



Fast communication

Decision-based non-local means filter for removing impulse noise from digital images

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ABSTRACT

The decision-based non-local means filter is proposed to remove fixed-value impulse noise from the corrupted digital images. The proposed filter first identifies the corrupted pixels using the local statistics based noise detector and then removes the detected impulses using the reference image-based non-local means filter while keeping the uncorrupted pixels unaltered. Extensive simulations demonstrate that the proposed filter can remove impulse noise from the corrupted images effectively while preserving image details very well at the various noise ratios, which leads to its significantly better image restoration performance than numerous state-of-the-art switching-based filters.

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1. Introduction

Images are often corrupted by impulse noise in the process of transmission over noisy communication channels or recording by noisy sensors [1]. The median filter has been widely used for removing impulse noise because of its superior performance in noise suppression and edge preservation in comparison with the linear filters. However, the standard median (MED) filter is implemented uniformly across the entire image without taking account of whether a pixel is corrupted or not. Inevitably, the MED filter will modify both noise pixels and undisturbed good pixels, thus resulting in blurring or loss of image details and edges.

To prevent the alteration of undisturbed pixels, switching-based filters have been proposed. In the switching filtering scheme, the noise detector is first used to classify the pixels in the images as noise pixels and noise-free pixels and then filtering is activated for the detected noise

pixels. Among the recently proposed switching-based filters are difference-type noise detection based cost function-type filter [2], second-order difference analysis based median filter [3], global-local noise detection-based adaptive median (GLAM) filter [4], switching median filter with boundary discriminative noise detection (BDND) [5], opening closing sequence (OCS) filter [6], fast switching median (FSM) filter [7], efficient edge-preserving (EEP) filter [8], switching adaptive weighted mean (SAWM) filter [9], convolutional noise detection-based switching median (CNDSM) filter [10], noise adaptive fuzzy switching median (NAFSM) filter [11] and switching-based filter using nonmonotone adaptive gradient method (NAGM) [12]. Although these switching-based filters perform better than the MED filter due to the adoption of noise detection mechanism, they only use the local statistics within a small neighborhood of pixels for image denoising and thus tend to damage image details at high noise ratios.

The non-local means (NLM) filter, recently proposed by Buades [13], replaces the considered pixel by the weighted mean of all the pixels in the whole image or the surrounding neighborhoods. This filter can preserve image details better than the point-wise filters in that it relies on the global self-redundancy of the images and

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measures the similarity between two pixels by evaluating the Gaussian weighted Euclidean distance between two image patches surrounding these pixels. Although the NLM filter has been widely used for removing Gaussian noise [14,15], speckle noise [16], Rician noise [17,18] and Poisson noise [19] in the images, it performs badly in suppressing impulse noise which follows the long-tailed non-Gaussian distribution.

To fully utilize the advantage of the NLM filter in preserving image details and overcome its drawback in removing impulse noise, the decision-based non-local means (DNLM) filter is proposed in this paper. The DNLM filter combines this local statistics based noise detector with the reference image-based non-local means filter to remove impulse noise. The proposed filter can restore the images corrupted by impulse noise effectively and it outperforms many well-known switching-based filters in terms of noise reduction and detail preservation.

This paper is organized as follows: Section 2 presents the local statistics based noise detector and the reference image based non-local means filter. Comparisons of denoised results on the standard test images and real images are made in Section 3. Finally, a brief conclusion is given in Section 4.

2. The DNLM filter

The framework of the DNLM filter is shown in Fig. 1. In the proposed filter, the local statistics based noise detector is first adopted to classify the pixels in the corrupted images as noise pixels and noise-free pixels. The noise pixels are processed by the weighted mean filter while the identity filter is applied to noise-free pixels, which will produce the reference image. Based on the noise detection results and the reference image, the non-local means filter is adopted to restore the original intensity values of noise pixels. The restored image will be obtained by combining the identity filtering result with the non-local means filtering result. Obviously, the crucial components of the DNLM filter involve the noise detector and the non-local means filter.

2.1. Local statistics based noise detector

Let f_{ij} and o_{ij} denote the intensity value of the image corrupted by impulse noise and that of the original image at pixel location (i, j) , respectively. The intensity value f_{ij} will be given by:

$$f_{ij} = \begin{cases} 0 & \text{with probability } u, \\ o_{ij} & \text{with probability } (1-u-v), \\ 255 & \text{with probability } v. \end{cases} \quad (1)$$

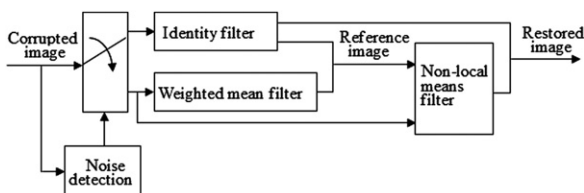


Fig. 1. Framework of the decision-based non-local means filter.

