# harry-browne-permanent-portfolio

April 12, 2025

# 1 Does Harry Browne's permanent portfolio withstand the test of time?

# 1.1 Python Imports

```
[1]: import os
     import pandas as pd
     import numpy as np
     import datetime
     import matplotlib.pyplot as plt
     import matplotlib.ticker as mtick
     import matplotlib.dates as mdates
     from matplotlib.ticker import FuncFormatter
     from matplotlib.ticker import FormatStrFormatter
     from matplotlib.ticker import MultipleLocator
     import warnings
     import seaborn as sns
     import statsmodels.api as sm
     from sklearn.decomposition import PCA
     from sklearn.preprocessing import StandardScaler
     import random
     warnings.filterwarnings("ignore")
```

# 1.2 Python Functions

# 1.2.1 bb\_data\_updater

```
[2]: # This function takes an excel export from Bloomberg and
# removes all excess data leaving date and close columns

# Imports
import pandas as pd

# Function definition
def bb_data_updater(fund):

# File name variable
file = fund + ".xlsx"
```

```
# Import data from file as a pandas dataframe
df = pd.read_excel(file, sheet_name = 'Worksheet', engine='openpyxl')
# Set the column headings from row 5 (which is physically row 6)
df.columns = df.iloc[5]
# Set the column heading for the index to be "None"
df.rename_axis(None, axis=1, inplace = True)
# Drop the first 6 rows, 0 - 5
df.drop(df.index[0:6], inplace=True)
# Set the date column as the index
df.set_index('Date', inplace = True)
# Drop the volume column
try:
   df.drop(columns = {'PX_VOLUME'}, inplace = True)
except KeyError:
   pass
# Rename column
df.rename(columns = {'PX_LAST':'Close'}, inplace = True)
# Sort by date
df.sort_values(by=['Date'], inplace = True)
# Export data to excel
file = fund + "_Clean.xlsx"
df.to_excel(file, sheet_name='data')
# Output confirmation
print(f"The last date of data for {fund} is: ")
print(df[-1:])
print(f"Bloomberg data conversion complete for {fund} data")
return print(f"----")
```

#### 1.2.2 dp

```
[3]: # Set number of decimal places in pandas

def dp(decimal_places):
    pd.set_option('display.float_format', lambda x: f'%.{decimal_places}f' % x)

dp(3)
```

# 1.2.3 df info

```
[4]: # The `df_info` function returns some useful information about
# a dataframe, such as the columns, data types, and size.

def df_info(df):
    print('The columns, shape, and data types are:')
    print(df.info())
    print('The first 5 rows are:')
    display(df.head())
    print('The last 5 rows are:')
    display(df.tail())
```

# 1.2.4 load\_data

```
[5]: def load_data(file):
    # Import CSV
    try:
        df = pd.read_csv(file)
    except:
        pass

# Import excel
    try:
        df = pd.read_excel(file, sheet_name='data', engine='openpyxl')
    except:
        pass
    return df
```

