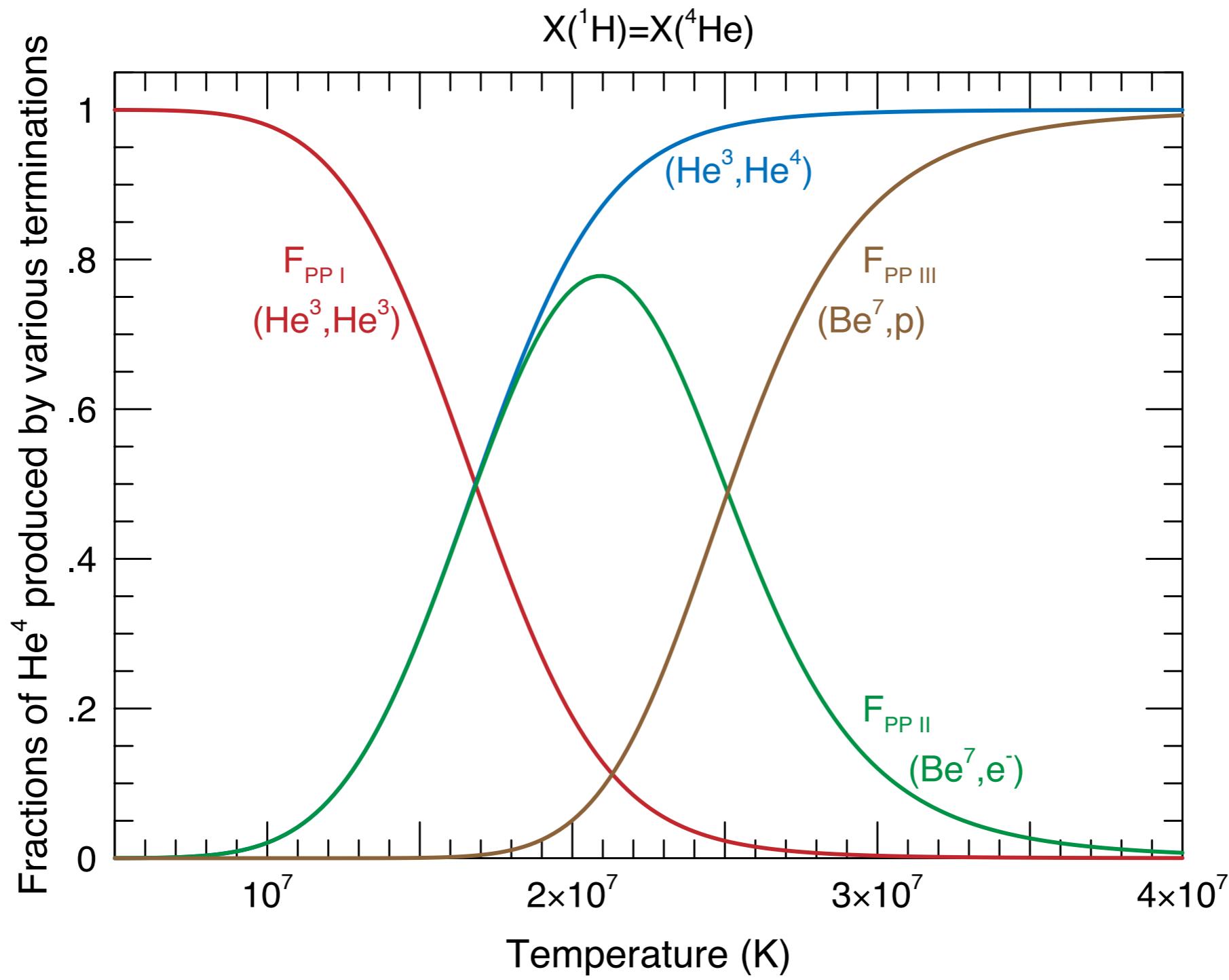


# pp chains



reaction	$Q$ (MeV)	$\langle E_\nu \rangle$ (MeV)	$S(0)$ (keV barn)	$dS/dE$ (barn)	$\tau$ (yr)
${}^1\text{H}(\text{p}, \text{e}^+ \nu) {}^2\text{H}$	1.442	0.265	$3.94 \times 10^{-22}$	$4.61 \times 10^{-24}$	$10^{10}$
${}^2\text{H}(\text{p}, \gamma) {}^3\text{He}$	5.493		$2.5 \times 10^{-4}$	$7.9 \times 10^{-6}$	$10^{-8}$
${}^3\text{He}({}^3\text{He}, 2\text{p}) {}^4\text{He}$	12.860		$5.18 \times 10^3$	$-1.1 \times 10^1$	$10^5$
${}^3\text{He}(\alpha, \gamma) {}^7\text{Be}$	1.587		$5.4 \times 10^{-1}$	$-3.1 \times 10^{-4}$	$10^6$
${}^7\text{Be}(\text{e}^-, \nu) {}^7\text{Li}$	0.862	0.814			$10^{-1}$
${}^7\text{Li}(\text{p}, \alpha) {}^4\text{He}$	17.347		$5.2 \times 10^1$	0	$10^{-5}$
${}^7\text{Be}(\text{p}, \gamma) {}^8\text{B}$	0.137		$2.4 \times 10^{-2}$	$-3 \times 10^{-5}$	$10^2$
${}^8\text{B}(\text{e}^+ \nu) {}^8\text{Be}^*(\alpha) {}^4\text{He}$	18.071	6.710			$10^{-8}$

## pp chains



# The CNO cycles

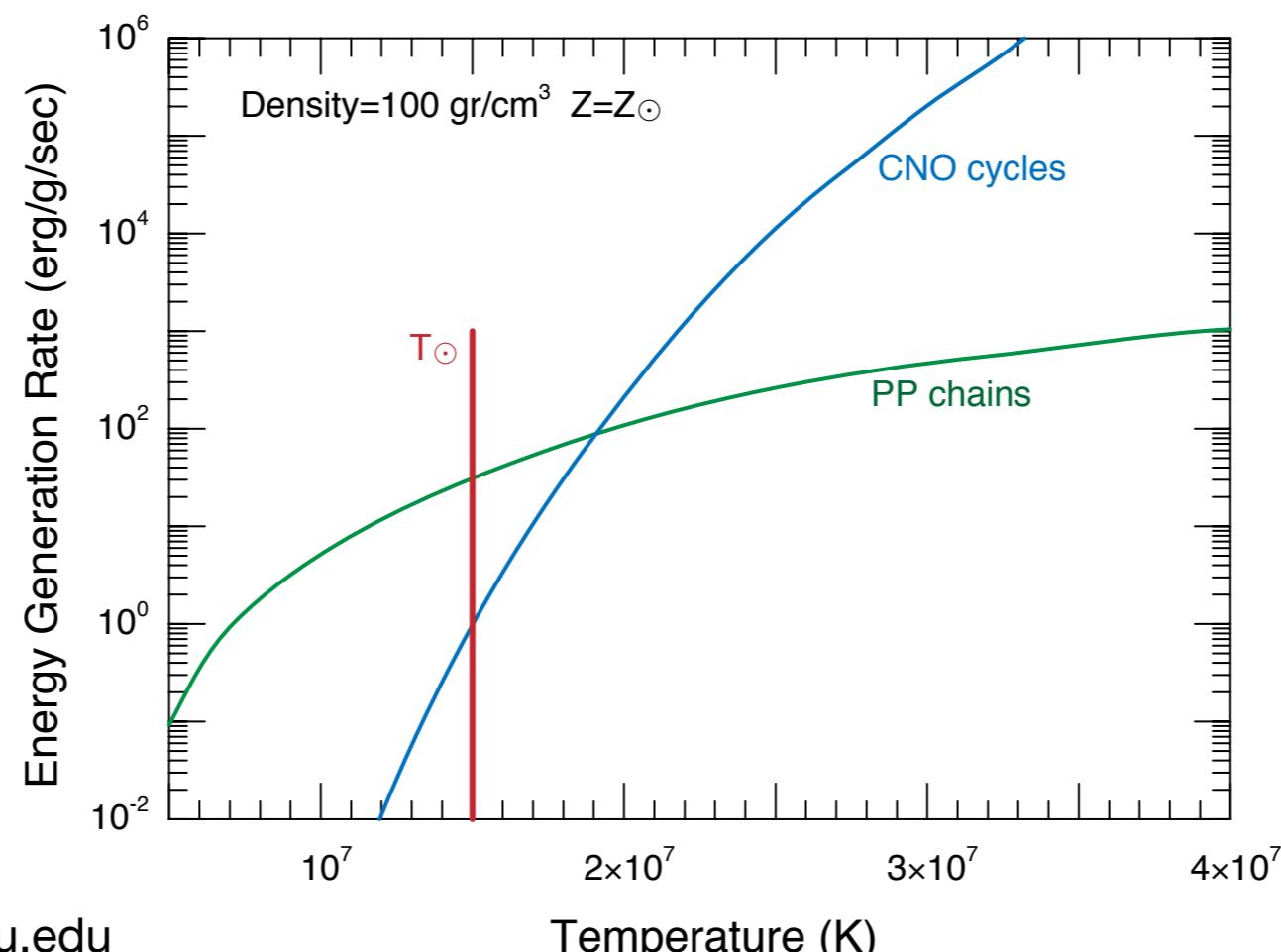
The pp chains can operate in pure H/He gasses to synthesise  ${}^4\text{He}$  from H. However, stars like our Sun also have a healthy admixture of heavier elements. Therefore, it becomes necessary to consider other reactions as possible sources of energy, even at “low” central temperatures typical on the main sequence.

Since lifetimes rise rapidly with increasing coulomb barrier, the best candidates must have charges such that the product  $Z_1 Z_2$  is as small as possible

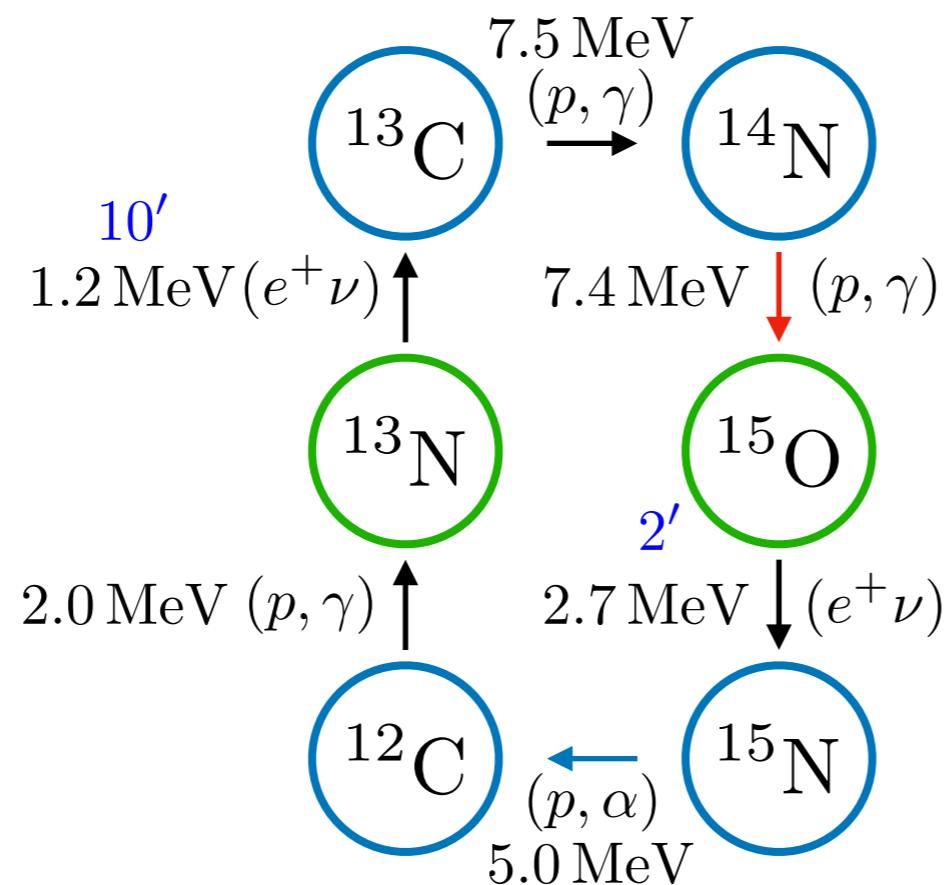
A series of such reactions, involving C and N nuclei was discovered by **Bethe & von Weizsäcker (1938)**

This series has the property that the CN nuclei serve only as catalysts for the conversion of H to He

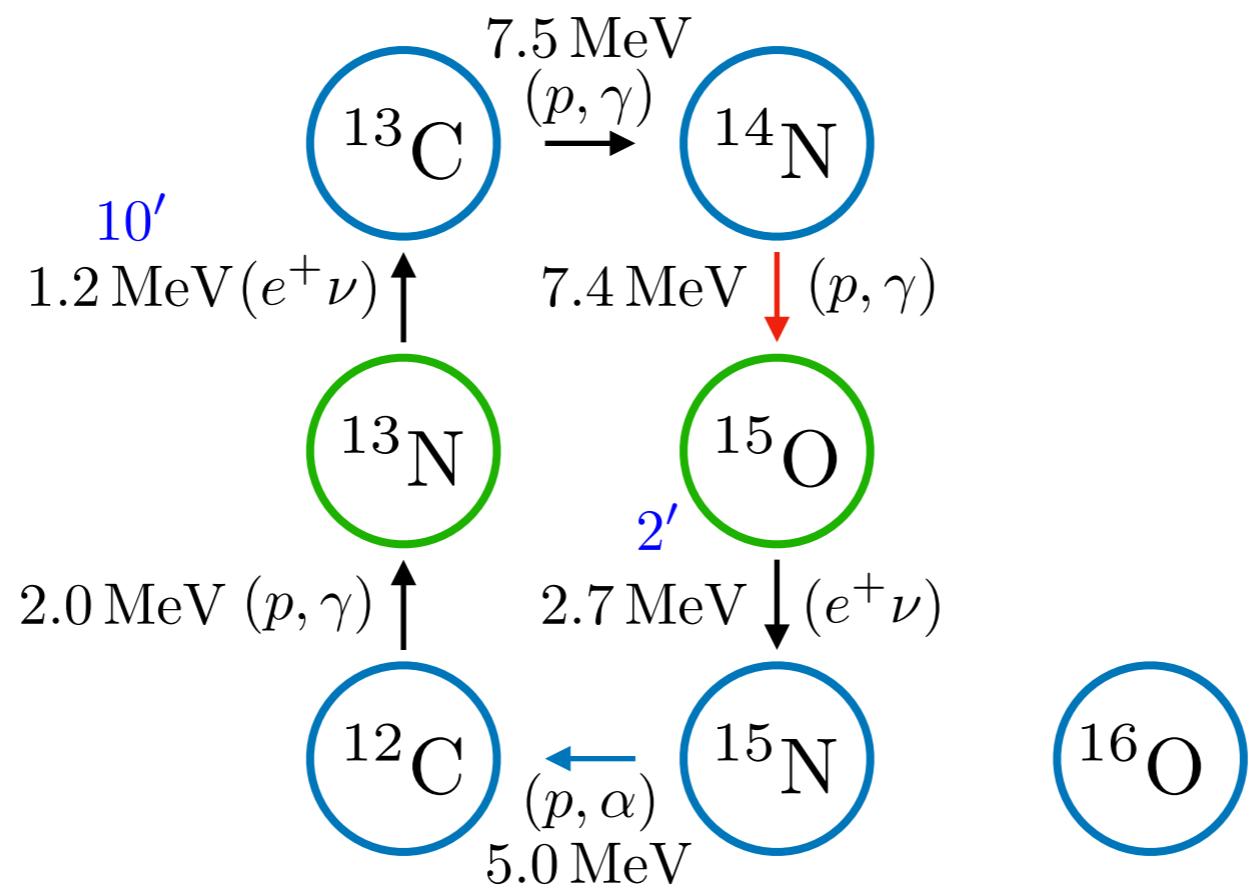
For solar composition, the CN cycle produces more energy than the pp-chains for  $T_6 > \sim 20$ ,