When $u=v$, the noise model given by (1) describes the so-called salt-and-pepper noise. It has been well known that the pixel corrupted by fixed valued impulse noise will generally take by far higher or lower intensity value than its neighboring uncorrupted pixels. Based on the above noise characteristics, the pixel at (i, j) will be regarded as noise candidate if it takes the maximum intensity value f_{ij}^{\max} or minimum one f_{ij}^{\min} of all the pixels in the $L_f \times L_f$ detection window $W_{ij}^{L_f}$, where $W_{ij}^{L_f} = \{(i+p, j+q) : -(L_f-1)/2 \leq p, q \leq (L_f-1)/2\}$. However, if only extreme intensity values are used to determine whether the considered pixel is corrupted or not, some noise-free edge pixels and flat-region pixels will be misclassified as noise candidates although the corrupted pixels can be identified very effectively.

To dismiss the misclassified noise-free pixels from noise candidates, the additional statistics will be adopted. Let F_{ij} denote the set of noise-free pixels in the $L_d \times L_d$ detection window $W_{ij}^{L_d}$, i.e., $F_{ij} = \{(i+p, j+q) : f_{i+p, j+q} \neq f_{ij}^{\max}, f_{i+p, j+q} \neq f_{ij}^{\min}, -(L_d-1)/2 \leq p, q \leq (L_d-1)/2\}$. To ensure accurate noise detection, L_d will be determined adaptively in the following way. Starting with $L_d=3$, this detection window iteratively extends outward by one pixel in its four sides (i.e., $L_d \leftarrow L_d+2$) until the number of elements in F_{ij} is not less than 3 or $L_d > L_f$. The weighted mean m_{ij} of all the pixels in F_{ij} is defined as

$$m_{ij} = \frac{\sum_{(i+p, j+q) \in F_{ij}} \omega_{i+p, j+q} \cdot f_{i+p, j+q}}{\sum_{(i+p, j+q) \in F_{ij}} \omega_{i+p, j+q}}, \quad (2)$$

where $\omega_{i+p, j+q}$ means the weight of $f_{i+p, j+q}$. Because the median d_{ij} of the pixels in F_{ij} has the least probability to be the value of the corrupted pixel, d_{ij} is utilized to determine $\omega_{i+p, j+q}$. It is easy to understand that the more $f_{i+p, j+q}$ and d_{ij} are similar, the greater value $\omega_{i+p, j+q}$ should take to strengthen the contribution of $f_{i+p, j+q}$ to m_{ij} . Accordingly, $\omega_{i+p, j+q}$ is a decreasing function of the absolute difference between $f_{i+p, j+q}$ and d_{ij} . Through extensive simulations, we choose $\omega_{i+p, j+q}$ as

$$\omega_{i+p, j+q} = \frac{1}{\left(1 + \frac{|f_{i+p, j+q} - d_{ij}|}{f_{ij}^{\max} - f_{ij}^{\min}}\right)^2}. \quad (3)$$

By comparing the absolute difference between f_{ij} and m_{ij} with the detection threshold T_d , the pixel at (i, j) will be classified as noise pixel with $b_{ij} = 1$ or noise-free pixel with $b_{ij} = 0$

$$b_{ij} = \begin{cases} 1 & (i, j) \notin F_{ij} \text{ and } |f_{ij} - m_{ij}| > T_d, \\ 0 & \text{otherwise.} \end{cases} \quad (4)$$

2.2. Reference image based non-local means filter

The detected impulses will be removed by the reference image-based non-local means filter. Here the reference image is produced based on the noise detection results and it is estimated as the denoised version of the input noisy image. The intensity value of any pixel at (i, j) in the reference image is represented by:

$$r_{ij} = b_{ij} \cdot m_{ij} + (1-b_{ij}) \cdot f_{ij}. \quad (5)$$

For the noise pixel at (ij) in the input noisy image, the corresponding non-local means denoised intensity NL_{ij} is obtained based on the reference image. Let Ω_{ij} denote the set of the selected pixels within the $L_s \times L_s$ search window $W_{ij}^{L_s}$ centered at (ij) in the reference image. The intensity NL_{ij} will be computed as the weighted average of all the pixels in Ω_{ij} , i.e.

$$NL_{ij} = \frac{\sum_{(k,l) \in \Omega_{ij}} s_{ij,k,l} \cdot r_{k,l}}{\sum_{(k,l) \in \Omega_{ij}} s_{ij,k,l}}, \quad (6)$$

where the weight $s_{ij,k,l}$ measures the similarity between two pixels at (ij) and (k,l) in the reference image.

For the set Ω_{ij} , it is the same to the search window in the traditional NLM filter while in the DNLM filter it will be determined adaptively based on the local characteristics of the pixels in $W_{ij}^{L_s}$. Let U_{ij} be the number of unaltered pixels in $W_{ij}^{L_s}$ whose intensity values are the same to those of the corresponding pixels in the input noisy image. If U_{ij} is less than half of the search window size, Ω_{ij} is presented as the set of all the pixels in $W_{ij}^{L_s}$ to achieve good image smoothing effect. Otherwise, Ω_{ij} is defined as the set of unaltered pixels in $W_{ij}^{L_s}$ to ensure excellent detail preservation performance

$$\Omega_{ij} = \begin{cases} \{(p,q) : |p-i| \leq L_s, |q-j| \leq L_s\}, & U_{ij} < \frac{L_s \times L_s}{2}, \\ \{(p,q) : r_{p,q} = f_{p,q}, |p-i| \leq L_s, |q-j| \leq L_s\}, & U_{ij} \geq \frac{L_s \times L_s}{2}. \end{cases} \quad (7)$$

