

Name Can, Jaren, Kelsey

ITCS 3153: Introduction to Artificial Intelligence
In-class assignment
Introduction to utility theory

1. Economists often use an exponential utility function for money: $U(x) = -e^{-x/R}$, where R is a positive constant representing an individual's risk tolerance. As R (measured in same units as x) becomes larger, the individual becomes less risk-averse.

Assume Mary has an exponential utility function with $R = \$500$. Mary is given the choice between receiving \$500 with certainty (probability 1) or participating in a lottery which has a 60% probability of winning \$5000 and a 40% probability of winning nothing. Assuming Mary acts rationally, which option should she choose? Show how you derive your answer.

IF Mary takes \$500:

$$U(500) = -2.71$$

$$\text{so } EU(A) = 1(-2.71) \\ = -2.71$$

choose to take the \$500
since we get higher returns.

The other option

$$U(5000) = -22026.5$$

$$U(0) = -1$$

$$EU(A) = -22026.5(.6) + \\ + 1(.4) \\ = -13216.3$$

2. Consider a student who has the choice to buy or not buy a textbook for a course. We'll model this as a decision problem with one Boolean decision node, B , indicating whether the agent chooses to buy the book, and two Boolean chance nodes, M , indicating whether the student has mastered the material in the book, and P , indicating whether the student passes the course. Of course, there is also a utility node, U . A certain student has an additive utility function: 0 for not buying the book and -\$100 for buying it; and \$2000 for passing the course and 0 for not passing. The student's conditional probability estimates are:

$$P(p|b, m) = 0.9$$

$$P(m|b) = 0.9$$

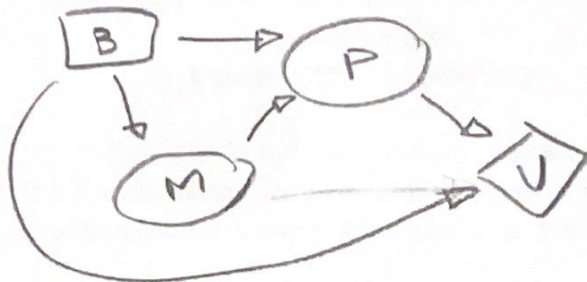
$$P(p|b, \neg m) = 0.5$$

$$P(m|\neg b) = 0.7$$

$$P(p|\neg b, m) = 0.8$$

$$P(p|\neg b, \neg m) = 0.3$$

- a) Draw the decision network for this problem. Remember that decision nodes are rectangles, chance nodes are ovals, and utility nodes are diamonds.



- b) Compute the expected utility of buying the book and of not buying it.

$$\begin{aligned}
 P(P|\neg b) &= P(P|\neg b, m) + P(P|\neg b, \neg m) \\
 &= P(m|\neg b)P(P|\neg b, m) + P(\neg m|\neg b)P(P|\neg b, \neg m) \\
 &= (.7)(.8) + (.3)(.3) = .65 \\
 2000(.65) &= \boxed{1300}
 \end{aligned}$$

$$\begin{aligned}
 P(P|b) &= P(P|b, m) + P(P|b, \neg m) \\
 &= P(m|b)P(P|b, m) + P(\neg m|b)P(P|b, \neg m) \\
 &= (.9)(.9) + (.1)(.5) = .86 \\
 &= (.9)(.1) + (.1)(.5) = .14 \\
 1900(.86) - 100(.14) &= \boxed{1620}
 \end{aligned}$$

- c) Acting rationally, what choice should the student make?

BUY THE TEXTBOOK :)