#### 1.2.5 strategy

```
[6]: def strategy(
    fund_list,
    starting_cash,
    cash_contrib,
    close_prices_df,
    rebal_month,
    rebal_day,
    rebal_per_high,
    rebal_per_low
):

#### Execute the rebalance strategy based on specified criteria.

Args:
```

```
fund_list (str): List of funds for data to be combined from. Funds are
\hookrightarrowstrings in the form "BTC-USD".
      starting_cash (int): Starting investment balance.
      cash_contrib (int): Cash contribution to be made daily.
      close\_prices\_df (pd.DataFrame): DataFrame containing date and close_{\sqcup}
⇔prices for all funds to be included.
      rebal_month (int): Month for annual rebalance.
      rebal_day (int): Day for annual rebalance.
      rebal_per_high (float): High percentage for rebalance.
      rebal_per_low (float): Low percentage for rebalance.
  Returns:
      pd.DataFrame: DataFrame containing strategy data for all funds to be_{\sqcup}
→included. Also dumps the df to excel for reference later.
  num_funds = len(fund_list)
  df = close_prices_df.copy()
  df.reset_index(inplace = True)
  # Date to be used for annual rebalance
  target month = rebal month
  target_day = rebal_day
  # Create a dataframe with dates from the specific month
  rebal_date = df[df['Date'].dt.month == target_month]
  # Specify the date or the next closest
  rebal_date = rebal_date[rebal_date['Date'].dt.day >= target_day]
  # Group by year and take the first entry for each year
  rebal_dates_by_year = rebal_date.groupby(rebal_date['Date'].dt.year).
→first().reset_index(drop=True)
   111
  Column order for the dataframe:
  df[fund + "_BA_Shares"]
  df[fund + "_BA_$_Invested"]
  df[fund + "_BA_Port_%"]
  df['Total_BA_$_Invested']
  df['Contribution']
  df['Rebalance']
  df[fund + "_AA_Shares"]
  df[fund + "_AA_$_Invested"]
  df[fund + "_AA_Port_%"]
  df['Total_AA_$_Invested']
```

```
# Calculate the columns and initial values for before action (BA) shares, \sharp_{\sqcup}
⇒invested, and port %
  for fund in fund_list:
       df[fund + " BA Shares"] = starting cash / num funds / df[fund + | |

¬" Close"]

       df[fund + "_BA_$_Invested"] = df[fund + "_BA_Shares"] * df[fund +__

¬"_Close"]

       df[fund + "_BA_Port_%"] = 0.25
   # Set column values initially
  df['Total_BA_$_Invested'] = starting_cash
  df['Contribution'] = 0
   # df['Contribution'] = cash_contrib
  df['Rebalance'] = "No"
   # Set columns and values initially for after action (AA) shares, \sharp_{\sqcup}
⇒invested, and port %
  for fund in fund list:
       df[fund + "_AA_Shares"] = starting_cash / num_funds / df[fund +__

¬" Close"]

       df[fund + "_AA_$_Invested"] = df[fund + "_AA_Shares"] * df[fund +__

¬" Close"]

       df[fund + "_AA_Port_%"] = 0.25
   # Set column value for after action (AA) total $ invested
  df['Total_AA_$_Invested'] = starting_cash
  # Iterate through the dataframe and execute the strategy
  for index, row in df.iterrows():
       # Ensure there's a previous row to reference by checking the index value
      if index > 0:
           # Initialize variable
           Total BA Invested = 0
           # Calculate before action (BA) shares and $ invested values
           for fund in fund_list:
               df.at[index, fund + "_BA_Shares"] = df.at[index - 1, fund +__

¬"_AA_Shares"]

               df.at[index, fund + "_BA_$_Invested"] = df.at[index, fund +__

¬"_BA_Shares"] * row[fund + "_Close"]
               # Sum the asset values to find the total
```

```
Total_BA_Invested = Total_BA_Invested + df.at[index, fund +
# Calculate before action (BA) port % values
          for fund in fund_list:
              df.at[index, fund + " BA Port " ] = df.at[index, fund + 11
→"_BA_$_Invested"] / Total_BA_Invested
          # Set column for before action (BA) total $ invested
          df.at[index, 'Total_BA_$_Invested'] = Total_BA_Invested
          # Initialize variables
          rebalance = "No"
          date = row['Date']
          # Check for a specific date annually
          # Simple if statement to check if date_to_check is in_
⇒ jan_28_or_after_each_year
          if date in rebal_dates_by_year['Date'].values:
              rebalance = "Yes"
          else:
              pass
          # Check to see if any asset has portfolio percentage of greater_
→than 35% or less than 15% and if so set variable
          for fund in fund_list:
              if df.at[index, fund + "_BA_Port_%"] > rebal_per_high or df.
→at[index, fund + "_BA_Port_%"] < rebal_per_low:</pre>
                 rebalance = "Yes"
              else:
                  pass
          # If rebalance is required, rebalance back to 25% for each asset,
⇔else just divide contribution evenly across assets
          if rebalance == "Yes":
              df.at[index, 'Rebalance'] = rebalance
              for fund in fund list:
                     df.at[index, fund + "_AA_$_Invested"] =__
→(Total_BA_Invested + df.at[index, 'Contribution']) * 0.25
          else:
              df.at[index, 'Rebalance'] = rebalance
              for fund in fund_list:
                     df.at[index, fund + "_AA_$_Invested"] = df.at[index,__
# Initialize variable
```

```
Total_AA_Invested = 0
                                   # Set column values for after action (AA) shares and port %
                                  for fund in fund_list:
                                               df.at[index, fund + "_AA_Shares"] = df.at[index, fund +__
Government of the state of
                                               # Sum the asset values to find the total
                                               Total_AA_Invested = Total_AA_Invested + df.at[index, fund +

¬"_AA_$_Invested"]

                                   # Calculate after action (AA) port % values
                                  for fund in fund list:
                                               df.at[index, fund + "_AA_Port_%"] = df.at[index, fund +__
→"_AA_$_Invested"] / Total_AA_Invested
                                   # Set column for after action (AA) total $ invested
                                  df.at[index, 'Total_AA_$_Invested'] = Total_AA_Invested
                      # If this is the first row
                     else:
                                  pass
        df['Return'] = df['Total_AA_$_Invested'].pct_change()
        df['Cumulative_Return'] = (1 + df['Return']).cumprod()
        plan_name = '_'.join(fund_list)
        file = plan_name + "_Strategy.xlsx"
        location = file
        df.to_excel(location, sheet_name="data")
        print(f"Strategy complete for {plan_name}.")
        return df
```

