## harry-browne-permanent-portfolio

July 21, 2025

# 1 Does Harry Browne's permanent portfolio withstand the test of time?

## 1.1 Python Imports

```
[1]: # Standard Library
     import datetime
     import io
     import os
     import random
     import sys
     import warnings
     from datetime import datetime, timedelta
     from pathlib import Path
     # Data Handling
     import numpy as np
     import pandas as pd
     # Data Visualization
     import matplotlib.dates as mdates
     import matplotlib.pyplot as plt
     import matplotlib.ticker as mtick
     import seaborn as sns
     from matplotlib.ticker import FormatStrFormatter, FuncFormatter, MultipleLocator
     # Data Sources
     import yfinance as yf
     # Statistical Analysis
     import statsmodels.api as sm
     # Machine Learning
     from sklearn.decomposition import PCA
     from sklearn.preprocessing import StandardScaler
```

```
# Suppress warnings
warnings.filterwarnings("ignore")
```

#### 1.2 Add Directories To Path

1: /usr/lib/python3.13

3:

2: /usr/lib/python3.13/lib-dynload

```
[2]: # Add the source subdirectory to the system path to allow import config from
     ⇔settings.py
     current_directory = Path(os.getcwd())
     website_base_directory = current_directory.parent.parent.parent
     src_directory = website_base_directory / "src"
     sys.path.append(str(src_directory)) if str(src_directory) not in sys.path else_
      ⊸None
     # Import settings.py
     from settings import config
     # Add configured directories from config to path
     SOURCE DIR = config("SOURCE DIR")
     sys.path.append(str(Path(SOURCE DIR))) if str(Path(SOURCE DIR)) not in sys.path
      ⇔else None
     QUANT_FINANCE_RESEARCH_BASE_DIR = config("QUANT_FINANCE_RESEARCH_BASE_DIR")
     sys.path.append(str(Path(QUANT_FINANCE_RESEARCH_BASE_DIR))) if_
      str(Path(QUANT_FINANCE_RESEARCH_BASE_DIR)) not in sys.path else None
     QUANT_FINANCE_RESEARCH_SOURCE_DIR = config("QUANT_FINANCE_RESEARCH_SOURCE_DIR")
     sys.path.append(str(Path(QUANT FINANCE RESEARCH SOURCE DIR))) if
     str(Path(QUANT_FINANCE_RESEARCH_SOURCE_DIR)) not in sys.path else None
     # Add other configured directories
     BASE_DIR = config("BASE_DIR")
     CONTENT_DIR = config("CONTENT_DIR")
     POSTS DIR = config("POSTS DIR")
     PAGES DIR = config("PAGES DIR")
     PUBLIC DIR = config("PUBLIC DIR")
     SOURCE_DIR = config("SOURCE_DIR")
     DATA DIR = config("DATA DIR")
     DATA_MANUAL_DIR = config("DATA_MANUAL_DIR")
     # Print system path
     for i, path in enumerate(sys.path):
        print(f"{i}: {path}")
    0: /usr/lib/python313.zip
```

```
2
```

- 4: /home/jared/python-virtual-envs/general\_313/lib/python3.13/site-packages
- 5: /home/jared/Cloud\_Storage/Dropbox/Websites/jaredszajkowski.github.io/src
- 6: /home/jared/Cloud\_Storage/Dropbox/Quant\_Finance\_Research
- 7: /home/jared/Cloud\_Storage/Dropbox/Quant\_Finance\_Research/src

## 1.3 Track Index Dependencies

```
[3]: # Create file to track markdown dependencies
dep_file = Path("index_dep.txt")
dep_file.write_text("")
```

[3]: 0

## 1.4 Python Functions

```
[4]: from bb_clean_data import bb_clean_data
from df_info import df_info
from df_info_markdown import df_info_markdown
from export_track_md_deps import export_track_md_deps
from load_data import load_data
from pandas_set_decimal_places import pandas_set_decimal_places
from strategy_harry_brown_perm_port import strategy_harry_brown_perm_port
from summary_stats import summary_stats
```

#### 1.5 Data Overview

## 1.5.1 Load Data

```
[5]: # Set decimal places
     pandas_set_decimal_places(2)
     # Bonds dataframe
     bb_clean_data(
         base_directory=DATA_DIR,
         fund ticker name="SPBDU10T S&P US Treasury Bond 7-10 Year Total Return,

Index",
         source="Bloomberg",
         asset_class="Indices",
         excel export=True,
         pickle_export=True,
         output_confirmation=True,
     )
     bonds_data = load_data(
         base directory=DATA DIR,
         ticker="SPBDU10T_S&P US Treasury Bond 7-10 Year Total Return Index_Clean",
         source="Bloomberg",
         asset_class="Indices",
```

The first and last date of data for SPBDU10T\_S&P US Treasury Bond 7-10 Year Total Return Index is:

Close
Date
1989-12-29 100
Close
Date
2024-04-30 579.02

Bloomberg data cleaning complete for SPBDU10T\_S&P US Treasury Bond 7-10 Year Total Return Index

\_\_\_\_\_

Bonds\_Close Bonds\_Daily\_Return Bonds\_Total\_Return Date 1990-01-02 99.97 NaNNaN 1990-01-03 99.73 -0.00 1.00 0.00 1.00 1990-01-04 99.81 1990-01-05 99.77 -0.00 1.00 1.00 1990-01-08 99.68 -0.00

```
[6]: # Copy this <!-- INSERT_01_Bonds_Data_Head_HERE --> to index_temp.md
export_track_md_deps(dep_file=dep_file, md_filename="01_Bonds_Data_Head.md",__
content=bonds_data.head().to_markdown(floatfmt=".3f"))
```

