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In[705]:= Clear[coord, L, nPart, dt, dx, k, s, xPos,
           u0, myTemp, uTemp, rightT, leftT, lastT, newT, newT];

L := 1 (*Length of rod *)
nPart := 10 (*Number of partitions *)
nTsamples := 100 (*Number of time samples*)
tTime := 10 (*How much time*)
dt := tTime / nTsamples (*Time interval size  $\Delta t$ *)
dx := L / nPart (*Section size  $\Delta x$ *)
k := 1 (*k value*)
(*s=k*dt/(dx^2)*) (*s constant*)
s = 0.50
(*Interesting to note that forcing various *)
(*values on s affects the stability of the solution*)

(*Here I define a function for the initial temperature distribution f0=f(x)*)

(*f0[x_] := Abs[Sin[6x]]+.2*)

f0[x_] := Piecewise[{{0, x >= 0 && x < 0.5 L},
                    {(x - 0.5 L) / L, x >= 0.5 L && x < 0.75 L}, {(0.75 L - x) / L + 0.25, x >= 0.75 L && x <= L}}]

(*Here is where I define the initial conditions at t=0*)
(*so u(x,0)=the function f0=f(x) acting on the xpos*)
xPos := (Range[nPart] - 1) * dx

(*This includes the very end of the rod*)
AppendTo[xPos, dx * nPart];

(*the symbol /@ maps the function onto xpos*)
u0 := f0 /@ xPos

(*Initialize the empty u temperature list, these are*)
(*our sample solution points*)
uTemp := {}

(*At t=1 we have our u0 list of temps*)
uTemp = Append[uTemp, u0];

(*This nested for loop sequence calculates the temps at time*)
(*t by using the difference equation on page 226 of the book*)
(*this is also the same one we derived in class*)

(*The outer loop only starts at t=2 because at t=1 this is t0 with*)
(*initial temp of u0 which we append before the loop*)
For[t = 2, t <= nTsamples, t++,

  (*Initialize an empty temporary list*)
  myTemp := {};

  (*This loop is where we go through each x and calculate*)
  (*u(x,t), where t is from the outer loop*)
  For[k = 1, k <= nPart + 1, k++, (*Remember we added the end*)
    lastT = uTemp[[t - 1, k]]; (*so we need to go nPart+1*)

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(*if we are at start position x0 or in this case x1*)
If[k == 1, rightT = 0;
  leftT = uTemp[[t - 1, k + 1]]];

(*if we reach the end of the rod*)
If[k == nPart + 1, leftT = 0; rightT = uTemp[[t - 1, k - 1]]];

(*if we are inside rod*)
If[k > 1 && k < nPart + 1,
  rightT = uTemp[[t - 1, k - 1]];
  leftT = uTemp[[t - 1, k + 1]]
];

(*This is the relationship: u[j][m+1]=u[j][m]...from page 226*)
newT = lastT + s * (leftT - 2 * lastT + rightT);

(*append temperatures to temporary list we started with*)
myTemp = Append[myTemp, newT];
];

(*append the temp list to our uTemp list which we began before*)
(*the outer loop*)
uTemp = Append[uTemp, myTemp];
];

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Out[713]= 0.5

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In[721]:= (*Here we define individual frames representing the solution*)
(*at different times of t*)

(*Initialize an empty frame list, we will collect the frames*)
frames := {}

(*We need to get the coordinates of the xpos and utemp at*)
(*those xpos at time t here I accidentally used the letter k instead*)
For[k = 1, k ≤ nTsamples, k++,
  coord := {};

