

Appendix A

List of Parameters

Table A.1: This table gives the parameters for UO_2 generating the energy function.

Array number	Parameter name	Parameter value
1	Energy Scaling Factor (e_{RGB})	1.6012 J/m^2
2	$\langle 100 \rangle$ Max Distance	0.405
3	$\langle 110 \rangle$ Max Distance	0.739
4	$\langle 111 \rangle$ Max Distance	0.352
5	$\langle 100 \rangle$ Weight	50.5
6	$\langle 110 \rangle$ Weight	4.55
7	$\langle 111 \rangle$ Weight	0.08
8	$\langle 100 \rangle$ Tilt/Twist Mix Power Law (1)	0.03325
9	$\langle 100 \rangle$ Tilt/Twist Mix Power Law (2)	0.00053125
10	Maximum $\langle 100 \rangle$ Twist Energy	0.60903
11	$\langle 100 \rangle$ Twist Shape Factor	1.4486
12	$\langle 100 \rangle$ Asymmetric Tilt Interpolation Power	35.8
13	$\langle 100 \rangle$ Symmetric Tilt First Peak Energy	1.0058
14	$\langle 100 \rangle$ Symmetric Tilt First $\Sigma 5$ Energy	0.84456
15	$\langle 100 \rangle$ Symmetric Tilt Second Peak Energy	0.97259
16	$\langle 100 \rangle$ Symmetric Tilt Second $\Sigma 5$ Energy	0.9379
17	$\langle 100 \rangle$ Symmetric Tilt $\Sigma 17$ Energy	0.96881
18	$\langle 100 \rangle$ Symmetric Tilt First Peak Angle	0.31569
19	$\langle 100 \rangle$ Symmetric Tilt Second Peak Angle	0.88538

Continued on next page.

Table A.1 – *Continued from previous page*

Array number	Parameter name	Parameter value
20	$\langle 110 \rangle$ Tilt/Twist Mix Power Law (1)	3.1573
21	$\langle 110 \rangle$ Tilt/Twist Mix Power Law (2)	1.9784
22	$\langle 110 \rangle$ Twist Peak Angle	0.46145
23	$\langle 110 \rangle$ Twist Peak Energy	1.1444
24	$\langle 110 \rangle$ Twist $\Sigma 3$ Energy	1.0931
25	$\langle 110 \rangle$ Twist 90° Energy	1.152
26	$\langle 110 \rangle$ Asymmetric Tilt Shape Factor	3.1843
27	$\langle 110 \rangle$ Symmetric Tilt Third Peak Energy	1.0514
28	$\langle 110 \rangle$ Symmetric Tilt $\Sigma 3$ Energy	0.61703
29	$\langle 110 \rangle$ Symmetric Tilt Second Peak Energy	1.0902
30	$\langle 110 \rangle$ Symmetric Tilt $\Sigma 11$ Energy	0.56686
31	$\langle 110 \rangle$ Symmetric Tilt First Peak Energy	1.1024
32	$\langle 110 \rangle$ Symmetric Tilt Third Peak Angle	0.88736
33	$\langle 110 \rangle$ Symmetric Tilt Second Peak Angle	1.8711
34	$\langle 110 \rangle$ Symmetric Tilt First Peak Angle	2.731
35	$\langle 111 \rangle$ Tilt-Twist Linear Interpolation	38.201
36	$\langle 111 \rangle$ Twist Shape Factor	1.2414
37	$\langle 111 \rangle$ Twist Peak Angle	0.49979
38	$\langle 111 \rangle$ Twist Peak Energy	0.7971
39	$\langle 111 \rangle$ Symmetric Tilt Peak Angle	0.25966
40	$\langle 111 \rangle$ Symmetric Tilt Max Energy	1.0288
41	$\langle 111 \rangle$ Symmetric Tilt $\Sigma 3$ Energy	1.1311
42	$\langle 111 \rangle$ Asymmetric Tilt Symmetry Point Energy	3.7674
43	$\langle 111 \rangle$ Asymmetric Tilt Scale Factor	0.053417

Appendix B

Grain Boundary Representations

Part of Bulatov *et al.*'s development of their 5D function was accomplished through visual representations of the GB space. However, the size of the five-space in which GBs reside makes representing them difficult. Different methods have been developed to represent them, each with their advantages and disadvantages. Three of these methods are the axis-angle representation, the Rodrigues representation, and the fundamental zone representation. These methods, though described separately, can be used together to form a better picture of what the GB space looks like (see for example ?? which combines the Rodrigues representation and the fundamental zone representation).

B.1 Axis-Angle Representation

The axis-angle representation is the simplest of the three described here. The axis of rotation of the GB specifies the point in axis-angle space, and the angle of misorientation between the two grains at the GB specifies the magnitude of the vector. Thus, the axis (\mathbf{a} , where \mathbf{a} has components a_x , a_y , and a_z) and the angle (θ) mathematically represent an axis-angle vector as:

$$\mathbf{A} = \mathbf{a} \theta \tag{B.1}$$

The axis-angle space can only take into account three degrees of freedom: the two angles specifying the axis, and the angle rotated through. Thus,

axis-angle space cannot fully visualize all of the necessary information contained in the full 5D space.[?] This representation suffers from the difficulties of understanding an infinite space because it maps an axis and an angle onto a Cartesian coordinate system. Without the help of additional methods, this infinite space remains difficult to understand. The best uses of this representation focus on using it as a starting point to move to other, more robust representations, and to represent the misorientation between two grains.[?]

