

p8106_hw2_jsg2145

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```
collegedf = read_csv("./data/College.csv") %>%  
  janitor::clean_names() %>%  
  mutate(college = factor(college)) %>%  
  select(outstate, everything())
```

```
## Parsed with column specification:  
## cols(  
##   College = col_character(),  
##   Apps = col_double(),  
##   Accept = col_double(),  
##   Enroll = col_double(),  
##   Top10perc = col_double(),  
##   Top25perc = col_double(),  
##   F.Undergrad = col_double(),  
##   P.Undergrad = col_double(),  
##   Outstate = col_double(),  
##   Room.Board = col_double(),  
##   Books = col_double(),  
##   Personal = col_double(),  
##   PhD = col_double(),  
##   Terminal = col_double(),  
##   S.F.Ratio = col_double(),  
##   perc.alumni = col_double(),  
##   Expend = col_double(),  
##   Grad.Rate = col_double()  
## )
```

```
college.train = collegedf %>%  
  filter(college != "Columbia University")
```

```
x.train = model.matrix(outstate ~ apps + accept + enroll + top10perc + top25perc + f_undergrad + p_unde
```

```
y.train = pull(college.train, outstate)
```

```
ctrl1 = trainControl(method = "cv", number = 5)
```

```
p1 = college.train %>%  
  ggplot(aes(x = apps, y = outstate)) +  
  geom_point()
```

```
p2 = college.train %>%  
  ggplot(aes(x = accept, y = outstate)) +  
  geom_point()
```

```
p3 = college.train %>%  
  ggplot(aes(x = enroll, y = outstate)) +
```

```

geom_point()

p4 = college.train %>%
  ggplot(aes(x = top10perc, y = outstate)) +
  geom_point()

p5 = college.train %>%
  ggplot(aes(x = top25perc, y = outstate)) +
  geom_point()

p6 = college.train %>%
  ggplot(aes(x = f_undergrad, y = outstate)) +
  geom_point()

p7 = college.train %>%
  ggplot(aes(x = p_undergrad, y = outstate)) +
  geom_point()

p8 = college.train %>%
  ggplot(aes(x = room_board, y = outstate)) +
  geom_point()

p9 = college.train %>%
  ggplot(aes(x = books, y = outstate)) +
  geom_point()

p16 = college.train %>%
  ggplot(aes(x = ph_d, y = outstate)) +
  geom_point()

p10 = college.train %>%
  ggplot(aes(x = personal, y = outstate)) +
  geom_point()

p11 = college.train %>%
  ggplot(aes(x = terminal, y = outstate)) +
  geom_point()

p12 = college.train %>%
  ggplot(aes(x = s_f_ratio, y = outstate)) +
  geom_point()

p13 = college.train %>%
  ggplot(aes(x = perc_alumni, y = outstate)) +
  geom_point()

p14 = college.train %>%
  ggplot(aes(x = grad_rate, y = outstate)) +
  geom_point()