Exported and tracked: 01\_Bonds\_Data\_Head.md

```
[7]: # Stocks dataframe

bb_clean_data(
    base_directory=DATA_DIR,
    fund_ticker_name="SPXT_S&P 500 Total Return Index",
    source="Bloomberg",
    asset_class="Indices",
    excel_export=True,
```

```
pickle_export=True,
         output_confirmation=True,
     )
     stocks_data = load_data(
         base_directory=DATA_DIR,
         ticker="SPXT_S&P 500 Total Return Index_Clean",
         source="Bloomberg",
         asset class="Indices",
         timeframe="Daily",
         file_format="excel",
     )
     stocks_data['Date'] = pd.to_datetime(stocks_data['Date'])
     stocks_data.set_index('Date', inplace = True)
     stocks_data = stocks_data[(stocks_data.index >= '1990-01-01') & (stocks_data.
      →index <= '2023-12-31')]</pre>
     stocks_data.rename(columns={'Close':'Stocks_Close'}, inplace=True)
     stocks_data['Stocks_Daily_Return'] = stocks_data['Stocks_Close'].pct_change()
     stocks_data['Stocks_Total_Return'] = (1 + stocks_data['Stocks_Daily_Return']).
      display(stocks_data.head())
    The first and last date of data for SPXT_S&P 500 Total Return Index is:
                Close
    Date
    1988-01-04 256.02
                  Close
    Date
    2024-04-30 10951.66
    Bloomberg data cleaning complete for SPXT_S&P 500 Total Return Index
                Stocks_Close Stocks_Daily_Return Stocks_Total_Return
    Date
    1990-01-01
                                               {\tt NaN}
                                                                    NaN
                         NaN
    1990-01-02
                      386.16
                                               NaN
                                                                    NaN
    1990-01-03
                      385.17
                                             -0.00
                                                                   1.00
    1990-01-04
                      382.02
                                             -0.01
                                                                   0.99
    1990-01-05
                      378.30
                                             -0.01
                                                                   0.98
[8]: # Copy this <!-- INSERT 01 Stocks Data Head HERE --> to index temp.md
     export_track_md_deps(dep_file=dep_file, md_filename="01_Stocks_Data_Head.md",_
      ⇔content=stocks_data.head().to_markdown(floatfmt=".3f"))
```

Exported and tracked: 01\_Stocks\_Data\_Head.md

```
[9]: # Gold dataframe
     bb_clean_data(
        base_directory=DATA_DIR,
        fund_ticker_name="XAU_Gold USD Spot",
         source="Bloomberg",
        asset_class="Commodities",
        excel_export=True,
        pickle_export=True,
        output_confirmation=True,
     )
     gold_data = load_data(
        base_directory=DATA_DIR,
        ticker="XAU_Gold USD Spot_Clean",
         source="Bloomberg",
        asset_class="Commodities",
        timeframe="Daily",
        file_format="excel",
     )
     gold_data['Date'] = pd.to_datetime(gold_data['Date'])
     gold_data.set_index('Date', inplace = True)
     gold_data = gold_data[(gold_data.index >= '1990-01-01') & (gold_data.index <=__
     gold_data.rename(columns={'Close':'Gold_Close'}, inplace=True)
     gold_data['Gold_Daily_Return'] = gold_data['Gold_Close'].pct_change()
     gold_data['Gold_Total_Return'] = (1 + gold_data['Gold_Daily_Return']).cumprod()
     display(gold_data.head())
    The first and last date of data for XAU_Gold USD Spot is:
               Close
    Date
    1949-12-30 34.69
                 Close
    Date
    2024-05-01 2299.31
    Bloomberg data cleaning complete for XAU_Gold USD Spot
                Gold_Close Gold_Daily_Return Gold_Total_Return
    Date
    1990-01-02
                    399.00
                                          NaN
                                                             NaN
    1990-01-03
                    395.00
                                        -0.01
                                                            0.99
    1990-01-04
                    396.50
                                         0.00
                                                            0.99
    1990-01-05
                    405.00
                                         0.02
                                                            1.02
    1990-01-08
                    404.60
                                        -0.00
                                                            1.01
```

Exported and tracked: O1\_Gold\_Data\_Head.md

## 1.5.2 Combine Data

```
[11]: # Merge the stock data and bond data into a single DataFrame using their
      ⇔indices (dates)
      perm_port = pd.merge(stocks_data['Stocks_Close'], bonds_data['Bonds_Close'],__
       →left_index=True, right_index=True)
      # Add gold data to the portfolio DataFrame by merging it with the existing data_
      →on indices (dates)
      perm_port = pd.merge(perm_port, gold_data['Gold_Close'], left_index=True,_u
       ⇔right_index=True)
      # Add a column for cash with a constant value of 1 (assumes the value of cash
      ⇔remains constant at $1 over time)
      perm_port['Cash_Close'] = 1
      # Remove any rows with missing values (NaN) to ensure clean data for further
       ⇔analysis
      perm_port.dropna(inplace=True)
      # Display the finalized portfolio DataFrame
      display(perm_port)
```