To determine the weight $s_{ij,k,l}$ in (6) accurately is the key to removing impulse noise by the DNLM filter. In the traditional NLM filter, $s_{ij,k,l}$ is defined as the exponential function of the Gaussian weighted Euclidean distance between two image patches centered at the two pixels (ij) and (k,l) in the noisy image. Because the weights computed by the exponential function will still take positive values when the Euclidean distances are quite large, the traditional NLM filter cannot attenuate the unfavorable influence of highly dissimilar image patches on the denoised results. A feasible solution to this problem is to dismiss such image patches from the filtering process by setting their weights to zero. Based on the above analysis, the DNLM filter uses the piecewise function for computing $s_{ij,k,l}$ and it is defined as

$$s_{ij,k,l} = \begin{cases} \left(1 - \sqrt{\frac{\|V(Q_{ij}) - V(Q_{k,l})\|_2}{h_{ij}}}\right)^4, & \|V(Q_{ij}) - V(Q_{k,l})\|_2 \leq h_{ij}, \\ 0 & \text{otherwise,} \end{cases} \quad (8)$$

where h_{ij} is the decay parameter controlling the filtering degree, $\|\cdot\|$ denotes the Euclidean norm, $V(Q_{ij})$ and $V(Q_{k,l})$ are the vectors of pixel intensities taken from the $L_p \times L_p$ image patches Q_{ij} and $Q_{k,l}$ centered at (ij) and (k,l) in the reference image, respectively.

It can be seen from (8) that the DNLM filter determines the weight $s_{ij,k,l}$ based on the reference image rather than the noisy image, which lays the core foundation for the DNLM filter to suppress impulse noise in the noisy image effectively. The reason will be explained in this way. For the detected noise pixel at (ij) and any other pixel at (k,l)

in the noisy image, the two image patches N_{ij} and $N_{k,l}$ centered at the two pixels are likely to include noise pixels. Because of the disadvantageous influence of these noise pixels, it is difficult to accurately determine $s_{ij,k,l}$ using the Euclidean distance between N_{ij} and $N_{k,l}$. However, no or very few noise pixels will remain in two image patches Q_{ij} and $Q_{k,l}$ in the reference image. Exclusion of noise pixels from the compared two image patches ensures that $s_{ij,k,l}$ can be computed more effectively using $\|V(Q_{ij}) - V(Q_{k,l})\|_2$ than using $\|V(N_{ij}) - V(N_{k,l})\|_2$. To illustrate this point better, the standard image Lena will be used as an example. The original Lena image, the image corrupted with 10% impulse noise and the reference image restored by (5) are shown in Fig. 2. Two pairs of 15×15 image patches surrounded by the white boxes and the black boxes are chosen from each of the three images. The Euclidean distances between the two image patches in the white boxes in the three images are 76.20, 114.69 and 74.32, respectively. For the two image patches in the black boxes, their Euclidean distances in the three images are 145.41, 166.51, 143.93, respectively. Obviously, the Euclidean distances between image patches in the reference image are much closer to those in the original image than those in the noisy image. The above example demonstrates that for the corrupted image, the DNLM filter can determine similarity between two pixels effectively by means of the Euclidean distance between two image patches in the reference image.

The decay parameter h_{ij} in (8) plays an important role in the DNLM filter. In the traditional NLM filter, the same decay parameter is chosen for all the pixels in the corrupted image. However, it is difficult to suppress noise effectively while preserving intricate image details very well using the globally fixed decay parameter for the whole image. To address this problem, h_{ij} will be adaptively determined based on the local image structure in a pixel-wise way. Experimentally, it has been shown that the decay parameter should take a large value for a smooth-region pixel to facilitate noise suppression and take a relatively small value for the edge-region pixel to preserve image details. The gradient magnitude g_{ij} of the pixel at (ij) in the reference image can indicate if it is an edge pixel or not. It follows that the pixel with the large gradient magnitude will take smaller decay parameter than that with the small gradient magnitude. It is obvious that h_{ij} is a decreasing function of g_{ij} , which can be estimated using Sobel operators. Meanwhile, simulations on a broad variety of gray-level images show that h_{ij} is also dependent on the noise ratio in the noisy image and it should increase with the increasing noise ratio. Based on the extensive simulations, h_{ij} is chosen as

$$h_{ij} = \beta_{ij}^{(1+R^2)}, \quad (9)$$

$$\beta_{ij} = \delta \cdot \frac{1}{1 + \left(\frac{g_{ij}}{g_{\max}}\right)^2}, \quad (10)$$

where R is the noise ratio which is estimated as the ratio of the number of detected noise pixels to the total number