B.2 Rodrigues Representation

The Rodrigues representation (sometimes called the “Rodrigues-Frank” representation) uses Rodrigues vectors to represent rotations in Rodrigues space. This representation takes ideas from the axis-angle space, but makes a few changes allowing crystal symmetries to be taken into account. The orientation of the GB normal still specifies the point in space, but the tangent of half the angle represents the magnitude of the vector. Thus, a Rodrigues vector can be represented as:[?, ?, ?, ?, ?]

$$\mathbf{R} = \mathbf{a} \tan\left(\frac{\theta}{2}\right) \quad (\text{B.2})$$

Some researchers favor this representation over others because of the lack of curvature such a mapping entails.[?, ?] However, still only three of the five degrees of freedom are specified. Bulatov *et al.* attached a unit vector at the points along the axis to represent the other two DoFs in ???. A parallel vector represents a twist boundary, and a perpendicular vector represents a tilt boundary. Anything else represents a mix of twist and tilt (or a mixed boundary). One limitation of Rodrigues space lies in the fact that it also maps to an infinite space.[?, ?].

B.3 Fundamental Zone Representation

The fundamental zone best graphically represents the full 5D GB. This representation takes advantage of the symmetries inherent in crystals[?] to simplify an infinite space into a compact, finite area called the fundamental zone.[?, ?, ?, ?, ?] Every point within the space represents a unique orientation, and every point outside the space can be represented as a point inside

the space through symmetry operations.[?, ?, ?] Bulatov *et al.* used this idea in connection with Rodrigues space to create ???. In Rodrigues space, the crystal symmetries of the material determine the shape of the fundamental zone.[?, ?] For fcc crystals, the fundamental zone takes the form of a truncated tetrahedron.[?] The edges of the fundamental zone in Rodrigues space represent the high-symmetry rotation axes, and points on one face can represent another point on a different face of the fundamental zone.

Appendix C

Graphs

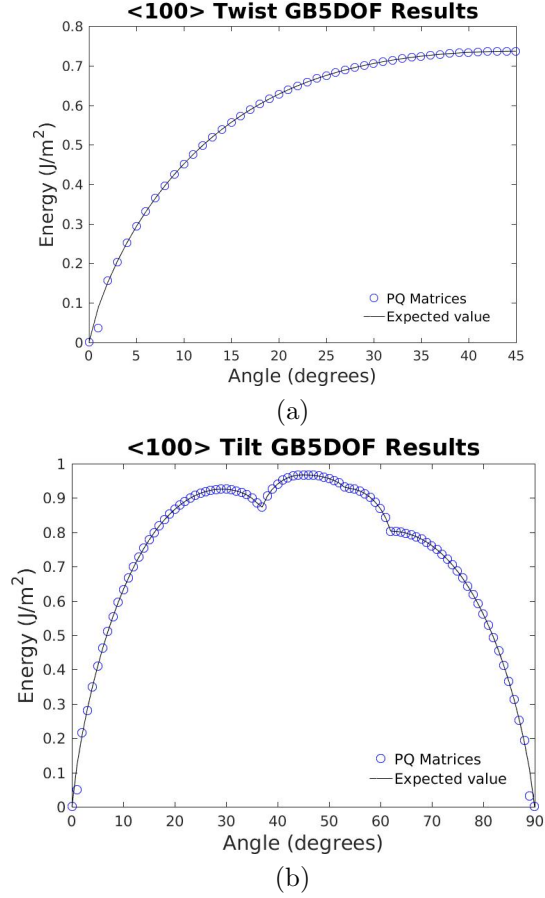


Figure C.1: The $\langle 100 \rangle$ twist (a) and tilt (b) results for the P and Q matrices as compared to Bulatov *et al.*'s energy profiles. Bulatov *et al.*'s GB5DOF .m MATLAB[®] script calculated the expected values by using the default parameters. The calculated values were found by inputting the matrices into the GB5DOF.m script. With the exception of the data points at 1° in both (a) and (b) and 89° in (b), the energies calculated from the matrices matches the expected curves exactly.

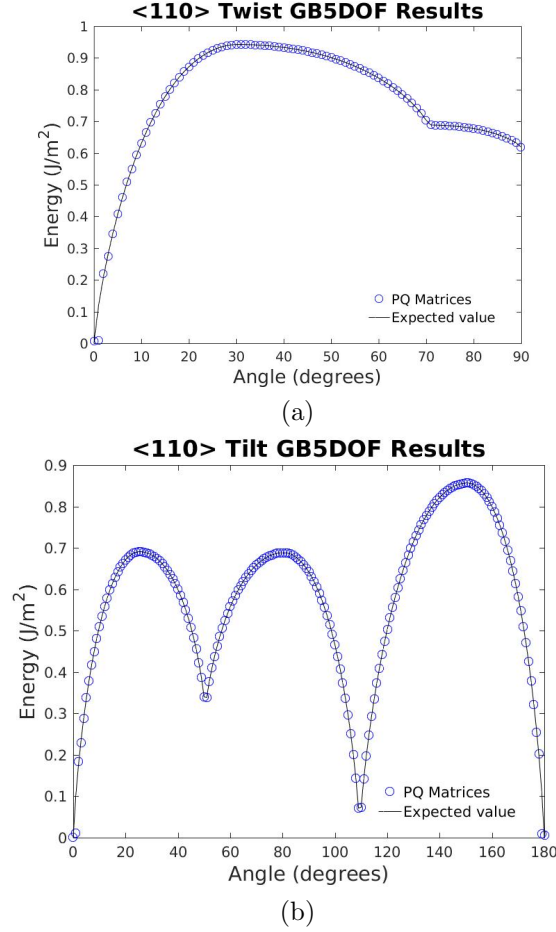
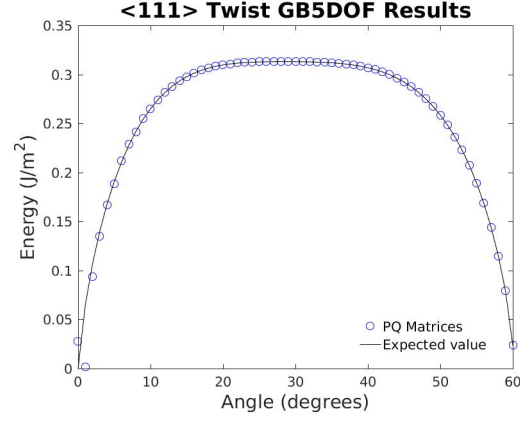
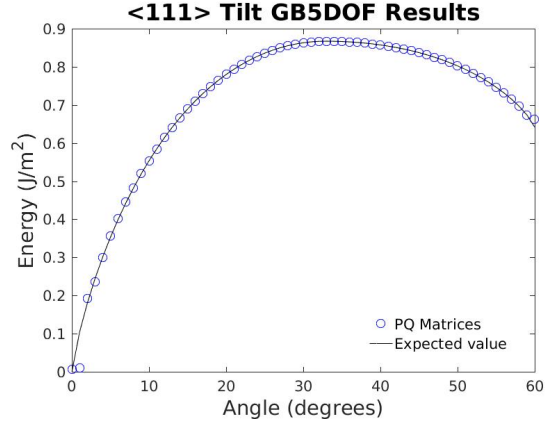