# The CNO reaction flow and branching



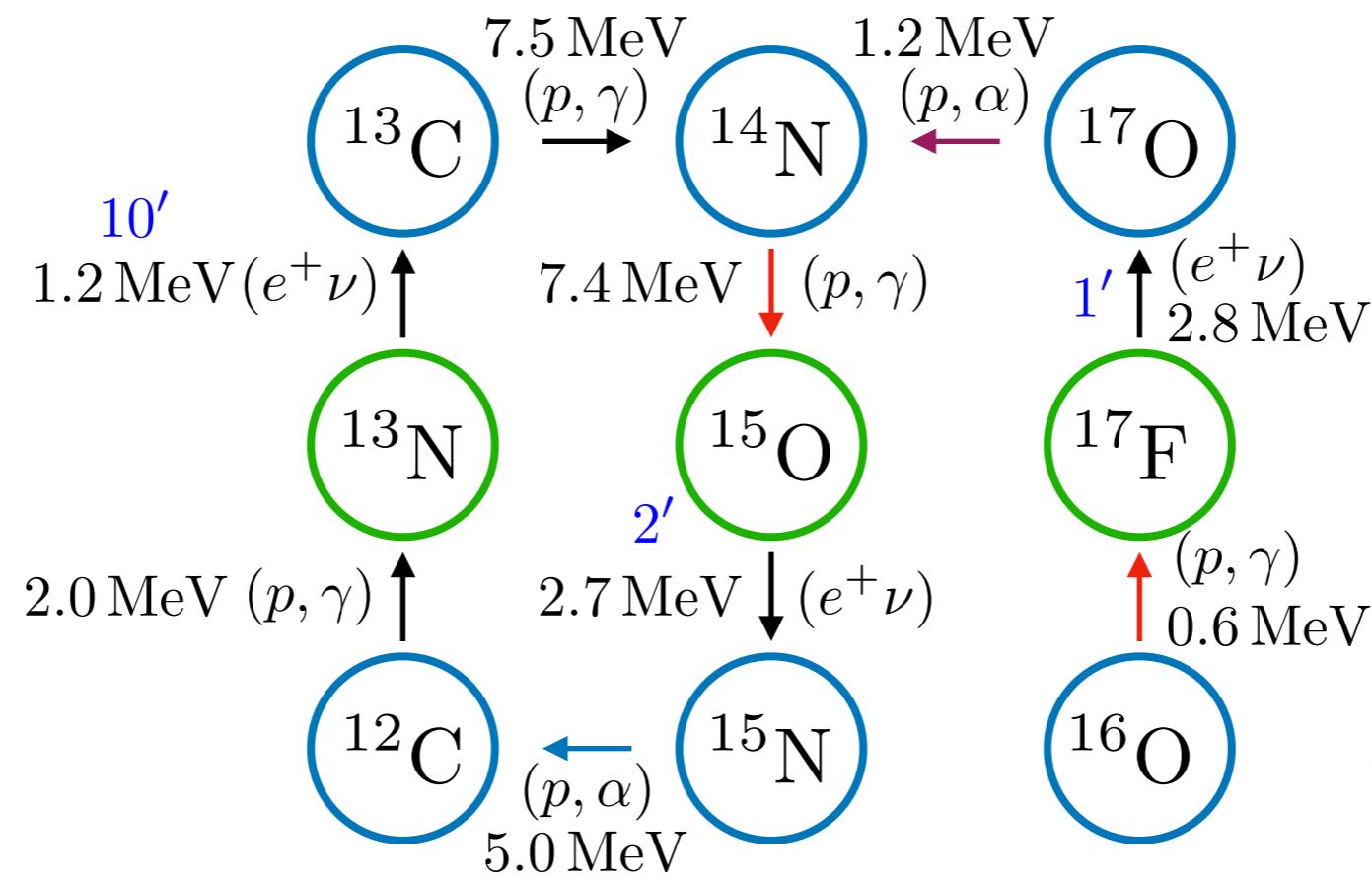
# The CNO reaction flow and branching



Second cycle initiated  
when oxygen is present



# The CNO reaction flow and branching

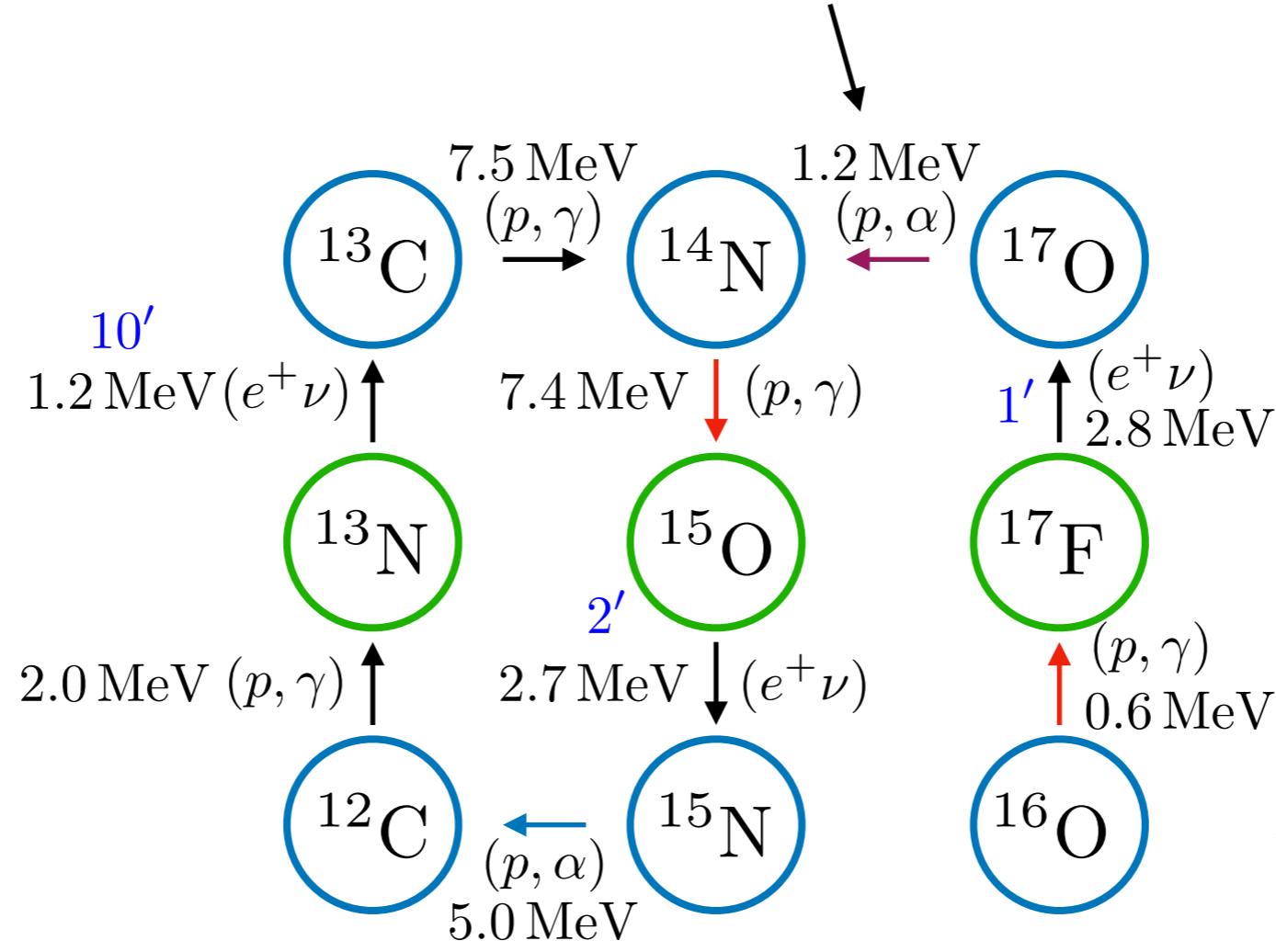


Second cycle initiated  
when oxygen is present



# The CNO reaction flow and branching

This is the first resonant reaction  
that we encounter! The resonance becomes  
important at relatively high T

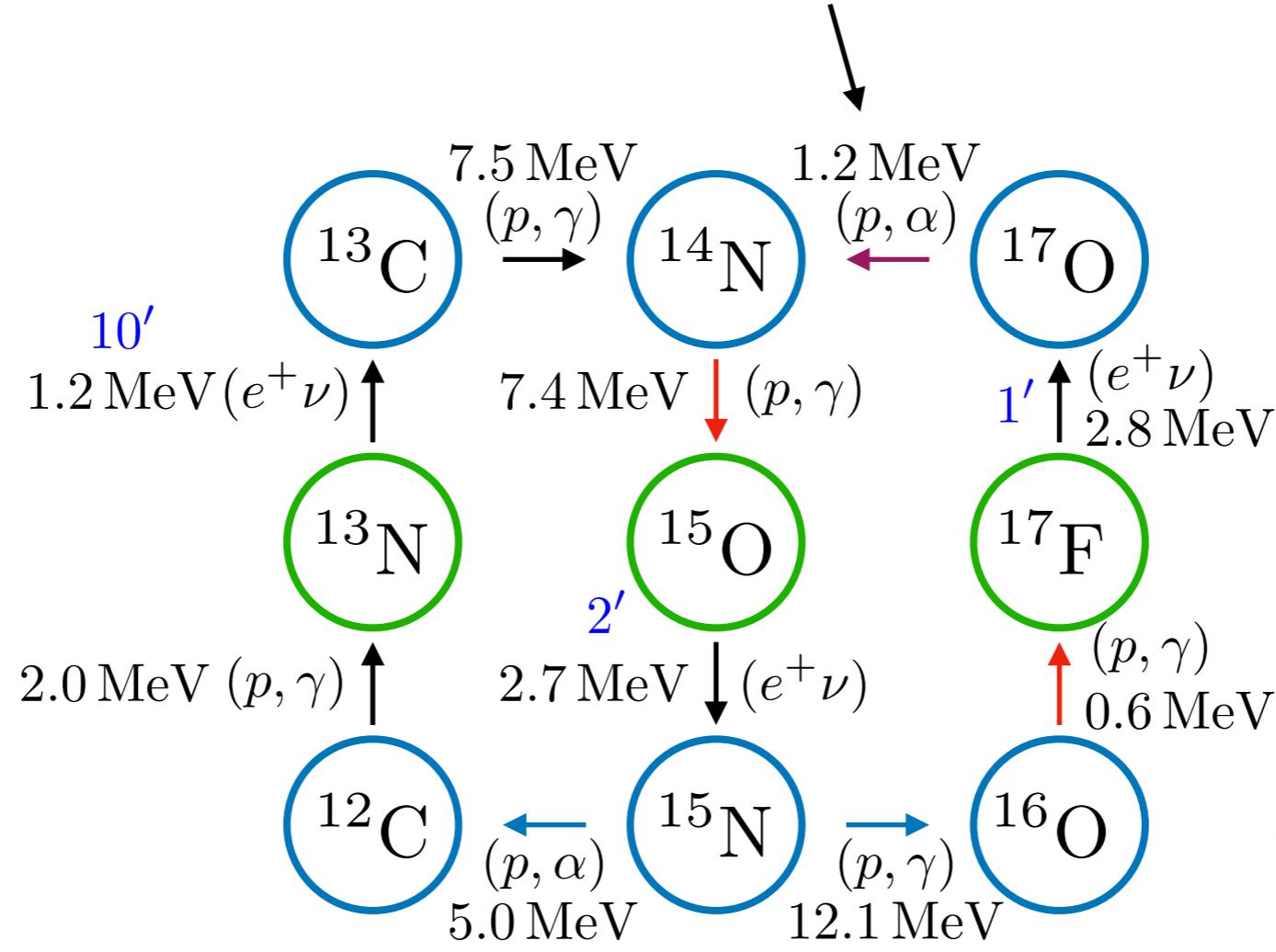


Second cycle initiated  
when oxygen is present



# The CNO reaction flow and branching

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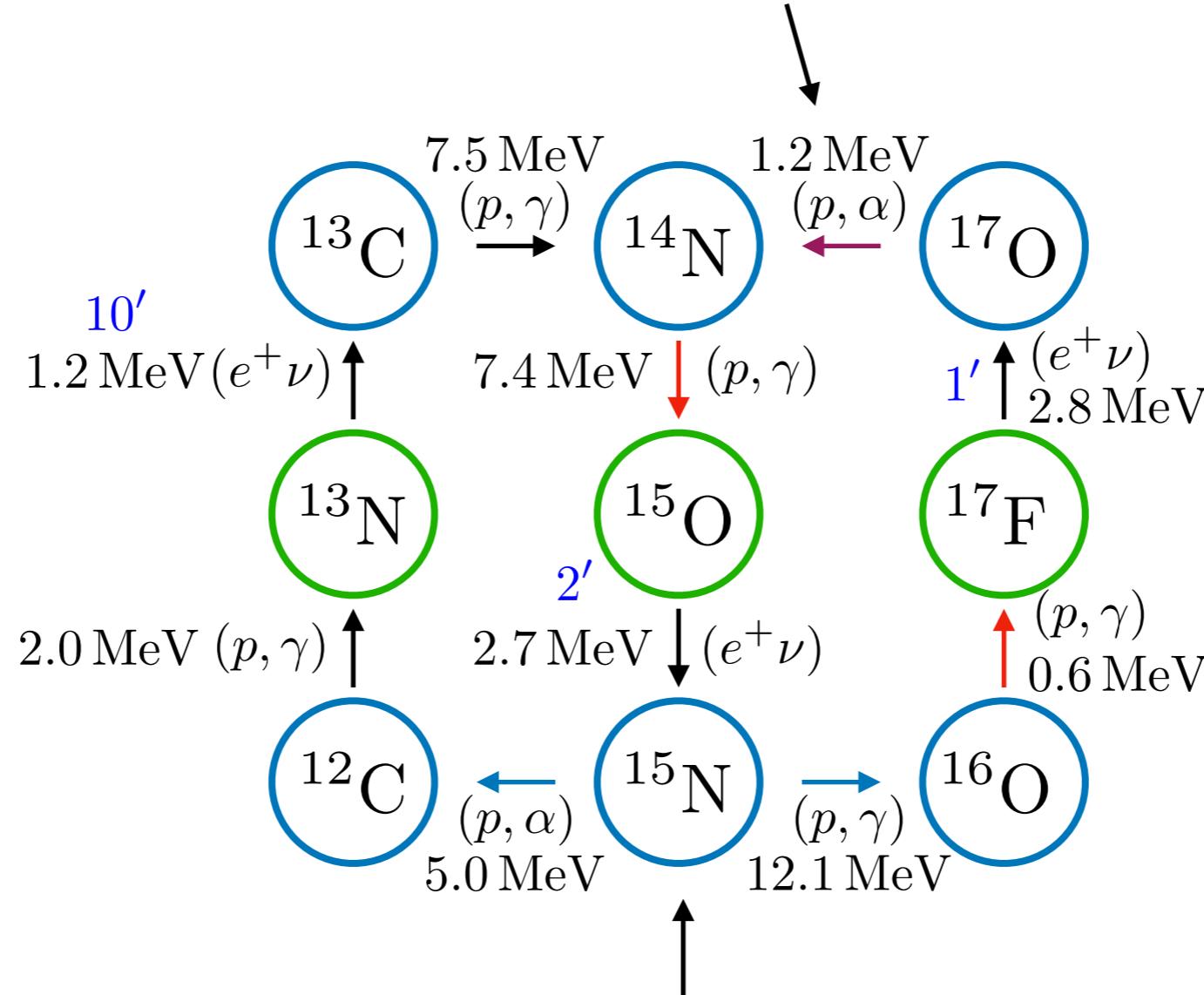