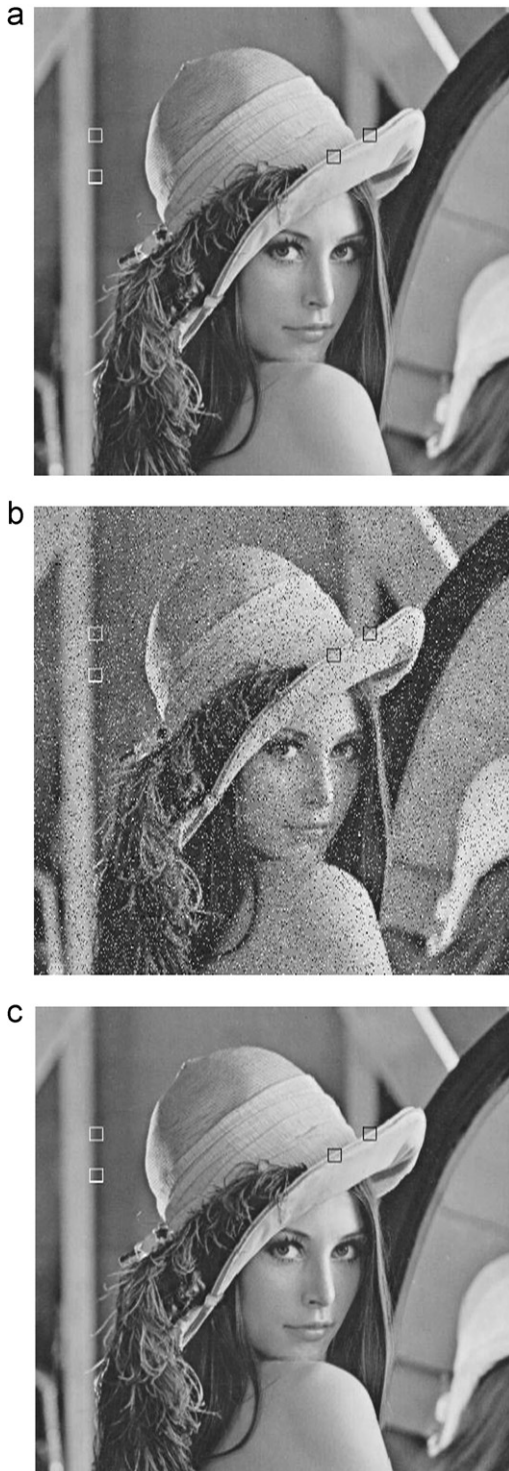


Fig. 2. The image Lena used to illustrate the effectiveness of the DNLM filter in determining the similarity between two pixels: (a) original image Lena, (b) noisy image with 10% impulse noise, and (c) reference image.

of pixels in the noisy image; δ is a predefined constant and g_{\max} is the maximum gradient magnitude of the pixels in the reference image.

3. Experiments on standard test images and real images

3.1. Simulation on standard test images

In this section, 512×512 gray-level images such as Lena, Mandrill, Goldhill, Boat and Barbara and Bridge are used as test images. The salt-and-pepper noise with uniform distribution is added to these images, which means that the pixel has equal probability of being corrupted by either a positive impulse (with value 255) or a negative impulse (with value 0). Simulations are conducted on test images corrupted by salt-and-pepper noise with the noise ratio varying from 10% to 80%. The noise detection accuracy of the DNLM filter is appreciated and its restoration performance is compared with that of other state-of-the-art switching-based filters.

3.1.1. Noise detection accuracy

The noise detection performance of the DNLM filter depends on the detection window W_d and the detection threshold T_d . For W_d , a big window contains more pixels and has higher statistical reliability than a small window and thus facilitates accurate noise detection. As regards T_d , a very large value will produce numerous misclassifications of noise pixels as noise-free ones while many uncorrupted pixels will be misdetected as noise pixels if T_d takes a very small value. The above analysis shows that using a very small value of L_f or T_d is likely to cause damage to image details and edges due to the participation of misdetected noise-free pixels into the filtering process. Meanwhile, using a very small L_f or a very large T_d results in the remaining of undetected noise pixels in the reference image and the final denoised image, which will attenuate the denoising performance of the DNLM filter because the remaining noise pixels are disadvantageous for the accurate computation of similarity between their neighboring pixels in the reference image. Extensive simulations indicate that good noise detection results can be obtained when T_d takes a value in the range [5,20] and L_f is not less than 9. Therefore, we set $T_d=5$ and $L_f=9$ for noise detection.

Table 1 lists the noise detection results of the DNLM filter operating on all the test images in terms of the total number of undetected noise pixels and misdetected noise-free pixels. We can see from Table 1 that the DNLM filter can realize noise detection with very few or no mistakes at the various noise ratios, which provides the DNLM filter with a solid foundation to achieve the outstanding restoration performance.

3.1.2. Restoration performance

The restoration performance of the DNLM filter depends on the search window size $L_s \times L_s$, the image patch size $L_p \times L_p$ and the predefined constant δ . As regards L_s and L_p , the small values should be chosen to preserve image details because very few impulses will remain in the reference image. For the constant δ , image details will be damaged if it takes a very large value while the image will be under-smoothed if it takes a very small value.

Table 1

Noise detection results of the DNLM filter operating on all the test images corrupted by salt-and-pepper noise with the various noise ratios.