Figure C.2: The $\langle 110 \rangle$ twist (a) and tilt (b) results for the P and Q matrices as compared to Bulatov *et al.*'s energy profiles. Bulatov *et al.*'s GB5DOF.m MATLAB[®] script calculated the expected values by using the default parameters. The calculated values were found by inputting the matrices into the GB5DOF.m script. With the exception of the data points at 1° in both (a) and (b) and 179° in (b), the energies calculated from the matrices matches the expected curves exactly.



(a)



(b)

Figure C.3: The $\langle 111 \rangle$ twist (a) and tilt (b) results for the P and Q matrices as compared to Bulatov *et al.*'s energy profiles. Bulatov *et al.*'s GB5DOF .m MATLAB[®] script calculated the expected values by using the default parameters. The calculated values were found by inputting the matrices into the GB5DOF.m script. With the exception of the data points at 1° in both (a) and (b) and 60° in (b), the energies calculated from the matrices matches the expected curves exactly.

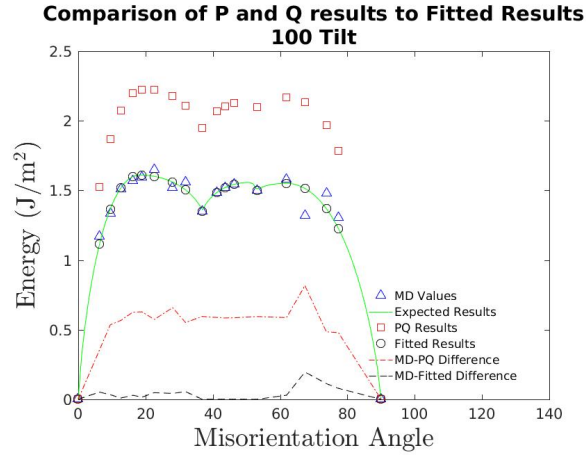
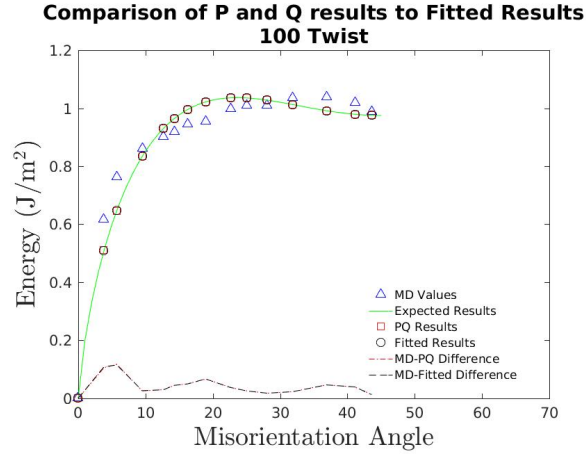


Figure C.4: A comparison of the expected value of the fitted function with the values calculated using the P and Q matrices for the $\langle 100 \rangle$ 1D subsets. The MD values are shown for reference. (a) PQ results follow exactly the fitted curve. (b) has a scaling issue yet to be fixed. The cause of the scaling issue remains unknown.

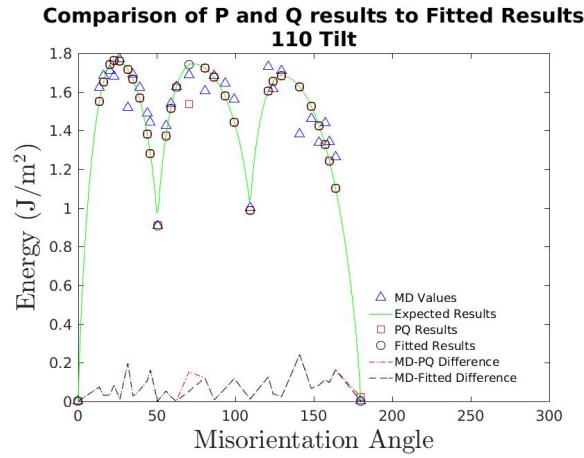
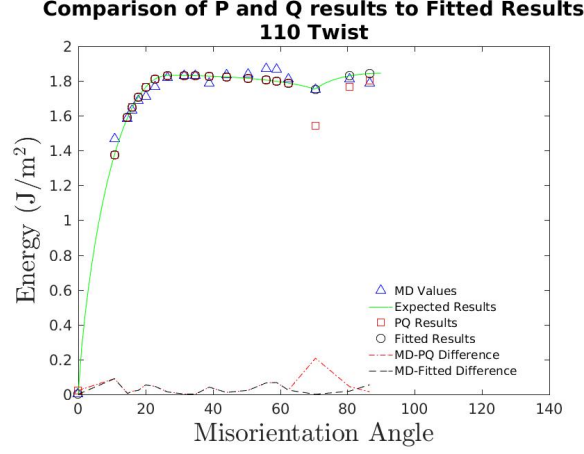


