

$$\cos(x) - \cos(v) = -2 \sin\left(\frac{x+v}{2}\right) \sin\left(\frac{x-v}{2}\right)$$