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# Quantum Circuits as Novel Activation Functions in Cryptography

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## (some) Concepts

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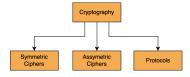
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#### Definition 1 (Cryptography)

Literature shows different definitions, and some of these are [2]

- The discipline that embodies the principles, means, and methods for transforming data to hide their semantic content, prevent unauthorized use or prevent undetected modification .
- It is the science of secret writing to hide the information .





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#### Definition 2 (Shannon Entropy)

It is given by

$$S = -\sum_{i=1}^{k} p_i \log_2 p_i \tag{1}$$

The entropy of uncertainty of a random variable X with probabilities  $p_i, \ldots, p_n$ .

#### Definition 3 (Von Neumann Entropy)

In the quantum information context,

$$H_V = -\sum_{i=1}^n \lambda_i \log_2 \lambda_i \tag{2}$$

Where  $\lambda_i$  are the eigenvalues of a density operator .

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#### Definition 4 (Trapdoor function, trapdoor one-way function )

A function  $f:\{0,1\}^* \to \{0,1\}^*$  is called **one-way** if the following two conditions hold . We additionally have the following two definitions,

- $1.\,$  A function that is easy to compute yet hard to invert without extra information is called a  $trapdoor\ function$  .
- 2. A function that is easily computed, and the calculation of its inverse is infeasible unless certain privileged information is known.

## Definition 5 (Protocol)

A **set of rules** used by two or more communicating entities that describe the message order and data structures for information exchanged between the entities is called **protocol** .

## Definition 6 (One-Time-Pad protocol)

The protocol encrypts a message using a public channel and uses the XOR operation.

## Implementation: QC and ML

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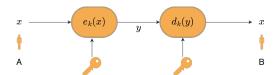
We use B the text in binary is  $H=1001000_2=72_{10}$  and ciphertext in binary system is  $Z=1011010_2=90_{10}$ . The subscripts refer to binary and decimal systems. We should notice

$$B = DEC(C, K) = DEC(ENC(B, K), K)$$

$$= DEC(B \oplus K, K)$$

$$= B \oplus K \oplus K$$

$$= B$$
(3)





# Example

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1. Encryption: To get the ciphertext,  $C = ENC(B, K) = B \oplus K$ 

2. Decryption: To get the text,  $B = DEC(C, K) = C \oplus K$ Example

1 Encryption

1. Encryption.

$$\begin{array}{c} 1001000 \ \to \ \mathsf{H} \\ \oplus \ 0010010 \ \to \ \mathsf{18} \\ \hline 1011010 \ \to \ \mathsf{Z} \end{array}$$

2. Decryption

$$\begin{array}{c} 1011010 \ \to \ Z \\ \oplus \ 0010010 \ \to \ 18 \\ \hline 1001000 \ \to \ H \end{array}$$



## Quantum Concepts

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### Definition 7 (Quantum key exchange (QKE))

It is the idea of exploiting quantum mechanics to improve classical protocols.

## Definition 8 (BB84 protocol)

Let A and B use two points to send information which should be two people; person-A implements two different orthogonal bases to send information.

## Definition 9 (B92 protocol)

This protocol implements one nonorthogonal basis to send information.



## **Applications**

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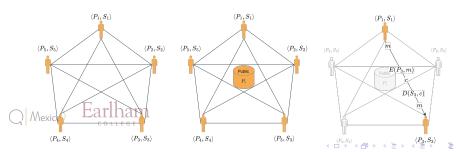
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Figure: Graph for n = 5 and k = 2: This represents a network with n = 5 users, where k = 2 users are engaged in pairwise communication.

- We will swap points and
- edges



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### Definition 10 (Activation Functions)

It is a nonlinear function to weight the sum of the inputs to a node.

Examples: Sigmoid, ReLU, softplus, tanh x

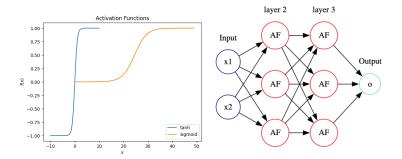


Figure: Examples of Activation functions and a fully connected network.

# Neural Networks for Cryptography

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### Theorem 11 (Cybenko)

Let  $f: \mathbb{R}^d \to \mathbb{R}$  be a function on a compact set  $K \subset \mathbb{R}^d$ . Then for any  $\epsilon > 0$  there exists a neural network with a single hidden layer of the form

$$\phi(x) = \sum_{i=1}^{N} \sum_{j=1}^{d} w_i^{(1)} \sigma(w_{ij}^{(0)} x_j + b_i^{(0)}) + b^{(1)},$$

 $\theta = \{w_{ii}^{(0)}, w_{i}^{(1)}, b_{i}^{(0)}, b^{(1)}\}$ , where  $\sigma : \mathbb{R} \to \mathbb{R}$  is an activation function<sup>2</sup>, such that

$$\sup_{x \in K} |f(x) - \phi(x)| < \epsilon.$$

The parameter N is known as the **width** [1].



1continuous

<sup>&</sup>lt;sup>2</sup>non-polynomial non-linear

## **Examples: Activation Function**

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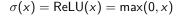
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$$\sigma(x) = \operatorname{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

$$\sigma(x) = \tanh x$$

$$\sigma(x) = \cos x, \sin x$$



Figure: Webbook: https://earlham-college.github.io/quaker-ece/

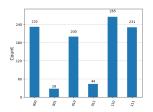
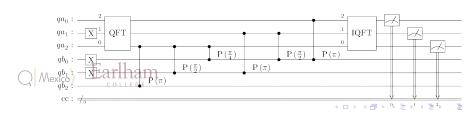


Figure: Addition=2+3 operation with QCircuits and simulator.



## Conclusions and Discussion

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• This paper examined key concepts in cybersecurity and their counterparts in the quantum domain.

- $\bullet$  It also provided foundational insights into prominent protocols in classical and quantum cryptography.
- We implemented a quantum circuit instead of an activation function.



## Future directions

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• Future work aims to expand on these fundamental concepts, incorporating emerging ideas from quantum computing, machine learning, and deep learning to contribute to developing next-generation cryptographic methods, particularly in the post-quantum cryptography era.

• Implement this and more experiments in a real quantum computer.



Figure: Webbook: https://github.com/jaorduz/QCandAI

### Thank you!



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References

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- [2] Javier Orduz. Mathematical foundations for Modern Cryptography in the Quantum Era. 2025. Accepted to be published soon.