Figure C.5: A comparison of the expected value of the fitted function with the values calculated using the P and Q matrices for the $\langle 110 \rangle$ 1D subsets. MD values are shown for reference. (a) follows the fitted result until the cusp, at which point some anomalies appear. The results from the PQ matrices dip well below the expected value at the cusp, and never make it back to the original fitted line. (b) has a similar issue on a lesser scale. Only two of the calculated points do not follow the fitted curve. At the endpoint the expected value is zero, but the PQ matrices calculated a value slightly higher. Also, an unexpected cusp from the PQ matrices appears in the middle of the second hump. All other data points follow the fitted curve exactly.

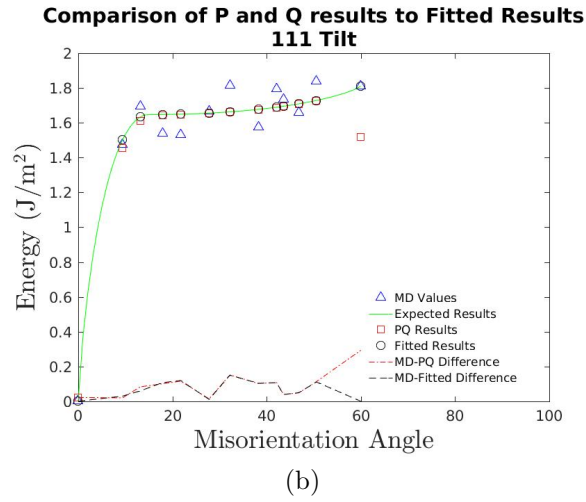
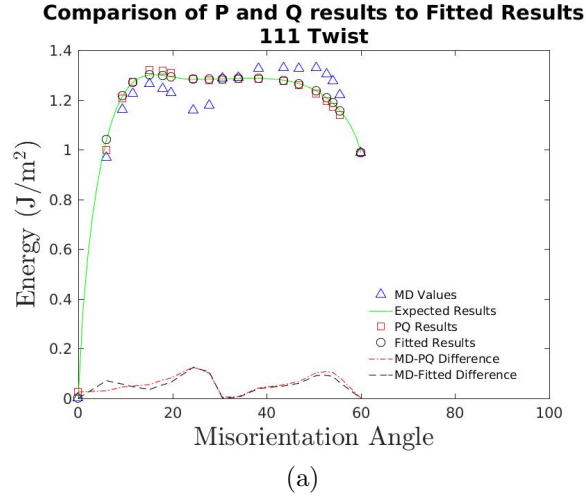


Figure C.6: A comparison of the expected value of the fitted function with the values calculated using the P and Q matrices for the $\langle 111 \rangle$ 1D subsets. MD values are shown for reference. (a) closely follows the expected fitted values, but has a slight error throughout. (b) follows the expected values exactly in the center of the fitting, but misses slightly for lower angle boundaries, and misses completely at the end.

Appendix D

Orientation Matrix Generator

This code generates the orientation matrices (known as the P and Q matrices in Bulatov *et al.*'s code). Provision for calculating the matrices one of two ways appears in-code through the use of command-line options.

```
from __future__ import division, print_function # To
    avoid numerical problems with division, and for ease
    of printing
from sys import argv # for CLI arguments
from math import cos, sin, pi, atan2, sqrt # Trig
    functions
from os.path import exists # For checking existence of
    a file
from numpy import array, linalg
from myModules import * # imports my functions from the
    file myModules.py

# Helper functions
def displayHelp():
    print(''''
        This script will calculate the orientation matrices
        for any given misorientation
        for any of the high-symmetry axes.
        Arguments:

        _axis: The axis of orientation (type: int)
```

_misorientation: The angle of misorientation (
type: float)

OR

(with option -e or --euler)

_z1: The first rotation angle (Z) (type:
float)

_x: The second rotation angle (X') (type:
float)

_z2: The third rotation angle (Z'') (type:
float)

If the option -e or --euler-angles is entered, the calculation skips to simply output the orientation matrices. Otherwise, the Euler angles are calculated from the axis, orientation, and grain boundary normal, and then the orientation matrix is created through the use of the Rodrigues Rotation Formula, which is:

$$R = I + \sin(\theta) * K + (1 - \cos(\theta)) * K^2$$

where I is the identity matrix, theta is the misorientation angle, and K is

the skew-symmetric matrix formed by the axis of rotation:

$$K = \begin{pmatrix} 0 & -k_z & k_y \\ k_z & 0 & -k_x \\ -k_y & k_x & 0 \end{pmatrix}$$

where the vector k is the unit vector defining the axis of rotation, or using

a set of predefined rotations for each axis (default is the predefined rotations).

The Euler angles are calculated in this case simply for the file to be written

to. If the user does not specify to save, then the angles are not used for anything.