Test images	10%	20%	30%	40%	50%	60%	70%	80%
Lena	32	0	0	0	0	0	0	0
Mandrill	84	0	0	0	0	0	0	0
Goldhill	55	0	0	0	0	0	0	0
Boat	55	0	0	0	0	0	0	0
Barbara	31	0	0	0	0	0	0	0
Bridge	151	57	96	130	161	172	182	173

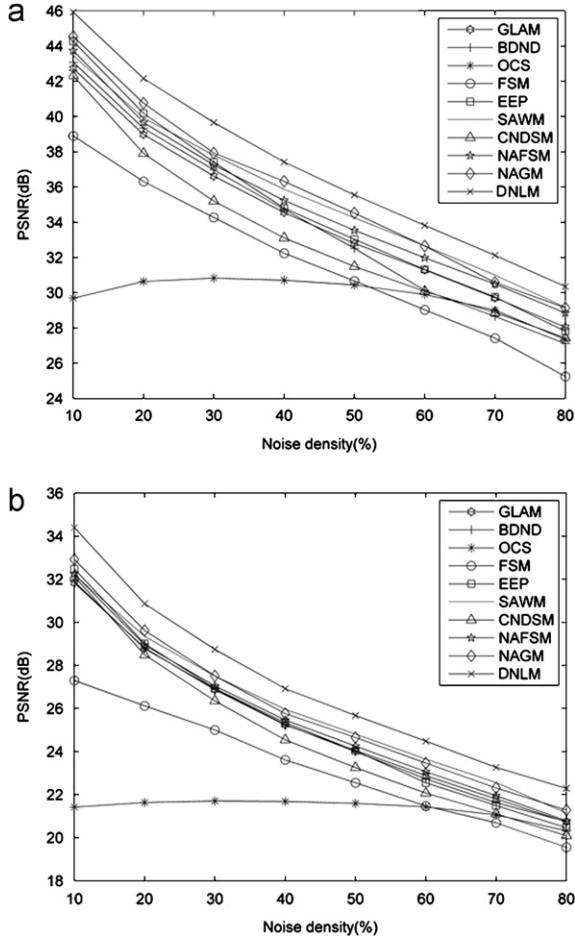


Fig. 3. Restoration results in PSNR (dB) of the various filters operating on the image Lena and the image Mandrill: (a) PSNR for the image Lena and (b) PSNR for the image Mandrill.

Simulations on all the test images show that δ in the range [160,200] can ensure satisfactory denoised results. Therefore, we set $L_s=3$, $L_p=3$ and $\delta=180$ for noise removal.

Restoration performance is quantitatively evaluated by peak signal-to-noise ratio (PSNR) and mean structural similarity (MSSIM) [20] which are defined as

$$\text{PSNR} = 10 \log_{10} \frac{D^2}{\frac{1}{MN} \sum_{i=1}^M \sum_{j=1}^N (o_{ij} - e_{ij})^2} \text{dB}, \quad (11)$$

$$\text{MSSIM}(O, E) = \frac{\sum_{k=1}^B \text{SSIM}(o_k, e_k)}{B}, \quad (12)$$

$$\text{SSIM}(o_k, e_k) = \frac{(2\mu_{o_k}\mu_{e_k} + C_1)(2\sigma_{o_k e_k} + C_2)}{(\mu_{o_k}^2 + \mu_{e_k}^2 + C_1)(\sigma_{o_k}^2 + \sigma_{e_k}^2 + C_2)}, \quad (13)$$

where D is the dynamic range of the pixel intensities (255 for 8-bit gray-level images); O and E denote the original image and the filtered image, respectively; o_k and e_k are the image contents at the k -th local window in the original and filtered images; B is the total number of local windows in the image; μ_{o_k} and μ_{e_k} are the mean intensity of o_k and e_k ; σ_{o_k} and σ_{e_k} are the standard deviation of o_k and e_k ; $\sigma_{o_k e_k}$ is the covariance between o_k and e_k ; $C_1 = (K_1 D)^2$ and $C_2 = (K_2 D)^2$ are small constants to stabilize SSIM using the following parameter settings: $K_1 = 0.01$ and $K_2 = 0.03$.

Figs. 3 and 4 show PSNR and MSSIM values of all the evaluated filters operating on the corrupted images Lena and Mandrill, respectively. Obviously, the DNLM filter produces higher PSNR and MSSIM values than the other filters at the various noise ratios. To demonstrate the