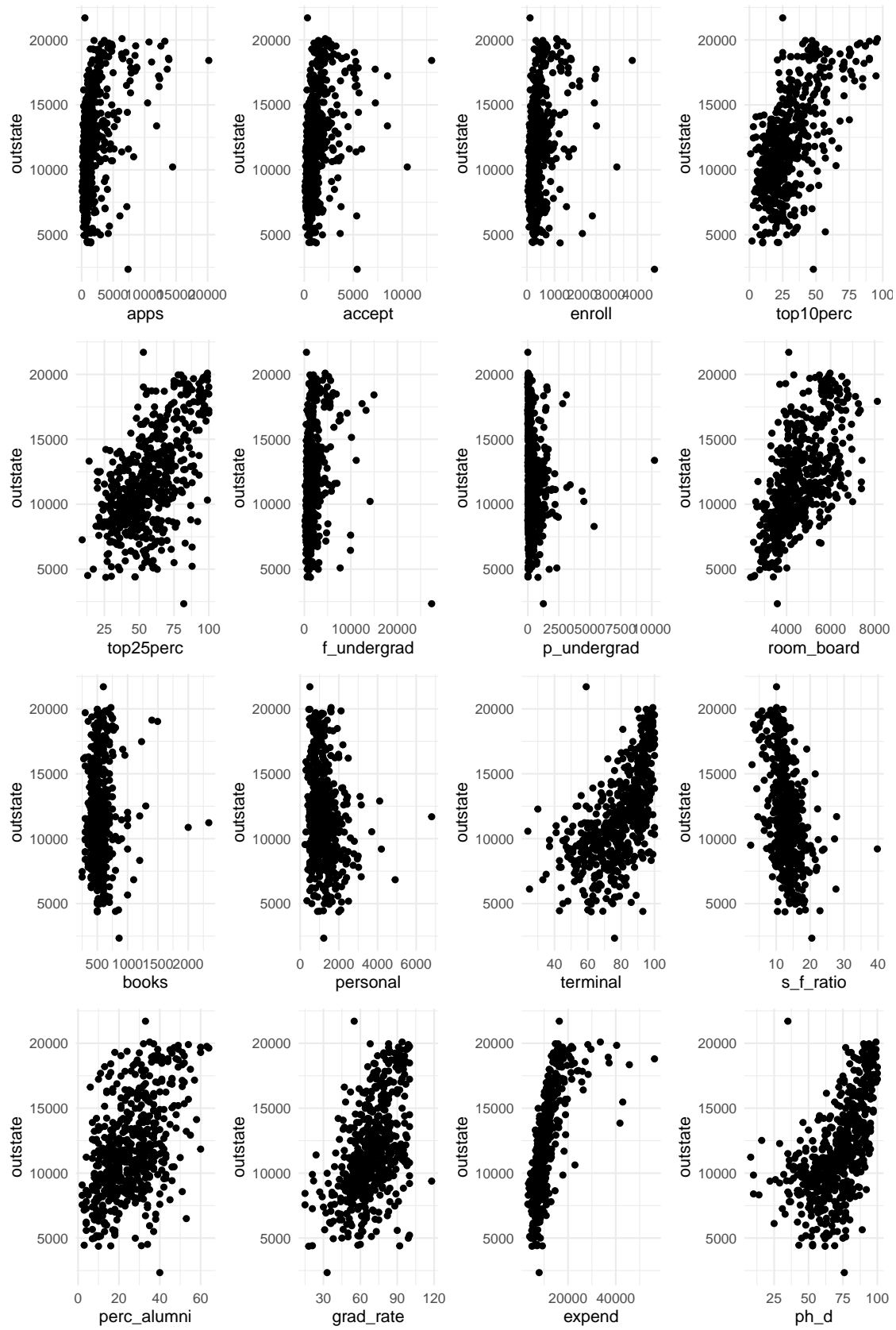
p15 = college.train %>%
  ggplot(aes(x = expend, y = outstate)) +
  geom_point() +

```

```
scale_x_continuous(breaks = c(0, 20000, 40000, 65000))
```

Part a

```
plots = list(p1, p2, p3, p4, p5, p6, p7, p8, p9, p10, p11, p12, p13, p14, p15, p16)  
wrap_plots(plots, ncol = 4)
```



Part

b

```

spline.term9 = smooth.spline(pull(college.train, terminal), pull(college.train, outstate), df = 9)
spline.term10 = smooth.spline(pull(college.train, terminal), pull(college.train, outstate), df = 10)
spline.term11 = smooth.spline(pull(college.train, terminal), pull(college.train, outstate), df = 11)
spline.term12 = smooth.spline(pull(college.train, terminal), pull(college.train, outstate), df = 12)
spline.term13 = smooth.spline(pull(college.train, terminal), pull(college.train, outstate), df = 13)
spline.termA = smooth.spline(pull(college.train, terminal), pull(college.train, outstate), cv = TRUE)
spline.termA$df