Options:

<p><i>-e —euler <_z1> <_x> <_z2></i> <i>Bunge orientation matrix</i></p>	<p><i>Returns the</i> <i>based on the</i> <i>euler angles</i> <i>provided.</i></p>
<p><i>-f —file <filename></i> <i>filename and uses the</i></p>	<p><i>Reads the file</i> <i>Euler angles</i> <i>from them to</i> <i>calculate</i> <i>the</i> <i>orientation</i> <i>matrix.</i></p>
<p><i>—rrf</i> <i>matrices using the Rodrigues</i></p>	<p><i>Calculates the</i> <i>Rotation</i> <i>Formula</i></p>
<p><i>-a —angles</i> <i>Euler angles. Can be used</i></p>	<p><i>Displays the</i> <i>in conjunction</i> <i>with -q or</i> <i>—quiet to</i> <i>display only</i> <i>the Euler</i> <i>angles.</i></p>
<p><i>-s —save</i> <i>resultant orientation matrix to</i></p>	<p><i>Saves the</i> <i>a database (</i> <i>orientation_matrix_database</i> <i>.m)</i> <i>with the</i> <i>accompanying</i> <i>Euler</i> <i>angles.</i></p>

`-q` —quiet *Suppresses
output of the orientation matrices
to the terminal*

`—help` *Displays this
help info*

Output:

*For an Euler angle set, the output is simply its
orientation matrix.
For the misorientations, the first matrix is the 'P'
' orientation matrix, and
the second matrix is the 'Q' orientation matrix (
see Bulatov et al., Acta Mater
65 (2014) 161–175).
'')*

return

```
def displayAngles(z1, x, z2): # Displays an Euler angle
    set (Bunge convention)
    print("Euler_angles:")
    # This is the "new" way to format strings. The 16
    # indicates the padding to
    # be done before the next character. The '<'
    # character below says which side
    # to pad (the right side).
    print("{:16}{:16}{:16}".format('Z', 'X', 'Z'))
    print("_____")
    print("{:<16}{:<16}{:<16}\n".format(rad2deg(z1),
        rad2deg(x), rad2deg(z2)))
    return
```

```
def check4RRF(args): # Check the args for the rrf
    command
    if "—rrf" in args:
        index = args.index("—rrf")
        del args[index]
```



```

        return True, args
    else:
        return False, args

def check4Euler(args): # Check the args for the -a or
—angles command
    if "-a" in args or "--angles" in args:
        try:
            index = args.index("-a")
        except:
            index = args.index("--angles")
        del args[index]
        return True, args
    else:
        return False, args

# Write the matrix and angles to a file
def writeMat(m, _z1, _x, _z2, grain, axis):
    # This is to avoid issues with duplicates
    if _z1 == 0:
        _z1 = abs(_z1)
    if _x == 0:
        _x = abs(_x)
    if _z2 == 0:
        _z2 = abs(_z2)

    lastVal = 1
    # This is the default filename to be used.
    # TODO: make provisions to provide the database
    file via command line
    tex_filename = "orientation_matrix_database.m"
    var_name = "%s%d"%(grain, axis) # Will generally
    look like P100 or Q100
    if not exists(tex_filename):
        tex_file = open(tex_filename, "a")
        tex_file.write("%Database_for_orientation_
matrices_for_specified_Euler_Angles\n")

```

```

tex_file.write("
%-----
n")
tex_file.write("%Orientation_Matrix-----
-----Euler_Angles\n")
tex_file.write("%s(:, :, %d)=[%2.6f__%2.6f__%2.6f
-----%%%2.4f__%2.4f__%2.4f\n"%(
var_name, lastVal, m[0][0], m[0][1], m
[0][2], _z1, _x, _z2))
tex_file.write(" %2.6f__%2.6f__%2.6f\n"%(m
[1][0], m[1][1], m[1][2]))
tex_file.write(" %2.6f__%2.6f__%2.6f];\n"%(m
[2][0], m[2][1], m[2][2]))
tex_file.write("
%-----
n")
tex_file.close()
else:
f = open(tex_filename, "r")
while True:
data = f.readline().split()
if not data:
break
elif len(data) != 6:
continue
else:
assert data[0][0] in {'P', 'Q'}, "
Unknown_orientation_matrix_type_(
should_be_\ 'P\'_or_\ 'Q\' )."
if not "%d"%(axis) in data[0][1:4]:
lastVal = 0
elif "%d"%(axis) in data[0][1:4]:
try:
try:
if data[0][0] == 'P': #
Handles anything 3
digits long

```

```

        lastVal = int(data
            [0][9:12]) - 1
    else:
        lastVal = int(data
            [0][9:12])
    except:
        if data[0][0] == 'P': #
            Handles anything 2
            digits long
            lastVal = int(data
                [0][9:11]) - 1
        else: # data[0][0] == 'Q'
            lastVal = int(data
                [0][9:11])
    except:
        if data[0][0] == 'P': # One
            digit case
            lastVal = int(data[0][9]) -
                1
        else: # data[0][0] == 'Q'
            lastVal = int(data[0][9])
    else:
        print("Error: _Unknown_last_index.")
        exit()

    # Checks to see if the Euler angles
    # have already been used before
    # If so, the calculated matrix is not
    # saved (assumed to already
    # be in the database)
    if data[0][0] == grain and data[3] == (
        '%' + "%2.4f"%_z1) and data[4] == "
        "%2.4f"%_x and data[5] == "%2.4f"%_z2
        :
        unique = False
        break
    else:
        unique = True

