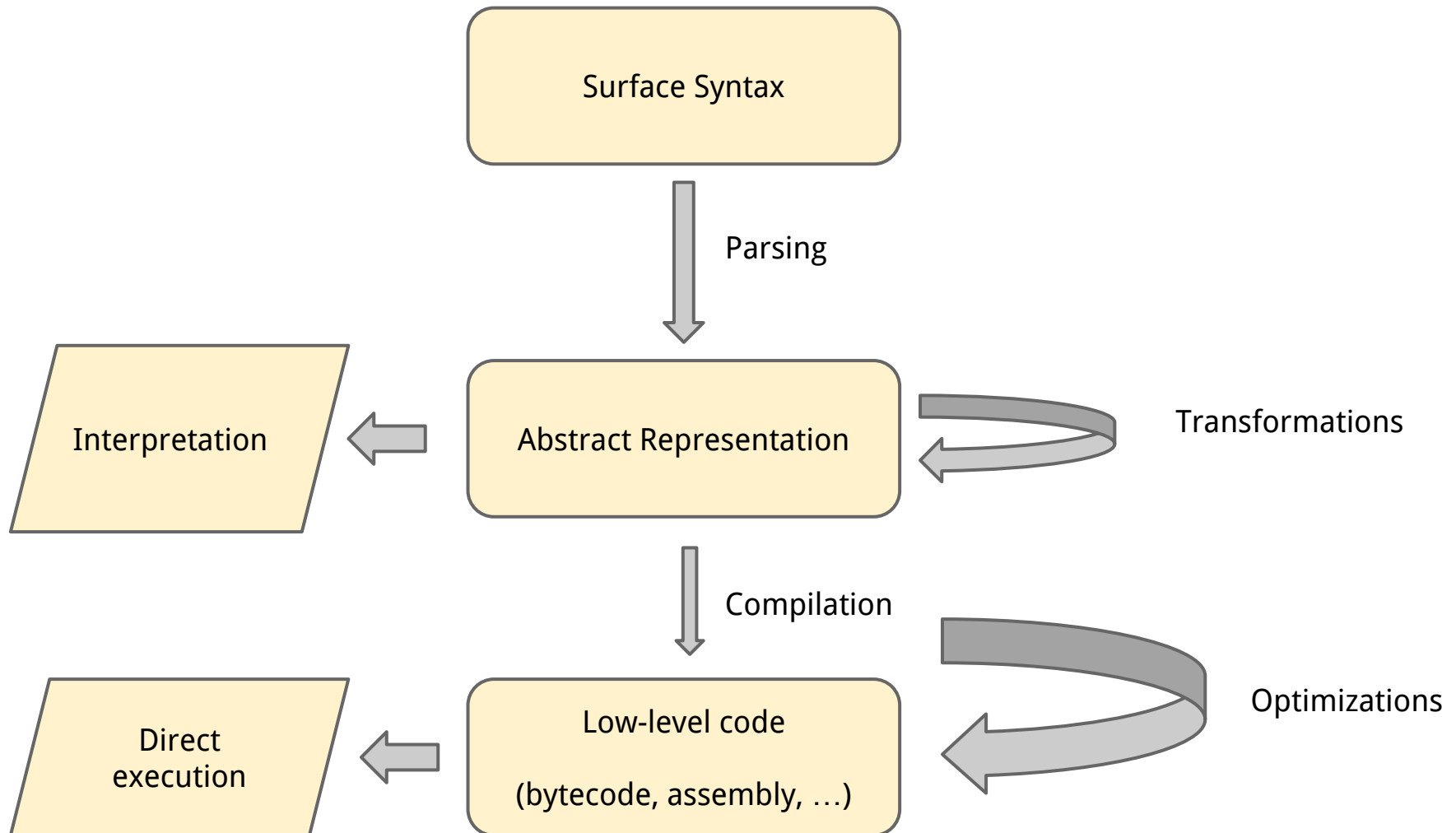


Introduction to Interpretation

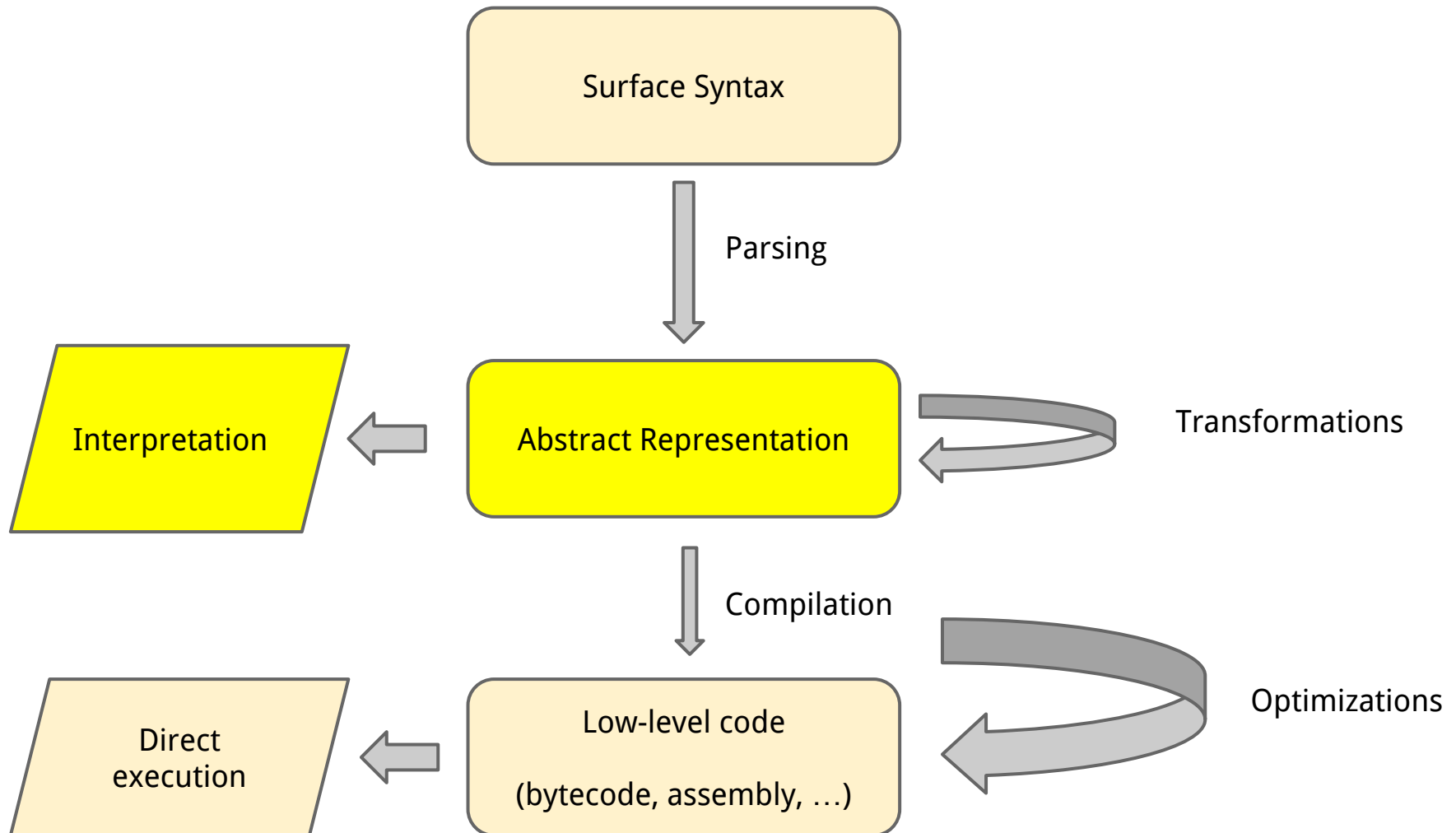
January 25, 2018

Riccardo Pucella

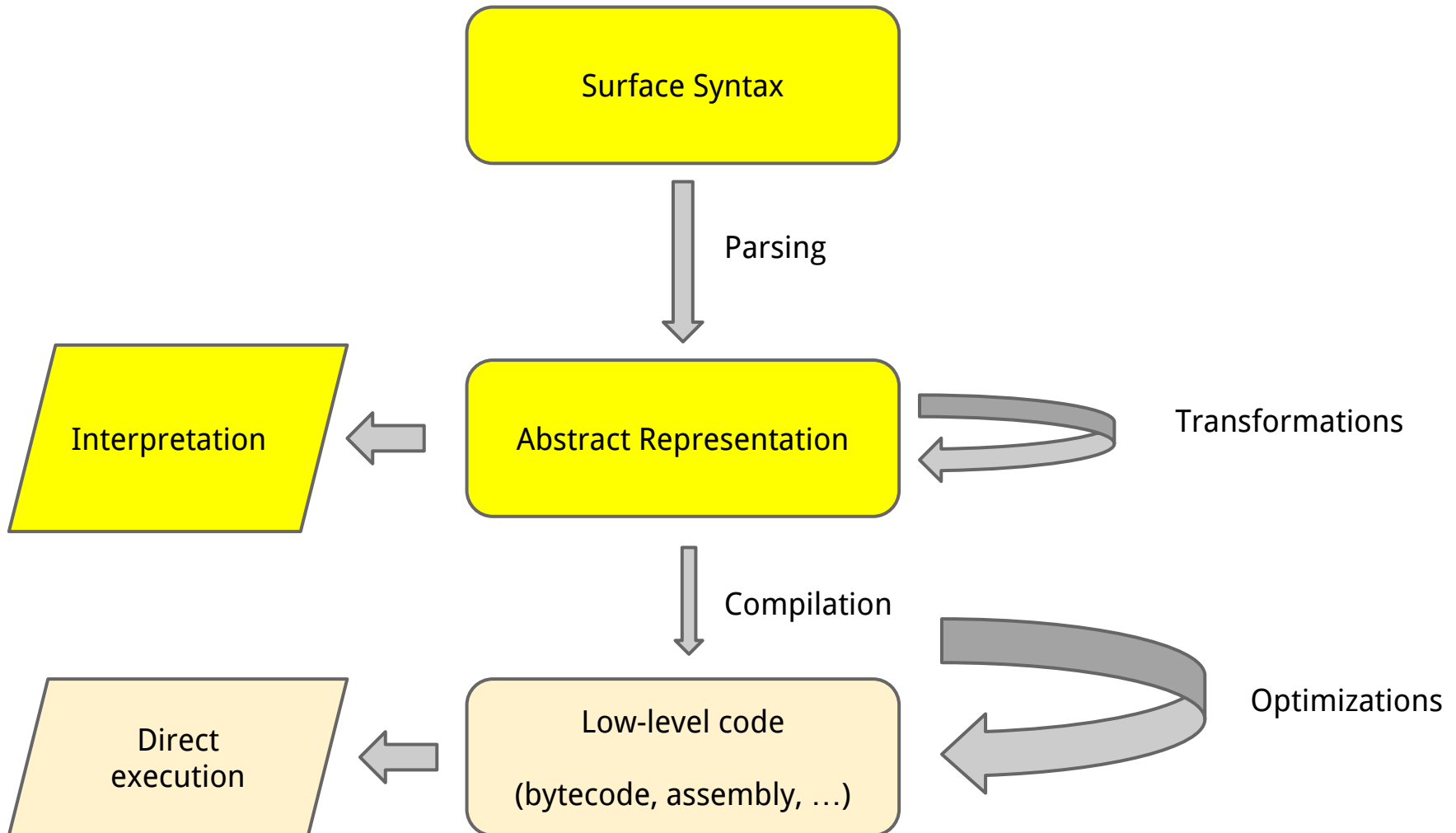
The structure of language execution



