$$\psi_{\rm n} = \frac{1}{\sqrt{n!}} (\hat{a}^{\dagger})^n \psi_0$$