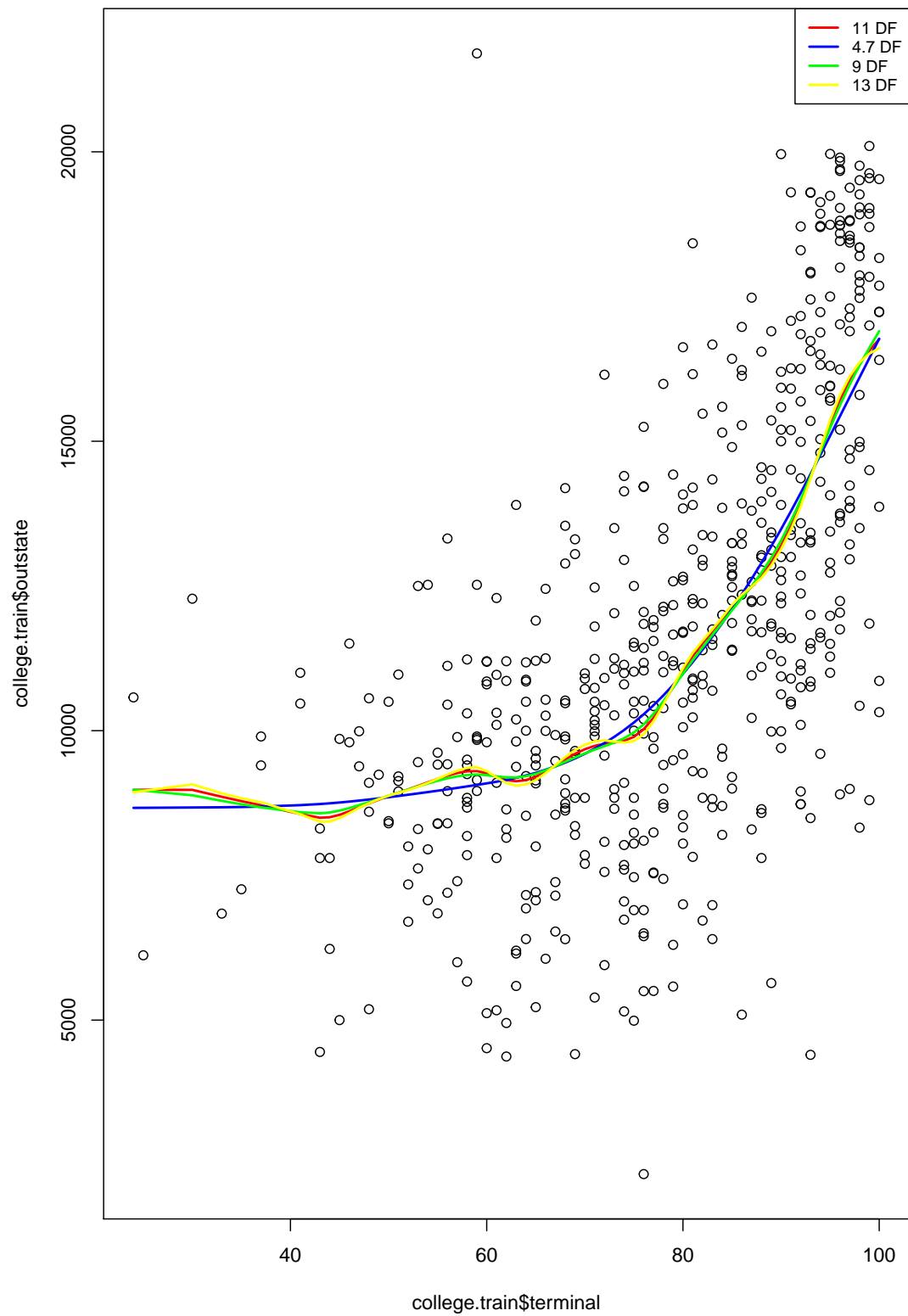
```

```
## [1] 4.686019
```

```

plot(college.train$terminal, college.train$outstate)
points(x.train, cex = .5,
       col = "darkgrey")
lines(spline.term11, col = "red ", lwd = 2)
lines(spline.termA, col = "blue", lwd = 2)
lines(spline.term9, col = "green", lwd = 2)
lines(spline.term13, col = "yellow", lwd = 2)
legend("topright", legend = c("11 DF", "4.7 DF", "9 DF", "13 DF"),