Second cycle initiated  
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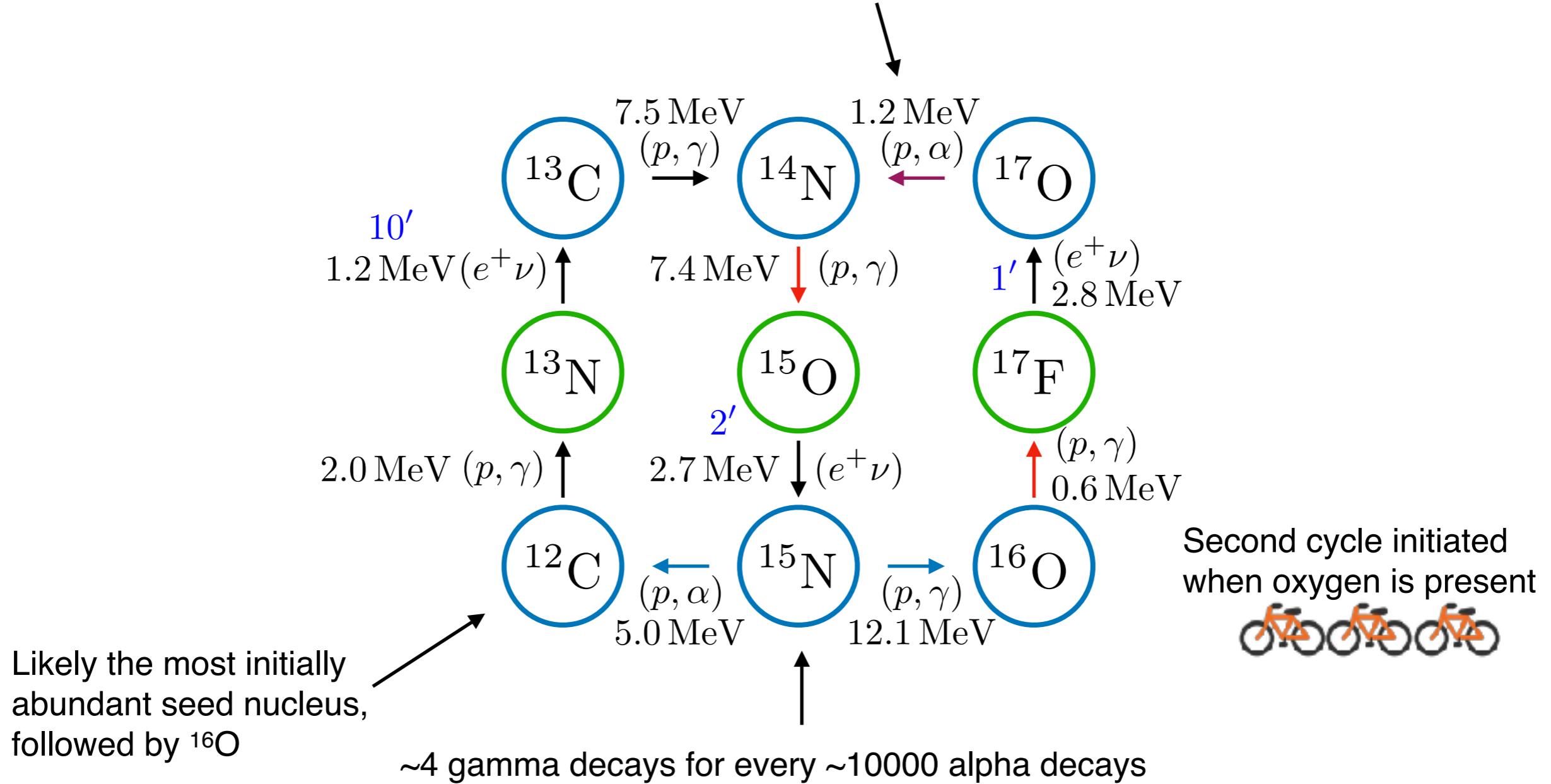
Second cycle initiated  
when oxygen is present



~4 gamma decays for every ~10000 alpha decays

# The CNO reaction flow and branching

This is the first resonant reaction that we encounter! The resonance becomes important at relatively high T



## The CNO bi-cycles

Just like in pp reactions, the key to understanding the CNO reactions lies in appreciating the lifetimes of nuclei against protons. Recall that for non-resonant reactions, the lifetime of a nucleus against proton capture is:

$$\frac{1}{\tau_p(X)} = 2.4 \times 10^{16} \rho X_H f S_0 \left[ \frac{(A_X + 1)Z_X}{A_X} \right]^{1/3} T_6^{-2/3} \left( 1 + \frac{5}{12BT_6^{1/3}} \right) \exp(-BT_6^{-1/3}) \text{ yr}^{-1}$$

where  $S_0 = S(0) + \frac{dS}{dE} \left[ 1.22 \left( \frac{Z_X A_X T_6}{A_X + 1} \right)^{1/3} + 0.072 T_6 \right]$ ;  $B = 42.48(Z_X^2 A_X)^{1/3}$

reaction	$Q$ (MeV)	$\langle E_\nu \rangle$ (MeV)	$S(0)$ (MeV barn)	$dS/dE$ (barn)	$\tau$ (yr)
$^{12}\text{C}(\text{p}, \gamma)^{13}\text{N}$	1.944		$1.45 \times 10^{-3}$	$2.45 \times 10^{-3}$	$6.6 \times 10^3$
$^{13}\text{N}(\text{e}^+ \nu)^{13}\text{C}$	2.220	0.707			863 s
$^{13}\text{C}(\text{p}, \gamma)^{14}\text{N}$	7.551		$5.50 \times 10^{-3}$	$1.34 \times 10^{-2}$	$1.6 \times 10^3$
$^{14}\text{N}(\text{p}, \gamma)^{15}\text{O}$	7.297		$3.32 \times 10^{-3}$	$-5.91 \times 10^{-3}$	$9.3 \times 10^5$
$^{15}\text{O}(\text{e}^+ \nu)^{15}\text{N}$	2.754	0.997			176 s
$^{15}\text{N}(\text{p}, \alpha)^{12}\text{C}$	4.965		$7.80 \times 10^1$	$3.51 \times 10^2$	$3.5 \times 10^1$
$^{15}\text{N}(\text{p}, \gamma)^{16}\text{O}$	12.127		$6.4 \times 10^{-2}$	$3 \times 10^{-2}$	$3.9 \times 10^4$
$^{16}\text{O}(\text{p}, \gamma)^{17}\text{F}$	0.600		$9.4 \times 10^{-3}$	$-2.3 \times 10^{-2}$	$7.1 \times 10^7$
$^{17}\text{F}(\text{e}^+ \nu)^{17}\text{O}$	2.761	0.999			93 s
$^{17}\text{O}(\text{p}, \alpha)^{14}\text{N}$	1.192		resonant reaction		$1.9 \times 10^7$

**WARNING: Most of these are outdated. For more recent values see Adelberger et al. 2011**

# CNO cycles approaching equilibrium

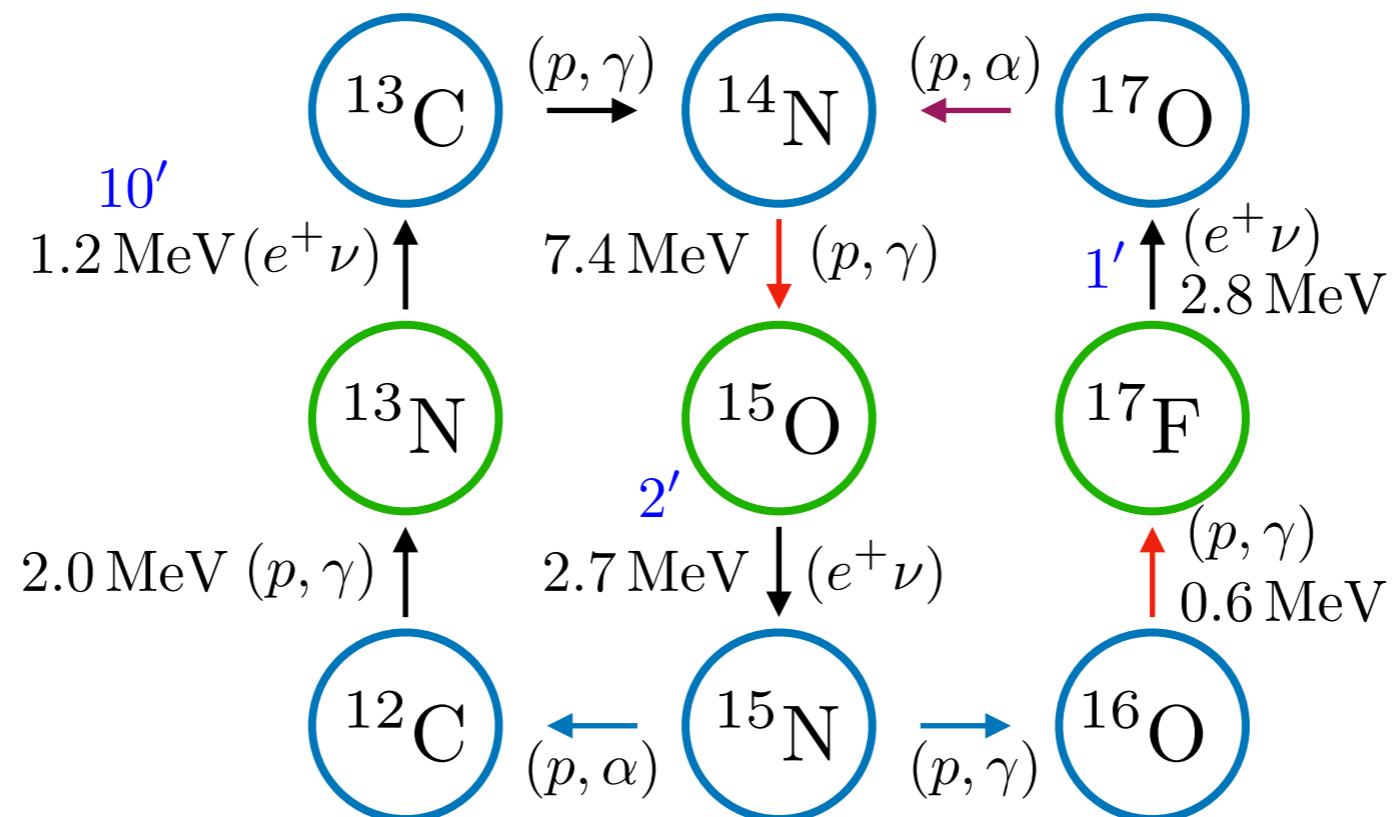
$$\tau_p(15) \ll \tau_p(13) \ll \tau_p(12) \ll \tau_p(14) : 35 \text{ yr} : 1600 \text{ yr} : 6600 \text{ yr} : 9 \times 10^5 \text{ yr}$$

To follow the abundance evolution, one needs to consider the differential equations for all reactants. Fortunately, some simplifications can be made due to the vastly different lifetimes.

It would help if the two cycles were independent. This would be the case if  $X(16\text{O})=0$  and  $^{15}\text{N}(p,\alpha)^{12}\text{C}$  only. Turns out we can treat them independently anyways!

Why?

In cycle I, the  $^{14}\text{N}(p,\gamma)^{15}\text{O}$  reaction determines the cycle speed. A  $^{15}\text{N}$  nucleus is produced every  $\tau_{14}$  years. One in every  $\sim 2500$  of these nuclei go to the second cycle. Similarly a  $^{14}\text{N}$  is produced by cycle II every  $\tau_{16}$  yr. Both these times are much longer than the  $\tau_{14}$



# CNO cycles approaching equilibrium

## Consequences

Cycle I reaches equilibrium much faster than Cycle II, and thus it can be treated independently.

When analysing Cycle II we can assume that  $^{14}\text{N}$  and  $^{15}\text{N}$  have reached their equilibrium abundances.

The ODEs for Cycle I are as follows. The  $\beta^+$  decays are taken to be instantaneous since the products reach their equilibrium abundances very fast, in times of order  $\tau_\beta$  (sec).

$$\frac{d^{15}\text{N}}{dt} = H \left( ^{14}\text{N} \langle \sigma v \rangle_{14} - ^{15}\text{N} \langle \sigma v \rangle_{15} \right)$$

$$\frac{d^{12}\text{C}}{dt} = H \left( ^{15}\text{N} \langle \sigma v \rangle_{15} - ^{12}\text{C} \langle \sigma v \rangle_{12} \right)$$

$$\frac{d^{13}\text{C}}{dt} = H \left( ^{12}\text{C} \langle \sigma v \rangle_{12} - ^{13}\text{C} \langle \sigma v \rangle_{13} \right)$$

$$\frac{d^{14}\text{N}}{dt} = H \left( ^{13}\text{C} \langle \sigma v \rangle_{13} - ^{14}\text{N} \langle \sigma v \rangle_{14} \right)$$

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$$\boxed{\frac{d^{15}\text{N}}{dt} = H \left( ^{14}\text{N} \langle \sigma v \rangle_{14} - ^{15}\text{N} \langle \sigma v \rangle_{15} \right)} \rightarrow \left( \frac{^{15}\text{N}}{^{14}\text{N}} \right)_e = \frac{\tau_{15}}{\tau_{14}} = 4 \times 10^{-5}$$

$$\frac{d^{12}\text{C}}{dt} = H \left( ^{15}\text{N} \langle \sigma v \rangle_{15} - ^{12}\text{C} \langle \sigma v \rangle_{12} \right) \quad \text{In times of order } \tau_{15} \text{ (years)}$$

$$\frac{d^{13}\text{C}}{dt} = H \left( ^{12}\text{C} \langle \sigma v \rangle_{12} - ^{13}\text{C} \langle \sigma v \rangle_{13} \right)$$

$$\frac{d^{14}\text{N}}{dt} = H \left( ^{13}\text{C} \langle \sigma v \rangle_{13} - ^{14}\text{N} \langle \sigma v \rangle_{14} \right)$$

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$$\frac{d}{dt} \left( \begin{array}{c} \cancel{\frac{d^{15}\text{N}}{dt}} \\ \frac{d^{12}\text{C}}{dt} \\ \frac{d^{13}\text{C}}{dt} \\ \frac{d^{14}\text{N}}{dt} \end{array} \right) = H \left( \begin{array}{c} {}^{14}\text{N} \langle \sigma v \rangle_{14} - {}^{15}\text{N} \langle \sigma v \rangle_{15} \\ {}^{15}\text{N} \langle \sigma v \rangle_{15} - {}^{12}\text{C} \langle \sigma v \rangle_{12} \\ {}^{12}\text{C} \langle \sigma v \rangle_{12} - {}^{13}\text{C} \langle \sigma v \rangle_{13} \\ {}^{13}\text{C} \langle \sigma v \rangle_{13} - {}^{14}\text{N} \langle \sigma v \rangle_{14} \end{array} \right) \rightarrow \left( \frac{{}^{15}\text{N}}{{}^{14}\text{N}} \right)_e = \frac{\tau_{15}}{\tau_{14}} = 4 \times 10^{-5}$$