# 1.2.6 summary\_stats

```
[7]: # Stats for entire data set
def summary_stats(
    fund_list,
    df,
    period,
    excel_export
):

"""
    Calculate summary statistics for the given fund list and return data.

Args:
```

```
fund\_list (str): List of funds for data to be combined from. Funds are \sqcup
\hookrightarrowstrings in the form "BTC-USD".
       df (df): Dataframe with return data.
       period (str): Period for which to calculate statistics. Options are \Box
\rightarrow "Monthly", "Weekly", "Daily", "Hourly".
       excel_export (bool): If True, export to excel file.
  Returns:
       pd.DataFrame: DataFrame containing various portfolio statistics.
  if period == "Monthly":
       timeframe = 12 # months
  elif period == "Weekly":
      timeframe = 52 # weeks
  elif period == "Daily":
       timeframe = 365 # days
   elif period == "Hourly":
       timeframe = 8760 # hours
  else:
       return print("Error, check inputs")
  df_stats = pd.DataFrame(df.mean(axis=0) * timeframe) # annualized
   \# df_stats = pd.DataFrame((1 + df.mean(axis=0)) ** timeframe - 1) #_U
→annualized, this is this true annualized return but we will simply use the
\rightarrowmean
  df stats.columns = ['Annualized Mean']
  df_stats['Annualized Volatility'] = df.std() * np.sqrt(timeframe) #_
\hookrightarrow annualized
  df_stats['Annualized Sharpe Ratio'] = df_stats['Annualized Mean'] /__
⇔df_stats['Annualized Volatility']
  df cagr = (1 + df['Return']).cumprod()
   cagr = (df_cagr.iloc[-1] / 1) ** (1/(len(df_cagr) / timeframe)) - 1
  df_stats['CAGR'] = cagr
  df_stats[period + ' Max Return'] = df.max()
  df_stats[period + ' Max Return (Date)'] = df.idxmax().values[0]
  df_stats[period + ' Min Return'] = df.min()
  df_stats[period + ' Min Return (Date)'] = df.idxmin().values[0]
  wealth_index = 1000*(1+df).cumprod()
  previous_peaks = wealth_index.cummax()
  drawdowns = (wealth_index - previous_peaks)/previous_peaks
  df_stats['Max Drawdown'] = drawdowns.min()
```

```
df_stats['Peak'] = [previous_peaks[col][:drawdowns[col].idxmin()].idxmax()_u
→for col in previous_peaks.columns]
  df_stats['Bottom'] = drawdowns.idxmin()
  recovery_date = []
  for col in wealth index.columns:
      prev_max = previous_peaks[col][:drawdowns[col].idxmin()].max()
      recovery_wealth = pd.DataFrame([wealth_index[col][drawdowns[col].
\rightarrowidxmin():]]).T
      recovery_date.append(recovery_wealth[recovery_wealth[col] >= prev_max].
→index.min())
  df_stats['Recovery Date'] = recovery_date
  plan_name = '_'.join(fund_list)
  # Export to excel
  if excel_export == True:
      file = plan_name + "_Summary_Stats.xlsx"
      location = file
      # location = f"{base_directory}/{strategy_name}/{file_name}.xlsx"
      df_stats.to_excel(location, sheet_name="data")
  else:
      pass
  print(f"Summary stats complete for {plan_name}.")
  return df_stats
```

# 1.2.7 plot\_cumulative\_return

```
[8]: def plot_cumulative_return(strat_df):
    # Generate plot
    plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')

# Plotting data
    plt.plot(strat_df.index, strat_df['Cumulative_Return'], label = 'Strategy_\_
Cumulative Return', linestyle='-', color='green', linewidth=1)

# Set X axis
    # x_tick_spacing = 5 # Specify the interval for x-axis ticks
    # plt.gca().xaxis.set_major_locator(MultipleLocator(x_tick_spacing))
    plt.gca().xaxis.set_major_locator(mdates.YearLocator())
    plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
    plt.xlabel('Year', fontsize = 9)
    plt.xticks(rotation = 45, fontsize = 7)
# plt.xlim(, )
```

```
# Set Y axis
y_tick_spacing = 0.5  # Specify the interval for y-axis ticks
plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
plt.ylabel('Cumulative Return', fontsize = 9)
plt.yticks(fontsize = 7)
# plt.ylim(0, 7.5)
# Set title, etc.
plt.title('Cumulative Return', fontsize = 12)
# Set the grid & legend
plt.tight_layout()
plt.grid(True)
plt.legend(fontsize=8)
# Save the figure
plt.savefig('03 Cumulative Return.png', dpi=300, bbox_inches='tight')
# Display the plot
return plt.show()
```

# 1.2.8 plot\_values

```
[9]: def plot_values(strat_df):
         # Generate plot
         plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
         # Plotting data
         plt.plot(strat_df.index, strat_df['Total_AA_$_Invested'], label='Total_u
      ⇔Portfolio Value', linestyle='-', color='black', linewidth=1)
         plt.plot(strat_df.index, strat_df['Stocks_AA_$_Invested'], label='Stocks_
      ⇔Position Value', linestyle='-', color='orange', linewidth=1)
         plt.plot(strat_df.index, strat_df['Bonds_AA_$_Invested'], label='Bond_
      →Position Value', linestyle='-', color='yellow', linewidth=1)
         plt.plot(strat_df.index, strat_df['Gold_AA_$_Invested'], label='Gold_
      →Position Value', linestyle='-', color='blue', linewidth=1)
         plt.plot(strat_df.index, strat_df['Cash_AA_$_Invested'], label='Cash_
      →Position Value', linestyle='-', color='brown', linewidth=1)
         # Set X axis
         # x_tick_spacing = 5  # Specify the interval for x-axis ticks
         \# plt.gca().xaxis.set\_major\_locator(MultipleLocator(x\_tick\_spacing))
         plt.gca().xaxis.set_major_locator(mdates.YearLocator())
         plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
         plt.xlabel('Year', fontsize = 9)
         plt.xticks(rotation = 45, fontsize = 7)
         # plt.xlim(, )
```

```
# Set Y axis
  y_tick_spacing = 5000 # Specify the interval for y-axis ticks
  plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
  plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:,..
\hookrightarrow0f}'.format(x))) # Adding commas to y-axis labels
  plt.ylabel('Total Value ($)', fontsize = 9)
  plt.yticks(fontsize = 7)
  # plt.ylim(0, 75000)
  # Set title, etc.
  plt.title('Total Values For Stocks, Bonds, Gold, and Cash Positions and ⊔
→Portfolio', fontsize = 12)
  # Set the grid & legend
  plt.tight_layout()
  plt.grid(True)
  plt.legend(fontsize=8)
  # Save the figure
  plt.savefig('04_Portfolio_Values.png', dpi=300, bbox_inches='tight')
  # Display the plot
  return plt.show()
```

