

Let's see how this constraint works

$$s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000 y_A$$

If $y_A = 1$, the constraint becomes $s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000$



Total shipments from Amadora cannot exceed capacity

If $y_A = 0$, the constraint becomes $s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 0$



$s_{A,V} = 0, s_{A,W} = 0, s_{A,X} = 0, s_{A,Y} = 0, s_{A,Z} = 0$



No shipments from Amadora

Proposal 1 Spreadsheet Model*

PARAMETERS

Supplier	Cost of supplying 1 ton to Facility					Supplier capacity
	Valencia	Wiesbaden	Xanten	York	Zaragoza	
Amadora	1.78	2.26	2.22	2.30	1.45	4,000
Bergamo	1.64	2.70	2.00	2.44	2.30	2,000
Casablanca	1.70	2.15	2.58	1.28	1.95	1,000
Quantity required	1,000	500	1,500	1,500	500	

DECISIONS VARIABLES

From Supplier	To Facility					Quantity supplied	Select supplier?	Effective capacity
	Valencia	Wiesbaden	Xanten	York	Zaragoza			
Amadora	1,000	500	1,500	500	500	4,000	1	4000
Bergamo	0	0	0	0	0	0	0	0
Casablanca	0	0	0	1,000	0	1,000	1	1000
Quantity received	1,000	500	1,500	1,500	500			2

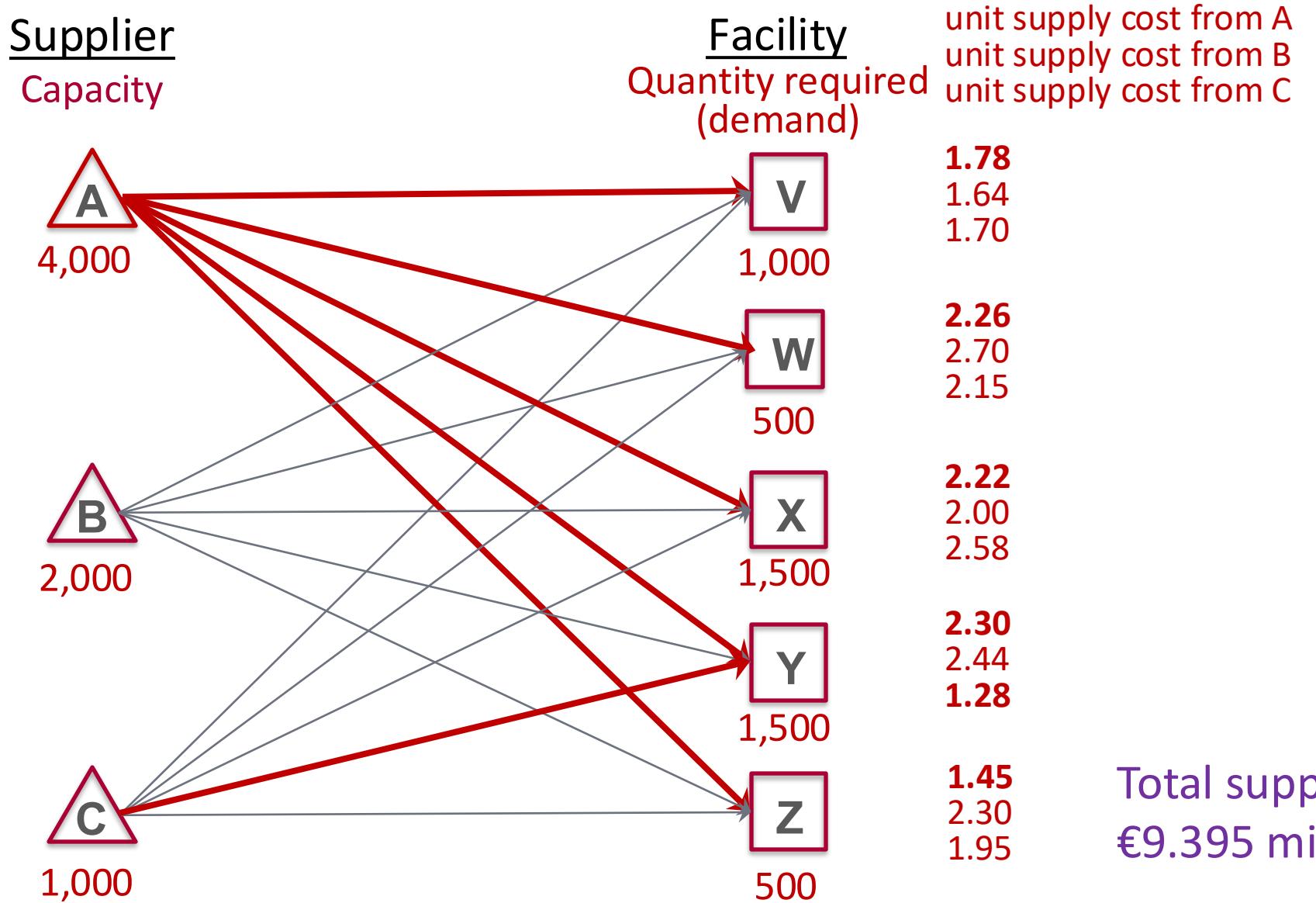
OBJECTIVE

Total Cost **9,395** minimize

CONSTRAINTS

- Supply does not exceed effective capacity
- Quantity delivered equals quantity required
- Select two suppliers
- Nonnegativity + binary selection variables