The structure of language execution



The structure of language execution

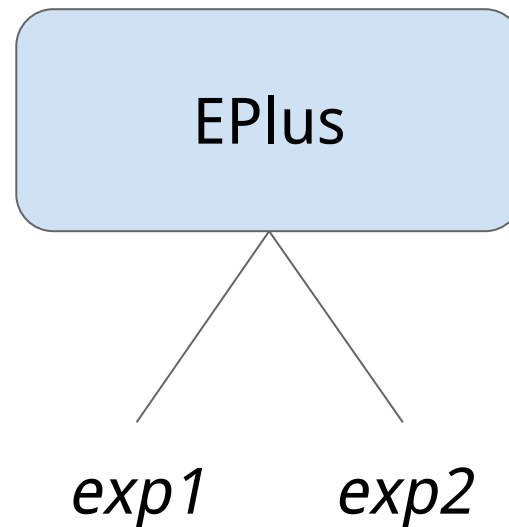
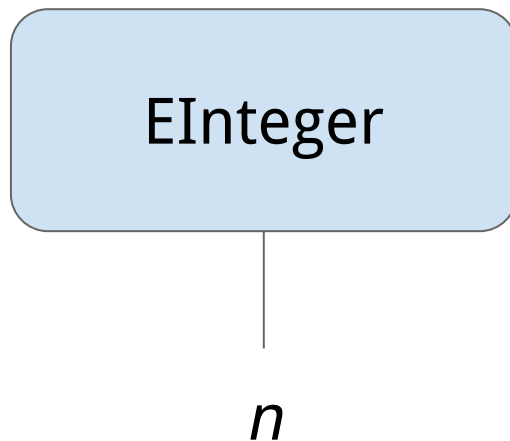


A simple expression language

- We're going to build-up a small language of mathematical expressions
- Computing over the integers
 - Operations $+$, $*$
 - Easy to expand ($-$, mod , div , ...)
- Abstract representation needs to account for nesting expressions
 - E.g., $(3 + 4) * (5 + 6)$

