$$a_\phi(t) = r \sin(\theta) \ddot{\phi} + 2 \sin(\theta) \dot{r} \dot{\phi} + 2 r \cos(\theta) \dot{\theta} \dot{\phi}$$