XCS221 Assignment 3 — Peeking Blackjack

Due Sunday, May 22 at 11:59pm PT.

Guidelines

- 1. If you have a question about this homework, we encourage you to post your question on our Slack channel, at http://xcs221-scpd.slack.com/
- 2. Familiarize yourself with the collaboration and honor code policy before starting work.
- 3. For the coding problems, you must use the packages specified in the provided environment description. Since the autograder uses this environment, we will not be able to grade any submissions which import unexpected libraries.

Submission Instructions

Written Submission: Some questions in this assignment require a written response. For these questions, you should submit a PDF with your solutions online in the online student portal. As long as the PDF is legible and organized, the course staff has no preference between a handwritten and a typeset LaTeX submission. If you wish to typeset your submission and are new to LaTeX, you can get started with the following:

- Type responses only in submission.tex.
- Submit the compiled PDF, not submission.tex.
- Use the commented instructions within the Makefile and README.md to get started.

Coding Submission: Some questions in this assignment require a coding response. For these questions, you should submit only the src/submission.py file in the online student portal. For further details, see Writing Code and Running the Autograder below.

Honor code

We strongly encourage students to form study groups. Students may discuss and work on homework problems in groups. However, each student must write down the solutions independently, and without referring to written notes from the joint session. In other words, each student must understand the solution well enough in order to reconstruct it by him/herself. In addition, each student should write on the problem set the set of people with whom s/he collaborated. Further, because we occasionally reuse problem set questions from previous years, we expect students not to copy, refer to, or look at the solutions in preparing their answers. It is an honor code violation to intentionally refer to a previous year's solutions. More information regarding the Stanford honor code can be foudn at https://communitystandards.stanford.edu/policies-and-guidance/honor-code.

Writing Code and Running the Autograder

All your code should be entered into src/submission.py. When editing src/submission.py, please only make changes between the lines containing ### START_CODE_HERE ### and ### END_CODE_HERE ###. Do not make changes to files other than src/submission.py.

The unit tests in src/grader.py (the autograder) will be used to verify a correct submission. Run the autograder locally using the following terminal command within the src/ subdirectory:

\$ python grader.py

There are two types of unit tests used by the autograder:

• basic: These tests are provided to make sure that your inputs and outputs are on the right track, and that the hidden evaluation tests will be able to execute.

• hidden: These unit tests are the evaluated elements of the assignment, and run your code with more complex inputs and corner cases. Just because your code passed the basic local tests does not necessarily mean that they will pass all of the hidden tests. These evaluative hidden tests will be run when you submit your code to the Gradescope autograder via the online student portal, and will provide feedback on how many points you have earned.

For debugging purposes, you can run a single unit test locally. For example, you can run the test case 3a-0-basic using the following terminal command within the src/ subdirectory:

```
$ python grader.py 3a-0-basic
```

Before beginning this course, please walk through the Anaconda Setup for XCS Courses to familiarize yourself with the coding environment. Use the env defined in src/environment.yml to run your code. This is the same environment used by the online autograder.

Test Cases

The autograder is a thin wrapper over the python unittest framework. It can be run either locally (on your computer) or remotely (on SCPD servers). The following description demonstrates what test results will look like for both local and remote execution. For the sake of example, we will consider two generic tests: 1a-0-basic and 1a-1-hidden.

Local Execution - Hidden Tests

All hidden tests rely on files that are not provided to students. Therefore, the tests can only be run remotely. When a hidden test like 1a-1-hidden is executed locally, it will produce the following result:

```
----- START 1a-1-hidden: Test multiple instances of the same word in a sentence.
----- END 1a-1-hidden [took 0:00:00.011989 (max allowed 1 seconds), ???/3 points] (hidden test ungraded)
```

Local Execution - Basic Tests

When a basic test like 1a-0-basic passes locally, the autograder will indicate success:

```
---- START 1a-0-basic: Basic test case.
---- END 1a-0-basic [took 0:00:00.000062 (max allowed 1 seconds), 2/2 points]
```

