

$$\partial_{\bar{z}} \left(\frac{1}{z} \right) = -\frac{1}{z^2}$$