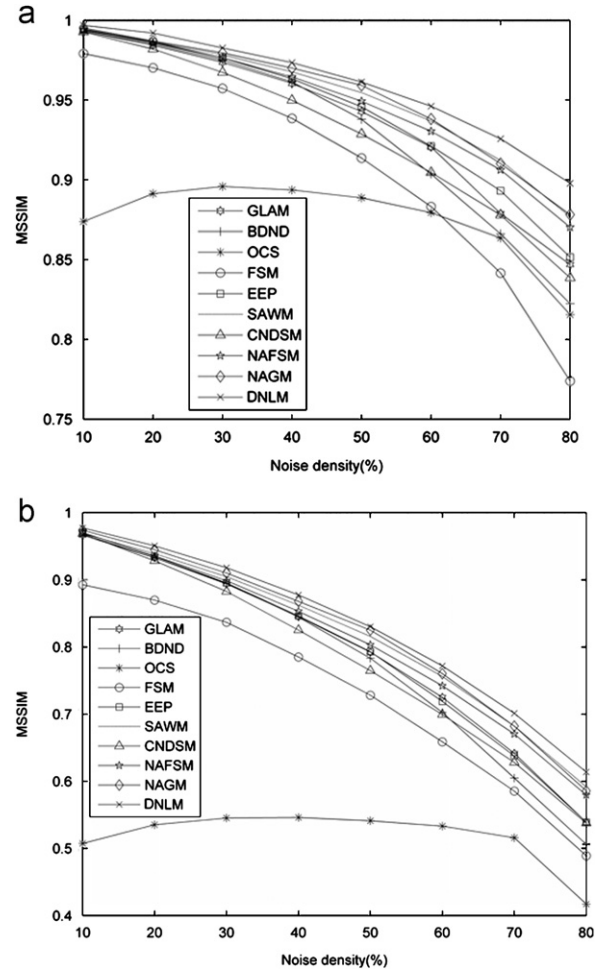


Fig. 4. Restoration results in MSSIM of the various filters operating on the image Lena and the image Mandrill: (a) MSSIM for the image Lena and (b) MSSIM for the image Mandrill.

Table 2

Restoration results in PSNR (dB) of the various filters operating on the four test images corrupted by 40% and 80% salt-and-pepper noise.

Filters	Goldhill		Boat		Barbara		Bridge	
	40%	80%	40%	80%	40%	80%	40%	80%
GLAM	32.45	26.81	31.54	25.38	26.50	22.34	27.73	22.49
BDND filter	32.47	26.33	31.78	24.59	26.89	23.15	26.30	22.10
OCS filter	29.37	25.63	27.93	24.12	24.21	21.85	24.40	21.32
FSM filter	30.55	25.23	29.60	23.97	25.19	20.91	25.85	21.24
EEP filter	32.66	26.46	32.01	24.86	26.59	22.28	27.73	21.93
SAWM filter	33.12	27.65	32.45	26.40	27.46	22.60	28.17	23.01
CNDSM filter	31.64	26.52	30.57	25.23	26.06	21.76	26.91	21.98
NAFSM filter	32.85	27.41	32.10	26.24	26.92	22.54	28.12	22.99
NAGM filter	33.38	27.82	32.88	26.78	27.76	22.82	28.21	23.18
DNLM filter	34.58	29.07	34.27	27.92	28.96	23.97	29.42	24.40

Table 3

Restoration results in MSSIM of the various filters operating on the four test images corrupted by 40% and 80% salt-and-pepper noise.

Filters	Goldhill		Boat		Barbara		Bridge	
	40%	80%	40%	80%	40%	80%	40%	80%
GLAM	0.9210	0.7294	0.9346	0.7756	0.9005	0.6937	0.8782	0.6056
BDND filter	0.9211	0.6977	0.9363	0.7457	0.9021	0.7052	0.8628	0.5565
OCS filter	0.8013	0.6959	0.8425	0.7399	0.7299	0.6558	0.6649	0.5381
FSM filter	0.8838	0.6837	0.9032	0.7373	0.8612	0.6322	0.8217	0.5583
EEP filter	0.9243	0.7194	0.9376	0.7655	0.9019	0.7009	0.8792	0.5959
SAWM filter	0.9331	0.7738	0.9443	0.8125	0.9151	0.7361	0.8912	0.6608
CNDSM filter	0.9093	0.7291	0.9227	0.7738	0.8875	0.6916	0.8595	0.6069
NAFSM filter	0.9259	0.7634	0.9387	0.8045	0.9065	0.7249	0.8866	0.6548
NAGM filter	0.9395	0.7816	0.9491	0.8174	0.9214	0.7320	0.8985	0.6553
DNLM filter	0.9413	0.7993	0.9532	0.8338	0.9321	0.7532	0.9042	0.6871

generalization of the proposed filter, the performance to restore other four corrupted images is compared among these switching-based filters. Tables 2 and 3 list PSNR and MSSIM values of the various filters for the four images corrupted by 40% and 80% salt-and-pepper noise, respectively. Likewise, the DNLM filter outperforms the other filters in terms of the above metrics. The objective evaluation based on PSNR and MSSIM measurement indicates that the DNLM filter has the best restoration performance among all the compared filters.

To verify the advantage of the DNLM filter over the other evaluated filters, the subjective visual comparisons among the restoration results of the various filters are also made. Figs. 5 and 6 show the enlarged portions of the restored results of all the evaluated filters for the image Lena corrupted by 80% impulse noise and those of the most competitive NAGM filter and the DNLM filter for the image Mandrill corrupted by 80% impulse noise, respectively. We can see from Figs. 5 and 6 that the BDND filter, the OCS filter and the NAGM filter lead to image over-smoothing. The FSM filter produces artifacts near the edges and in the textural areas. The EEP filter, the SAWM filter, the CNDSM filter and the NAFSM filter damage image details to some extent. By comparison, the DNLM filter provides the best restoration results among all these filters in that it preserves image details very well while removing impulse noise effectively.