# 1.2.9 plot drawdown

```
[10]: def plot_drawdown(strat_df):
          rolling_max = strat_df['Total_AA_$_Invested'].cummax()
          drawdown = (strat_df['Total_AA_$_Invested'] - rolling_max) / rolling_max *_
       →100
          # Generate plot
          plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
          # Plotting data
          plt.plot(strat_df.index, drawdown, label='Drawdown', linestyle='-',u
       ⇔color='red', linewidth=1)
          # Set X axis
          \# x\_tick\_spacing = 5 \# Specify the interval for x-axis ticks
          # plt.gca().xaxis.set_major_locator(MultipleLocator(x_tick_spacing))
          plt.gca().xaxis.set_major_locator(mdates.YearLocator())
          plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
          plt.xlabel('Year', fontsize = 9)
          plt.xticks(rotation = 45, fontsize = 7)
          # plt.xlim(, )
```

```
# Set Y axis
  y_tick_spacing = 1  # Specify the interval for y-axis ticks
  plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
  # plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:
\hookrightarrow, .0f}'.format(x))) # Adding commas to y-axis labels
  plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:.
\hookrightarrow 0f}'.format(x))) # Adding 0 decimal places to y-axis labels
  plt.ylabel('Drawdown (%)', fontsize = 9)
  plt.yticks(fontsize = 7)
  # plt.ylim(-20, 0)
  # Set title, etc.
  plt.title('Portfolio Drawdown', fontsize = 12)
  # Set the grid & legend
  plt.tight_layout()
  plt.grid(True)
  plt.legend(fontsize=8)
  # Save the figure
  plt.savefig('05_Portfolio_Drawdown.png', dpi=300, bbox_inches='tight')
  # Display the plot
  return plt.show()
```

# 1.2.10 plot\_asset\_weights

```
[11]: def plot_asset_weights(strat_df):
          # Generate plot
          plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
          # Plotting data
          plt.plot(strat_df.index, strat_df['Stocks_AA_Port_%'] * 100, label='Stocks_
       →Portfolio Weight', linestyle='-', color='orange', linewidth=1)
          plt.plot(strat_df.index, strat_df['Bonds_AA_Port_%'] * 100, label='Bonds_u
       →Portfolio Weight', linestyle='-', color='yellow', linewidth=1)
          plt.plot(strat_df.index, strat_df['Gold_AA_Port_%'] * 100, label='Gold_
       →Portfolio Weight', linestyle='-', color='blue', linewidth=1)
          plt.plot(strat_df.index, strat_df['Cash_AA_Port_%'] * 100, label='Cash_
       →Portfolio Weight', linestyle='-', color='brown', linewidth=1)
          # Set X axis
          \# x\_tick\_spacing = 5 \# Specify the interval for x-axis ticks
          # plt.qca().xaxis.set_major_locator(MultipleLocator(x tick_spacing))
          plt.gca().xaxis.set_major_locator(mdates.YearLocator())
          plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
```

```
plt.xlabel('Year', fontsize = 9)
  plt.xticks(rotation = 45, fontsize = 7)
  # plt.xlim(, )
  # Set Y axis
  y_tick_spacing = 1  # Specify the interval for y-axis ticks
  plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
  # plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:
\hookrightarrow, .0f}'.format(x))) # Adding commas to y-axis labels
  plt.ylabel('Asset Weight (%)', fontsize = 9)
  plt.yticks(fontsize = 7)
  # plt.ylim(14, 36)
  # Set title, etc.
  plt.title('Portfolio Asset Weights For Stocks, Bonds, Gold, and Cash⊔
→Positions', fontsize = 12)
  # Set the grid & legend
  plt.tight_layout()
  plt.grid(True)
  plt.legend(fontsize=8)
  # Save the figure
  plt.savefig('07_Portfolio_Weights.png', dpi=300, bbox_inches='tight')
  # Display the plot
  return plt.show()
```