	Stocks_Close	Bonds_Close	${\tt Gold\_Close}$	${\tt Cash\_Close}$
Date				
1990-01-02	386.16	99.97	399.00	1
1990-01-03	385.17	99.73	395.00	1
1990-01-04	382.02	99.81	396.50	1
1990-01-05	378.30	99.77	405.00	1
1990-01-08	380.04	99.68	404.60	1
•••	•••	•••	•••	•••
2023-12-22	10292.37	604.17	2053.08	1
2023-12-26	10335.98	604.55	2067.81	1
2023-12-27	10351.60	609.36	2077.49	1
2023-12-28	10356.59	606.83	2065.61	1
2023-12-29	10327.83	606.18	2062.98	1

[8479 rows x 4 columns]

## 1.5.3 Check For Missing Values

```
[12]: # Check for any missing values in each column perm_port.isnull().any()
```

[12]: Stocks\_Close False
Bonds\_Close False
Gold\_Close False
Cash\_Close False

dtype: bool

## 1.5.4 Permanent Portfolio DataFrame Info

## [13]: df\_info(perm\_port)

The columns, shape, and data types are: <class 'pandas.core.frame.DataFrame'>

DatetimeIndex: 8479 entries, 1990-01-02 to 2023-12-29

Data columns (total 4 columns):

#	Column	Non-Null Count	Dtype
0	Stocks_Close	8479 non-null	float64
1	Bonds_Close	8479 non-null	float64
2	${\tt Gold\_Close}$	8479 non-null	float64
3	Cash_Close	8479 non-null	int64

dtypes: float64(3), int64(1)

memory usage: 331.2 KB

None

The first 5 rows are:

	Stocks_Close	${\tt Bonds\_Close}$	${\tt Gold\_Close}$	${\tt Cash\_Close}$
Date				
1990-01-02	386.16	99.97	399.00	1
1990-01-03	385.17	99.73	395.00	1
1990-01-04	382.02	99.81	396.50	1
1990-01-05	378.30	99.77	405.00	1
1990-01-08	380.04	99.68	404.60	1

The last 5 rows are:

	Stocks_Close	Bonds_Close	${\tt Gold\_Close}$	Cash_Close
Date				
2023-12-22	10292.37	604.17	2053.08	1
2023-12-26	10335.98	604.55	2067.81	1
2023-12-27	10351.60	609.36	2077.49	1
2023-12-28	10356.59	606.83	2065.61	1
2023-12-29	10327.83	606.18	2062.98	1

```
[14]: # Copy this <!-- INSERT_02_Perm_Port_DF_Info_HERE --> to index_temp.md
export_track_md_deps(dep_file=dep_file, md_filename="02_Perm_Port_DF_Info.md",

→content=df_info_markdown(perm_port))
```

Exported and tracked: 02\_Perm\_Port\_DF\_Info.md

#### 1.6 Execute Strategy

```
[15]: # List of funds to be used
      fund_list = ['Stocks', 'Bonds', 'Gold', 'Cash']
      # Starting cash contribution
      starting_cash = 10000
      # Monthly cash contribution
      cash_contrib = 0
      strat = strategy_harry_brown_perm_port(
          fund_list=fund_list,
          starting_cash=starting_cash,
          cash_contrib=cash_contrib,
          close_prices_df=perm_port,
          rebal_month=1,
          rebal_day=1,
          rebal_per_high=0.35,
          rebal_per_low=0.15,
          excel_export=True,
          pickle_export=True,
          output_confirmation=True,
      )
      strat = strat.set_index('Date')
```

Strategy complete for Stocks\_Bonds\_Gold\_Cash

#### [16]: df\_info(strat)

```
The columns, shape, and data types are:
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 8479 entries, 1990-01-02 to 2023-12-29
Data columns (total 34 columns):
```

#	Column	Non-Null Count	Dtype
0	Stocks_Close	8479 non-null	float64
1	Bonds_Close	8479 non-null	float64
2	Gold_Close	8479 non-null	float64
3	Cash_Close	8479 non-null	int64
4	Stocks_BA_Shares	8479 non-null	float64
5	Stocks BA \$ Invested	8479 non-null	float64

```
Stocks_BA_Port_%
                            8479 non-null
                                            float64
 6
 7
     Bonds_BA_Shares
                            8479 non-null
                                            float64
 8
     Bonds_BA_$_Invested
                            8479 non-null
                                            float64
 9
     Bonds_BA_Port_%
                           8479 non-null
                                            float64
     Gold BA Shares
 10
                            8479 non-null
                                            float64
     Gold_BA_$_Invested
 11
                           8479 non-null
                                            float64
     Gold_BA_Port_%
                            8479 non-null
                                            float64
 13
     Cash_BA_Shares
                           8479 non-null
                                            float64
 14 Cash_BA_$_Invested
                           8479 non-null
                                            float64
 15
     Cash_BA_Port_%
                            8479 non-null
                                            float64
     Total_BA_$_Invested
 16
                           8479 non-null
                                            float64
     Contribution
 17
                            8479 non-null
                                            int64
     Rebalance
                            8479 non-null
 18
                                            object
     Stocks_AA_Shares
                            8479 non-null
                                            float64
 20
     Stocks_AA_$_Invested
                           8479 non-null
                                            float64
     Stocks_AA_Port_%
                            8479 non-null
 21
                                            float64
 22
     Bonds_AA_Shares
                            8479 non-null
                                            float64
 23
     Bonds_AA_$_Invested
                            8479 non-null
                                            float64
 24
    Bonds_AA_Port_%
                           8479 non-null
                                            float64
 25
     Gold_AA_Shares
                           8479 non-null
                                            float64
     Gold_AA_$_Invested
 26
                           8479 non-null
                                            float64
 27
     Gold_AA_Port_%
                           8479 non-null
                                            float64
 28
     Cash_AA_Shares
                           8479 non-null
                                            float64
 29
     Cash_AA_$_Invested
                           8479 non-null
                                            float64
 30
     Cash_AA_Port_%
                            8479 non-null
                                            float64
    Total_AA_$_Invested
 31
                           8479 non-null
                                            float64
 32
    Return
                            8478 non-null
                                            float64
     Cumulative_Return
                            8478 non-null
                                            float64
dtypes: float64(31), int64(2), object(1)
```

memory usage: 2.3+ MB

None

The first 5 rows are:

	Stocks_Close H	Bonds_Close	Gold_Close	Cash_Close	\	
Date						
1990-01-02	386.16	99.97	399.00	1		
1990-01-03	385.17	99.73	395.00	1		
1990-01-04	382.02	99.81	396.50	1		
1990-01-05	378.30	99.77	405.00	1		
1990-01-08	380.04	99.68	404.60	1		
	Stocks_BA_Share	es Stocks_B	A_\$_Invested	Stocks_BA_	Port_%	\
Date						
1990-01-02	6.4	17	2500.00		0.25	
1990-01-03	6.4	17	2493.59		0.25	
1990-01-04	6.4	17	2473.20		0.25	
1990-01-05	6.4	47	2449.11		0.25	
1990-01-08	6.4	47	2460.38		0.25	

```
Bonds_BA_Shares Bonds_BA_$_Invested Bonds_BA_Port_% ... \
Date
1990-01-02
                      25.01
                                                               0.25
                                          2500.00
1990-01-03
                      25.01
                                          2494.02
                                                               0.25
1990-01-04
                      25.01
                                          2496.02
                                                               0.25
1990-01-05
                      25.01
                                          2494.92
                                                               0.25 ...
1990-01-08
                      25.01
                                          2492.72
                                                               0.25 ...
            Bonds_AA_Port_% Gold_AA_Shares Gold_AA_$_Invested \
Date
1990-01-02
                       0.25
                                        6.27
                                                          2500.00
                       0.25
                                        6.27
                                                          2474.94
1990-01-03
1990-01-04
                       0.25
                                        6.27
                                                          2484.34
1990-01-05
                       0.25
                                        6.27
                                                          2537.59
                       0.25
                                        6.27
1990-01-08
                                                          2535.09
            Gold_AA_Port_% Cash_AA_Shares Cash_AA_$_Invested \
Date
1990-01-02
                      0.25
                                    2500.00
                                                         2500.00
1990-01-03
                       0.25
                                    2500.00
                                                         2500.00
1990-01-04
                      0.25
                                    2500.00
                                                         2500.00
1990-01-05
                      0.25
                                    2500.00
                                                         2500.00
1990-01-08
                      0.25
                                    2500.00
                                                         2500.00
            Cash AA Port % Total AA $ Invested Return Cumulative Return
Date
1990-01-02
                      0.25
                                        10000.00
                                                     NaN
                                                                        NaN
1990-01-03
                       0.25
                                         9962.55
                                                  -0.00
                                                                       1.00
1990-01-04
                      0.25
                                         9953.56 -0.00
                                                                       1.00
1990-01-05
                                                   0.00
                                                                       1.00
                      0.25
                                         9981.63
1990-01-08
                      0.25
                                         9988.19
                                                   0.00
                                                                       1.00
[5 rows x 34 columns]
The last 5 rows are:
            Stocks Close Bonds Close Gold Close Cash Close \
Date
2023-12-22
                                604.17
                                           2053.08
                10292.37
                                                              1
2023-12-26
                10335.98
                                604.55
                                           2067.81
                                                              1
2023-12-27
                                609.36
                                           2077.49
                                                              1
                10351.60
2023-12-28
                10356.59
                                606.83
                                           2065.61
                                                              1
2023-12-29
                10327.83
                                606.18
                                           2062.98
                                                              1
            Stocks_BA_Shares Stocks_BA_$_Invested Stocks_BA_Port_% \
Date
2023-12-22
                         1.81
                                           18595.87
                                                                  0.29
```