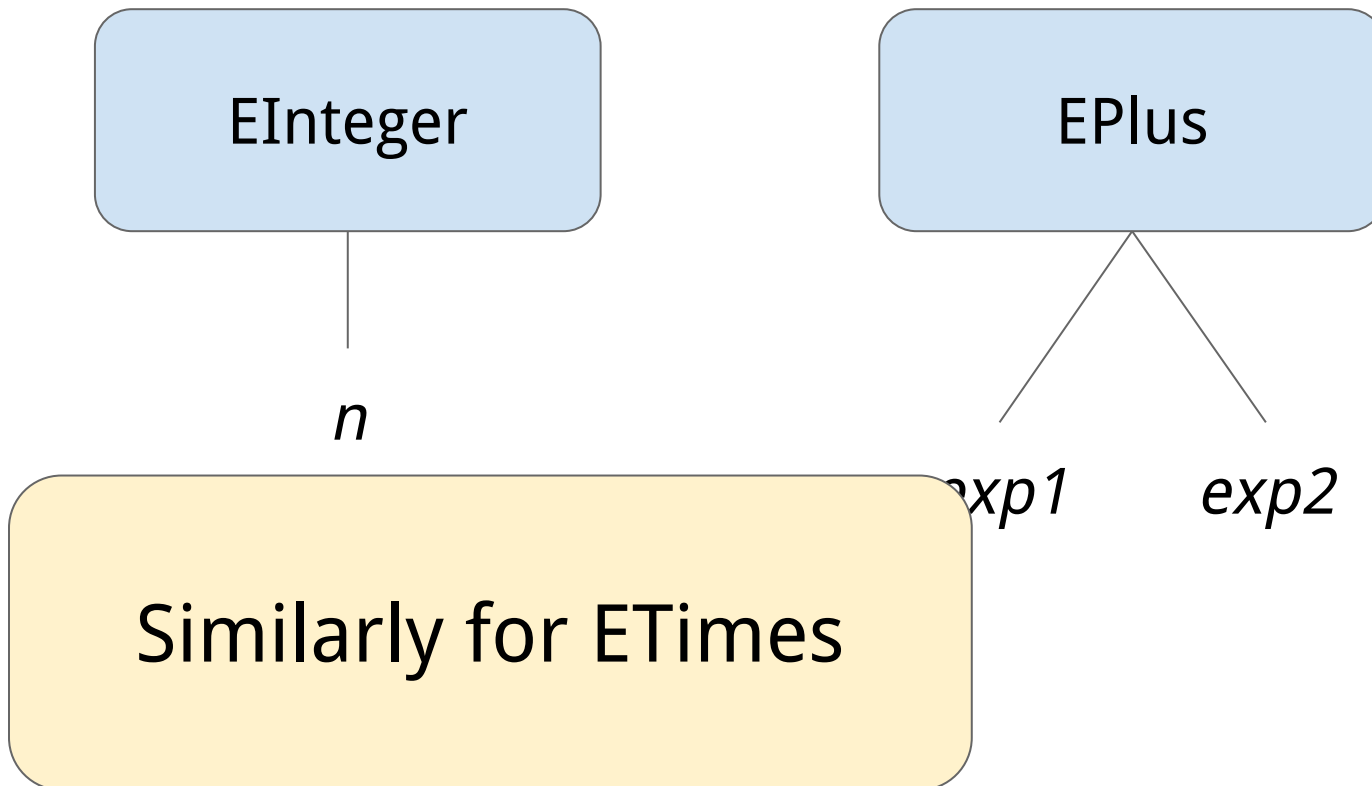
Abstract representation

An expression is a tree. Nodes are kinds of expressions:

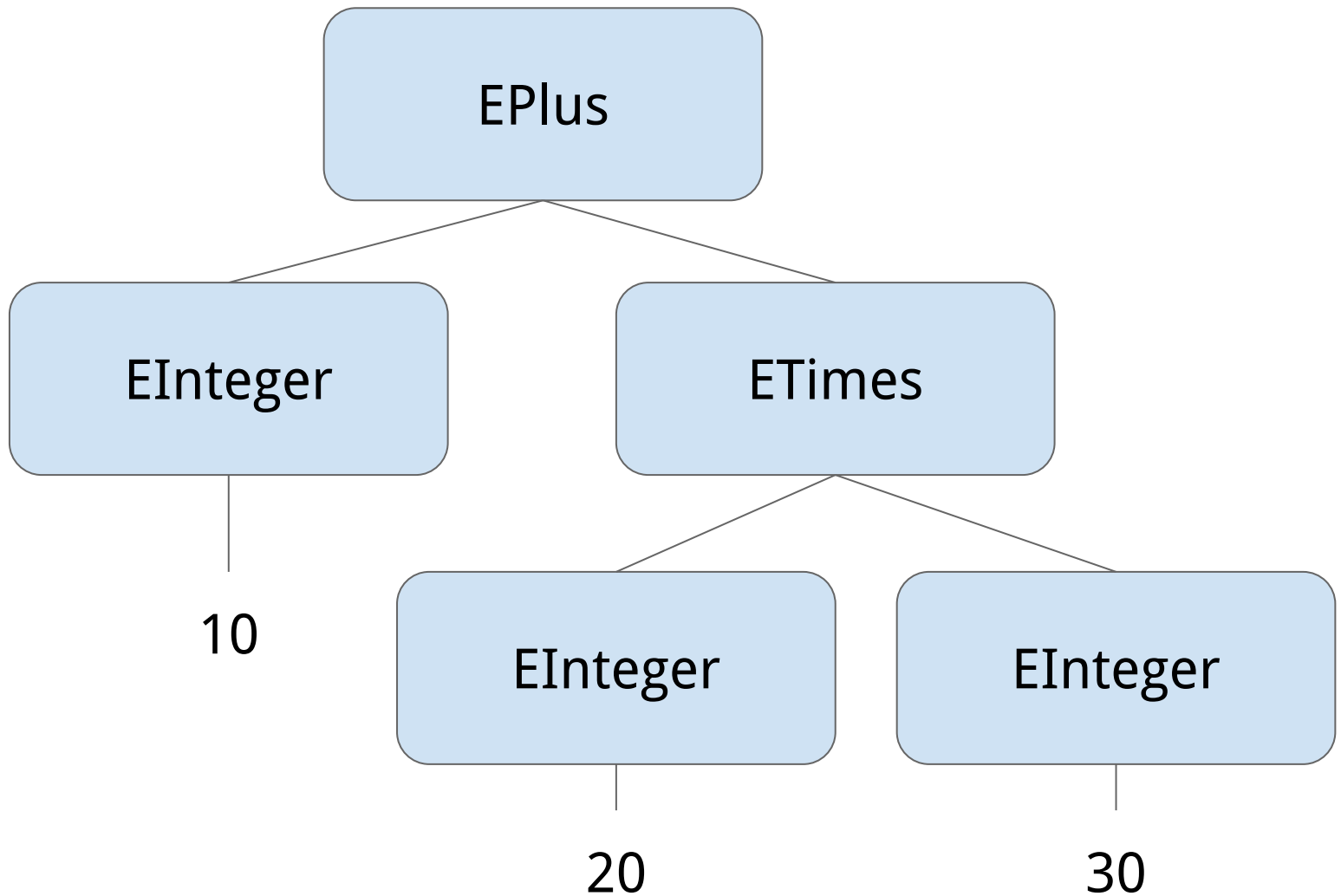


Abstract representation

An expression is a tree. Nodes are kinds of expressions:



Example: $10 + (20 * 30)$



Abstract Representation in Scala

```
abstract class Exp
```

```
class EInteger (val i:Int) extends Exp {  
  override def toString () : String =  
    "EInteger(" + i + ")"
```

```
class EPlus (val e1:Exp, val e2:Exp) extends Exp {  
  override def toString () : String =  
    "EPlus(" + e1 + "," + e2 + ")"
```

```
class ETimes (val e1:Exp, val e2:Exp) extends Exp {  
  override def toString () : String =  
    "ETimes(" + e1 + "," + e2 + ")"
```

Abstract Representation in Scala

```
abstract class Exp
```

```
class EInteger (val i:Int) extends Exp {
```

```
  override def toString(): String = i.toString
```

Constructing our example:

```
new EPlus(new EInteger(10),  
          new ETimes(new EInteger(20),  
                     new EInteger(30)))
```

Evaluation

Evaluation is the process of taking an expression and reducing it to a value

- aka *execution*

Every node in the abstract representation has an evaluation method that evaluates the expression to a value

- evaluating an expression generally requires recursively evaluating subexpressions

Evaluation

```
abstract class Exp {  
    def eval (): Int  
}
```

Evaluation for integer literals

