

# Let's see how this constraint works

$$s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000 y_A$$

If  $y_A = 1$ , the constraint becomes  $s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000$



*Total shipments from Amadora cannot exceed capacity*

If  $y_A = 0$ , the constraint becomes  $s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 0$



$$s_{A,V} = 0, s_{A,W} = 0, s_{A,X} = 0, s_{A,Y} = 0, s_{A,Z} = 0$$



*No shipments from Amadora*

# Proposal 1 Spreadsheet Model\*

## PARAMETERS

Supplier	Cost of supplying 1 ton to Facility					Supplier capacity
	Valencia	Wiesbaden	Xanten	York	Zaragoza	
<b>Amadora</b>	1.78	2.26	2.22	2.30	1.45	4,000
<b>Bergamo</b>	1.64	2.70	2.00	2.44	2.30	2,000
<b>Casablanca</b>	1.70	2.15	2.58	1.28	1.95	1,000
Quantity required	1,000	500	1,500	1,500	500	

## DECISIONS VARIABLES

From Supplier	To Facility					Quantity supplied	Select supplier?	Effective capacity
	Valencia	Wiesbaden	Xanten	York	Zaragoza			
<b>Amadora</b>	1,000	500	1,500	500	500	4,000	1	4000
<b>Bergamo</b>	0	0	0	0	0	0	0	0
<b>Casablanca</b>	0	0	0	1,000	0	1,000	1	1000
Quantity received	1,000	500	1,500	1,500	500		2	

## OBJECTIVE

<b>Total Cost</b>	<b>9,395</b>
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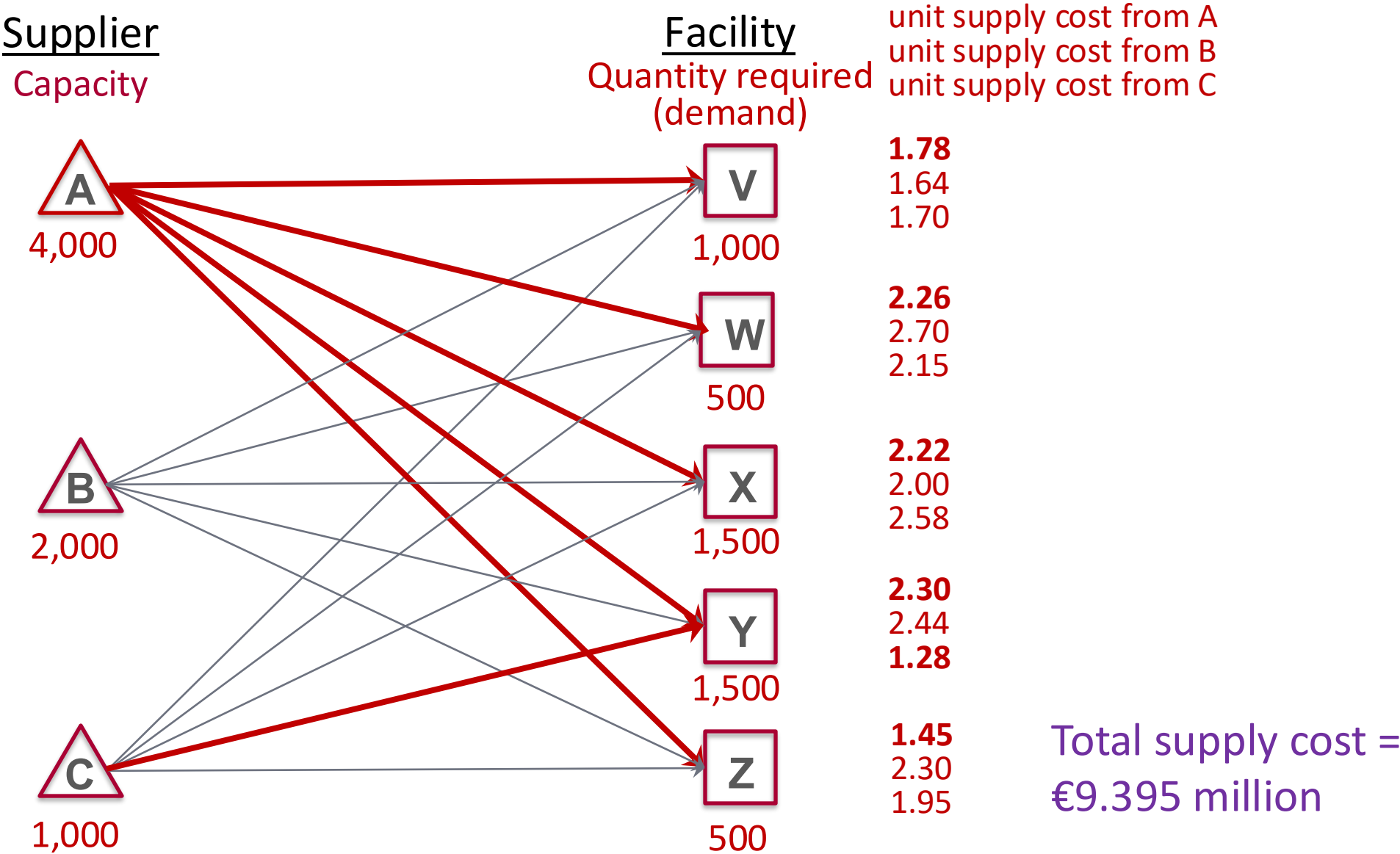
*minimize*