# 1.2.11 plot annual returns

```
def plot_annual_returns(return_df):
    # Generate plot
    plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')

# Plotting data
    plt.bar(return_df.index, return_df['Return'] * 100, label='Annual Returns', width=0.5) # width adjusted for better spacing

# Set X axis
    x_tick_spacing = 1 # Specify the interval for x-axis ticks
    plt.gca().xaxis.set_major_locator(MultipleLocator(x_tick_spacing))
    # plt.gca().xaxis.set_major_locator(mdates.YearLocator())
    # plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
    plt.xlabel('Year', fontsize = 9)
    plt.xticks(rotation = 45, fontsize = 7)
    # plt.xlim(, )
```

```
# Set Y axis
  y_tick_spacing = 1  # Specify the interval for y-axis ticks
  plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
  # plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:
\rightarrow,.0f}'.format(x))) # Adding commas to y-axis labels
  plt.ylabel('Annual Return (%)', fontsize = 9)
  plt.yticks(fontsize = 7)
  # plt.ylim(-20, 20)
  # Set title, etc.
  plt.title('Portfolio Annual Returns', fontsize = 12)
  # Set the grid & legend
  plt.tight_layout()
  plt.grid(True)
  plt.legend(fontsize=8)
  # Save the figure
  plt.savefig('08_Portfolio_Annual_Returns.png', dpi=300, bbox_inches='tight')
  # Display the plot
  return plt.show()
```

# 1.3 Import Data

The last date of data for SPBDU10T\_S&P US Treasury Bond 7-10 Year Total Return Index is:

Close

Date

2024-04-30 579.024

Bloomberg data conversion complete for SPBDU10T\_S&P US Treasury Bond 7-10 Year Total Return Index data

\_\_\_\_\_\_

```
Date
      1990-01-02
                       99.972
                                                                    NaN
                                               NaN
      1990-01-03
                       99.733
                                            -0.002
                                                                  0.998
      1990-01-04
                       99.813
                                            0.001
                                                                  0.998
      1990-01-05
                       99.769
                                            -0.000
                                                                  0.998
      1990-01-08
                       99.681
                                            -0.001
                                                                  0.997
      2023-12-22
                      604.166
                                            -0.001
                                                                  6.043
      2023-12-26
                      604.555
                                             0.001
                                                                  6.047
      2023-12-27
                      609.355
                                             0.008
                                                                  6.095
      2023-12-28
                      606.828
                                            -0.004
                                                                  6.070
      2023-12-29
                      606.185
                                            -0.001
                                                                  6.064
      [8527 rows x 3 columns]
[14]: # Stocks dataframe
      bb_data_updater('SPXT_S&P 500 Total Return Index')
      stocks_data = load_data('SPXT_S&P 500 Total Return Index Clean.xlsx')
      stocks_data['Date'] = pd.to_datetime(stocks_data['Date'])
      stocks_data.set_index('Date', inplace = True)
      stocks_data = stocks_data[(stocks_data.index >= '1990-01-01') & (stocks_data.
       →index <= '2023-12-31')]</pre>
      stocks_data.rename(columns={'Close':'Stocks_Close'}, inplace=True)
      stocks_data['Stocks_Daily_Return'] = stocks_data['Stocks_Close'].pct_change()
      stocks_data['Stocks_Total_Return'] = (1 + stocks_data['Stocks_Daily_Return']).
       →cumprod()
      stocks_data
     The last date of data for SPXT_S&P 500 Total Return Index is:
                    Close
     Date
     2024-04-30 10951.660
     Bloomberg data conversion complete for SPXT_S&P 500 Total Return Index data
[14]:
                  Stocks_Close Stocks_Daily_Return Stocks_Total_Return
      Date
      1990-01-01
                           NaN
                                                                       NaN
                                                 NaN
      1990-01-02
                       386.160
                                                                       NaN
                                                 NaN
      1990-01-03
                       385.170
                                              -0.003
                                                                     0.997
      1990-01-04
                       382.020
                                              -0.008
                                                                     0.989
      1990-01-05
                       378.300
                                              -0.010
                                                                     0.980
      2023-12-22
                     10292.370
                                               0.002
                                                                    26.653
      2023-12-26
                     10335.980
                                               0.004
                                                                    26.766
                                               0.002
      2023-12-27
                     10351.600
                                                                    26.807
      2023-12-28
                     10356.590
                                               0.000
                                                                    26.819
```

Bonds\_Close Bonds\_Daily\_Return Bonds\_Total\_Return

[13]:

2023-12-29 10327.830 -0.003 26.745

[8584 rows x 3 columns]

```
[15]: # Gold dataframe
     bb data updater('XAU Gold USD Spot')
     gold data = load data('XAU Gold USD Spot Clean.xlsx')
     gold_data['Date'] = pd.to_datetime(gold_data['Date'])
     gold_data.set_index('Date', inplace = True)
     gold_data = gold_data[(gold_data.index >= '1990-01-01') & (gold_data.index <=__
      gold_data.rename(columns={'Close':'Gold_Close'}, inplace=True)
     gold_data['Gold_Daily_Return'] = gold_data['Gold_Close'].pct_change()
     gold_data['Gold_Total_Return'] = (1 + gold_data['Gold_Daily_Return']).cumprod()
     gold data
     The last date of data for XAU_Gold USD Spot is:
                 Close
     Date
     2024-05-01 2299.310
     Bloomberg data conversion complete for XAU_Gold USD Spot data
[15]:
                Gold_Close Gold_Daily_Return Gold_Total_Return
     Date
     1990-01-02
                   399.000
                                        NaN
                                                          NaN
                                                        0.990
     1990-01-03
                   395.000
                                      -0.010
     1990-01-04
                   396.500
                                      0.004
                                                        0.994
     1990-01-05
                 405.000
                                      0.021
                                                        1.015
     1990-01-08
                   404.600
                                      -0.001
                                                        1.014
     2023-12-22
                                      0.003
                  2053.080
                                                        5.146
     2023-12-26
                  2067.810
                                      0.007
                                                        5.182
     2023-12-27
                                      0.005
                                                        5.207
                  2077.490
     2023-12-28
                  2065.610
                                      -0.006
                                                        5.177
     2023-12-29
                  2062.980
                                      -0.001
                                                        5.170
     [8819 rows x 3 columns]
[16]: # Merge the stock data and bond data into a single DataFrame using their
      ⇔indices (dates)
     Gleft_index=True, right_index=True)
     # Add gold data to the portfolio DataFrame by merging it with the existing data_
      →on indices (dates)
```

```
perm_port = pd.merge(perm_port, gold_data['Gold_Close'], left_index=True,_u
       →right_index=True)
      # Add a column for cash with a constant value of 1 (assumes the value of cash
       →remains constant at $1 over time)
      perm_port['Cash_Close'] = 1
      # Remove any rows with missing values (NaN) to ensure clean data for further
       ⇔analysis
      perm_port.dropna(inplace=True)
      # Display the finalized portfolio DataFrame
      perm_port
[16]:
                  Stocks_Close Bonds_Close Gold_Close Cash_Close
     Date
      1990-01-02
                       386.160
                                     99.972
                                                 399.000
                                                                   1
                                                                   1
      1990-01-03
                       385.170
                                     99.733
                                                 395.000
      1990-01-04
                       382.020
                                     99.813
                                                                   1
                                                 396.500
      1990-01-05
                       378.300
                                     99.769
                                                405.000
                                                                   1
      1990-01-08
                                     99.681
                       380.040
                                                 404.600
                                                                   1
      2023-12-22
                     10292.370
                                    604.166
                                               2053.080
                                                                   1
      2023-12-26
                     10335.980
                                    604.555
                                                2067.810
                                                                   1
                                                2077.490
      2023-12-27
                     10351.600
                                    609.355
                                                                   1
      2023-12-28
                     10356.590
                                    606.828
                                                2065.610
                                                                   1
      2023-12-29
                     10327.830
                                    606.185
                                                2062.980
                                                                   1
      [8479 rows x 4 columns]
[17]: # Check for any missing values in each column
      missing_values = perm_port.isnull().any()
      # Display columns with missing values
      print(missing_values)
     Stocks_Close
                     False
     Bonds Close
                     False
     Gold Close
                     False
     Cash Close
                     False
     dtype: bool
```

```
The columns, shape, and data types are: <class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 8479 entries, 1990-01-02 to 2023-12-29
Data columns (total 4 columns):
```

[18]: df\_info(perm\_port)

```
Column
 #
                  Non-Null Count Dtype
    _____
                   _____
 0
    Stocks_Close 8479 non-null
                                  float64
 1
    Bonds_Close
                  8479 non-null
                                  float64
 2
    Gold Close
                  8479 non-null
                                  float64
    Cash_Close
                  8479 non-null
                                  int64
dtypes: float64(3), int64(1)
memory usage: 331.2 KB
None
The first 5 rows are:
            Stocks_Close
                         Bonds_Close Gold_Close Cash_Close
Date
                              99.972
                386.160
                                         399.000
1990-01-02
                                                           1
1990-01-03
                385.170
                              99.733
                                         395.000
                                                           1
                                                           1
1990-01-04
                382.020
                              99.813
                                         396.500
                378.300
                              99.769
                                         405.000
                                                           1
1990-01-05
1990-01-08
                380.040
                              99.681
                                         404.600
                                                           1
The last 5 rows are:
            Stocks_Close Bonds_Close Gold_Close Cash_Close
Date
2023-12-22
              10292.370
                             604.166
                                        2053.080
                                                           1
2023-12-26
               10335.980
                             604.555
                                        2067.810
                                                           1
                                                           1
2023-12-27
              10351.600
                             609.355
                                        2077.490
2023-12-28
              10356.590
                             606.828
                                        2065.610
```

606.185

2062.980

1

# 1.4 Execute Strategy

10327.830

2023-12-29

```
[19]: # List of funds to be used
  fund_list = ['Stocks', 'Bonds', 'Gold', 'Cash']

# Starting cash contribution
  starting_cash = 10000

# Monthly cash contribution
  cash_contrib = 0

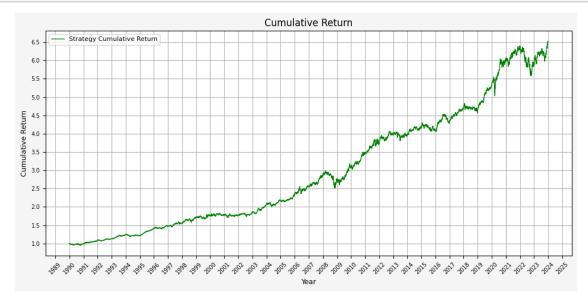
strat = strategy(
    fund_list=fund_list,
    starting_cash=starting_cash,
    cash_contrib=cash_contrib,
    close_prices_df=perm_port,
    rebal_month=1,
    rebal_day=1,
    rebal_per_high=0.35,
    rebal_per_low=0.15)
```

