

Tree's and Trie's

Ukkonan's Alg

Implicit trees for S

1. in iteration i , tree I_{i+1} is constructed from I_i
2. this is done by $i+1$ extensions one for each of the $i+1$ suffixes of $S[1,...,i+1]$
3. In iteration (i,j) , alg finds the end of path from root w/ substrings $S[j,...,i]$
4. Extend substring by adding char $S(i+1)$ to end unless it's already there

Summary in iteration i $s[1,...,i+1]$ is put in tree $s[1,...,i+1]$, $s[2,...,i+1]$...

Cases;

Constant I_1

```
for i in range(1,m):
    for j in range(1,i+1):
        find the end of path from root to S[j...i] # Suffix
        if needed, extend by appending S(i+1)
        so now s[j...i+1] is in the tree
```

LEMMA: If some internal node v with path label $x\alpha$ was just added into tree at extension j , then

1. α already ends at internal node
2. an internal node at the end of α will be created in $j+1$