       col = c("red", "blue", "green", "yellow"), lty = 1, lwd = 2, cex = .8)

```

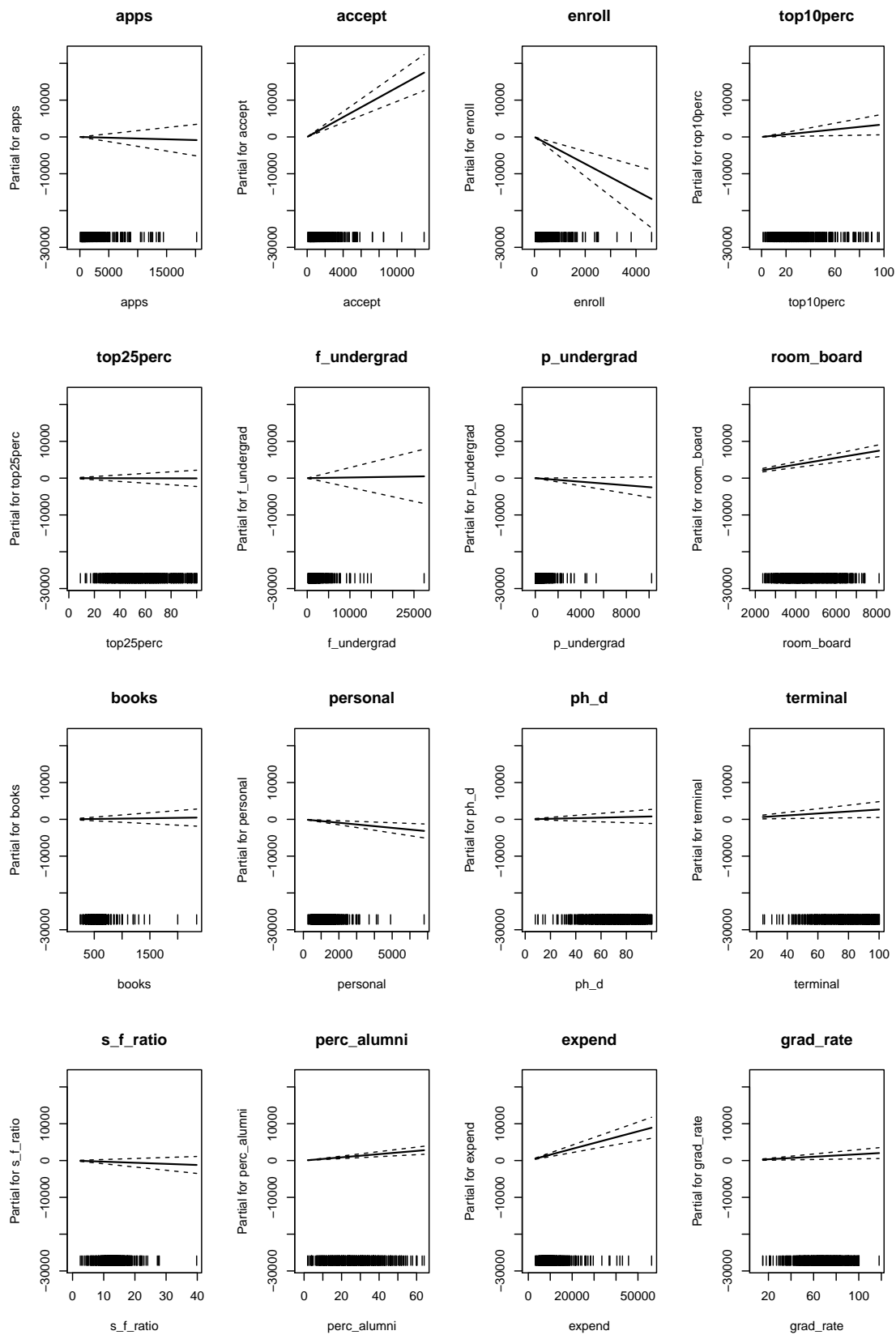


This graph shows a smoothing spline using cross validation to choose degrees of freedom compared with various other degrees of freedom.

Part c

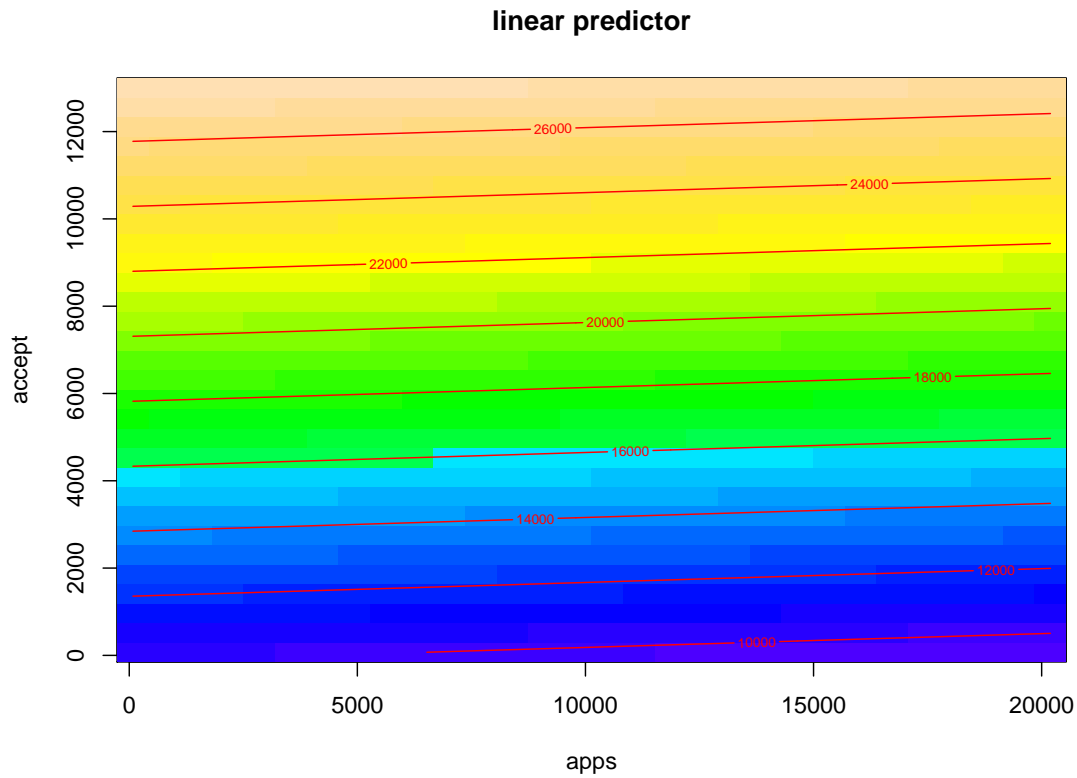
```
gam1 = gam(outstate ~ apps + accept + enroll + top10perc + top25perc + f_undergrad + p_undergrad + room,
            data = data)