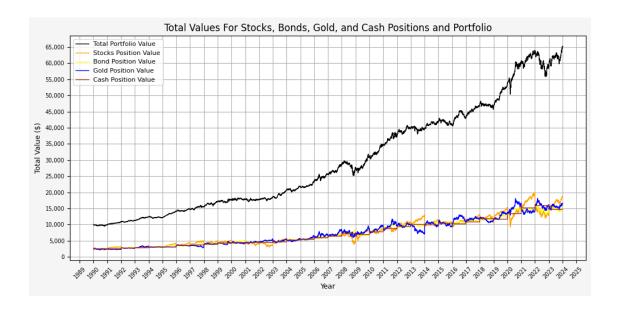
```
strat = strat.set_index('Date')
      sum_stats = summary_stats(
          fund_list=fund_list,
          df=strat[['Return']],
          period="Daily",
          excel_export=False)
      strat_pre_1999 = strat[strat.index < '2000-01-01']
      sum stats pre 1999 = summary stats(
          fund_list=fund_list,
          df=strat_pre_1999[['Return']],
          period="Daily",
          excel_export=False)
      strat_post_1999 = strat[strat.index >= '2000-01-01']
      sum_stats_post_1999 = summary_stats(
          fund_list=fund_list,
          df=strat_post_1999[['Return']],
          period="Daily",
          excel_export=False)
      strat post 2009 = strat[strat.index >= '2010-01-01']
      sum_stats_post_2009 = summary_stats(
          fund list=fund list,
          df=strat_post_2009[['Return']],
          period="Daily",
          excel_export=False)
     Strategy complete for Stocks_Bonds_Gold_Cash.
     Summary stats complete for Stocks_Bonds_Gold_Cash.
     Summary stats complete for Stocks_Bonds_Gold_Cash.
     Summary stats complete for Stocks Bonds Gold Cash.
     Summary stats complete for Stocks_Bonds_Gold_Cash.
[20]: all_sum_stats = pd.concat([sum_stats])
      all sum stats = all sum stats.rename(index={'Return': '1990 - 2023'})
      all_sum_stats = pd.concat([all_sum_stats, sum_stats_pre_1999])
      all sum stats = all sum stats.rename(index={'Return': 'Pre 1999'})
      all_sum_stats = pd.concat([all_sum_stats, sum_stats_post_1999])
      all sum stats = all sum stats.rename(index={'Return': 'Post 1999'})
      all_sum_stats = pd.concat([all_sum_stats, sum_stats_post_2009])
      all_sum_stats = all_sum_stats.rename(index={'Return': 'Post 2009'})
      all_sum_stats
```

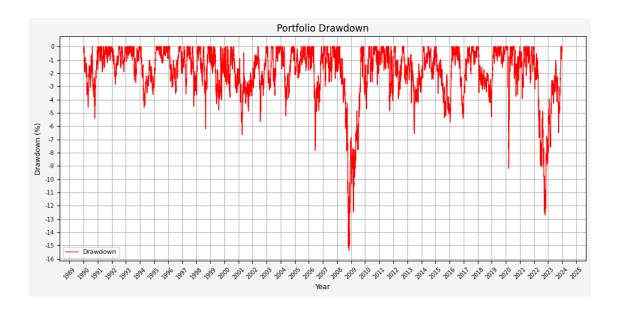
```
Annualized Mean Annualized Volatility Annualized Sharpe Ratio \
                             0.083
      1990 - 2023
                                                    0.072
                                                                             1.152
     Pre 1999
                             0.088
                                                    0.060
                                                                             1.453
     Post 1999
                             0.081
                                                    0.077
                                                                             1.063
     Post 2009
                             0.081
                                                    0.073
                                                                             1.115
                   CAGR Daily Max Return Daily Max Return (Date) Daily Min Return \
      1990 - 2023 0.084
                                    0.029
                                                       2020-03-24
                                                                             -0.030
                  0.089
                                    0.022
                                                                             -0.018
     Pre 1999
                                                       1999-09-28
      Post 1999
                  0.082
                                    0.029
                                                       2020-03-24
                                                                             -0.030
      Post 2009
                  0.082
                                    0.029
                                                                             -0.030
                                                       2020-03-24
                  Daily Min Return (Date) Max Drawdown
                                                              Peak
                                                                       Bottom \
      1990 - 2023
                               2020-03-12
                                                 -0.154 2008-03-18 2008-11-12
                                                 -0.062 1998-07-20 1998-08-31
     Pre 1999
                               1993-08-05
     Post 1999
                               2020-03-12
                                                 -0.154 2008-03-18 2008-11-12
     Post 2009
                               2020-03-12
                                                 -0.127 2021-12-27 2022-10-20
                  Recovery Date
      1990 - 2023
                     2009-10-06
     Pre 1999
                     1998-11-05
     Post 1999
                     2009-10-06
     Post 2009
                     2023-12-01
[21]: plot_cumulative_return(strat)
      plot values(strat)
      plot drawdown(strat)
      plot_asset_weights(strat)
      # Create dataframe for the annual returns
      strat annual returns = strat['Cumulative Return'].resample('Y').last().
       →pct_change().dropna()
      strat_annual_returns_df = strat_annual_returns.to_frame()
      strat_annual_returns_df['Year'] = strat_annual_returns_df.index.year # Add a_
       →'Year' column with just the year
      strat_annual_returns_df.reset_index(drop=True, inplace=True) # Reset the index_
       →to remove the datetime index
      # Now the DataFrame will have 'Year' and 'Cumulative Return' columns
      strat_annual_returns_df = strat_annual_returns_df[['Year',__
       → 'Cumulative_Return']] # Keep only 'Year' and 'Cumulative_Return' columns
      strat_annual_returns_df.rename(columns = {'Cumulative_Return':'Return'},__
       →inplace=True)
      strat_annual_returns_df.set_index('Year', inplace=True)
      display(strat_annual_returns_df)
      plan_name = '_'.join(fund_list)
```