## CONSTRAINTS

Supply does not exceed effective capacity  
 Quantity delivered equals quantity required  
 Select two suppliers  
 Nonnegativity + binary selection variables

\*will be uploaded after class

# Proposal 1 Supply Plan



# Proposal 2 Formulation – *Will this work?*

**minimize**

(total supply cost)

$$1.78 s_{A,V} + 2.26 s_{A,W} + \dots + 1.95 s_{C,Z}$$

**subject to**

(capacity at A)

$$s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000$$

(capacity at B)

$$s_{B,V} + s_{B,W} + s_{B,X} + s_{B,Y} + s_{B,Z} \leq 2,000$$

(capacity at C)

$$s_{C,V} + s_{C,W} + s_{C,X} + s_{C,Y} + s_{C,Z} \leq 1,000$$

(single sourcing for V)

$$y_{A,V} + y_{B,V} + y_{C,V} = 1$$

(linking constraint for A)

$$s_{A,V} \leq 4,000$$

(linking constraint for B)

$$s_{B,V} \leq 2,000$$

(linking constraint for C)

$$s_{C,V} \leq 1,000$$

(demand at V)

$$s_{A,V} + s_{B,V} + s_{C,V} \geq 1,000$$

(demand at W)

$$s_{A,W} + s_{B,W} + s_{C,W} \geq 500$$

(demand at X)

$$s_{A,X} + s_{B,X} + s_{C,X} \geq 1,500$$

(demand at Y)

$$s_{A,Y} + s_{B,Y} + s_{C,Y} \geq 1,500$$

(demand at Z)

$$s_{A,Z} + s_{B,Z} + s_{C,Z} \geq 500$$

(nonnegativity / binary)

$$s_{A,V}, s_{A,W}, \dots, s_{C,Z} \geq 0, y_{A,V}, y_{B,V}, y_{C,V} \text{ are binary}$$

Idea:

$y_{i,V} = 1$  if we use Supplier  $i$  to serve Valencia, and 0 if we don't...

# Proposal 2 Formulation

(Answer)

**minimize**

(total supply cost)

$$1.78 s_{A,V} + 2.26 s_{A,W} + \dots + 1.95 s_{C,Z}$$

**subject to**

(capacity at A)

$$s_{A,V} + s_{A,W} + s_{A,X} + s_{A,Y} + s_{A,Z} \leq 4,000$$

(capacity at B)

$$s_{B,V} + s_{B,W} + s_{B,X} + s_{B,Y} + s_{B,Z} \leq 2,000$$

(capacity at C)

$$s_{C,V} + s_{C,W} + s_{C,X} + s_{C,Y} + s_{C,Z} \leq 1,000$$

(single sourcing for V)

$$y_{A,V} + y_{B,V} + y_{C,V} = 1$$

(linking constraint for A)

$$s_{A,V} \leq 4,000 y_{A,V}$$

(linking constraint for B)

$$s_{B,V} \leq 2,000 y_{B,V}$$

(linking constraint for C)

$$s_{C,V} \leq 1,000 y_{C,V}$$

(demand at V)

$$s_{A,V} + s_{B,V} + s_{C,V} \geq 1,000$$

(demand at W)

$$s_{A,W} + s_{B,W} + s_{C,W} \geq 500$$

(demand at X)

$$s_{A,X} + s_{B,X} + s_{C,X} \geq 1,500$$

(demand at Y)

$$s_{A,Y} + s_{B,Y} + s_{C,Y} \geq 1,500$$

(demand at Z)

$$s_{A,Z} + s_{B,Z} + s_{C,Z} \geq 500$$

(nonnegativity / binary)

$$s_{A,V}, s_{A,W}, \dots, s_{C,Z} \geq 0, y_{A,V}, y_{B,V}, y_{C,V} \text{ are binary}$$

Idea:

$y_{i,V} = 1$  if we use Supplier  $i$  to serve Valencia, and 0 if we don't...

# Proposal 2 Spreadsheet Model\*

## PARAMETERS

Supplier	Cost of supplying 1 ton to Facility					Supplier capacity
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Amadora	1.78	2.26	2.22	2.30	1.45	4,000
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Quantity required	1,000	500	1,500	1,500	500	

## DECISIONS VARIABLES

From Supplier	To Facility					Quantity supplied	Used to source Valencia?	Valencia demand * binary
	Valencia	Wiesbaden	Xanten	York	Zaragoza			
Amadora	0	500	500	500	500	2,000	0	0
Bergamo	1,000	0	1,000	0	0	2,000	1	1000
Casablanca	0	0	0	1,000	0	1,000	0	0
Quantity received	1,000	500	1,500	1,500	500		1	