par(mfrow = c(4,4))
plot(gam1, pages=1, residuals=TRUE, all.terms=TRUE, shade=TRUE, shade.col=2)
```



The above graph shows a plot of the partial dependence of each predictor in relation to the tuition.

```
vis.gam(gam1, view = c("apps", "accept"),
        plot.type = "contour", color = "topo")
```



This plot shows a contour of the dependence of two predictors on each other.

```
set.seed(22)
college.gam = train(x.train, y.train,
                    method = "gam",
                    tuneGrid = data.frame(method = "GCV.Cp",
                                           select = c(TRUE, FALSE)),
                    trControl = ctrl1)

college.gam$bestTune
```

```
## select method
## 1 FALSE GCV.Cp
```

```
college.gam$finalModel
```

```
##
## Family: gaussian
## Link function: identity
##
```

```
## Formula:
## .outcome ~ s(perc_alumni) + s(terminal) + s(top10perc) + s(ph_d) +
##       s(grad_rate) + s(books) + s(top25perc) + s(s_f_ratio) + s(personal) +
##       s(p_undergrad) + s(enroll) + s(room_board) + s(accept) +
##       s(f_undergrad) + s(apps) + s(expend)
##
## Estimated degrees of freedom:
## 1.90 5.14 3.64 6.32 4.27 2.35 1.00
## 4.33 1.00 1.00 1.00 2.13 3.58 6.28
## 4.59 6.45 total = 55.98
##
## GCV score: 2761951
```

Part d