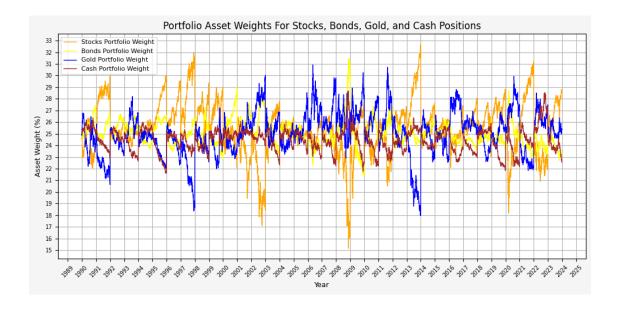
[20]:

```
file = plan_name + "_Annual_Returns.xlsx"
location = file
strat_annual_returns_df.to_excel(location, sheet_name='data')
plot_annual_returns(strat_annual_returns_df)
```



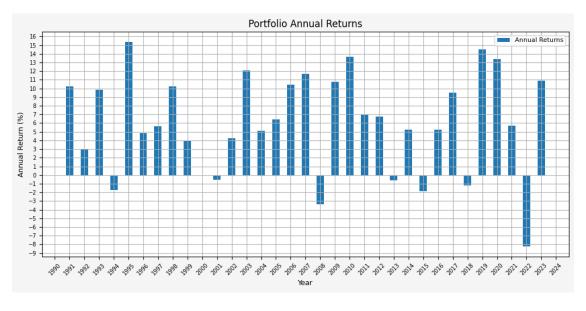






	Return
Year	
1991	0.102
1992	0.030
1993	0.099
1994	-0.017
1995	0.153
1996	0.049
1997	0.056
1998	0.102

```
1999
       0.039
2000
       0.000
2001
      -0.005
2002
       0.043
2003
       0.121
2004
       0.051
       0.064
2005
2006
       0.104
2007
       0.117
2008
      -0.033
2009
       0.107
2010
       0.137
2011
       0.070
2012
       0.068
2013
      -0.006
2014
       0.052
2015
     -0.018
2016
       0.052
2017
       0.095
2018
     -0.012
2019
       0.145
2020
       0.134
2021
       0.057
2022 -0.082
2023
       0.109
```



# 1.5 Calculate stats for various rebalance dates

```
[22]: # # List of funds to be used
      # fund_list = ['Stocks', 'Bonds', 'Gold', 'Cash']
      # # Starting cash contribution
      # starting_cash = 10000
      # # Monthly cash contribution
      \# cash contrib = 0
      # months = list(range(1, 13))
      \# days = list(range(1, 28))
      \# stats = pd.DataFrame(columns = ['Rebal_Month', 'Rebal_Day', 'Annualized_
       Mean', 'Annualized Volatility', 'Annualized Sharpe Ratio', 'CAGR',
                                         'Daily Max Return', 'Daily Max Return
       → (Date)', 'Daily Min Return', 'Daily Min Return (Date)', 'Max Drawdown',
                                        'Peak', 'Bottom', 'Recovery Date'])
      # for month in months:
           for day in days:
                strat = strategy(fund_list, starting_cash, cash_contrib, perm_port,_
       ⇔month, day).set_index('Date')
                sum_stats = summary_stats(fund_list, strat[['Return']], 'Daily')
                stats = pd.concat([stats, sum_stats], ignore_index=True)
                stats.loc[stats.index[-1], 'Rebal_Month'] = month
                stats.loc[stats.index[-1], 'Rebal_Day'] = day
                display(stats)
      # plan_name = '_'.join(fund_list)
      # file = plan_name + "_All_Summary_Stats.xlsx"
      # location = file
      # stats.to_excel(location, sheet_name='data')
      # print(f"All summary stats complete for {plan_name}.")
```