The reason why the DNLM filter can restore the corrupted images more effectively than other evaluated

filters will be simply discussed here. The difference between the DNLM filter and the compared filters lies in the strategy to restore the original intensity values of the detected noise pixels. The DNLM filter exploits the self-similarity of the images in the non-local neighborhoods and suppress impulse noise by averaging the noise-free pixels in the duplicated structures. However, the compared filters are generally the point-wise filters which attenuate the influence of impulse noise only by averaging the pixels in the same structure. It is because of the utilization of redundancy from similar patterns in the image that the DNLM filter provides better restoration performance than these point-wise filters.

3.2. Test on real images

To demonstrate the applicability of the DNLM filter to denoising real images, the denoised results of such images as the TV image, the panoramic radiograph and the cephalometric radiograph are shown in Fig. 7. The observation from Fig. 7 shows that the DNLM filter has successfully suppressed impulse noise in these real images with image details and edges being preserved very well.

4. Conclusion

In this paper, we have presented a novel decision-based non-local means filter for impulse noise removal.

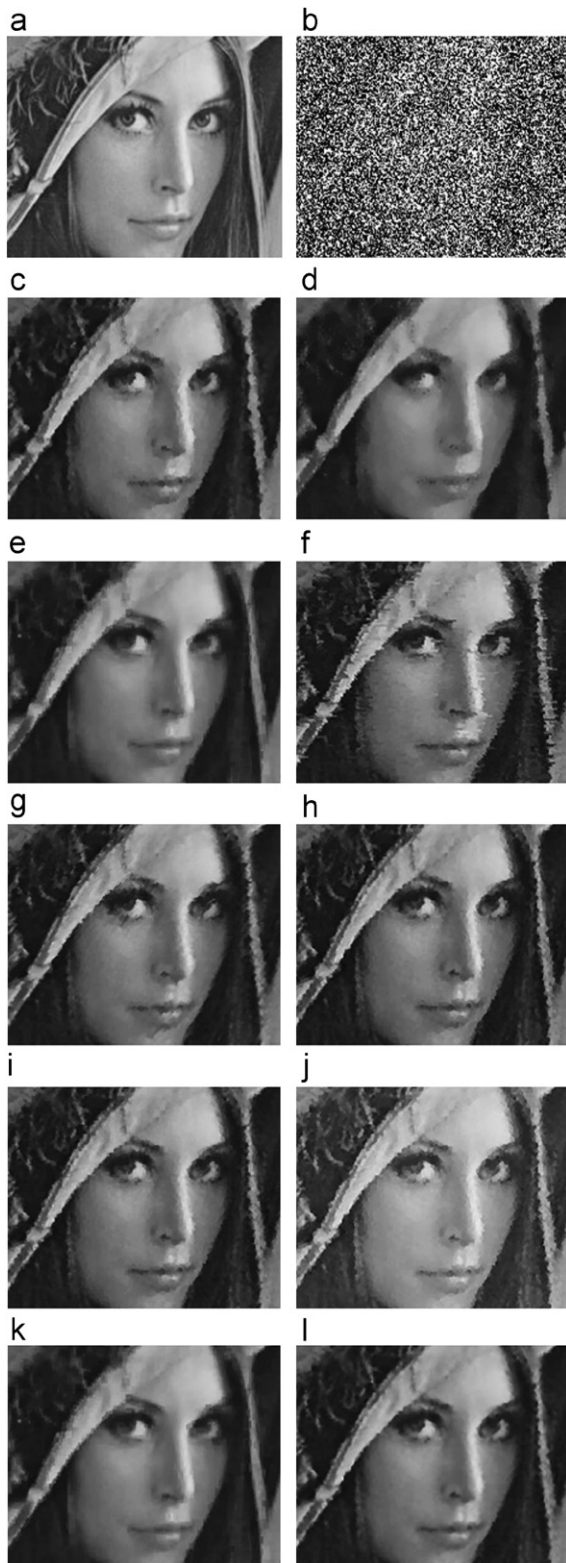


Fig. 5. Comparisons of restoration results using the various filters for the image Lena corrupted by 80% salt-and-pepper noise: (a) original image, (b) noisy image, (c) GLAM filter, (d) BDND filter, (e) OCS filter, (f) FSM filter, (g) EEP filter, (h) SAWM filter, (i) CNDSM filter, (j) NAFSM filter, (k) NAGM filter, and (l) DNLM filter.