```

```

    if unique:
        tex_file = open(tex_filename, "a")
        tex_file.write("%s(,;, %d)=[%2.6f%%2.6f%%2.6f%%2.4f%%2.4f%%2.4f\n"
            %(var_name, lastVal + 1, m[0][0], m[0][1], m[0][2], _z1, _x, _z2))
        tex_file.write("%2.6f%%2.6f%%2.6f\n"%(m[1][0], m[1][1], m[1][2]))
        tex_file.write("%2.6f%%2.6f%%2.6f];\n"%(m[2][0], m[2][1], m[2][2]))
        tex_file.write("
            %-----
            n")
        tex_file.close()

    return

if "--help" in argv: # Help info
    displayHelp()
    exit()

orientation_matrix = []
save, argv = check4Save(argv) # Save the file? Delete
    the save argument
quiet, argv = check4Quiet(argv) # Checks for
    suppressing output. Delete the quiet argument.
useRRF, argv = check4RRF(argv) # Checks for using the
    RRF method. Delete the rrf argument.
dispEuler, argv = check4Euler(argv) # Checks for
    displaying the Euler angles. Delete the angle
    argument

# If the arguments come from a file...
if "-f" in argv or "--file" in argv: #input arguments
    come from file
    try:
        try:
            index = argv.index("-f")
        except:

```

```

        index = argv.index("--file")
except:
    print("ERROR: _Unable_to_find_filename.")
    exit()
filename = argv[index + 1]
try:
    f1 = open(filename, 'r')
except:
    print("ERROR: _Unable_to_read_file.", filename)

while True: # Read the file line by line.
    line = f1.readline()
    # break if we don't read anything. If there
    # are blank lines in the
    # file, this will evaluate to TRUE!
    if not line:
        break;
    data = line.split()
    if len(data) != 4: # If there are less than 4
        # parts to the data, move along (format of
        # file MUST be _z1 _x _z2 1.00)
        continue
    else:
        # Convert the data to stuff we can use
        _z1 = float(data[0])
        _x  = float(data[1])
        _z2 = float(data[2])

        _z1 = deg2rad(_z1)
        _x  = deg2rad(_x)
        _z2 = deg2rad(_z2)
        orientation_matrix = calcRotMat(_z1, _x,
            _z2)
        if not quiet:
            displayMat(orientation_matrix)
        if save:
            writeMat(orientation_matrix, _z1, _x,
                _z2, 'P', _axis)

```

```

# Input is a set of euler angles
elif "-e" in argv or "--euler-angles" in argv:
    try:
        try:
            index = argv.index("-e")
        except:
            index = argv.index("--euler-angles")
    except:
        print("ERROR: Unable to read Euler angles.")
        exit()
    _z1 = float(argv[index + 1])
    _x = float(argv[index + 2])
    _z2 = float(argv[index + 3])
    _z1 = deg2rad(_z1)
    _x = deg2rad(_x)
    _z2 = deg2rad(_z2)

    orientation_matrix = calcRotMat(_z1, _x, _z2)

    if not quiet:
        displayMat(orientation_matrix)
    if save:
        writeMat(orientation_matrix, _z1, _x, _z2, 'P',
            _axis)

else:
    if len(argv) < 3:
        print("ERROR: Not enough command line arguments
            .")
        print("Input either an axis, and a
            misorientation, or a ZXZ Euler angle set
            with the option -e or --euler-angles.")
        displayHelp()
        exit()
    try:
        _axis = int(argv[1])
        _misorientation = float(argv[2])

```

```

except:
    print( '''
    ERROR: Command line argument(s) is (are) not of
           correct type.
           Please enter an int for argument 1, a float for
           argument 2, and an int for argument 3.
           ''' )
    exit()

if not len(str(_axis)) == 3: # axis length greater
    than 3
    print("ERROR: _Argument_1_must_by_a_3_digit_
          number_like_\`100\`'." )
    exit()

_misorientation = deg2rad(_misorientation) # Change
        input to radians
axis = [None]*3
_z1 = [None]*2
_x = [None]*2
_z2 = [None]*2
q = [None]*2
for i in range(0, len(str(_axis))):
    axis[i] = int(str(_axis)[i])

#


---


#-----The Actual Calculations
#-----#
#


---



# First convert to a quaternion
# These functions are from a myModules.py.
q[0] = axis2quat(axis, _misorientation / 2)
q[1] = axis2quat(axis, -_misorientation / 2)

```

```

# Convert the quaternion to Euler Angles
for i in range(0, len(_z1)):
    _z1[i], _x[i], _z2[i] = quat2euler(q[i])

#

```

```

# Using the Rodrigues Rotation Formula, defined as
#  $R = I + \sin(\theta) * K + (1 - \cos(\theta)) * K^2$ 
# with  $K = [0 \ -k_z \ k_y; k_z \ 0 \ -k_x; -k_y \ k_x \ 0]$ , and the components of
#  $k$  coming from the vector being rotated about.
# Theta is specified by the misorientation.
if useRRF:
    orientation_matrix1, orientation_matrix2 =
        calcRotMatRRF(axis, _misorientation)

# Normalize the matrices using their
# determinants
orientation_matrix1 = orientation_matrix1 /
    linalg.det(orientation_matrix1)
orientation_matrix2 = orientation_matrix2 /
    linalg.det(orientation_matrix2)

if not quiet:
    displayMat(orientation_matrix1)
    displayMat(orientation_matrix2)

for i in range(0, len(_z1)):
    if dispEuler:
        displayAngles(_z1[i], _x[i], _z2[i])

    if save:
        assert i < 2, "ERROR: Too many Euler
            angles."
        if i == 0:
            writeMat(orientation_matrix1, _z1[i],
                _x[i], _z2[i], 'P', _axis)

```



```

else:
    writeMat(orientation_matrix2, _z1[i]
             ], _x[i], _z2[i], 'Q', _axis)
#