Proposal 1 Supply Plan



Proposal 2 Formulation – Will this work?

minimize

(total supply cost)

$$1.78 s_{A,V} + 2.26 s_{A,W} + \dots + 1.95 s_{C,Z}$$

subject to

(capacity at A)

$$s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000$$

(capacity at B)

$$s_{B,V} + s_{B,W} + s_{B,X} + s_{B,Y} + s_{B,Z} \leq 2,000$$

(capacity at C)

$$s_{C,V} + s_{C,W} + s_{C,X} + s_{C,Y} + s_{C,Z} \leq 1,000$$

(single sourcing for V)

$$y_{A,V} + y_{B,V} + y_{C,V} = 1$$

(linking constraint for A)

$$s_{A,V} \leq 4,000$$

(linking constraint for B)

$$s_{B,V} \leq 2,000$$

(linking constraint for C)

$$s_{C,V} \leq 1,000$$

(demand at V)

$$s_{A,V} + s_{B,V} + s_{C,V} \geq 1,000$$

(demand at W)

$$s_{A,W} + s_{B,W} + s_{C,W} \geq 500$$

(demand at X)

$$s_{A,X} + s_{B,X} + s_{C,X} \geq 1,500$$

(demand at Y)

$$s_{A,Y} + s_{B,Y} + s_{C,Y} \geq 1,500$$

(demand at Z)

$$s_{A,Z} + s_{B,Z} + s_{C,Z} \geq 500$$

(nonnegativity / binary)

$$s_{A,V}, s_{A,W}, \dots, s_{C,Z} \geq 0, \quad y_{A,V}, y_{B,V}, y_{C,V} \text{ are binary}$$

Idea:

$y_{i,V} = 1$ if we use Supplier
i to serve Valencia, and 0
if we don't...

Proposal 2 Formulation

(Answer)

minimize

(total supply cost)

$$1.78 s_{A,V} + 2.26 s_{A,W} + \dots + 1.95 s_{C,Z}$$

subject to

(capacity at A)

$$s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000$$

(capacity at B)

$$s_{B,V} + s_{B,W} + s_{B,X} + s_{B,Y} + s_{B,Z} \leq 2,000$$

(capacity at C)

$$s_{C,V} + s_{C,W} + s_{C,X} + s_{C,Y} + s_{C,Z} \leq 1,000$$

(single sourcing for V)

$$y_{A,V} + y_{B,V} + y_{C,V} = 1$$

(linking constraint for A)

$$s_{A,V} \leq 4,000$$

(linking constraint for B)

$$s_{B,V} \leq 2,000$$

(linking constraint for C)

$$s_{C,V} \leq 1,000$$

(demand at V)

$$s_{A,V} + s_{B,V} + s_{C,V} \geq 1,000$$

(demand at W)

$$s_{A,W} + s_{B,W} + s_{C,W} \geq 500$$

(demand at X)

$$s_{A,X} + s_{B,X} + s_{C,X} \geq 1,500$$

(demand at Y)

$$s_{A,Y} + s_{B,Y} + s_{C,Y} \geq 1,500$$

(demand at Z)

$$s_{A,Z} + s_{B,Z} + s_{C,Z} \geq 500$$

(nonnegativity / binary)

$$s_{A,V}, s_{A,W}, \dots, s_{C,Z} \geq 0$$

$y_{A,V}, y_{B,V}, y_{C,V}$ are binary

Idea:

$y_{i,V} = 1$ if we use Supplier i to serve Valencia, and 0 if we don't...

Proposal 2 Spreadsheet Model*

PARAMETERS

Supplier	Cost of supplying 1 ton to Facility					Supplier capacity
	Valencia	Wiesbaden	Xanten	York	Zaragoza	
Amadora	1.78	2.26	2.22	2.30	1.45	4,000
Bergamo	1.64	2.70	2.00	2.44	2.30	2,000
Casablanca	1.70	2.15	2.58	1.28	1.95	1,000
Quantity required	1,000	500	1,500	1,500	500	

DECISIONS VARIABLES

From Supplier	To Facility					Quantity supplied	Used to source Valencia?	Valencia demand * binary
	Valencia	Wiesbaden	Xanten	York	Zaragoza			
Amadora	0	500	500	500	500	2,000	0	0
Bergamo	1,000	0	1,000	0	0	2,000	1	1000
Casablanca	0	0	0	1,000	0	1,000	0	0
Quantity received	1,000	500	1,500	1,500	500		1	