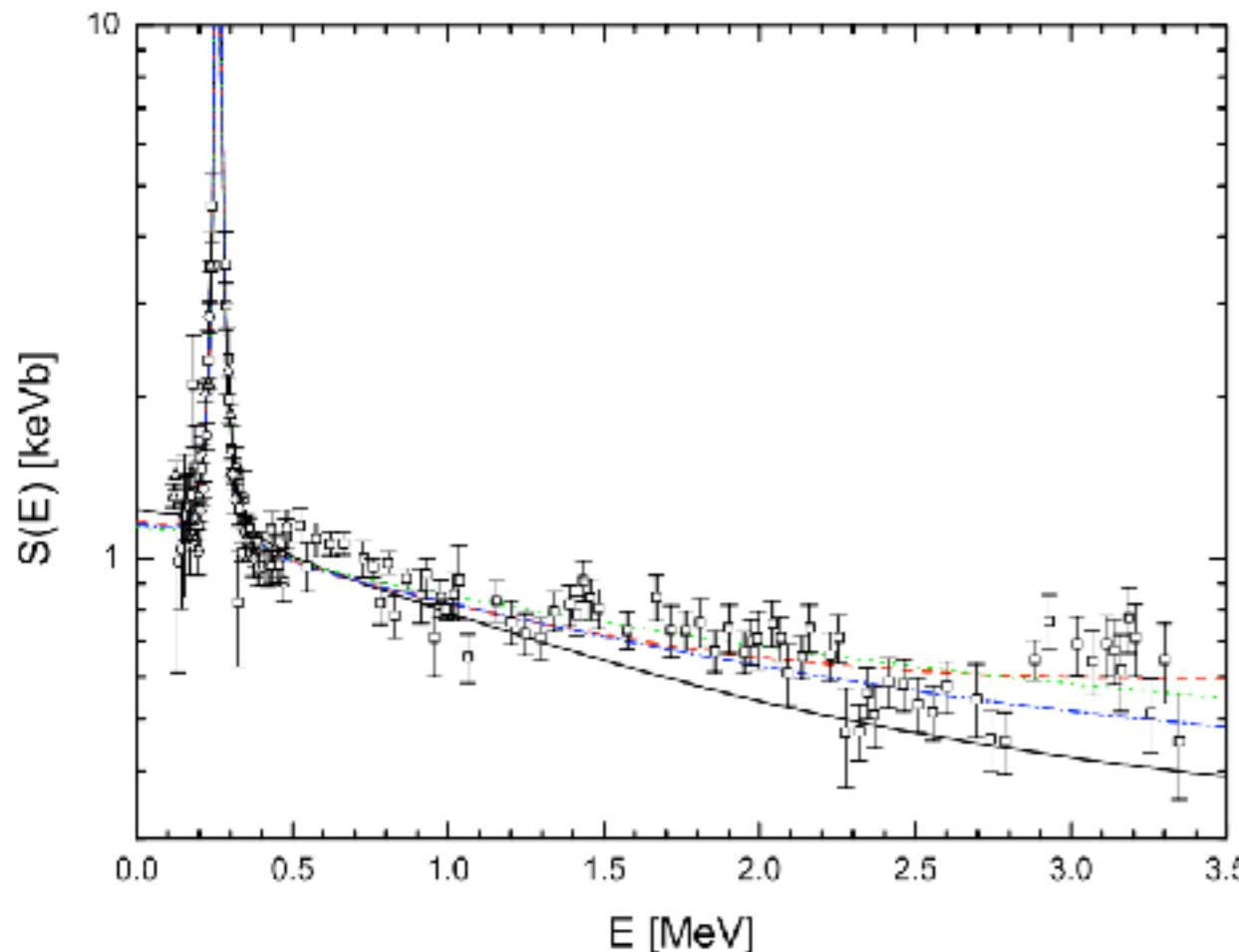
In times of order  $\tau_{15}$  (years)

On earth:  $\left( \frac{{}^{15}\text{N}}{{}^{14}\text{N}} \right)_{\text{earth}} \simeq 4 \times 10^{-3}$  What could be the reason for the discrepancy?

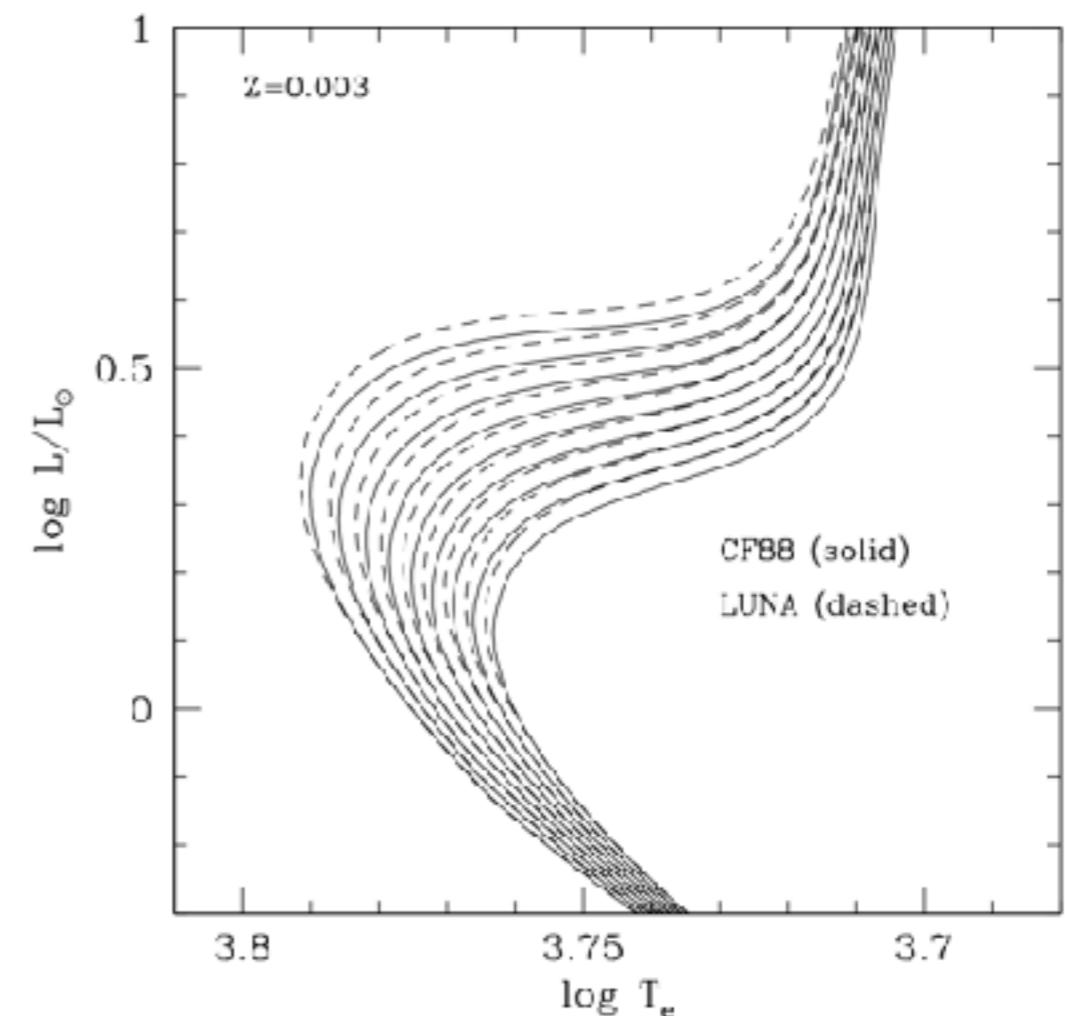
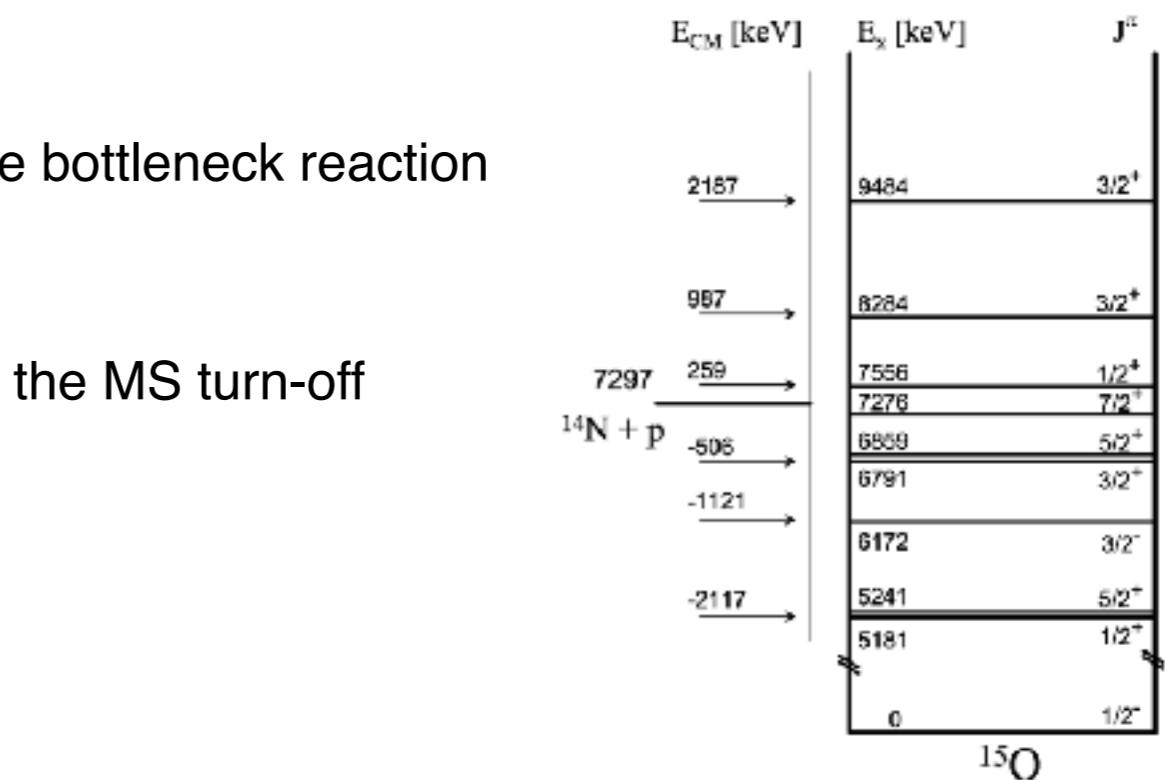
# CNO cycles approaching equilibrium

One possible reason could be a hidden resonance in the bottleneck reaction  $^{14}\text{N}(\text{p},\gamma)^{15}\text{O}(\text{,e+ v})^{15}\text{N}$ , producing more  $^{15}\text{N}$

This would also affect the age determination of GCs via the MS turn-off

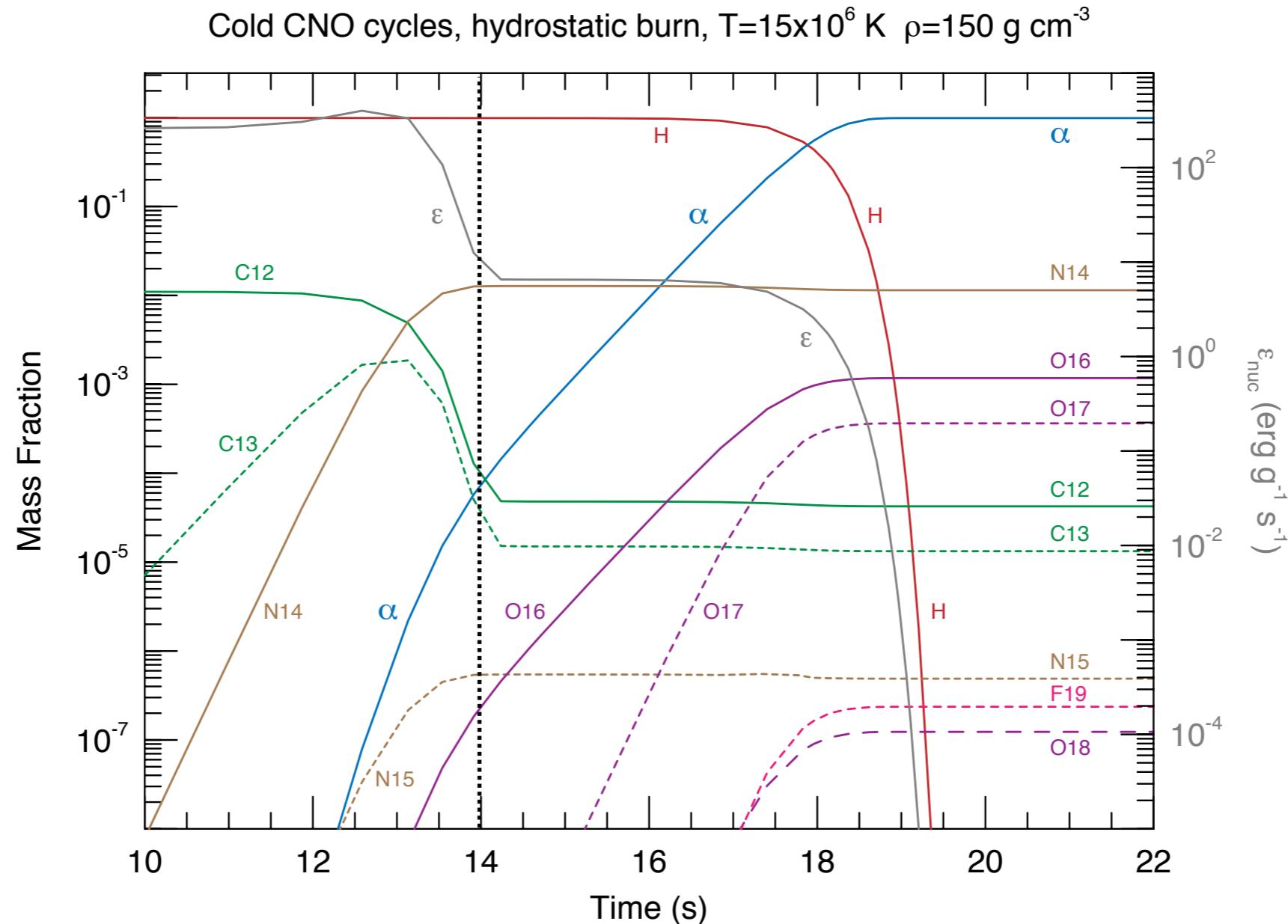


No evidence for resonances at low energies.  
Some at high energy could influence explosive burning



## CNO cycles approaching equilibrium

Similar analysis can be performed for the remaining three ODEs (see CLAYTON for a detailed discussion). Once CNO-I reaches equilibrium, the same analysis can follow for CNO-II, adopting the CNO-I equilibrium abundances



