$$\vec{a}(t) = \left(\ddot{\rho} - \rho\,\dot{\phi}^2\right)\vec{e}_\rho + \left(\rho\,\ddot{\phi} + 2\,\dot{\rho}\,\dot{\phi}\right)\vec{e}_\phi + \ddot{z}\,\vec{e}_z$$