```
mars_grid <- expand.grid(degree = 1:2,
                        nprune = 2:16)

college.earth = train(x.train, y.train,
                     method = "earth", tuneGrid = mars_grid, trControl = ctrl1)
```

```
## Loading required package: earth
```

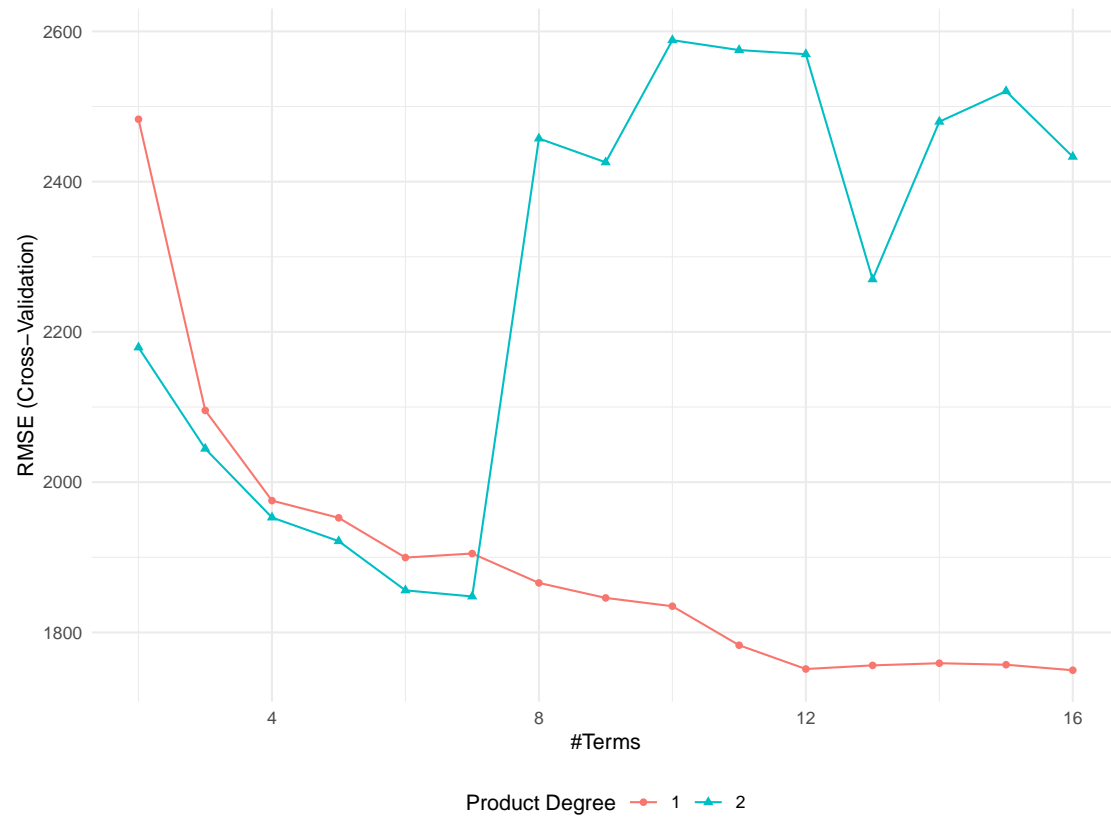
```
## Loading required package: Formula
```