CNO-I: C12 is the last to reach equilibrium. N14 is strongly produced

CNO-II: O16 is the last to reach equilibrium. N14 and O16 produced

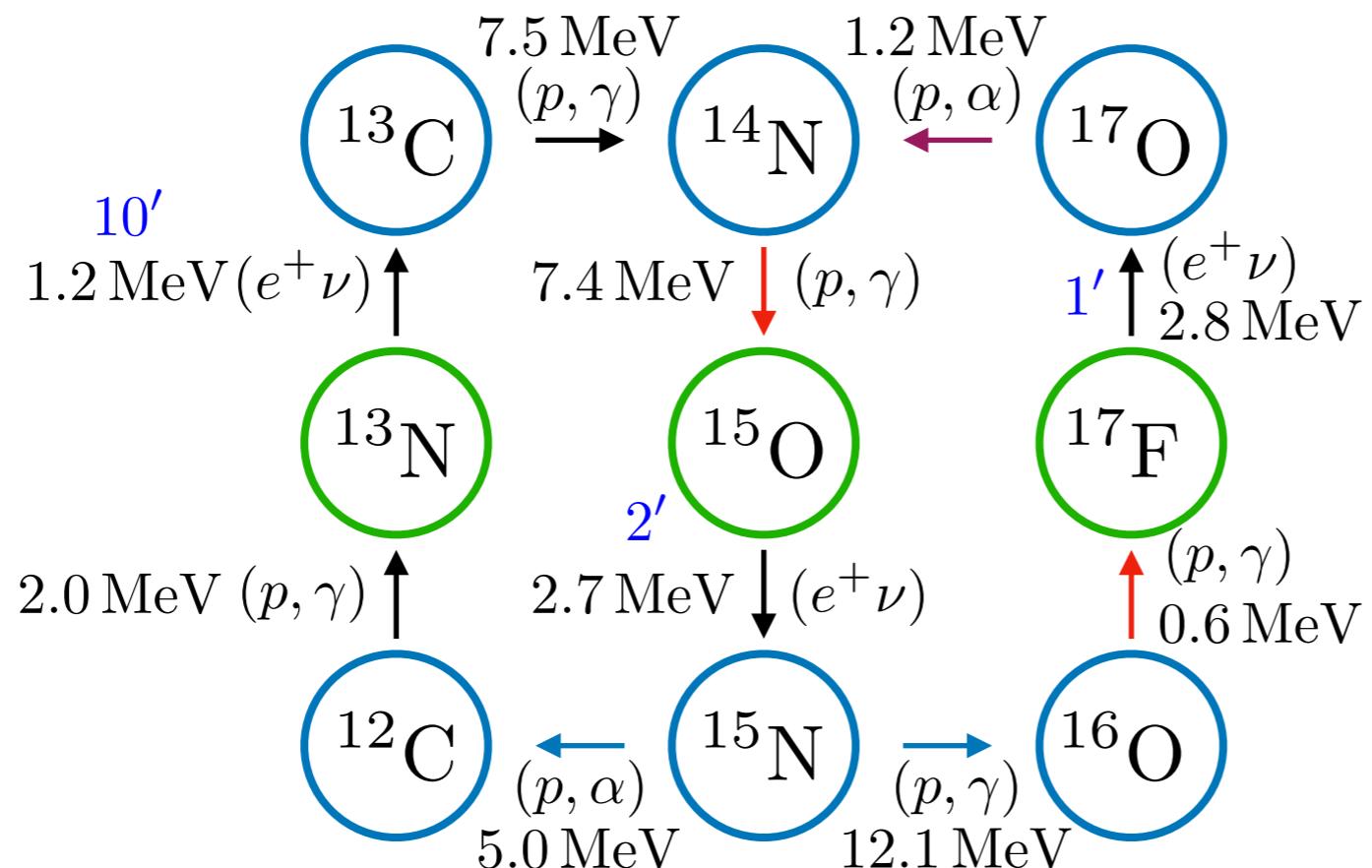
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	$^{12}\text{C}$	$^{13}\text{C}$	$^{14}\text{N}$	$^{15}\text{N}$	$^{16}\text{O}$	$^{17}\text{O}$	$^{18}\text{O}$	$^{19}\text{F}$
equil. mass fraction $(Z = 2\%, T = 3 \cdot 10^7 \text{ K})$	$10^{-4}$	$6 \cdot 10^{-5}$	$10^{-2}$	$3 \cdot 10^{-7}$	$3 \cdot 10^{-4}$	$4 \cdot 10^{-6}$	$10^{-9}$	$10^{-9}$
solar mass fraction	$3.5 \cdot 10^{-3}$	$4 \cdot 10^{-5}$	$10^{-3}$	$4 \cdot 10^{-6}$	$10^{-2}$	$4 \cdot 10^{-6}$	$2 \cdot 10^{-5}$	$4 \cdot 10^{-7}$
ratio	$\frac{1}{30}$	1.5	10	$\frac{1}{10}$	$\frac{1}{30}$	1	$\frac{1}{20\,000}$	$\frac{1}{400}$

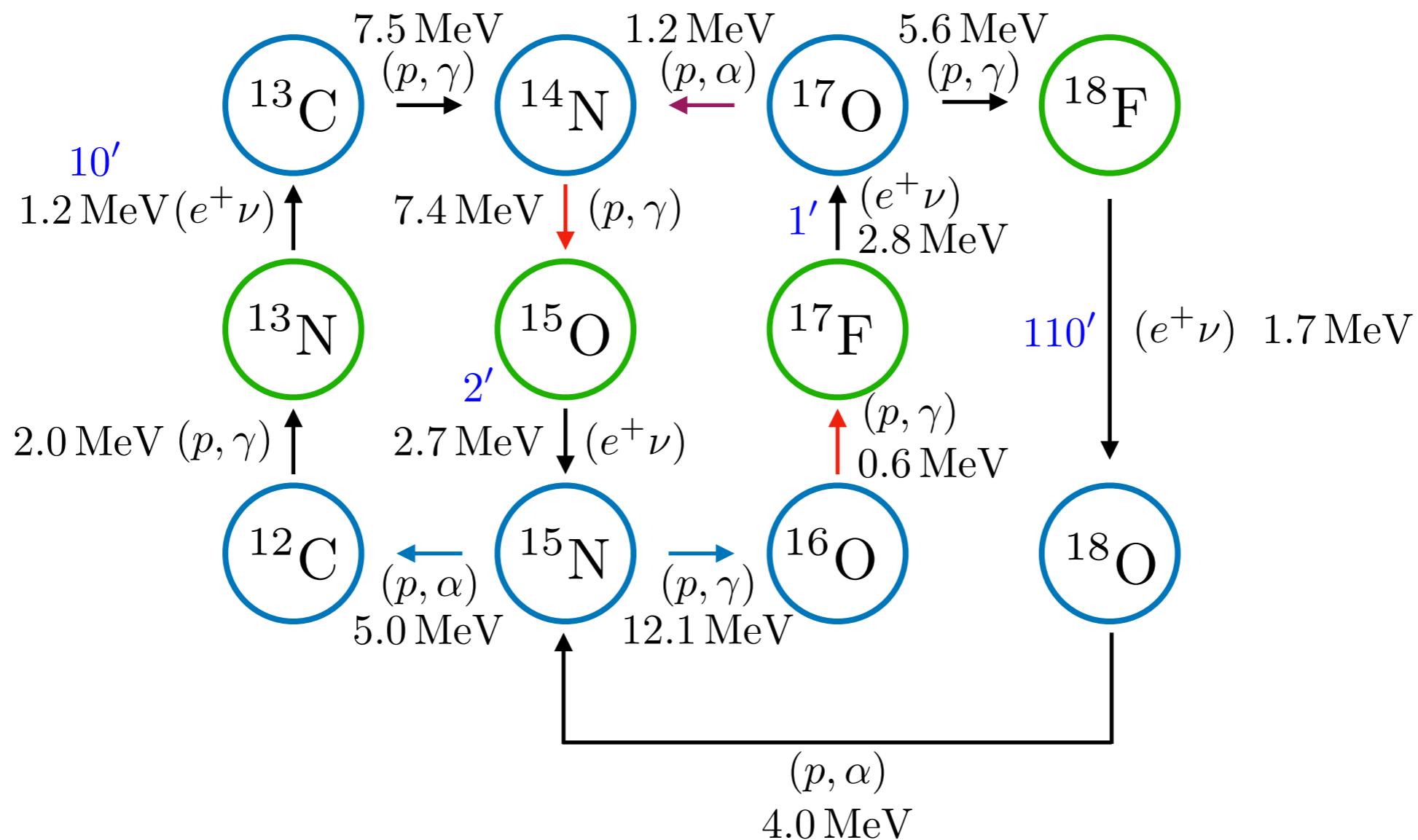
## More CNO branches. HCNO and breakout

Is there a limit to how fast the CNO cycles can run? At high temperatures, some reactions become faster than beta decays



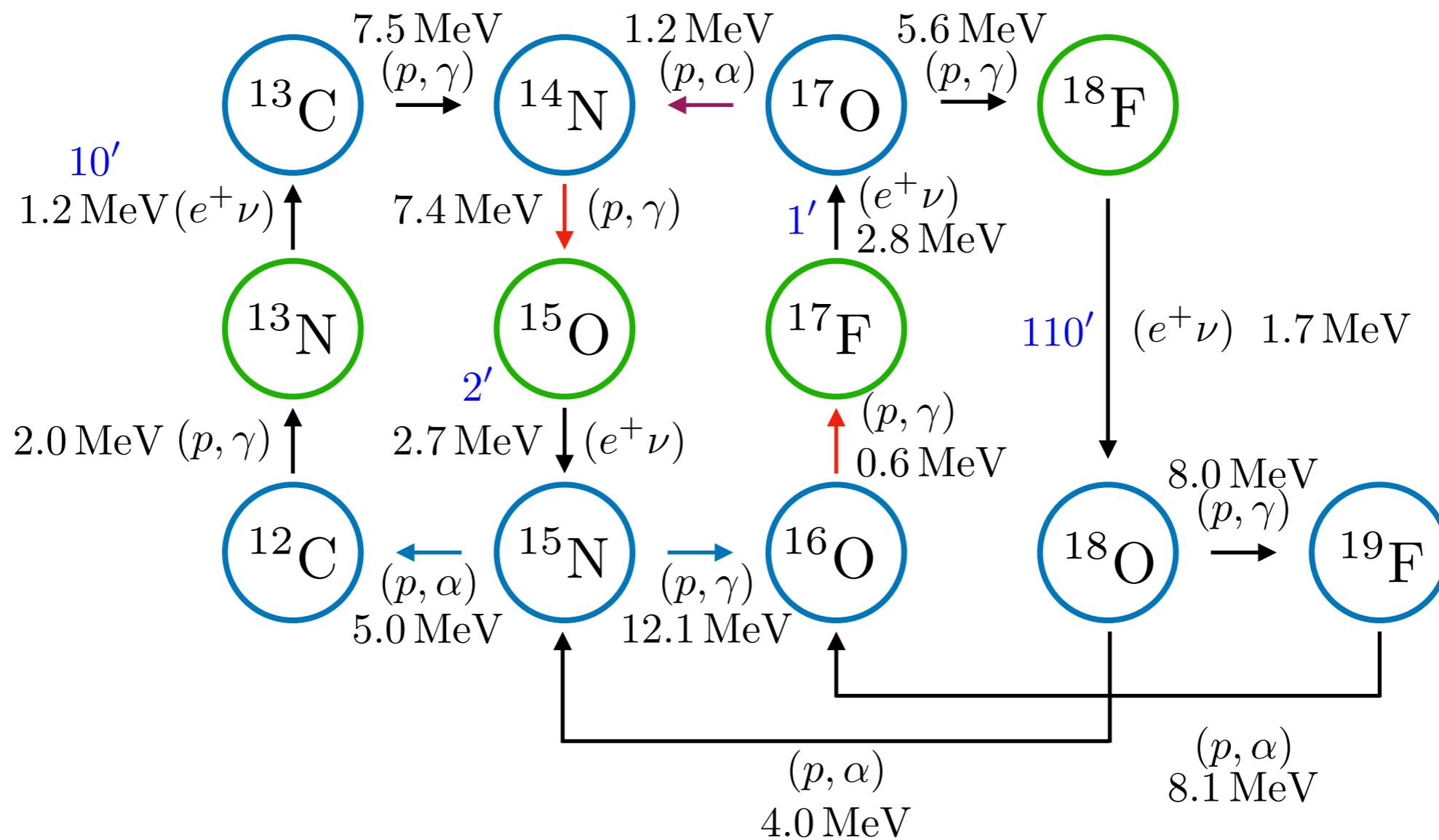
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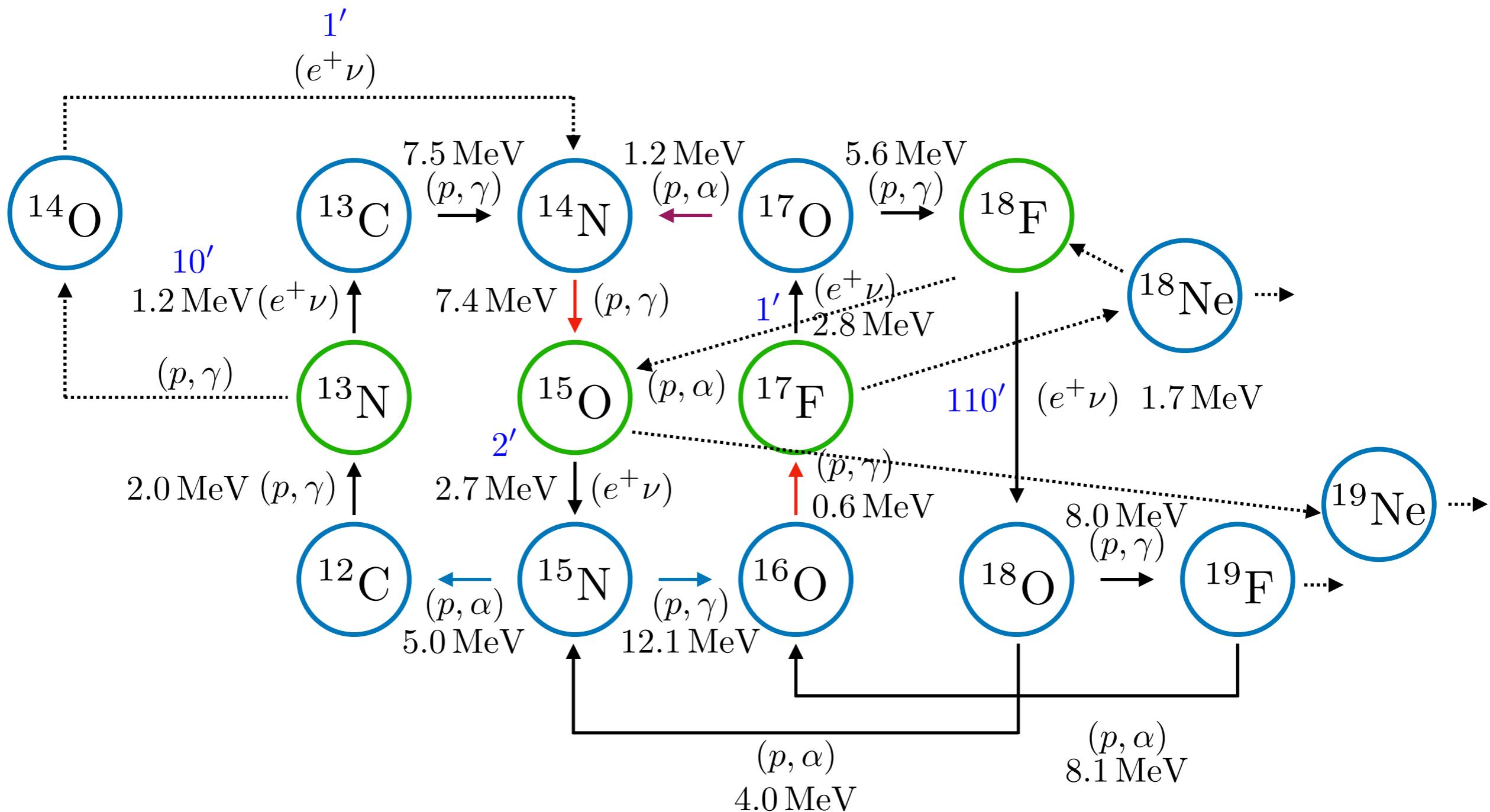
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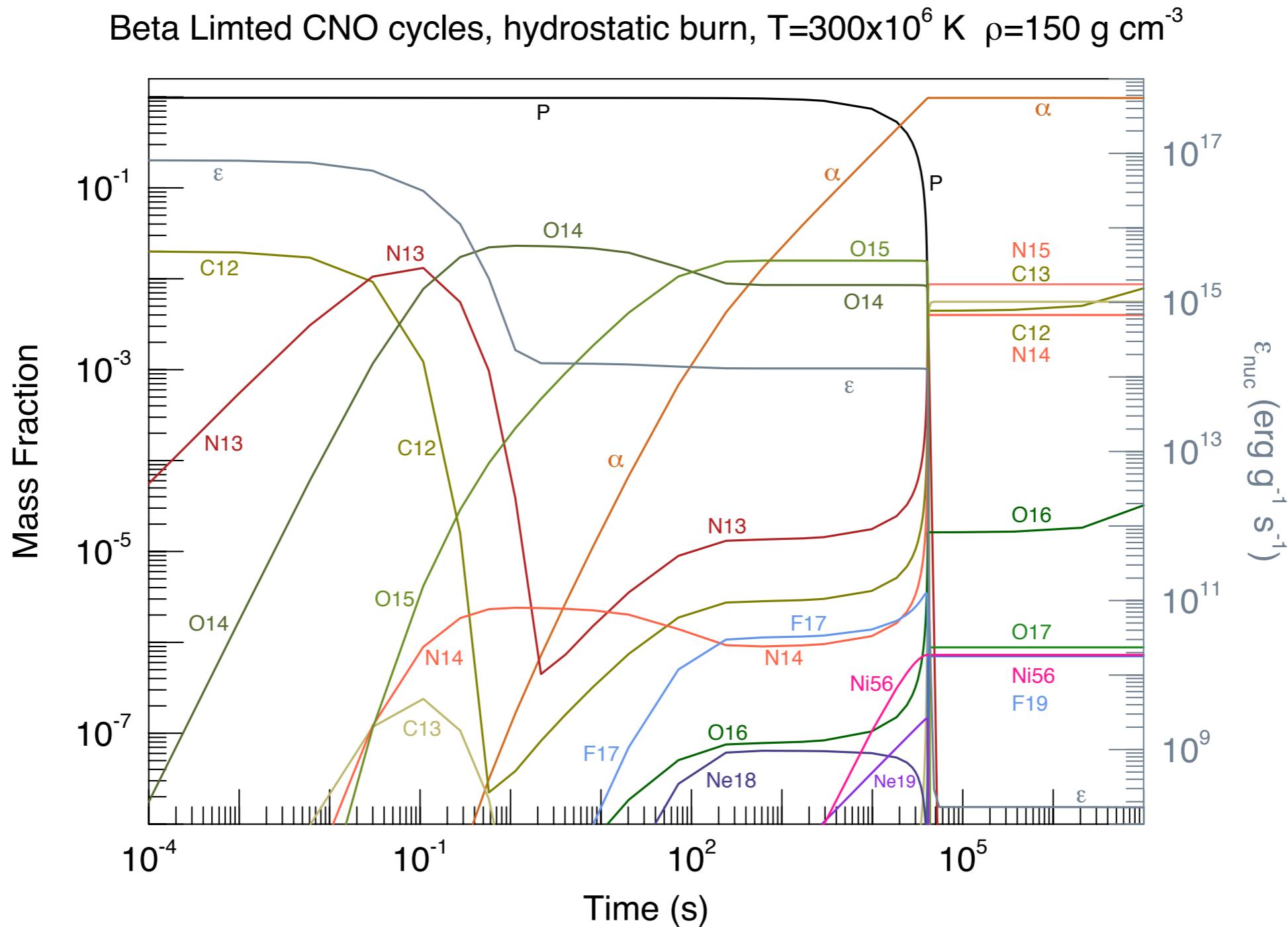