18674.66

0.29

1.81

2023-12-26

```
2023-12-27
                        1.81
                                           18702.89
                                                                  0.29
2023-12-28
                        1.81
                                           18711.90
                                                                  0.29
2023-12-29
                        1.81
                                           18659.94
                                                                 0.29
            Bonds_BA_Shares Bonds_BA_$_Invested Bonds_BA_Port_% ... \
Date
2023-12-22
                      25.03
                                         15124.46
                                                              0.23 ...
2023-12-26
                      25.03
                                         15134.20
                                                              0.23 ...
2023-12-27
                      25.03
                                         15254.36
                                                              0.23 ...
2023-12-28
                                                              0.23 ...
                      25.03
                                         15191.10
2023-12-29
                      25.03
                                         15175.01
                                                              0.23 ...
            Bonds_AA_Port_% Gold_AA_Shares Gold_AA_$_Invested \
Date
2023-12-22
                       0.23
                                        8.00
                                                        16426.12
                       0.23
                                        8.00
2023-12-26
                                                        16543.97
2023-12-27
                       0.23
                                        8.00
                                                        16621.42
2023-12-28
                       0.23
                                        8.00
                                                        16526.37
2023-12-29
                       0.23
                                        8.00
                                                        16505.33
            Gold_AA_Port_% Cash_AA_Shares Cash_AA_$_Invested \
Date
2023-12-22
                      0.25
                                  14717.17
                                                       14717.17
2023-12-26
                      0.25
                                   14717.17
                                                       14717.17
2023-12-27
                      0.25
                                  14717.17
                                                       14717.17
2023-12-28
                      0.25
                                   14717.17
                                                       14717.17
                      0.25
2023-12-29
                                   14717.17
                                                       14717.17
            Cash AA Port % Total AA $ Invested Return Cumulative Return
Date
                                                                       6.49
2023-12-22
                      0.23
                                        64863.62
                                                   0.00
                                        65070.01
2023-12-26
                      0.23
                                                   0.00
                                                                       6.51
                                                                       6.53
2023-12-27
                      0.23
                                        65295.84
                                                   0.00
2023-12-28
                      0.23
                                        65146.54 -0.00
                                                                       6.51
2023-12-29
                      0.23
                                        65057.44 -0.00
                                                                       6.51
[5 rows x 34 columns]
```

Exported and tracked: 03\_Strategy.md

⇔content=df info markdown(strat))

[17]: # Copy this <!-- INSERT 03 Strategy HERE --> to index temp.md

export\_track\_md\_deps(dep\_file=dep\_file, md\_filename="03\_Strategy.md",\_

## 1.7 Summary Statistics

```
[18]: sum_stats = summary_stats(
          fund_list=fund_list,
          df=strat[['Return']],
          period="Daily",
          use_calendar_days=False,
          excel_export=True,
          pickle_export=True,
          output_confirmation=True,
      )
      strat_pre_1999 = strat[strat.index < '2000-01-01']
      sum_stats_pre_1999 = summary_stats(
          fund_list=fund_list,
          df=strat_pre_1999[['Return']],
          period="Daily",
          use_calendar_days=False,
          excel_export=False,
          pickle_export=False,
          output_confirmation=True,
      )
      strat_post_1999 = strat[strat.index >= '2000-01-01']
      sum_stats_post_1999 = summary_stats(
          fund list=fund list,
          df=strat_post_1999[['Return']],
          period="Daily",
          use_calendar_days=False,
          excel_export=False,
          pickle_export=False,
          output_confirmation=True,
      )
      strat_post_2009 = strat[strat.index >= '2010-01-01']
      sum_stats_post_2009 = summary_stats(
          fund_list=fund_list,
          df=strat_post_2009[['Return']],
          period="Daily",
          use_calendar_days=False,
          excel export=False,
          pickle_export=False,
          output_confirmation=True,
      )
```

Summary stats complete for Stocks\_Bonds\_Gold\_Cash Summary stats complete for Stocks\_Bonds\_Gold\_Cash Summary stats complete for Stocks\_Bonds\_Gold\_Cash Summary stats complete for Stocks\_Bonds\_Gold\_Cash

```
[19]: all_sum_stats = pd.concat([sum_stats])
      all_sum_stats = all_sum_stats.rename(index={'Return': '1990 - 2023'})
      all_sum_stats = pd.concat([all_sum_stats, sum_stats_pre_1999])
      all_sum_stats = all_sum_stats.rename(index={'Return': 'Pre 1999'})
      all_sum_stats = pd.concat([all_sum_stats, sum_stats_post_1999])
      all_sum_stats = all_sum_stats.rename(index={'Return': 'Post 1999'})
      all sum stats = pd.concat([all sum stats, sum stats post 2009])
      all_sum_stats = all_sum_stats.rename(index={'Return': 'Post 2009'})
      display(all sum stats)
                  Annualized Mean
                                   Annualized Volatility
                                                           Annualized Sharpe Ratio \
     1990 - 2023
                              0.06
                                                     0.06
                                                                              0.96
     Pre 1999
                              0.06
                                                     0.05
                                                                              1.21
     Post 1999
                             0.06
                                                     0.06
                                                                              0.88
     Post 2009
                             0.06
                                                     0.06
                                                                              0.93
                  CAGR Daily Max Return Daily Max Return (Date) Daily Min Return
     1990 - 2023
                  0.06
                                    0.03
                                                       2020-03-24
                                                                              -0.03
                  0.06
                                    0.02
     Pre 1999
                                                       1999-09-28
                                                                              -0.02
     Post 1999
                  0.06
                                     0.03
                                                       2020-03-24
                                                                              -0.03
     Post 2009
                  0.06
                                     0.03
                                                       2020-03-24
                                                                              -0.03
                 Daily Min Return (Date) Max Drawdown
                                                              Peak
                                                                       Bottom \
     1990 - 2023
                              2020-03-12
                                                  -0.15 2008-03-18 2008-11-12
                                                  -0.06 1998-07-20 1998-08-31
     Pre 1999
                              1993-08-05
     Post 1999
                              2020-03-12
                                                  -0.15 2008-03-18 2008-11-12
     Post 2009
                              2020-03-12
                                                  -0.13 2021-12-27 2022-10-20
                 Recovery Date
     1990 - 2023
                    2009-10-06
     Pre 1999
                    1998-11-05
     Post 1999
                    2009-10-06
     Post 2009
                    2023-12-01
[20]: # Copy this <!-- INSERT_04_Summary_Stats_HERE --> to index_temp.md
      export_track_md_deps(dep_file=dep_file, md_filename="04_Summary_Stats.md",_

content=all_sum_stats.to_markdown(floatfmt=".3f"))
```