When a basic test like 1a-0-basic fails locally, the error is printed to the terminal, along with a stack trace indicating where the error occurred:

```
START 1a-0-basic: Basic test case.
                                This error caused the test to fail.
{'a': 2, 'b': 1} != None
     "/Users/grinch/Local_Documents/Software/anaconda3/envs/XCS221/lib/python3.6/unittest/case.py", line 59, in testPartExecutor
 File "/Users/grinch/Local_Documents/Software/anaconda3/envs/XCS221/lib/python3.6/unittest/case.py", line 605, in run
   testMethod()
 File "/Users/grinch/Local_Documents/SCPD/XCS221/A1/src/graderUtil.py", line 54, in wrapper
   result = func(*args, **kwargs)
 File "/Users/grinch/Local_Documents/SCPD/XCS221/A1/src/graderUtil.py", line 83, in wrapper
   result = func(*args, **kwargs)
 File "/Users/grinch/Local_Documents/SCPD/XCS221/A1/src/grader.py", line 23, in test_0
  submission.extractWordFeatures("a b a"))
 File "/Users/grinch/Local_Documents/Software/anaconda3/envs/XCS221/lib/python3.6/unittest/case.py", line 829, in assertEqual
   assertion_func(first, second, msg=msg)
 File "/Users/grinch/Local_Documents/Software/anaconda3/envs/XCS221/lib/python3.6/unittest/case.py", line 822, in _baseAssertEqual
   raise self.failureException(msg)
     END 1a-0-basic [took 0:00:00.003809 (max allowed 1 seconds), 0/2 points]
```

Remote Execution

Basic and hidden tests are treated the same by the remote autograder. Here are screenshots of failed basic and hidden tests. Notice that the same information (error and stack trace) is provided as the in local autograder, now for both basic and hidden tests.

Finally, here is what it looks like when basic and hidden tests pass in the remote autograder.

```
1a-O-basic) Basic test case. (2.0/2.0)
```

1a-1-hidden) Test multiple instances of the same word in a sentence. (3.0/3.0)

Introduction

The search algorithms explored in the previous assignment work great when you know exactly the results of your actions. Unfortunately, the real world is not so predictable. One of the key aspects of an effective AI is the ability to reason in the face of uncertainty.

Markov decision processes (MDPs) can be used to formalize uncertain situations. In this homework, you will implement algorithms to find the optimal policy in these situations. You will then formalize a modified version of Blackjack as an MDP, and apply your algorithm to find the optimal policy.

1. Value Iteration

In this problem, you will perform the value iteration updates manually on a very basic game just to solidify your intuitions about solving MDPs. The set of possible states in this game is $\{-2, -1, 0, 1, 2\}$. You start at state 0, and if you reach either -2 or 2, the game ends. At each state, you can take one of two actions: $\{-1, +1\}$.

If you're in state s and choose -1:

- You have an 80% chance of reaching the state s-1.
- You have a 20% chance of reaching the state s + 1.

If you're in state s and choose +1:

- You have a 30% chance of reaching the state s + 1.
- You have a 70% chance of reaching the state s-1.

If your action results in transitioning to state -2, then you receive a reward of 20. If your action results in transitioning to state 2, then your reward is -5. Assume the discount factor γ is 1.

- (a) [4 points (Written)] Give the value of $V_{\text{opt}}(s)$ for each state s after 0, 1, and 2 iterations of value iteration. Iteration 0 just initializes all the values of V to 0. Terminal states do not have any optimal policies and take on a value of 0.
- (b) [4 points (Written)] Based on $V_{\text{opt}}(s)$ after the second iteration, what is the corresponding optimal policy π_{opt} for all non-terminal states?

2. Transforming MDPs

Equipped with an understanding of a basic algorithm for computing optimal value functions in MDPs, let's gain intuition about the dynamics of MDPs which either carry some special structure, or are defined with respect to a different MDP.

(a) [4 points (Coding)] If we add noise to the transitions of an MDP, does the optimal value always get worse? Specifically, consider an MDP with reward function Reward(s, a, s'), states States, and transition function T(s, a, s'). Let's define a new MDP which is identical to the original, except that on each action, with probability $\frac{1}{2}$, we randomly jump to one of the states that we could have reached before with positive probability.

Formally, this modified transition function is:

$$T'(s, a, s') = \frac{1}{2}T(s, a, s') + \frac{1}{2} \cdot \frac{1}{\{s'' : T(s, a, s'') > 0\}}.$$

Let V_1 be the optimal value function for the original MDP, and V_2 the optimal value function for the modified MDP. Is it always the case that $V_1(s_{\text{start}}) \geq V_2(s_{\text{start}})$? If so, prove it in blackjack.pdf and put return None for each of the code blocks. Otherwise, construct a counterexample by filling out CounterexampleMDP in submission.py.

- (b) [4 points (Written)] Suppose we have an acyclic MDP for which we want to find the optimal value at each node. We could run value iteration, which would require multiple iterations but it would be nice to be more efficient for MDPs with this acyclic property. Briefly explain an algorithm that will allow us to compute V_{opt} for each node with only a single pass over all the (s, a, s') triples.
- (c) [4 points (Written)]

Suppose we have an MDP with states S and a discount factor $\lambda < 1$, but we have an MDP solver that can only solve MDPs with discount factor of 1. How can we leverage the MDP solver to solve the original MDP?