```
## Loading required package: plotmo
```

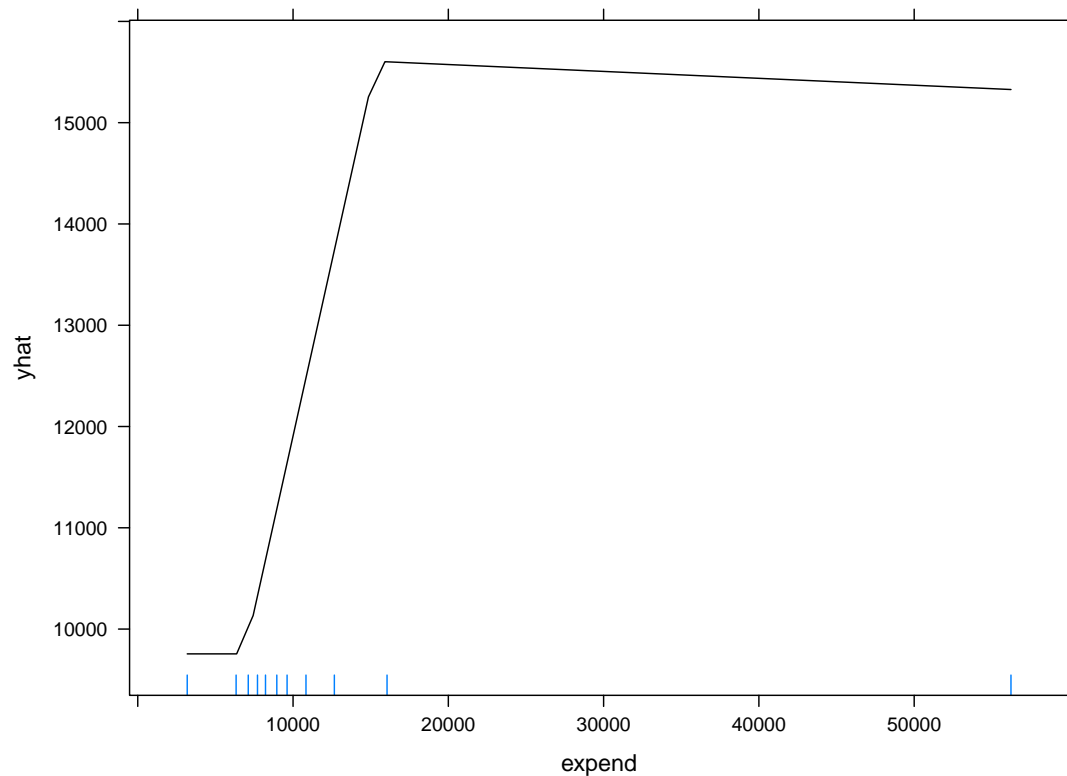
```
## Loading required package: plotrix
```

