Computer Performance



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CSE3666: Introduction to Computer Architecture

Outline

- Metrics to compare computer performance
- CPU time (a.k.a. CPU Execution time or Execution time)
- CPI
- Speedup
- Amdahl's law

Reading: Sections 1.6 and 1.10

Math background | UConn CSE-3666

Metrics to compare computer performance

Response Time

How long it takes to complete a task

Throughput

- Total work done per unit time
 - e.g., tasks/transactions/... per hour





Throughput vs. Latency (delay)

Rates

- MFLOPS (million floating-point operations per second)
- MIPS (million instructions per second)
 - Not the same MIPS in MIPS ISA

Measuring Time

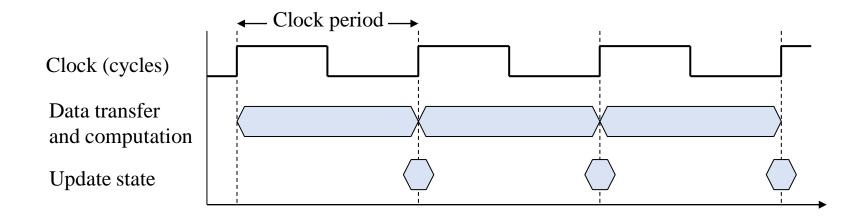
- Elapsed time
 - Total response time, including all aspects
 - Processing, I/O, OS overhead, idle time
 - Determines system performance

CPU Execution time

- Time the processor needs to process a given job
 - Excluding I/O time and other jobs' shares
- Comprises user CPU time and system CPU time
- Also called CPU time, or execution time
 - We do not consider I/O, OS, etc. in this course

CPU Clocking

Operation of digital hardware governed by a constant-rate clock



Clock period (cycle time): duration of a clock cycle

e.g.,
$$250ps = 0.25ns = 250 \times 10^{-12} s$$

Clock frequency (rate): cycles per second

e.g.,
$$4.0$$
GHz = 4000 MHz = 4.0×10^9 Hz

CPU Time

or

$$CPU Time = \frac{Clock Cycles}{Clock Rate}$$

- Performance improved by
 - Reducing number of clock cycles
 - Increasing clock rate
 - Hardware designer must often trade off clock rate against cycle count

Performance

We can define performance as

Performance =
$$\frac{1}{\text{CPU Time}}$$

It is CPU execution time

As CPU execution time decreases, performance increases

Comparing performance

"X is *n* time faster than Y"

"... than Y"
Y's time is the top number

$$n = \frac{\text{Performance}_{x}}{\text{Performance}_{y}} = \frac{\frac{1}{\text{ExecutionTime}_{x}}}{\frac{1}{\text{ExecutionTime}_{y}}} = \frac{\text{ExecutionTime}_{y}}{\text{ExecutionTime}_{x}}$$

We will use the execution time, to avoid confusion.

n can be less than 1. What does that mean?

Example

Time taken to run a program is 10s on A and 15s on B. Intuitively, A is faster than B.

$$n = \frac{\text{ExecutionTime}_B}{\text{ExecutionTime}_A} = \frac{15}{10} = 1.5$$

So A is 1.5 times faster than B.

B's time is at the top.

Question - Performance

Processor A's clock rate is 2 GHz

Processor B's clock rate is 3 GHz

An application needs 30% more clock cycles on Processor B.

How much faster is the application on Processor B?

Solutions

CC: Clock cycles

ExecutionTime_A =
$$CC_A \times 0.5 \text{ ns} = 0.5 \times CC_A \text{ ns}$$

B is faster...

ExecutionTime_B = $(1.30 \times CC_A) \times 0.333$ ns = $0.433 \times CC_A$ ns

$$\frac{\text{ExecutionTime}_{A}}{\text{ExecutionTime}_{B}} = \frac{0.5 \times \text{CC}_{A} \text{ ns}}{0.433 \times \text{CC}_{A} \text{ ns}} = 1.15$$
...by this much

Processor B is 1.15 times faster than process A.

Question

Processor A: 2GHz clock, 10s CPU time for an application

Designing Processor B, using the same ISA

Processor B can run at a faster clock rate, but needs $1.2 \times$ clock cycles.

If we want to achieve 6s CPU time on process B, how fast must processor B's clock be?

Solutions

Compute the number of clock cycles (CC_A) for A first.