```

```

else:
    for i in range(0, len(_z1)):
        orientation_matrix = calcRotMat(_z1[i], _x[
            i], _z2[i])

        # Normalize the matrix using the
        # determinant
        orientation_matrix = orientation_matrix /
            linalg.det(orientation_matrix)

        if not quiet: # Display the results
            displayMat(orientation_matrix)

        if dispEuler: # Display the Euler Angles
            displayAngles(_z1[i], _x[i], _z2[i])

        if save: # We only calculate 2 angles at a
            time. If there are more, that's a
            problem.
            assert i < 2, "ERROR: Too many Euler
                angles."
            if i == 0:
                writeMat(orientation_matrix, _z1[i]
                     ], _x[i], _z2[i], 'P', _axis)
            else:
                writeMat(orientation_matrix, _z1[i]
                     ], _x[i], _z2[i], 'Q', _axis)

```

Appendix E

Rotation Matrix Generator

This code generates the rotation matrices used to rotate the axes to the [100] direction as required by Bulatov *et al.*'s script.

```
from __future__ import division, print_function #
    Automatically divides as floats, and considers print
    () a function
from sys import argv # for CLI arguments
from numpy import array, linalg # for matrix operations
from os.path import exists # For checking existence of
    a file
from myModules import * # For using my user-defined
    functions

# Helper functions
def displayHelp():
    print(''''
        This script will generate the rotation matrix for
        the given misorientation axis
        Input:
            _rotation_axis      This specifies the axis
            around which the grains are
            rotated. (type: int (100)
            or string ('100'))

            _gbnormal          This specifies the boundary
            plane normal. (type:
```

*int (100) or string
('100')*

Options:

*-s --save Saves the resultant
rotation matrix to a database
(rotation_matrix_database.m
) with the accompanying
rotation axis and
misorientation type.*

*-q --quiet Suppresses output of the
rotation matrix*

--help Display this help info.

Output:

*The output displayed will be the resultant rotation
matrix for the given
misorientation.
,,')*

*# This function is an adaptation from MOOSE
RotationMatrix class.*

def rotVecToZ(vec): *# Creates the rotation matrix to
rotate vec to the z direction
REALLY make sure vec is normalized
vec = vec / linalg.norm(vec)*

Initialize our vectors
v1 = array ([[0.,0.,0.]])
v0 = array ([[0.,0.,0.]])

*# Temp vector that gives a prototype of v1 by
looking at the smallest component of vec*
w = array ([[abs(vec[0][0]), abs(vec[0][1]), abs(vec
[0][2])]])
if ((w[0][2] >= w[0][1] **and** w[0][1] >= w[0][0]) **or**
(w[0][1] >= w[0][2] **and** w[0][2] >= w[0][0])):
v1[0][0] = 1.0

```

elif ( (w[0][2] >= w[0][0] and w[0][0] >= w[0][1])
        or (w[0][0] >= w[0][2] and w[0][2] >= w[0][1]) )
    :
        v1[0][1] = 1.0
else:
        v1[0][2] = 1.0

# Gram-Schmidt method to find v1
v1 = v1 - ((v1.dot(vec.T))*vec)
v1 = v1 / linalg.norm(v1)

# v0 = v1 x vec
v0[0][0] = v1[0][1]*vec[0][2] - v1[0][2]*vec[0][1]
v0[0][1] = v1[0][2]*vec[0][0] - v1[0][0]*vec[0][2]
v0[0][2] = v1[0][0]*vec[0][1] - v1[0][1]*vec[0][0]

# Rotation matrix is just:
rot = array([[v0[0][0], v0[0][1], v0[0][2]],
             [v1[0][0], v1[0][1], v1[0][2]],
             [vec[0][0], vec[0][1], vec[0][2]]])

return rot

def rotVec1ToVec2(vec1, vec2):
    rot1_to_z = rotVecToZ(vec1)
    rot2_to_z = rotVecToZ(vec2)
    return (rot2_to_z.T).dot(rot1_to_z)

def writeMat(m, _axis, gbnormal): # Write the matrix
and angles to a file
    tex_filename = "rotation_matrix_database.m"
    normName = _axis + '_' + gbnormal
    var_name = "rot%snorm"%(normName)
    if not exists(tex_filename):
        tex_file = open(tex_filename, "a")
        tex_file.write("%Database_for_rotation_matrices
        _for_specified_misorientation_axes\n")
        tex_file.write("
        %

```

```

        n")
    tex_file.write("%Rotation_Matrix\n")
    tex_file.write("%s=[%2.4f_%2.4f_%2.4f\n"%(
        var_name, m[0][0], m[0][1], m[0][2]))
    tex_file.write("%2.4f_%2.4f_%2.4f\n"%(m
        [1][0], m[1][1], m[1][2]))
    tex_file.write("%2.4f_%2.4f_%2.4f];\n"%(m
        [2][0], m[2][1], m[2][2]))
    tex_file.write("
%
n")
    tex_file.close()
else:
    # Check for already written
    numlines = countFileLines(tex_filename)
    if numlines <= 4:
        tex_file = open(tex_filename, "a")
        tex_file.write("%s=[%2.4f_%2.4f_%2.4f\n"
            % (var_name, m[0][0], m[0][1], m[0][2]))
        tex_file.write("%2.4f_%2.4f_%2.4f\n"%(m
            [1][0], m[1][1], m[1][2]))
        tex_file.write("%2.4f_%2.4f_%2.4f];\n"%(m
            [2][0], m[2][1], m[2][2]))
        tex_file.write("
%
n")
        tex_file.close()
    else:
        f = open(tex_filename, "r")
        while True:
            data = f.readline().split()
            if not data:
                break
            elif len(data[0]) > 14:
                if not data[0][14] == '=':
                    continue
            else:
                if data[0][0:10] == var_name:

```

```

        unique = False
    else:
        unique = True
    if unique:
        tex_file = open(tex_filename, "a")
        tex_file.write("%s=[%2.4f_ _%2.4f_ _%2.4f\n"
            \n"%(var_name, m[0][0], m[0][1], m
            [0][2]))
        tex_file.write("%2.4f_ _%2.4f_ _%2.4f\n"
            \n"%(m[1][0], m[1][1], m[1][2]))
        tex_file.write("%2.4f_ _%2.4f_ _%2.4f\n";\n"
            \n"%(m[2][0], m[2][1], m[2][2]))
        tex_file.write("
            %
            n")
        tex_file.close()

# Check what we were given...
if "--help" in argv: # Help info
    displayHelp()
    exit()

save, argv = check4Save(argv)
quiet, argv = check4Quiet(argv) # Checks for
    suppressing output

if len(argv) != 3: # if not both values given
    print("ERROR: _Incorrect_number_of_command_line_
        arguments._Line_150")
    displayHelp()
    exit()
else: # len(argv) == 3
    script, _rotation_axis, _gbnormal = argv

if not type(_gbnormal) in {int, str}:
    print("ERROR: _Grain_boundary_normal_type_is_
        incorrect._Please_enter_an_int_or_a_string._
        Line_157")

```

```

    print("You entered %s with type %s"%(str(_gbnormal)
        , type(_gbnormal)))
    exit()
else:
    if type(_gbnormal) == int:
        _gbnormal = '0' + '0' + '0' + str(_gbnormal)
        _gbnormal = _gbnormal[-3:] # gets the last three
            characters
        assert _gbnormal != '000', "ERROR: invalid _
            boundary_normal. Line 173"

    assert(len(_rotation_axis) == 3), "ERROR: Something
        went wrong converting _gbnormal into a string.
        Line 166"

    if not type(_rotation_axis) in {int, str}:
        print("ERROR: Grain boundary rotation axis type is
            incorrect. Please enter an int or a string.
            Line 169")
        print("You entered %s with type %s"%(str(
            _rotation_axis), type(_rotation_axis)))
        exit()
    else: # Convert anything besides a string into a string
        if type(_rotation_axis) == int:
            _rotation_axis = '0' + '0' + '0' + str(
                _rotation_axis)
            _rotation_axis = _rotation_axis[-3:] # Get the
                last three characters
            assert _rotation_axis != '000', "ERROR: invalid
                _rotation_axis. Line 176"

        assert(len(_rotation_axis) == 3), "ERROR: Something
            went wrong converting _rotation_axis into a
            string. Line 178"

# Now that the input is taken care of, do the work
axis = array([1, 0, 0]) # This is the axis that we
    rotate the grain boundary normal to

```

```

# This part converts _gbnormal to an array for use in
  the rotation functions
gbnormal = array ([[None]*3])
j = 0
indices = []
for i in range(0, len(gbnormal[0])):
    try:
        gbnormal[0][i] = int(_gbnormal[j])
        j = j+1
    except:
        #print(_gbnormal[i:i+2])
        gbnormal[0][i] = int(_gbnormal[j:j + 2])
        j = j + 2
        indices.append(i)

# So much work...
gbnorm = ''
for i in range(0, len(gbnormal[0])):
    if gbnormal[0][i] < 0:
        gbnorm += str(abs(gbnormal[0][i])) + 'bar'
    else:
        gbnorm += str(gbnormal[0][i])
gbnormal = gbnorm / linalg.norm(gbnorm) # Normalize
  the gbnorm vector.
axis = axis / linalg.norm(axis) # Just to be sure...
rotation_matrix = rotVec1ToVec2(gbnorm, axis)

if not quiet:
    displayMat(rotation_matrix)
if save:
    writeMat(rotation_matrix, _rotation_axis, gbnorm)

```


Appendix F

genOrientationMatrix.sh Bash Script

This bash script reads a CSV file containing misorientation angles data, and uses those angles to generate the P and Q matrices. This script calls the script orientation_matrix.py.

```
#!/bin/bash

# This script will generate the orientation matrices
# through python by looping
# through the CSV values given in the input files.
# Argument(s):
#   $1          Should be a filename that specifies the
#               angles and relative
#               energies for the 100, 110, and 111
#               symmetric tilt and twist
#               boundaries

# Command-line argument counter that checks for the
# correct number of arguments.
# Does not check for correct syntax.
if [ "$#" -ne 1 ]; then
    echo "Illegal number of parameters"
    exit 1
fi
```

```

# This takes the first argument from the command line -
# this is assumed to be a
# filename of the format 100Tilt.
FN=$1

echo "Determining_the_axis..."
# Pulls out the axis from the input file name. This
# uses regex syntax to find
# a series of numbers that match either 100, 110, or
# 111. This also has an issue
# where it will find a match for 101, but as long as
# the files are named correctly
# it shouldn't be an issue.
AXIS='echo $FN | grep -o "1[01][01]" '

echo "Reading_the_file..."
IFS="," # separation character is the comma
# Exit with error code 99 if unable to read the file
[ ! -f $FN ] && { echo "$FN_file_not_found"; exit 99; }

# This makes the assumption that the file
# orientation_matrix.py has executable
# rights.
echo "Running_the_command: ~/projects/scripts/
orientation_matrix.py_$AXIS_<angle>_s_q"
while read -r angle en; do # read the file with comma
separated values

~/projects/scripts/orientation_matrix.py $AXIS $angle
-s -q
done < "$FN" # the "$FN" is required if it's going to
run properly!

IFS=$OLDIFS # go back to the old separation character
based on the system value.

```