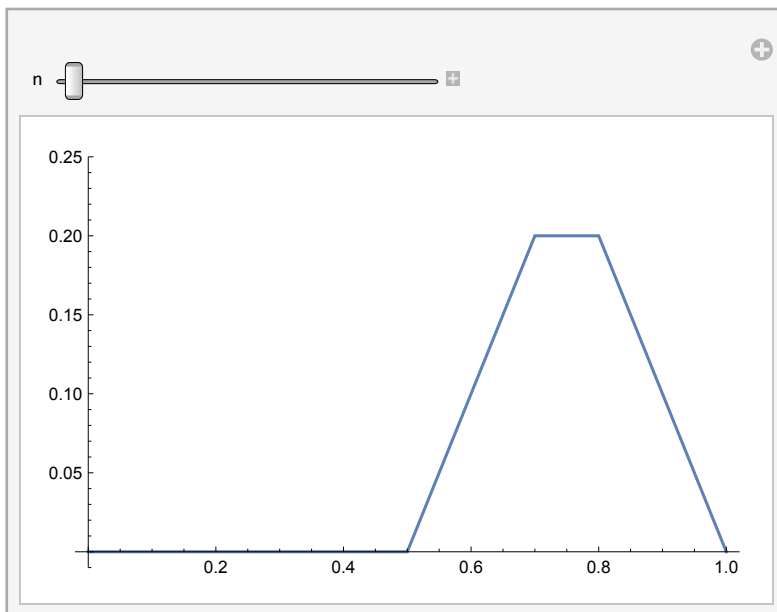
  For[i = 1, i ≤ nPart + 1, i++,
    coord = Append[coord, {xPos[[i]], uTemp[[k, i]]}];
  ];

  tempframe := ListLinePlot[coord, PlotRange → {-0.01, 0.25}];
  frames = Append[frames, tempframe];
];

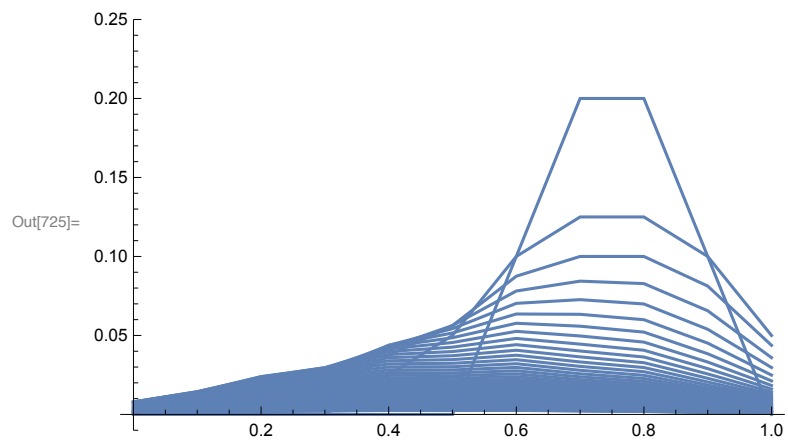
(*Try manipulating the plot*)
Manipulate[Show[frames[[n]]], {n, 1, nTsamples, 1}]

```

Out[723]=



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(*Here are the snapshots of the solution*)  
myTablePlot = Table[Graphics[frames[[n]]], {n, 1, nTsamples, 2}];  
Show[myTablePlot]
```



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In[726]:= (*This will generate a contour and 3d plot overlayed together*)
coord := {};

For[t = 1, t ≤ nTsamples, t++,
  For[i = 1, i ≤ nPart + 1, i++,
    coord = Append[coord, {xPos[[i]], (t - 1) * dt, uTemp[[t, i]]}];
  ];
];

ctPlot = ListContourPlot[coord, ColorFunction -> "Rainbow"];
listPlot = ListPlot3D[coord, ColorFunction -> "Rainbow", PlotRange -> {- .01, 0.25}];

level = -0.01;
gr = Graphics3D[{Texture[ctPlot], EdgeForm[], Polygon[{0, 0, level}, {L, 0, level},
  {L, tTime, level}, {0, tTime, level}], VertexTextureCoordinates ->
  {{0, 0}, {1, 0}, {1, 1}, {0, 1}}], Lighting -> {{ "Ambient", White}}];

Show[listPlot, gr, PlotRange -> {- .01, 0.21}, BoxRatios -> {1, 1, 1}]
(*Notice that the plot somewhat jagged on some
  of the contours starting to become unstable! for s = 0.50*)

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