## More CNO branches. HCNO and breakout

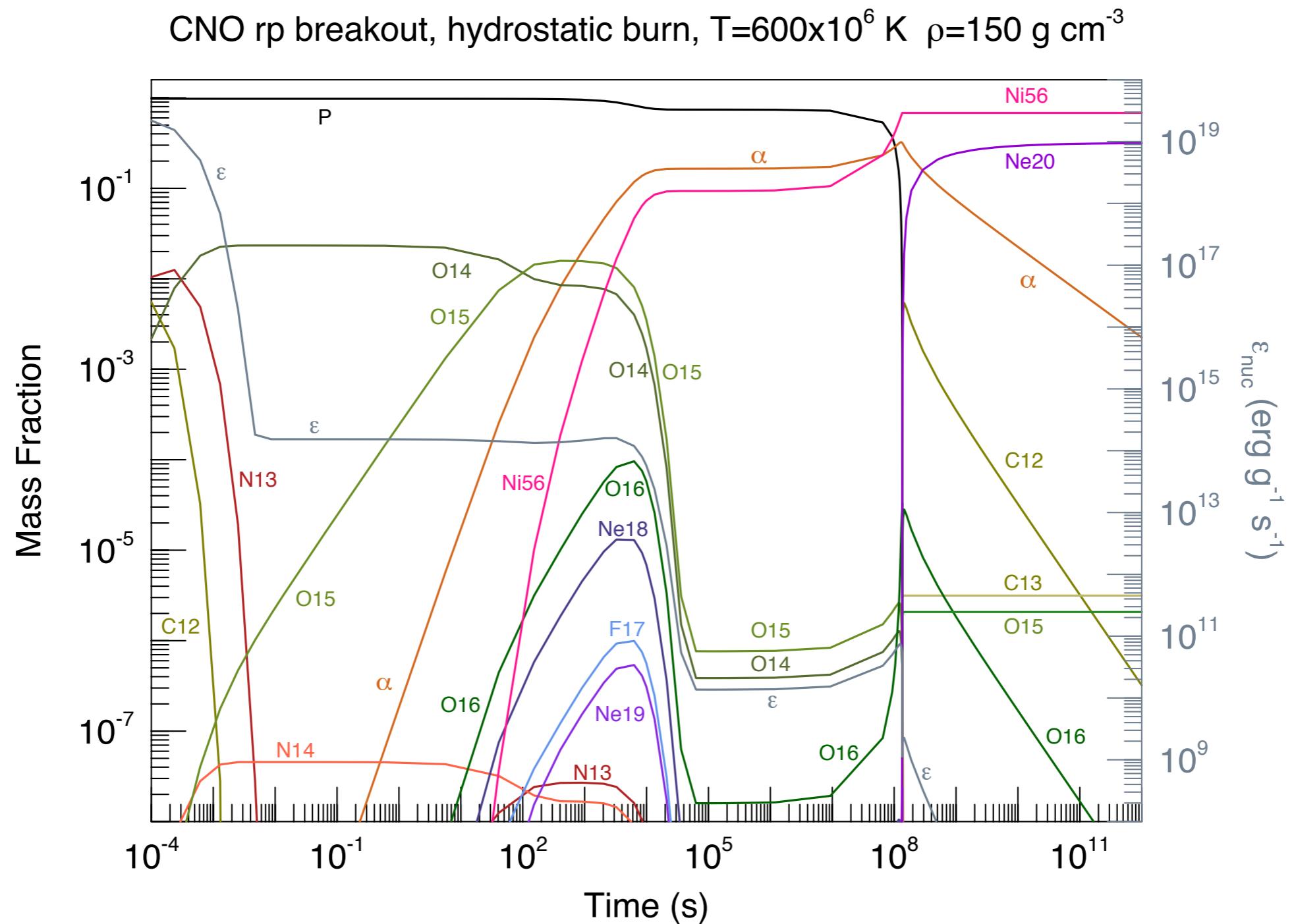
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# More CNO branches. HCNO and breakout

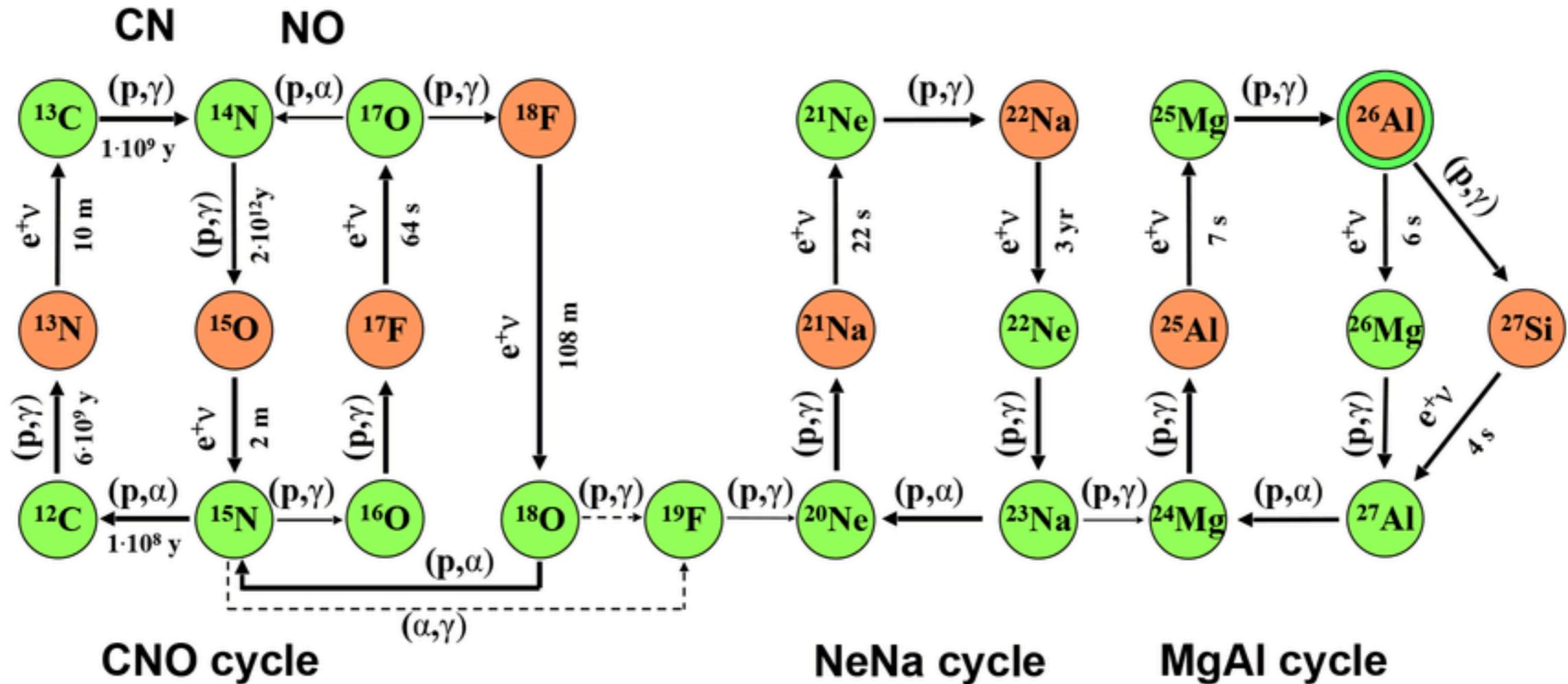


# More CNO branches. HCNO and breakout



# High temperature hydrogen burning

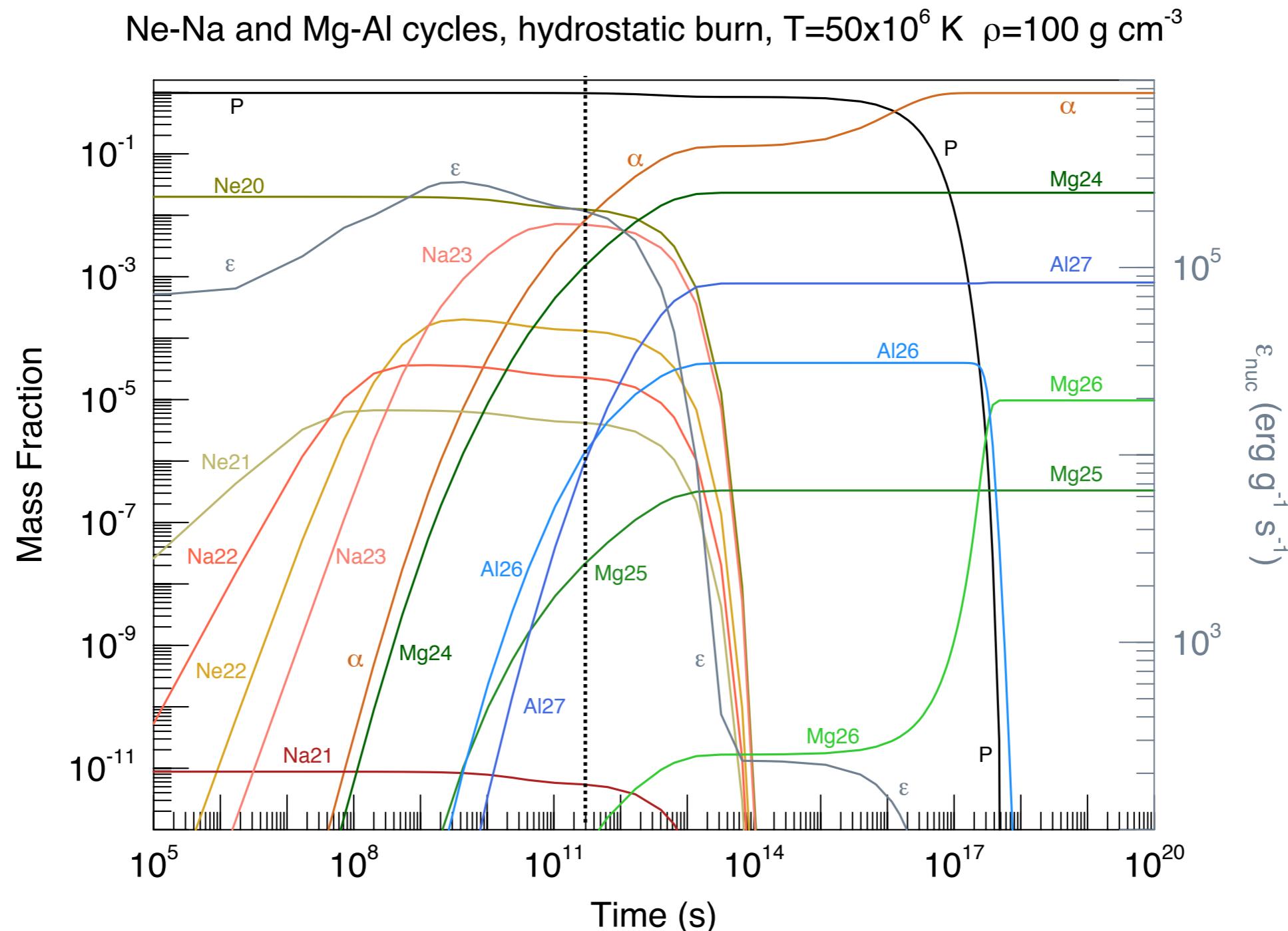
More possibilities open up at high temperatures. Two important reaction chains for hydrogen burning are the NeNa and MgAl cycles



# High temperature hydrogen burning

Example for T=50 million K. The most important product is Mg24 which reaches equilibrium after ~10000 yr. Aluminium is also strongly produced, first as Al26 and then as Al27.