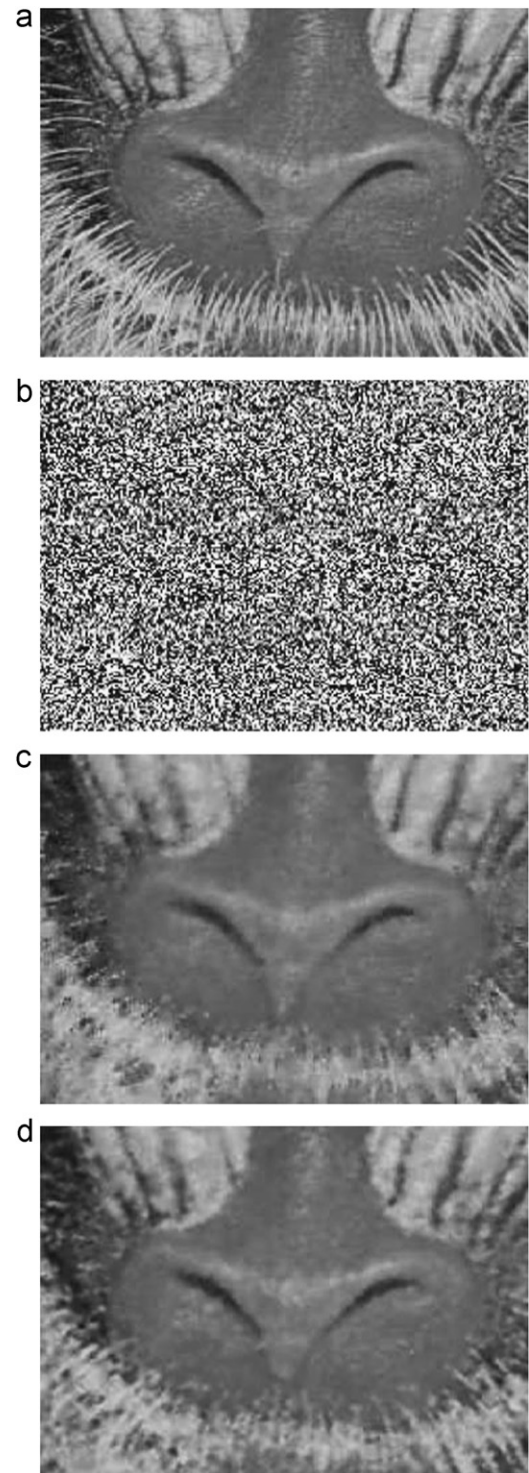


Fig. 6. Comparisons of restoration results using the NAGM filter and the DNLM filter for the image Mandrill corrupted by 80% salt-and-pepper noise: (a) original image, (b) noisy image, (c) NAGM filter, and (d) DNLM filter.

The proposed filter realizes noisy image restoration by identifying the corrupted pixels using the local statistics based noise detector and removing them using the

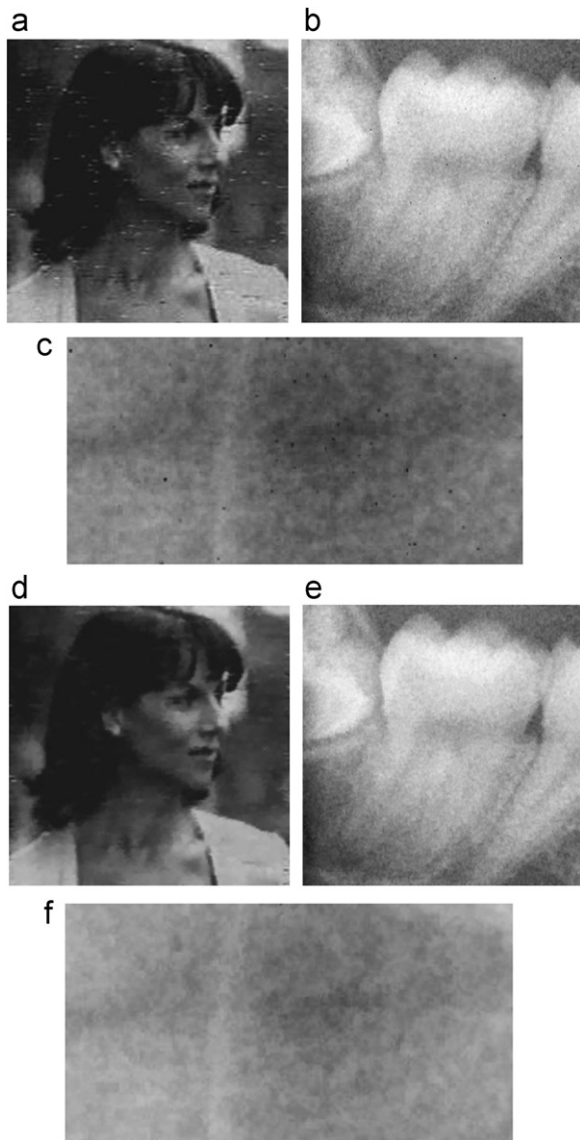


Fig. 7. The denoised results of the DNLM filter operating on the real corrupted images: (a) corrupted TV image, (b) corrupted panoramic radiograph, (c) corrupted cephalometric radiograph, (d) denoised TV image, (e) denoised panoramic radiograph, (f) denoised cephalometric radiograph.

distinctive reference image based non-local means filter, which computes the similarity between two pixels by the piecewise weight function with the adaptive decay parameters. Comparisons of restoration performance among the proposed filter and numerous switching-based techniques show that it outperforms the compared filters in suppressing noise and retaining image details.

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