$$\dot{\vec{e}}_{\theta} = \dot{\phi} \cos(\theta) \vec{e}_{\phi} - \dot{\theta} \, \vec{e}_{r}$$