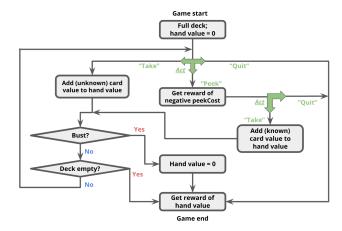
Let us define a new MDP with states $S' = S \cup \{o\}$, where o is a new state. Let's use the same actions (A'(s) = A(s)), but we need to keep the discount $\lambda' = 1$. Your job is to define new transition probabilities T'(s, a, s') and rewards R'(s, a, s') in terms of the old MDP such that the optimal values $V_{\text{opt}}(s)$ for all $s \in S$ are equal under the original MDP and the new MDP.

Hint: If you're not sure how to approach this problem, go back to the first MDP lecture and read closely the slides on convergence.

3. Peeking Blackjack

Now that we have gotten a bit of practice with general-purpose MDP algorithms, let's use them to play (a modified version of) Blackjack. For this problem, you will be creating an MDP to describe states, actions, and rewards in this game.

For our version of Blackjack, the deck can contain an arbitrary collection of cards with different face values. At the start of the game, the deck contains the same number of each cards of each face value; we call this number the 'multiplicity'. For example, a standard deck of 52 cards would have face values [1, 2, ..., 13] and multiplicity 4. You could also have a deck with face values [1, 5, 20]; if we used multiplicity 10 in this case, there would be 30 cards in total (10 each of 1s, 5s, and 20s). The deck is shuffled, meaning that each permutation of the cards is equally likely.



The game occurs in a sequence of rounds. Each round, the player either (i) takes the next card from the top of the deck (costing nothing), (ii) peeks at the top card (costing peekCost, in which case the next round, that card will be drawn), or (iii) quits the game. (Note: it is not possible to peek twice in a row; if the player peeks twice in a row, then succAndProbReward() should return [].)

The game continues until one of the following conditions becomes true:

- The player quits, in which case her reward is the sum of the face values of the cards in her hand.
- The player takes a card and "goes bust". This means that the sum of the face values of the cards in her hand is strictly greater than the threshold specified at the start of the game. If this happens, her reward is 0.
- The deck runs out of cards, in which case it is as if she quits, and she gets a reward which is the sum of the cards in her hand. Make sure that if you take the last card and go bust, then the reward becomes 0 not the sum of values of cards.

In this problem, your state s will be represented as a 3-element tuple:

```
(totalCardValueInHand, nextCardIndexIfPeeked, deckCardCounts)
```

As an example, assume the deck has card values [1,2,3] with multiplicity 1, and the threshold is 4. Initially, the player has no cards, so her total is 0; this corresponds to state (0, None, (1, 1, 1)). At this point, she can take, peek, or quit.

• If she takes, the three possible successor states (each of which has equal probability of 1/3) are:

```
(1, None, (0, 1, 1))
(2, None, (1, 0, 1))
(3, None, (1, 1, 0))
```

She will receive a reward of 0 for reaching any of these states. (Remember, even though she now has a card in her hand for which she may receive a reward at the end of the game, the reward is not actually granted until the game ends.)

• If she peeks, the three possible successor states are:

```
(0, 0, (1, 1, 1))
(0, 1, (1, 1, 1))
(0, 2, (1, 1, 1))
```

She will receive (immediate) reward -peekCost for reaching any of these states. Things to remember about the states after a peek action:

- From (0, 0, (1, 1, 1)), taking a card will lead to the state (1, None, (0, 1, 1)) deterministically.
- The second element of the state tuple is not the face value of the card that will be drawn next, but the index into the deck (the third element of the state tuple) of the card that will be drawn next. In other words, the second element will always be between 0 and len(deckCardCounts)-1, inclusive.
- If she quits, then the resulting state will be (0, None, None). (Remember that setting the deck to None signifies the end of the game.)

As another example, let's say the player's current state is (3, None, (1, 1, 0)), and the threshold remains 4.

- If she quits, the successor state will be (3, None, None).
- If she takes, the successor states are (3 + 1, None, (0, 1, 0)) or (3 + 2, None, None).

Note that in the second successor state, the deck is set to None to signify the game ended with a bust. You should also set the deck to None if the deck runs out of cards.