OBJECTIVE

Total Cost **9,035** minimize

CONSTRAINTS

Supply does not exceed capacity

Quantity delivered equals quantity required

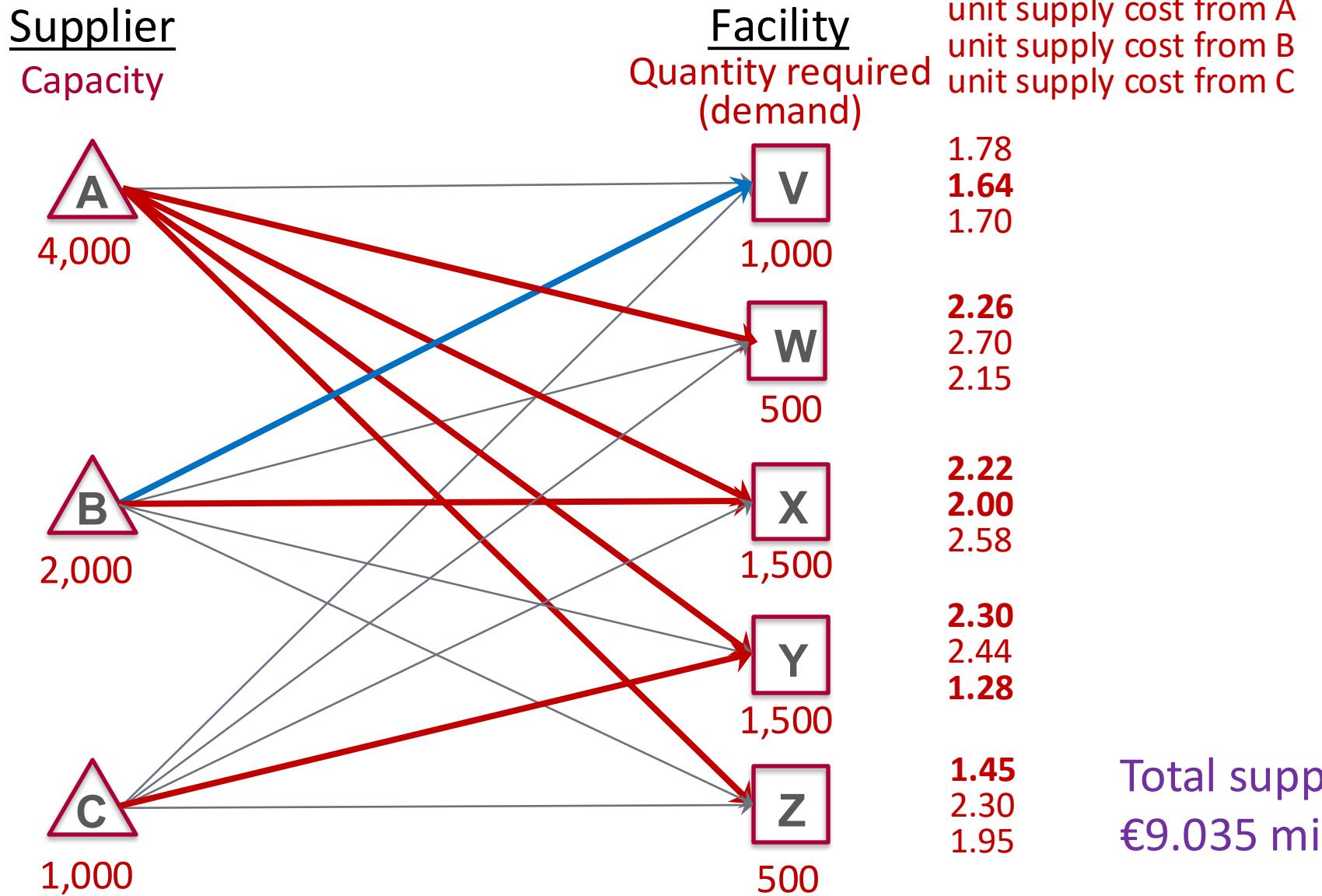
Sum of binaries equals 1 (select only one supplier for location 1)

Cells C12:14 cannot exceed Cells J12:J14

Nonegativity

Binary

Proposal 2 Supply Plan



Operational Proposals: Cost Implications Summary

	Without supplier consolidation	With supplier consolidation
Without single sourcing	€8.995 million	€9.395 million
With single sourcing	€9.035 million	(optional)

↓ +0.44%

+4.44%

Class Exercise 2

Assessing Impact of New Supply Conditions

- Bergamo's Condition: The supplier at Bergamo has indicated that a renewal of their supply contract would require a **fixed cost** of €1 million for ordering any amount from the supplier. This is on top of the variable cost.
- Amadora's Condition: The supplier at Amadora has indicated that a renewal of their supply contract would require a **minimum order quantity** of 3,000 tons.

The retailer's senior management wants to understand the cost implications of each of these two new contract conditions (separate and jointly) in order to inform its contract negotiations