Compute the number of clock cycles for B: $CC_B = 1.2 \times CC_A$ Compute the targeted clock rate.

$$CC_A = \frac{CPU \text{ Time}_A}{Clock \text{ Cycle Time}_A} = CPU \text{ Time}_A \times Clock \text{ Rate}_A$$

= $10s \times 2GHz = 20 \times 10^9$
 $CC_B = 1.2 \times CC_A = 1.2 \times 20 \times 10^9 = 24 \times 10^9$

$$\begin{aligned} & \text{Clock Cycle Time}_{B} = \frac{\text{CPU Time}_{B}}{\text{CC}_{B}} = \frac{6\text{s}}{24\times10^{9}} = 0.25 \text{ ns} \\ & \text{Clock Rate}_{B} = \frac{1}{\text{Clock Cycle Time}_{B}} = \frac{1}{0.25 \text{ ns}} = 4\text{GHz} \end{aligned}$$

Calculating the number of cycles

How many cycles do these instructions take?

```
# Method 1 RISC-V code
                s0, x0, 0
        addi
                s1, x0, 0
        addi
        addi
                s2, x0, 100
        bge
                s0, s2, exit
loop:
                s1, s1, s0
        add
        addi
                s0, s0, 1
        beg
                x0, x0, loop
exit:
```

How many instructions are executed?

CPI (clock Cycles Per Instruction)

$$CPI = \frac{Clock Cycles}{Instruction Count}$$

or

Clock Cycles = Instruction Count \times CPI

- Instructions take different number of cycles to execute
 - Example: One cycle for add, 10 cycles for mul, 20 cycles for lw
- Very often we need to compute average CPI with mixed types of instructions

Computing average CPI

• If we know the clock cycles and the instruction count:

$$CPI = \frac{Clock Cycles}{Instruction Count}$$

Compute weighted average

$$CPI = \sum_{i=1}^{n} \left(CPI_i \times \frac{Instruction Count_i}{Instruction Count} \right)$$

$$Clock \ cycles \ that \ frequency \ (or \ weight) \ of \ class \ i \ instructions$$

Example

- A processor has three classes of instructions: A, B, and C
- A program can be compiled differently and has two instruction (execution) sequences.
- Find average CPI for each sequence.

Instruction counts (ICs) are in billions.

Class	A	В	С
CPI of each class	1	2	3
IC in Sequence 1	2	1	2
IC in Sequence 2	4	1	1

What is the CPI for Sequence 1?

Example: Sequence 1

Class	A	В	С
CPI of each class	1	2	3
IC in Sequence 1	2	1	2
IC in Sequence 2	4	1	1

Sequence 1

$$IC = 2 + 1 + 2 = 5$$
 billion

Clock Cycles =
$$2 \times 1 + 1 \times 2 + 2 \times 3 = 10$$
 billion

Average
$$CPI = 10 / 5 = 2$$

What is the CPI for Sequence 2?

Answer for Sequence 2

Sequence 2

IC =
$$4 + 1 + 1 = 6$$

Clock Cycles = $4 \times 1 + 1 \times 2 + 1 \times 3 = 9$
Average CPI = $9 / 6 = 1.5$

Questions

• Find average CPI for sequences 1 and 2.

Class	A	В	С
CPI of each class	1	2	3
Sequence 1	50%	10%	40%
Sequence 2	40%	35%	25%

Solutions

Sequence 1

Avg.
$$CPI = 0.5 \times 1 + 0.1 \times 2 + 0.4 \times 3 = 1.9$$

Sequence 2

Avg. CPI =
$$0.4 \times 1 + 0.35 \times 2 + 0.25 \times 3 = 1.85$$

Earlier Example: Sequence 1

Class	A	В	С
CPI of each class	1	2	3
IC in Sequence 1	2	1	2
IC in Sequence 2	4	1	1

Sequence 1

$$IC = 2 + 1 + 2 = 5$$
 billion

Clock Cycles =
$$2 \times 1 + 1 \times 2 + 2 \times 3 = 10$$
 billion

Average
$$CPI = 10 / 5 = 2$$

Another method:

Find the frequency of each class of instructions and compute weighted average

Class A:
$$2/5 = 0.4$$
 Class B: $1/5 = 0.2$ Class C: $2/5 = 0.4$

Average CPI =
$$1 * 0.4 + 2 * 0.2 + 3 * 0.4 = 2$$

Compute clock cycles

• Compute average CPI (of all instructions) first

Clock Cycles = Instruction Count
$$\times$$
 CPI_{average}

Add up clock cycles of each class of instructions

Clock Cycles =
$$\sum_{i=1}^{n} (CPI_i \times Instruction Count_i)$$
clock cycles for class i