Al26 is radioactive with a half life of  $7 \times 10^5$  yr

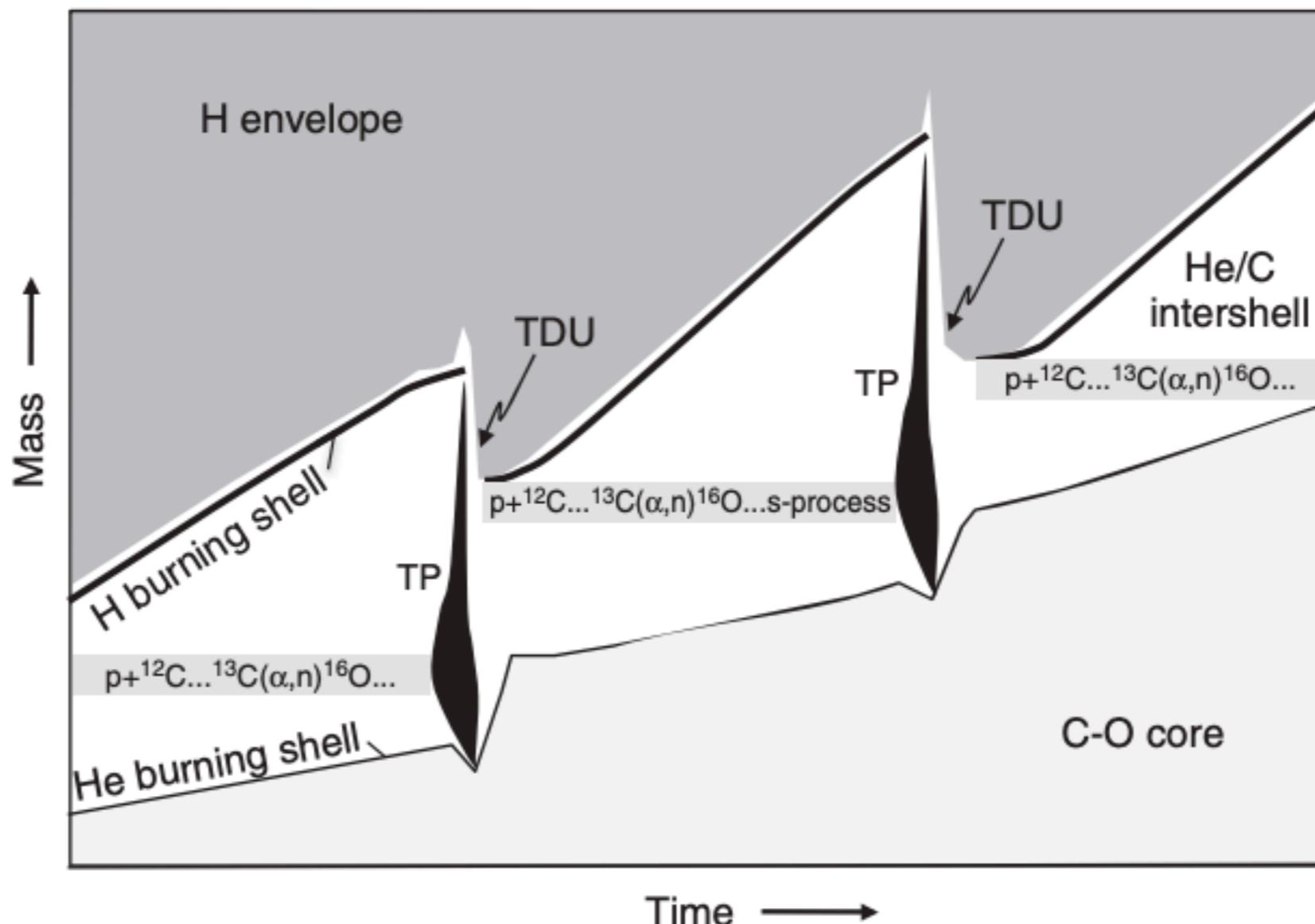


# High temperature hydrogen burning

High temperatures possible in special astrophysical environments!

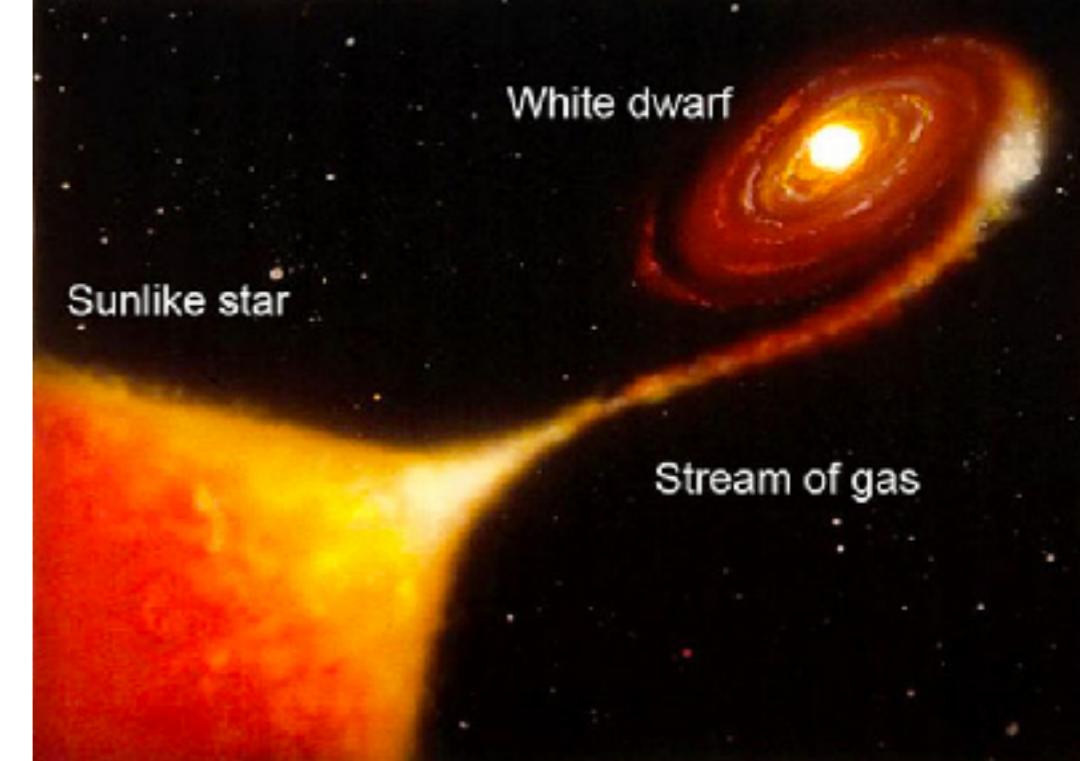
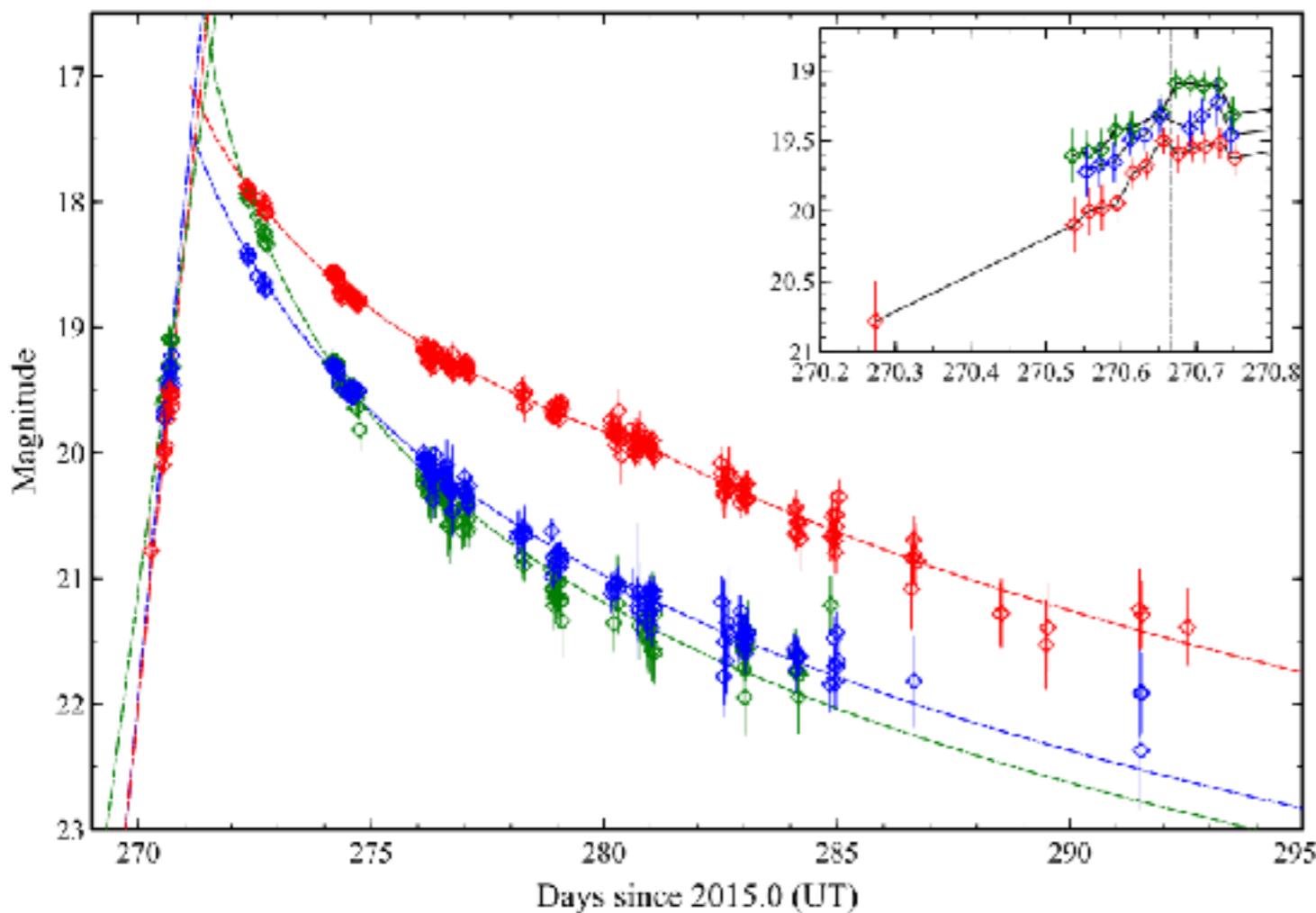
Cold CNO:  $T_9 < 0.08$ , Hot CNO and NeNa:  $T_9 \sim 0.08\text{--}0.3$ , breakout:  $T_9 > 0.3$

Hot-bottom burning on the AGB



# Nova eruptions

Nova explosions on accreting white dwarfs ( $T_9 = 0.4$ )



A WD accretes hydrogen-rich material from a companion star at slow rate (ca:  $10^{-9} M_{\text{sun}}/\text{yr}$ ).  
Runaway ignition occurs once the matter piles up and becomes dense (partly degenerate) and hot with  $T > 10^7 \text{ K}$   
Nuclear burning can continue for up to a few weeks. After that the temperature drops.  
All H-burning cycles can operate but for a limited time.  
An earth-mass of material or so is ejected into the ISM:  $^{15}\text{O}$ ,  $^{17}\text{O}$ ,  $^{22}\text{Na}$ ,  $^{26}\text{Al}$   
**For H- accretion, models suggest that more material is ejected than accreted —> WD mass is shrinking!**

# Nova eruptions

Detection of radioactive  $^{7}\text{Be}$  in a nova explosion!