## OBJECTIVE

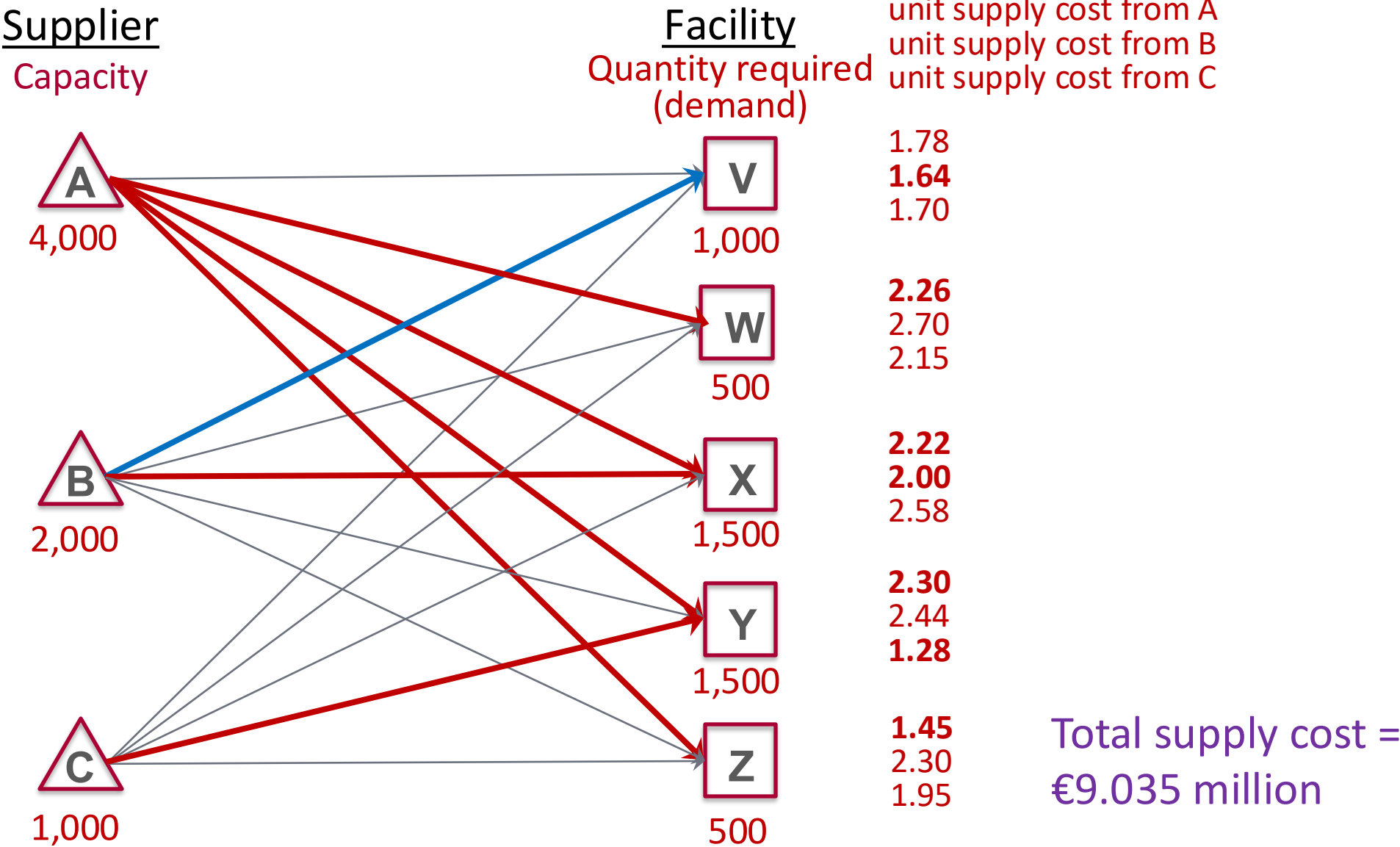
<b>Total Cost</b>	<b>9,035</b>	<i>minimize</i>
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## CONSTRAINTS

Supply does not exceed capacity  
 Quantity delivered equals quantity required  
 Sum of binaries equals 1 (select only one supplier for location 1)  
 Cells C12:14 cannot exceed Cells J12:J14  
 Nonnegativity  
 Binary

\*will be uploaded after class

# Proposal 2 Supply Plan



# Operational Proposals: Cost Implications Summary

	Without supplier consolidation		With supplier consolidation
Without single sourcing	€8.995 million	+4.44% →	€9.395 million
With single sourcing	↓ +0.44% €9.035 million		(optional)



# Class Exercise 2

# Assessing Impact of New Supply Conditions

- Bergamo's Condition: The supplier at **B**ergamo has indicated that a renewal of their supply contract would require a **fixed cost** of €1 million for ordering any amount from the supplier. This is on top of the variable cost.
- Amadora's Condition: The supplier at **A**madora has indicated that a renewal of their supply contract would require a **minimum order quantity** of 3,000 tons.

The retailer's senior management wants to understand the cost implications of each of these two new contract conditions (separate and jointly) in order to inform its contract negotiations