

$$\dot{x}_1 = x_2 - x_1^3$$

$$\dot{x}_2 = -x_1 - x_2^3$$

$$\text{let } V = \frac{1}{2} (x_1^2 + x_2^2)$$

$$\dot{V} = x_1 \dot{x}_1 + x_2 \dot{x}_2$$

$$= x_1 x_2 - x_1^4 + -x_2 x_1 - x_2^4$$

$$= -x_1^4 - x_2^4$$

$$\dot{V} < 0 \quad \text{in } \mathbb{R} - \{0\}$$

\Rightarrow Asymptotically stable (And is in fact Globally asymptotically stable)