```
## Loading required package: TeachingDemos
```

```
ggplot(college.earth)
```



```
partial(college.earth, pred.var = "expend", plot = TRUE, rug = TRUE)
```



```
college.earth$bestTune
```

```
##      nprune degree
## 15      16      1
```

```
coef(college.earth$finalModel)
```

```
##      (Intercept)      h(expend-15365) h(4450-room_board)
##      11157.3323100      -0.6964270      -1.2721516
##      h(grad_rate-97)      h(97-grad_rate) h(f_undergrad-1355)
##      -242.9852028      -24.1380627      -0.3567241
## h(1355-f_undergrad)      h(22-perc_alumni)      h(apps-3712)
##      -1.7564383      -77.0359905      7.0815293
##      h(1300-personal)      h(913-enroll)      h(2193-accept)
##      1.0492662      5.2944664      -1.9951560
##      h(expend-6881)      h(apps-3877)      h(s_f_ratio-10.1)
##      0.6896165      -6.7393719      -97.7224105
##      h(s_f_ratio-17.8)
##      222.5913868
```

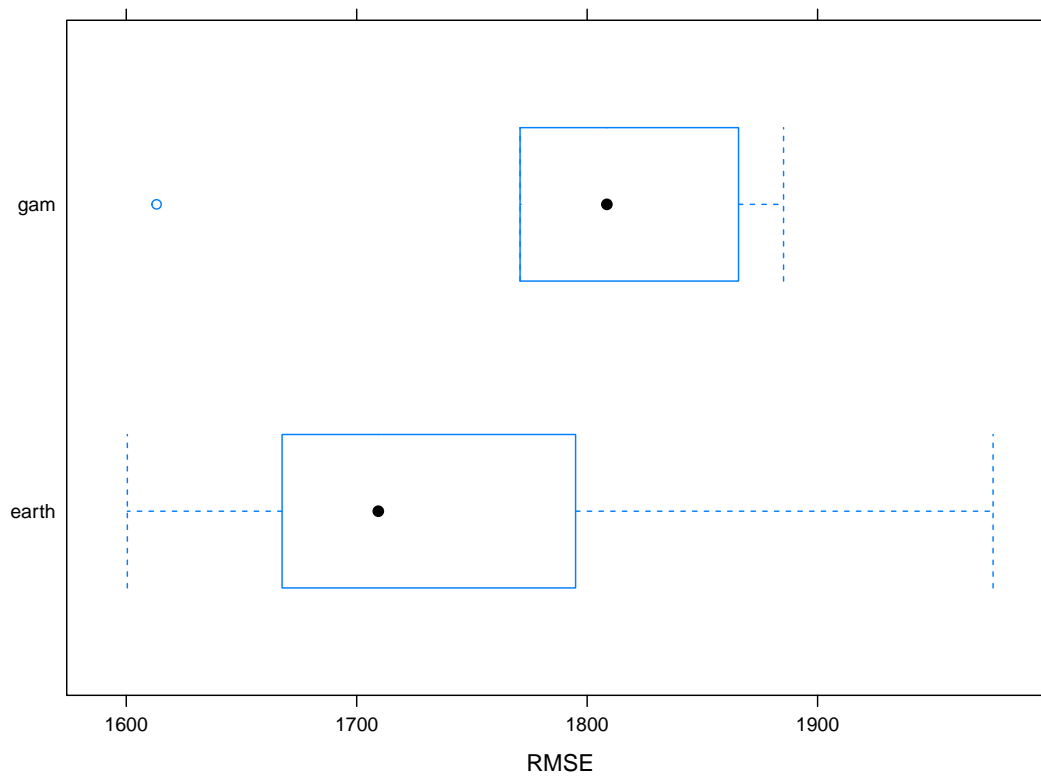
Using multivariate adaptive regression spline (MARS), a final model is $-0.745 \text{ "expend"} - 1.294 \text{ "room_board"} - 21.71 \text{ "grad_rate"} - 0.337 \text{ "f_undergrad"} - 1.442 \text{ "f_undergrad"} - 79.612 \text{ "perc_alumni"} + 0.417 \text{ "apps"} + 0.947 \text{ "personal"} + 4.572 \text{ "enroll"} - 1.922 \text{ "accept"} + 0.745 \text{ "expend"}.$

```
resamp <- resamples(list(earth = college.earth,
                        gam = college.gam))
```

```
summary(resamp)
```

```
##
## Call:
## summary.resamples(object = resamp)
##
## Models: earth, gam
## Number of resamples: 5
##
## MAE
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max. NA's
## earth 1304.020 1308.502 1351.310 1359.150 1367.087 1464.831    0
## gam   1305.207 1369.317 1376.875 1384.362 1393.167 1477.245    0
##
## RMSE
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max. NA's
## earth 1600.466 1667.612 1709.368 1749.716 1794.982 1976.150    0
## gam   1613.150 1770.887 1808.560 1788.702 1865.690 1885.225    0
##
## Rsquared
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max. NA's
## earth 0.7487180 0.7546039 0.7868256 0.7838266 0.8063247 0.8226606    0
## gam   0.7228419 0.7489326 0.7796175 0.7721217 0.7929478 0.8162689    0
```

```
bwplot(resamp, metric = "RMSE")
```



Part

e

```
columbia = colgedf %>%
  filter(college == "Columbia University")

pred.earth = predict(college.earth, newdata = columbia)

pred.gam = predict(gam1, newdata = columbia)
```

The MARS model predicts a tuition of 1.8521×10^4 dollars and the GAM model predicts a tuition of 1.944176×10^4 dollars. Because the MARS model has a lower RMSE it is appropriate to accept this model and predict a tuition of 1.8521×10^4 dollars.