Combining two equations

We have two equations:

CPU Time =
$$\frac{\text{Clock Cycles}}{\text{Cycles}} \times \frac{\text{Clock Cycle Time}}{\text{Eq. 1}}$$

Clock Cycles = Instruction Count
$$\times$$
 CPI Eq. 2

Substitute Eq. 2 into Eq. 1:

Classic equation

CPU Time = Instruction Count \times CPI \times Clock Cycle Time

• To reduce CPU Time, reduce any of the three factors

Hardware/software	Affects what?
Algorithm	Instruction count, CPI
Programming language	Instruction count, CPI
Compiler	Instruction count, CPI
Instruction set architecture	Instruction count, CPI, clock cycle time
Microarchitecture	CPI, clock cycle time
Circuit design	CPI, clock cycle time

Example

Run the same program on two processors that have the same ISA.

Computer A: Cycle Time = 250ps, CPI = 2.0

Computer B: Cycle Time = 500ps, CPI = 1.2

Which computer is faster, and by how much?

Solutions

Run the same program on two processors that have the same ISA.

Computer A: Cycle Time = 250ps, CPI = 2.0

Computer B: Cycle Time = 500ps, CPI = 1.2

Which computer is faster, and by how much?

CPU Time_B = IC × CPI_B × Cycle Time_B
= IC ×
$$1.2 \times 500$$
ps = IC × 600 ps

$$\frac{\text{CPU Time}_{\text{B}}}{\text{CPU Time}_{\text{A}}} = \frac{\text{IC} \times 600 \text{ ps}}{\text{IC} \times 500 \text{ ps}} = 1.2$$

...by this much

Speedup

Compare the performance of design options.

The new design is _____ times faster than the original.

" than the original."
The original time is at the top

$$Speedup = \frac{CPU Time_{before_enhancement}}{CPU Time_{after_enhancement}}$$

Example:

Using a new method, 40% of an application can execute 10 times faster. What is the overall speedup of the new method on the application?

Solution

Speedup =
$$\frac{1}{0.6 + \frac{0.4}{10}} = \frac{1}{0.64} = 1.56$$

Amdahl's law

• The performance improvement to be gained from using some faster mode of execution is limited by the fraction of the time the faster mode can be used.

Make common case fast!

The best speedup you can achieve by optimizing the 40% code is

BestSpeedup =
$$\frac{1}{0.6} \approx 1.6$$

Pitfall: Amdahl's Law

• Improving an aspect of a computer and expecting a proportional improvement in overall performance

$$T_{improved} = \frac{T_{affected}}{improvement factor} + T_{unaffected}$$

Example:

Multiplication accounts for 80% of the execution time.

How much improvement in multiplication performance is needed to get 5× overall speedup?

$$\frac{1}{\frac{0.8}{x} + 0.2} = 5$$

Performance Summary

CPU Time = Instruction Count \times CPI \times Clock Cycle Time

- Performance depends on all three factors
- Optimization can be done at many levels
 - Algorithm, programming language, compiler, instruction set architecture, microarchitecture, and hardware implementation
- Amdahl's Law

Question

Processors A and B have the same ISA.

Processor A runs at 2 GHZ and Processor B runs at 2.5 GHZ.

For an application, the CPI is 1.5 on Processor A, and 1.7 on Processor B.

If you switch from Processor A to Processor B, what is the speedup?

Truncate to the first digit after the decimal point, e.g., 4.15 to 4.1

Answer

Instruction count (IC) is the same.

$$\frac{\text{CPU Time}_{A}}{\text{CPU Time}_{B}} = \frac{\text{IC} \times 1.5 \times \frac{1}{2 \times 10^{9}}}{\text{IC} \times 1.7 \times \frac{1}{2.5 \times 10^{9}}} = \frac{1.5 \times 2.5}{1.7 \times 2} = 1.10$$

B (the new system) is 1.10 times faster than A. A's time is at the top.

To Improve Performance

- Algorithm
 - Determines number of operations executed
- Programming language, compiler, architecture
 - Determine number of machine instructions executed per operation
- Processor and memory system
 - Determine how fast instructions are executed
- I/O system (including OS)
 - Determines how fast I/O operations are executed

Defining Performance

• Which airplane has the best performance?