```
class EInteger (val i:Int) extends Exp {  
  
  override def toString () : String =  
    "EInteger(" + i + ")"  
  
  def eval () : Int =  
    i  
  
}
```

Evaluation for addition

```
class EPlus (val e1:Exp, val e2:Exp) extends Exp {  
  
  override def toString () : String =  
    "EPlus(" + e1 + "," + e2 + ")"  
  
  def eval () : Int = {  
    val i1 = e1.eval()  
    val i2 = e2.eval()  
    return i1 + i2  
  }  
  
}
```

Evaluation for multiplication

```
class ETimes (val e1:Exp, val e2:Exp) extends Exp {  
  
  override def toString () : String =  
    "ETimes(" + e1 + "," + e2 + ")"  
  
  def eval () : Int = {  
    val i1 = e1.eval()  
    val i2 = e2.eval()  
    return i1 * i2  
  }  
  
}
```

Conditionals

Let's make evaluation depends on a condition

In C / Javascript, you have expression

cond ? then : else

Evaluates to *then* if *cond* is true, *else* otherwise

For now, a condition is true if it is non-zero

- Next time, we add actual Booleans

Conditionals

```
class EIf (val c:Exp, val t:Exp, val e:Exp) extends Exp {  
  
  override def toString () : String =  
    "EIf(" + c + "," + t + "," + e + ")"  
  
  def eval () : Int = {  
    val ci = c.eval()  
    if (ci == 0) {  
      return e.eval()  
    } else {  
      return t.eval()  
    }  
  }  
}
```