Exported and tracked: 04\_Summary\_Stats.md

#### 1.8 Annual Returns

```
strat_annual_returns_df['Year'] = strat_annual_returns_df.index.year # Add a_\'
    'Year' column with just the year
strat_annual_returns_df.reset_index(drop=True, inplace=True) # Reset the index_\'
    *to remove the datetime index

# Now the DataFrame will have 'Year' and 'Cumulative_Return' columns
strat_annual_returns_df = strat_annual_returns_df[['Year',_\'
    \'Cumulative_Return']] # Keep only 'Year' and 'Cumulative_Return' columns
strat_annual_returns_df.rename(columns = {'Cumulative_Return':'Return'},_\'
    \'inplace=True)
strat_annual_returns_df.set_index('Year', inplace=True)
display(strat_annual_returns_df)
```

#### Return Year 1991 0.10 1992 0.03 1993 0.10 1994 -0.02 1995 0.15 1996 0.05 1997 0.06 0.10 1998 1999 0.04 2000 0.00 2001 -0.01 2002 0.04 2003 0.12 2004 0.05 2005 0.06 2006 0.10 2007 0.12 2008 -0.03 2009 0.11 2010 0.14 2011 0.07 2012 0.07 2013 -0.01 2014 0.05 2015 -0.02 2016 0.05 2017 0.09 2018 -0.01 2019 0.15 2020 0.13 2021 0.06

2022

-0.08

```
2023 0.11
```

```
[22]: # Copy this <!-- INSERT_05_Annual_Returns_HERE --> to index_temp.md
export_track_md_deps(dep_file=dep_file, md_filename="05_Annual_Returns.md",
content=strat_annual_returns_df.to_markdown(floatfmt=".3f"))
```

Exported and tracked: 05\_Annual\_Returns.md

#### 1.9 Plots

#### 1.9.1 Plot Cumulative Return

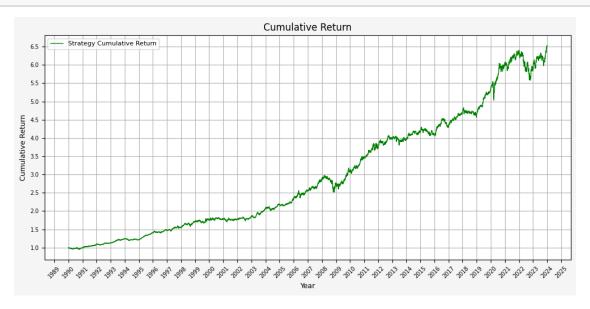
```
[24]: def plot_cumulative_return(strat_df):
                               # Generate plot
                              plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
                               # Plotting data
                              plt.plot(strat_df.index, strat_df['Cumulative_Return'], label = 'Strategy_
                      →Cumulative Return', linestyle='-', color='green', linewidth=1)
                               # Set X axis
                               \# x\_tick\_spacing = 5 \# Specify the interval for x-axis ticks
                               # plt.qca().xaxis.set_major_locator(MultipleLocator(x_tick_spacing))
                              plt.gca().xaxis.set_major_locator(mdates.YearLocator())
                              plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('\( \frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\fracc}\frac{\frac{\frac{\frac{\frac
                              plt.xlabel('Year', fontsize = 9)
                              plt.xticks(rotation = 45, fontsize = 7)
                               # plt.xlim(, )
                               # Set Y axis
                              y_tick_spacing = 0.5 # Specify the interval for y-axis ticks
                              plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
                              plt.ylabel('Cumulative Return', fontsize = 9)
                              plt.yticks(fontsize = 7)
                               # plt.ylim(0, 7.5)
                               # Set title, etc.
                              plt.title('Cumulative Return', fontsize = 12)
                               # Set the grid & legend
                              plt.tight_layout()
                              plt.grid(True)
```

```
plt.legend(fontsize=8)

# Save the figure
plt.savefig('06_Cumulative_Return.png', dpi=300, bbox_inches='tight')

# Display the plot
return plt.show()
```

