$$\dot{\vec{e}}_{\phi} = -\dot{\phi} \cos(\theta) \vec{e}_{\theta} - \dot{\phi} \sin(\theta) \vec{e}_{r}$$