- (a) [8 points (Coding)] Implement the game of Blackjack as an MDP by filling out the succAndProbReward() function of class BlackjackMDP.
- (b) [4 points (Coding)] Let's say you're running a casino, and you're trying to design a deck to make people peek a lot. Assuming a fixed threshold of 20, and a peek cost of 1, design a deck where for at least 10% of states, the optimal policy is to peek. Fill out the function peekingMDP() to return an instance of BlackjackMDP where the optimal action is to peek in at least 10% of states.

Hint: Before randomly assinging values, think of the case when you really want to peek instead of blindly taking a card.

4. Learning to Play Blackjack

So far, we've seen how MDP algorithms can take an MDP which describes the full dynamics of the game and return an optimal policy. But suppose you go into a casino, and no one tells you the rewards or the transitions. We will see how reinforcement learning can allow you to play the game and learn its rules and strategy at the same time!

(a) [8 points (Coding)] You will first implement a generic Q-learning algorithm QLearningAlgorithm, which is an instance of an RLAlgorithm. As discussed in class, reinforcement learning algorithms are capable of executing a policy while simultaneously improving that policy. Look in simulate(), in util.py to see how the RLAlgorithm will be used. In short, your QLearningAlgorithm will be run in a simulation of the MDP, and will alternately be asked for an action to perform in a given state (QLearningAlgorithm.getAction), and then be informed of the result of that action (QLearningAlgorithm.incorporateFeedback), so that it may learn better actions to perform in the future.

We are using Q-learning with function approximation, which means $\hat{Q}_{\text{opt}}(s, a) = \mathbb{W} \cdot \phi(s, a)$, where in code, \mathbb{W} is self.weights, ϕ is the featureExtractor function, and \hat{Q}_{opt} is self.getQ.

We have implemented QLearningAlgorithm.getAction as a simple ϵ -greedy policy. Your job is to implement QLearningAlgorithm.incorporateFeedback(), which should take an (s, a, r, s') tuple and update self.weights according to the standard Q-learning update.

- (b) [5 points (Written)] Now let's apply Q-learning to an MDP and see how well it performs in comparison with value iteration. First, call simulate using your Q-learning code and the identityFeatureExtractor() on the MDP smallMDP (defined for you in submission.py), with 30000 trials. How does the Q-learning policy compare with a policy learned by value iteration (i.e., for how many states do they produce a different action)? (Don't forget to set the explorationProb of your Q-learning algorithm to 0 after learning the policy.) Now run simulate() on largeMDP, again with 30000 trials. How does the policy learned in this case compare to the policy learned by value iteration? What went wrong?
- (c) [5 points (Coding)] To address the problems explored in the previous exercise, let's incorporate some domain knowledge to improve generalization. This way, the algorithm can use what it has learned about some states to improve its prediction performance on other states. Implement blackjackFeatureExtractor as described in the code comments. Using this feature extractor, you should be able to get pretty close to the optimum on the largeMDP.
- (d) [5 points (Written)] Sometimes, we might reasonably wonder how an optimal policy learned for one MDP might perform if applied to another MDP with similar structure but slightly different characteristics. For example, imagine that you created an MDP to choose an optimal strategy for playing "traditional" blackjack, with a standard card deck and a threshold of 21. You're living it up in Vegas every weekend, but the casinos get wise to your approach and decide to make a change to the game to disrupt your strategy: going forward, the threshold for the blackjack tables is 17 instead of 21. If you continued playing the modified game with your original policy, how well would you do? (This is just a hypothetical example; we won't look specifically at the blackjack game in this problem.)

To explore this scenario, let's take a brief look at how a policy learned using value iteration responds to a change in the rules of the MDP.

- First, run value iteration on the originalMDP (defined for you in submission.py) to compute an optimal policy for that MDP.
- Next, simulate your policy on newThresholdMDP (also defined for you in submission.py) by calling simulate with an instance of FixedRLAlgorithm that has been instantiated using the policy you computed with value iteration. What is the expected reward from this simulation?
 - Hint: read the documentation (comments) for the simulate function in util.py, and look specifically at the format of the function's return value.
- Now try simulating Q-learning directly on newThresholdMDP with blackjackFeatureExtractor and the default exploration probability. What is your expected reward under the new Q-learning policy? Provide some explanation for how the rewards compare, and why they are different.

This handout includes space for every question that requires a written response. Please feel free to use it to handwrite your solutions (legibly, please). If you choose to typeset your solutions, the README.md for this assignment includes instructions to regenerate this handout with your typeset LATEX solutions.

1.a

1.b

2.b

2.c

4.b

4.d