## [25]: plot\_cumulative\_return(strat)



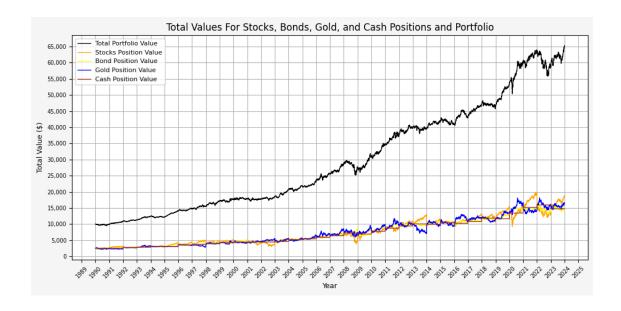
#### 1.9.2 Plot Portfolio & Component Values

```
def plot_values(strat_df):
    # Generate plot
    plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')

# Plotting data
    plt.plot(strat_df.index, strat_df['Total_AA_$_Invested'], label='Total_
Portfolio Value', linestyle='-', color='black', linewidth=1)
    plt.plot(strat_df.index, strat_df['Stocks_AA_$_Invested'], label='Stocks_
Position Value', linestyle='-', color='orange', linewidth=1)
    plt.plot(strat_df.index, strat_df['Bonds_AA_$_Invested'], label='Bond_
Position Value', linestyle='-', color='yellow', linewidth=1)
    plt.plot(strat_df.index, strat_df['Gold_AA_$_Invested'], label='Gold_
Position Value', linestyle='-', color='blue', linewidth=1)
    plt.plot(strat_df.index, strat_df['Cash_AA_$_Invested'], label='Cash_
Position Value', linestyle='-', color='brown', linewidth=1)
```

```
# Set X axis
  # x_tick_spacing = 5  # Specify the interval for x-axis ticks
  # plt.qca().xaxis.set_major_locator(MultipleLocator(x_tick_spacing))
  plt.gca().xaxis.set_major_locator(mdates.YearLocator())
  plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
  plt.xlabel('Year', fontsize = 9)
  plt.xticks(rotation = 45, fontsize = 7)
  # plt.xlim(, )
  # Set Y axis
  y_tick_spacing = 5000 # Specify the interval for y-axis ticks
  plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
  plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:,..
\rightarrow0f}'.format(x))) # Adding commas to y-axis labels
  plt.ylabel('Total Value ($)', fontsize = 9)
  plt.yticks(fontsize = 7)
  # plt.ylim(0, 75000)
  # Set title, etc.
  plt.title('Total Values For Stocks, Bonds, Gold, and Cash Positions and U
→Portfolio', fontsize = 12)
  # Set the grid & legend
  plt.tight_layout()
  plt.grid(True)
  plt.legend(fontsize=8)
  # Save the figure
  plt.savefig('07_Portfolio_Values.png', dpi=300, bbox_inches='tight')
  # Display the plot
  return plt.show()
```

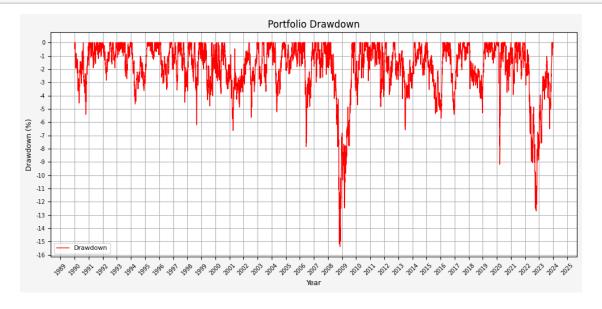
#### [27]: plot\_values(strat)



#### 1.9.3 Plot Portfolio Drawdown

```
[28]: def plot_drawdown(strat_df):
                              rolling_max = strat_df['Total_AA_$_Invested'].cummax()
                              drawdown = (strat_df['Total_AA_$_Invested'] - rolling_max) / rolling_max *__
                      →100
                               # Generate plot
                              plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
                              # Plotting data
                              plt.plot(strat_df.index, drawdown, label='Drawdown', linestyle='-',u
                      ⇔color='red', linewidth=1)
                               # Set X axis
                               # x_tick_spacing = 5 # Specify the interval for x-axis ticks
                               # plt.qca().xaxis.set_major_locator(MultipleLocator(x tick_spacing))
                              plt.gca().xaxis.set_major_locator(mdates.YearLocator())
                              plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('\( \frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\fracc}\frac{\frac{\frac{\frac{\frac
                              plt.xlabel('Year', fontsize = 9)
                              plt.xticks(rotation = 45, fontsize = 7)
                              # plt.xlim(, )
                               # Set Y axis
                              y_tick_spacing = 1 # Specify the interval for y-axis ticks
                              plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
                               # plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:
                       \rightarrow, .0f}'.format(x))) # Adding commas to y-axis labels
```

