

### 3 Self-organized criticality: the Oslo model

This section provides the tasks and questions related to implementing and analyzing the Oslo model of self-organized criticality. **The tasks should be finished till 21.11.2024.**

The Oslo rice-pile model is a theoretical model of self-organized criticality (SOC) used to study the behavior of granular materials and avalanche-like phenomena in a simple, discrete system. It was introduced as a variation of the sandpile model, and it's named after the city of Oslo, Norway, where it was developed.

1. Implement the Oslo model using the following algorithm focusing on slopes  $z_i$ :

- (a) Initialize the system in arbitrary stable configuration  $z_i \leq z_i^T$ , where  $z_i^T$  is  $i$ -th slope threshold  $\in \{1, 2\}$ ;
- (b) Drive the system by adding a grain at left-most site;
- (c) If  $z_i > z_i^T$ , relax the site  $i$ ,

for  $i = 1 : z_1 \rightarrow z_1 - 2, z_2 \rightarrow z_2 + 1$ ;  
for  $i = 2 \dots L - 1 : z_i = z_i - 2, z_{i\pm 1} \rightarrow z_{i\pm 1} + 1$ ;  
for  $i = L : z_L \rightarrow z_L - 1, z_{L-1} \rightarrow z_{L-1} + 1$ .

During relaxation do not forget about choosing randomly new threshold  $z_i^T \in \{1, 2\}$  for the relaxed site. Continue relaxation until  $z_i \leq z_i^T$  for all  $i$ ;

- (d) Return to point (b).
2. Plot scaled avalanche size  $s/s_{max}$  in function of time  $t$  (measured in terms of grain additions). Does it makes sense to analyze data for small  $t$ ? Which condition should be satisfied in avalanche size statistical analysis?
  3. Plot in log-log scale avalanche size probability  $P(s, L)$  with respect to avalanche size  $s$  for several lengths of the system ( $L$  should be at least 64). Do you observe power law behavior? Why this power law breaks for large  $s$ ?