Novae may be important production sites for Lithium



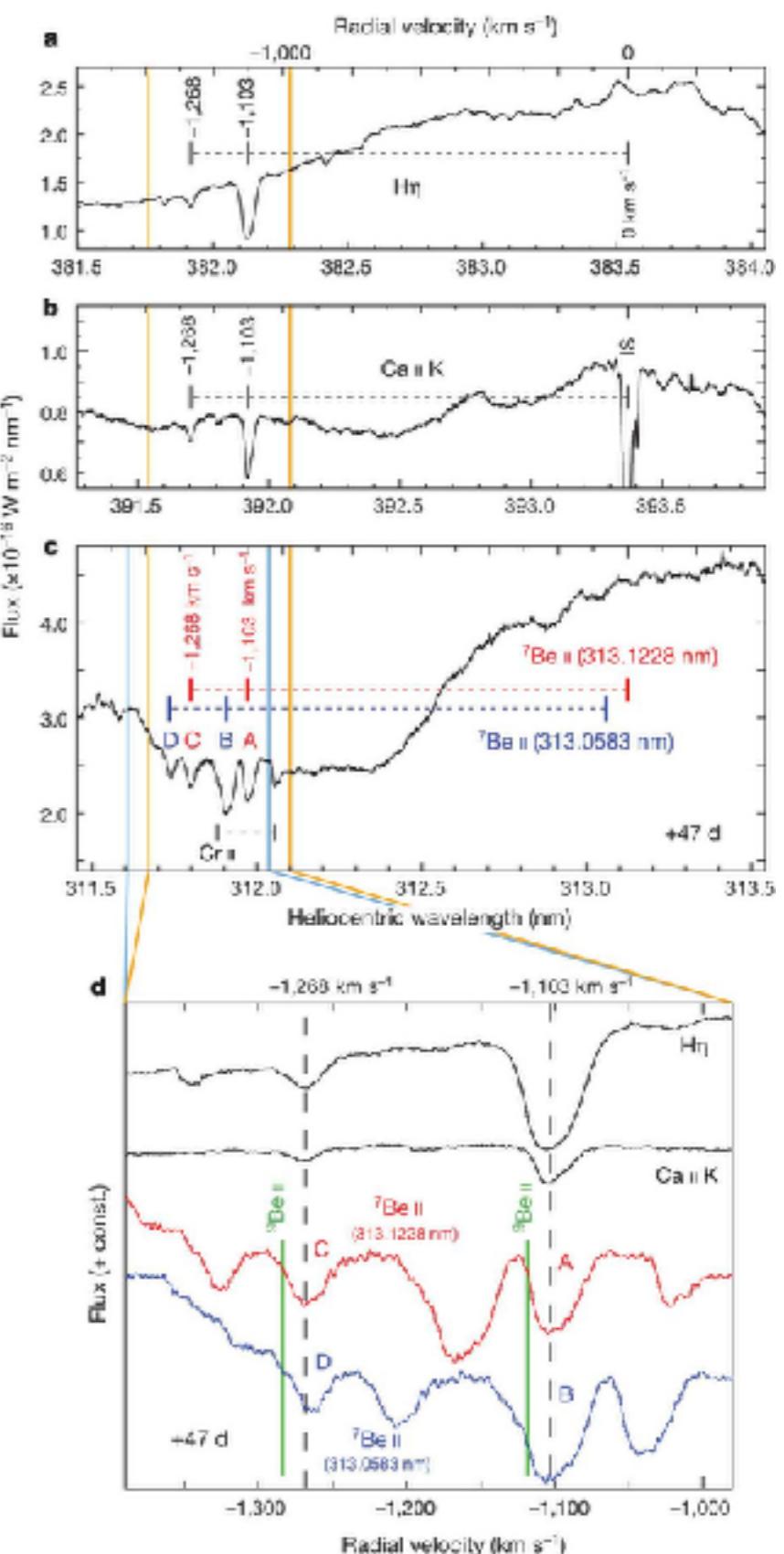
Letter | Published: 18 February 2015

## Explosive lithium production in the classical nova V339 Del (Nova Delphini 2013)

Akito Tajitsu , Kozo Sadakane, Hiroyuki Naito, Akira Arai & Wako Aoki

*Nature* 518, 381–384 (19 February 2015) | Download Citation

Type I X-ray bursts



## Type I X-ray bursts

A similar situation can arise when the accretion is a neutron star

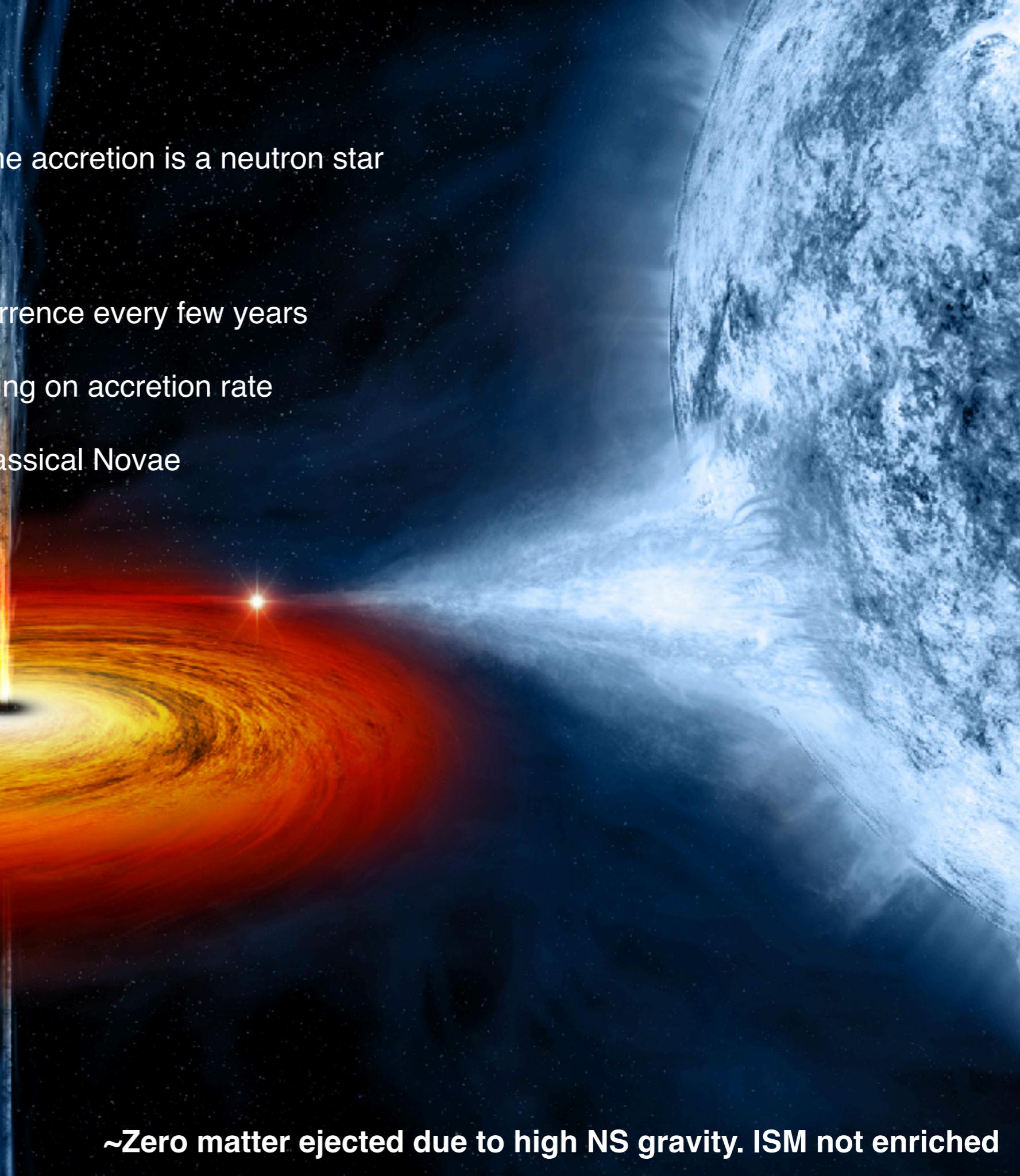
Typical bursts last for 10-100s

Recurrence: hours-days

Superbursts: duration ~hour, recurrence every few years

Burning can be H/He or C depending on accretion rate

Much higher temperatures than classical Novae

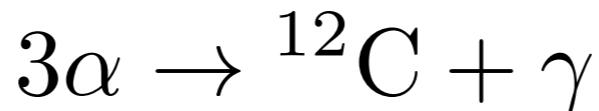


~Zero matter ejected due to high NS gravity. ISM not enriched

## Beyond H-burning: Helium at T<sub>8</sub>>1

An important problem with the formation of elements heavier than He: **No stable nuclei at A=5 and A=8!**

How can one explain the existence of Carbon?



The reaction proceeds in two steps:

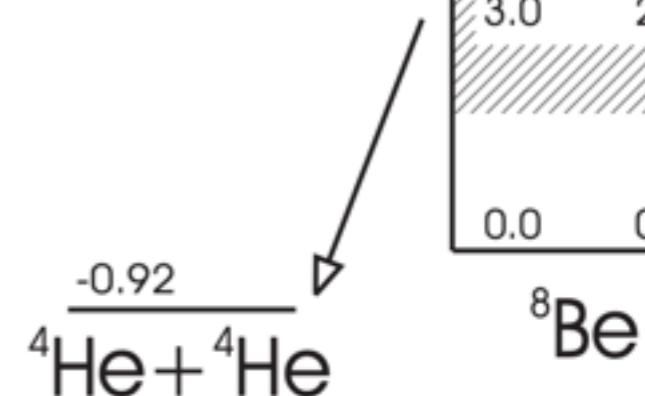
First 2 alpha particles fuse to  $^8\text{Be}$ .



This product is unstable, but only by 92 keV.

The ground state lifetime is  $\sim 10^{-16}$  s, which is longer than the timescale of a non-resonant scatter

**This means that both forward and backward reactions take place and a small equilibrium amount of  $^8\text{Be}$  is build up**



Once  $^8\text{Be}$  is in equilibrium it can capture another  $\alpha$  particle to form  $^{12}\text{C}$ .

This reaction is also dominated by a resonance at stellar energies, first predicted by Hoyle



# Beyond H-burning: Helium at $T_8 > 1$

Next:  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$

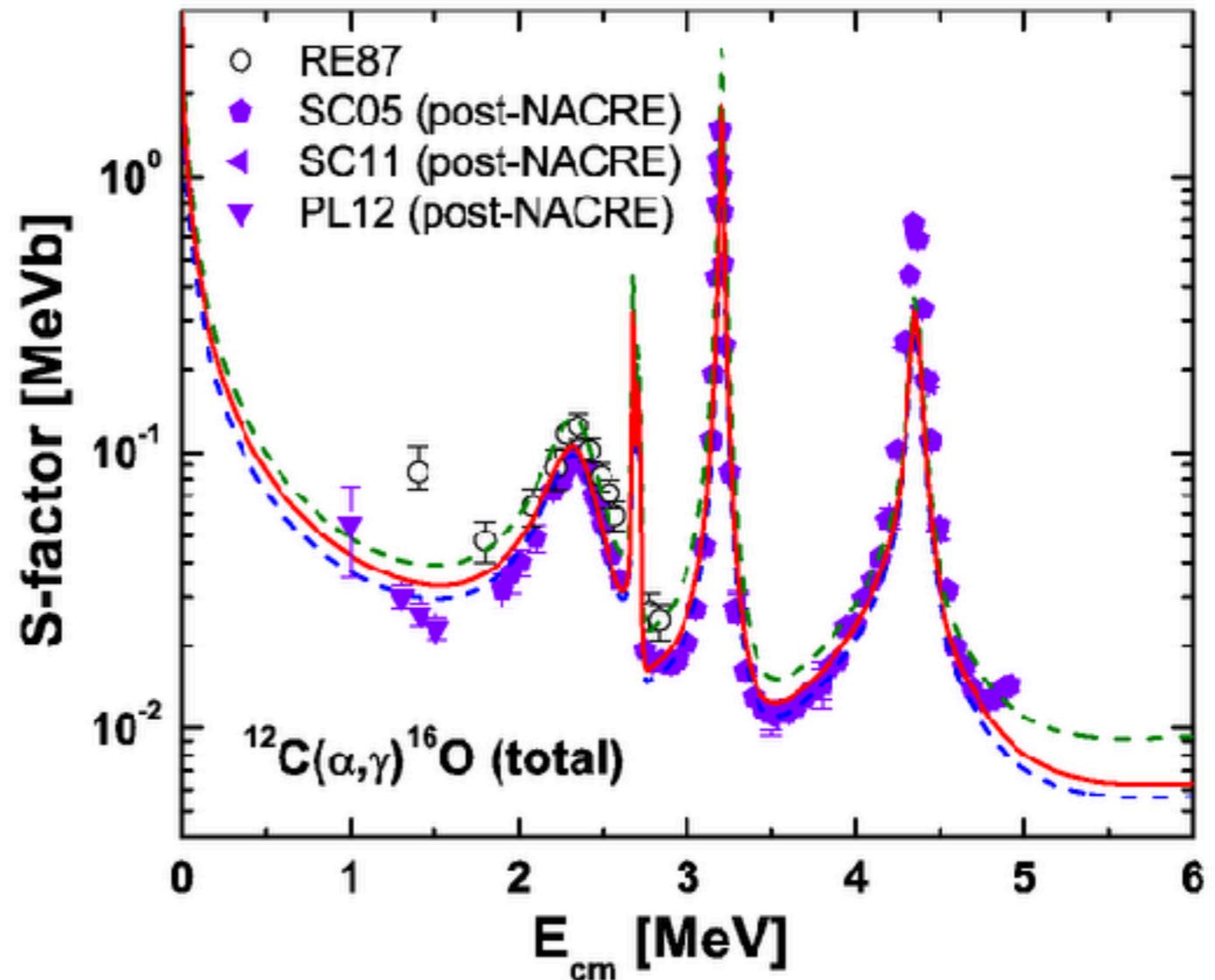
The reaction rate for a long time was highly uncertain, due to many resonances at low energies.  
The situation has somewhat improved in the past few years

## Other reactions

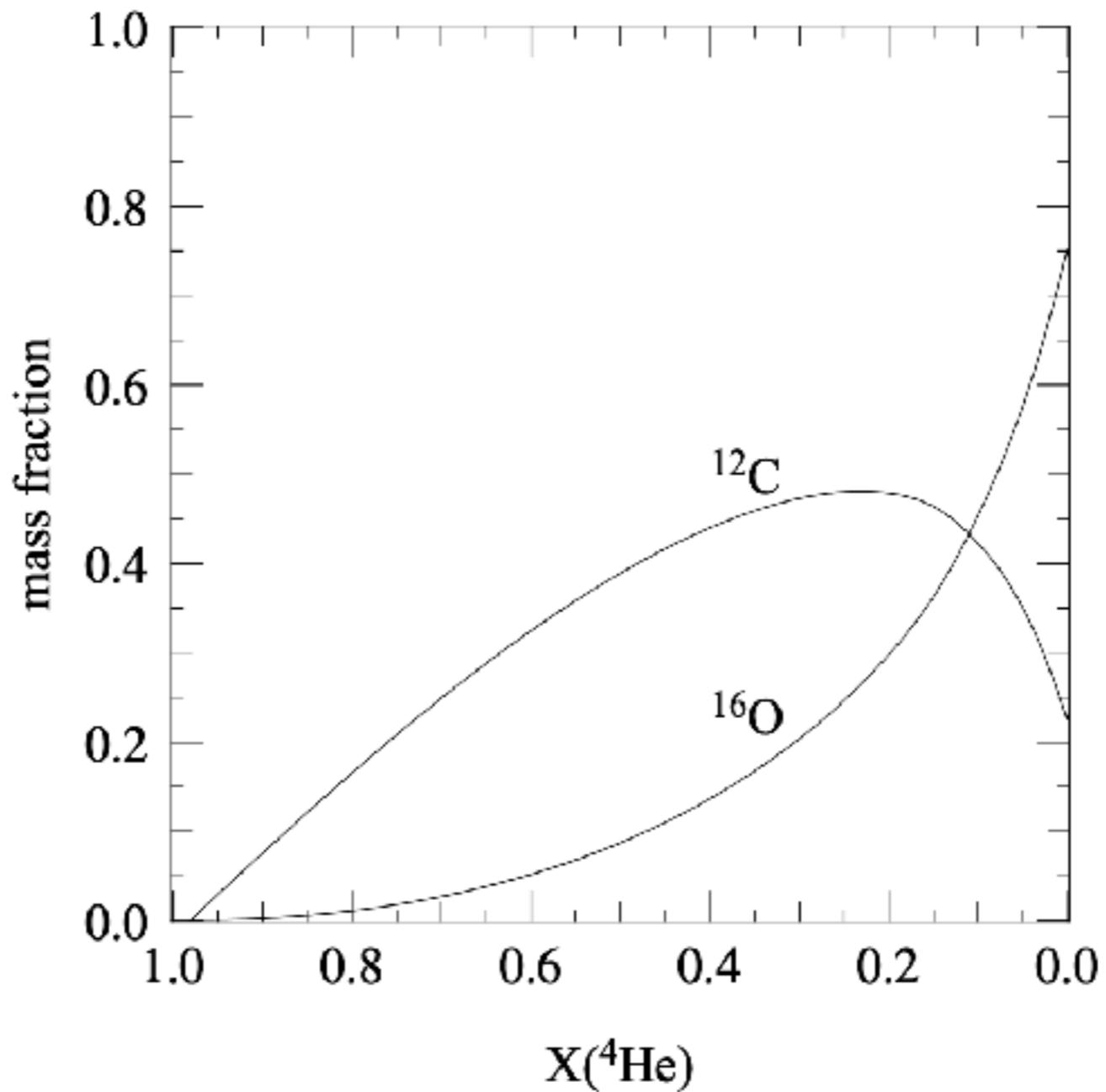
$^{16}\text{O}(\alpha, \gamma)^{20}\text{Ne}$  less important

$^{14}\text{N}(2\alpha, 2\gamma)^{22}\text{Ne}$  occurs at low  $T_8$

$^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  neutron source!

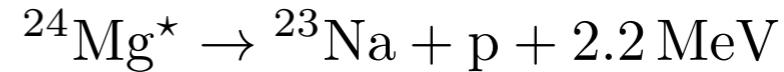
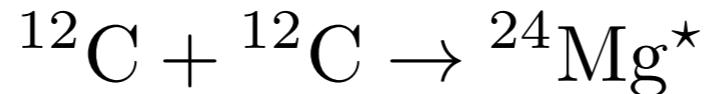


## Beyond H-burning: Helium at $T_8 > 1$



## Advanced burning

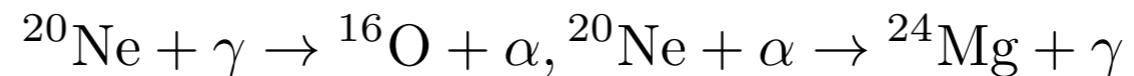
**Carbon burning:** Initially no light elements are present. The main reaction is:



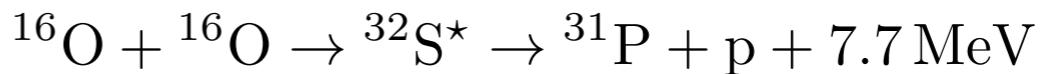
These “exit channels” have roughly the same probability. The light particles emitted are easily captured by other particles  $^{23}\text{Na}(p, \alpha)^{20}\text{Ne}$ ,  $^{20}\text{Ne}(\alpha, \gamma)^{24}\text{Mg}$ ... The final composition is a mixture of O, Ne, Mg ,Na  
 $^{23}\text{Na}$  is important as it can participate in urca cooling

## Neon and Oxygen burning

Oxygen is a doubly magic nucleus and consequently more stable than Neon. Neon burning initiates at lower temperatures. Two main reactions, one of which is endothermic (photo-disintegration)



Oxygen burning proceeds via 2 main channels       $^{16}\text{O} + ^{16}\text{O} \rightarrow ^{32}\text{S}^* \rightarrow ^{28}\text{Si} + \alpha + 9.6 \text{ MeV}$



The light particles are again immediately captured allowing for many side reactions

# Advanced burning

Silicon nuclei cannot fuse due to the extremely large Coulomb barrier. Instead, Si is transformed via a series of photo-disintegrations and alpha captures.  $T^9 > 9$  leads to nuclear statistical equilibrium.

Mostly Ni56 and a healthy mixture of iron-group elements. Ni decays to iron with a half-life of 6 days