## [29]: plot\_drawdown(strat)

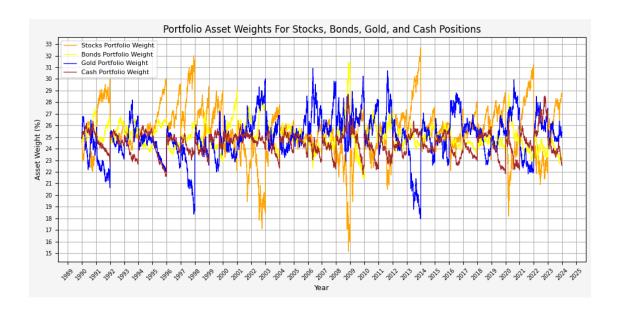


## 1.9.4 Plot Asset Weights

```
[30]: def plot_asset_weights(strat_df):
    # Generate plot
    plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
```

```
# Plotting data
  plt.plot(strat_df.index, strat_df['Stocks_AA_Port_%'] * 100, label='Stocks_I
→Portfolio Weight', linestyle='-', color='orange', linewidth=1)
  plt.plot(strat df.index, strat df['Bonds AA Port %'] * 100, label='Bonds_1
→Portfolio Weight', linestyle='-', color='yellow', linewidth=1)
  plt.plot(strat_df.index, strat_df['Gold_AA_Port_%'] * 100, label='Gold_
→Portfolio Weight', linestyle='-', color='blue', linewidth=1)
  plt.plot(strat df.index, strat df['Cash AA Port %'] * 100, label='Cash,
→Portfolio Weight', linestyle='-', color='brown', linewidth=1)
  # Set X axis
  # x_tick_spacing = 5 # Specify the interval for x-axis ticks
  # plt.gca().xaxis.set_major_locator(MultipleLocator(x_tick_spacing))
  plt.gca().xaxis.set_major_locator(mdates.YearLocator())
  plt.gca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
  plt.xlabel('Year', fontsize = 9)
  plt.xticks(rotation = 45, fontsize = 7)
  # plt.xlim(, )
  # Set Y axis
  y_tick_spacing = 1 # Specify the interval for y-axis ticks
  plt.gca().yaxis.set major locator(MultipleLocator(y tick spacing))
  # plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:
\hookrightarrow, .0f}'.format(x))) # Adding commas to y-axis labels
  plt.ylabel('Asset Weight (%)', fontsize = 9)
  plt.yticks(fontsize = 7)
  # plt.ylim(14, 36)
  # Set title, etc.
  plt.title('Portfolio Asset Weights For Stocks, Bonds, Gold, and Cash⊔
→Positions', fontsize = 12)
  # Set the grid & legend
  plt.tight_layout()
  plt.grid(True)
  plt.legend(fontsize=8)
  # Save the figure
  plt.savefig('09_Portfolio_Weights.png', dpi=300, bbox_inches='tight')
  # Display the plot
  return plt.show()
```

```
[31]: plot_asset_weights(strat)
```



#### 1.9.5 Plot Annual Returns

```
[32]: def plot_annual_returns(return_df):
          # Generate plot
          plt.figure(figsize=(10, 5), facecolor = '#F5F5F5')
          # Plotting data
          plt.bar(return_df.index, return_df['Return'] * 100, label='Annual Returns',
       ⇒width=0.5) # width adjusted for better spacing
          # Set X axis
          x_tick_spacing = 1 # Specify the interval for x-axis ticks
          plt.gca().xaxis.set major locator(MultipleLocator(x tick spacing))
          # plt.gca().xaxis.set_major_locator(mdates.YearLocator())
          # plt.qca().xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
          plt.xlabel('Year', fontsize = 9)
          plt.xticks(rotation = 45, fontsize = 7)
          # plt.xlim(, )
          # Set Y axis
          y_tick_spacing = 1  # Specify the interval for y-axis ticks
          plt.gca().yaxis.set_major_locator(MultipleLocator(y_tick_spacing))
          # plt.gca().yaxis.set_major_formatter(mtick.FuncFormatter(lambda x, pos: '{:
       \hookrightarrow, .0f}'.format(x))) # Adding commas to y-axis labels
          plt.ylabel('Annual Return (%)', fontsize = 9)
          plt.yticks(fontsize = 7)
          # plt.ylim(-20, 20)
```

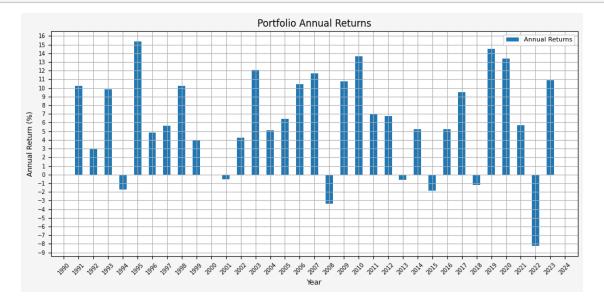
```
# Set title, etc.
plt.title('Portfolio Annual Returns', fontsize = 12)

# Set the grid & legend
plt.tight_layout()
plt.grid(True)
plt.legend(fontsize=8)

# Save the figure
plt.savefig('10_Portfolio_Annual_Returns.png', dpi=300, bbox_inches='tight')

# Display the plot
return plt.show()
```

## [33]: plot\_annual\_returns(strat\_annual\_returns\_df)



## 1.10 Portfolio Summary Statistics For Various Rebalance Dates

```
# # Loop through each combination of month and day
      # for month in months:
            for day in days:
      #
                try:
      #
                     strat = strategy_harry_brown_perm_port(
      #
                         fund list=fund list,
      #
                         starting_cash=starting_cash,
      #
                         cash contrib=cash contrib,
      #
                         close_prices_df=perm_port,
      #
                         rebal month=month,
                        rebal_day=day,
                        rebal_per_high=0.35,
      #
      #
                        rebal_per_low=0.15,
      #
                         excel export=False.
      #
                        pickle_export=False,
                         output_confirmation=False,
      #
                    ).set_index('Date')
      #
                    sum_stats = summary_stats(
      #
                         fund_list=fund_list,
      #
                         df=strat[['Return']],
      #
                        period="Daily",
      #
                         excel export=False,
      #
                        pickle_export=False,
                        output confirmation=False,
                    )
      #
      #
                    stats = pd.concat([stats, sum_stats], ignore_index=True)
                    stats.loc[stats.index[-1], 'Rebal_Month'] = month
                    stats.loc[stats.index[-1], 'Rebal_Day'] = day
      #
                    print(f"Month: {month}, Day: {day} - Stats added successfully.")
      #
                except Exception as e:
                    print(f"Error for month {month} and day {day}: {e}")
      #
                    continue
[35]: # # Export the stats DataFrame to Excel and pickle files
      # plan name = ' '.join(fund list)
      # stats.to_excel(f"{plan_name}_Various_Rebalance_Summary_Stats.xlsx",_
       ⇔sheet_name="data")
      \# stats.to_pickle(f"{plan_name}_Various_Rebalance_Summary_Stats.pkl")
[36]: # Load the stats DataFrame from the pickle file
      # stats = load_data(f"{plan_name}_Various_Rebalance_Summary_Stats.pkl")
[37]: # stats
```