

$$2\phi(\theta) = r\sin(\theta)\dot{\phi} + 2\sin(\theta)\dot{r}\phi + 2r\cos(\theta)\dot{\theta}\phi$$