

```

In[345]:= Clear[a, b, c, n, m, f, g, K, L, x, y];
k := 0.5
L := 10
H := 10
nTerms := 10
tVal := {0, 0.1, 0.2, 1, 10, 25, 50, 100, 500}
f[x_, y_] := Piecewise[{{1, 4 < x < 6 && 4 < y < 6}, {0, x ≤ 4 && x ≥ 6 && y ≤ 4 && y ≥ 6}}]

lambda[m_, n_] :=  $\left(\frac{\pi m}{H}\right)^2 + \left(\frac{\pi n}{L}\right)^2$ 

phi[x_, n_] := Sin $\left[\frac{\pi n x}{L}\right]$ 

psi[y_, m_] := Sin $\left[\frac{\pi m y}{H}\right]$ 

ht[t_, m_, n_] := ek t (-lambda[m,n])

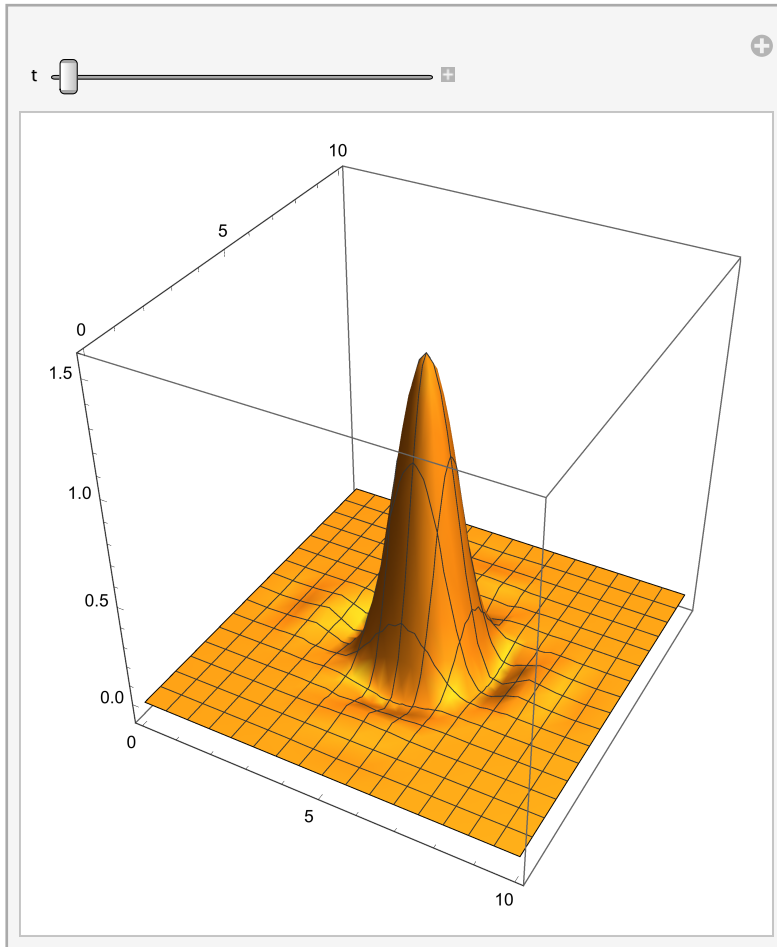
Cmn[m_, n_] := 
$$\frac{4 \int_0^L \text{phi}[x, n] \int_0^H f[x, y] \text{psi}[y, m] \, dy \, dx}{H L}$$


u[x_, y_, t_, M_, N_] := 
$$\sum_{m=1}^M \left( \sum_{n=1}^N \text{Cmn}[m, n] \text{psi}[y, m] \text{phi}[x, n] \text{ht}[t, m, n] \right)$$


z[x_, y_, t_] := Evaluate[u[x, y, t, nTerms, nTerms]]

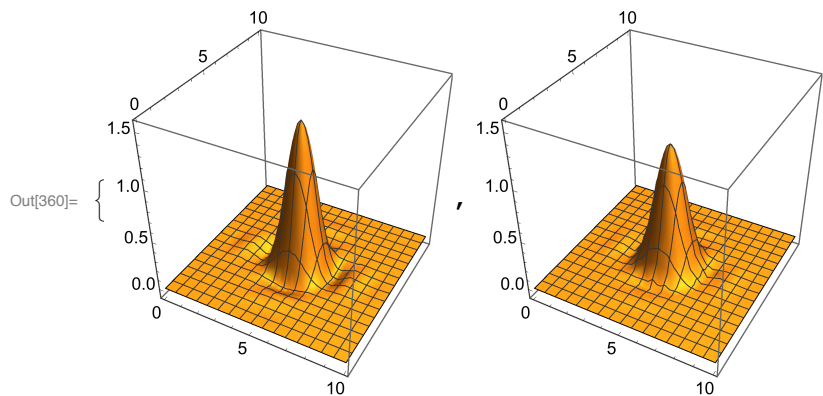
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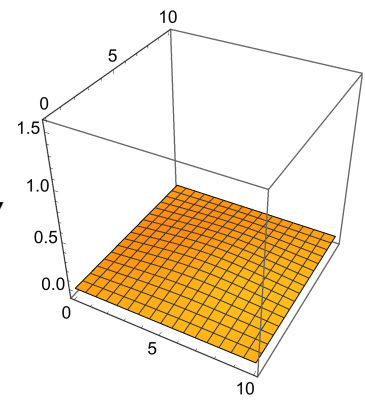
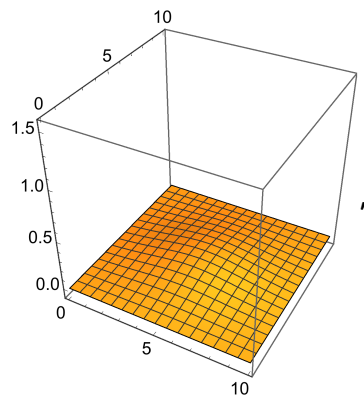
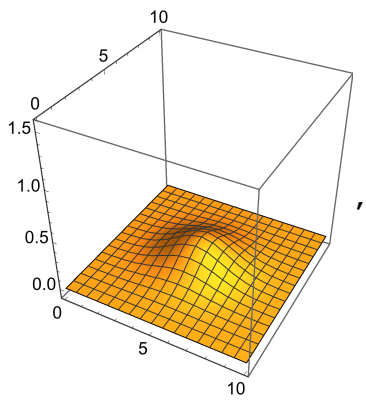
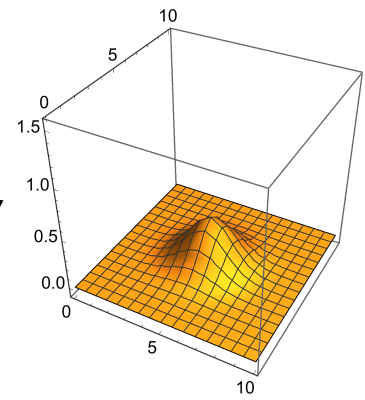
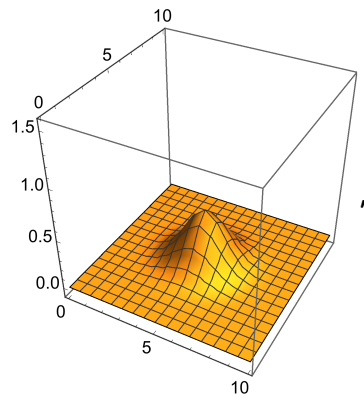
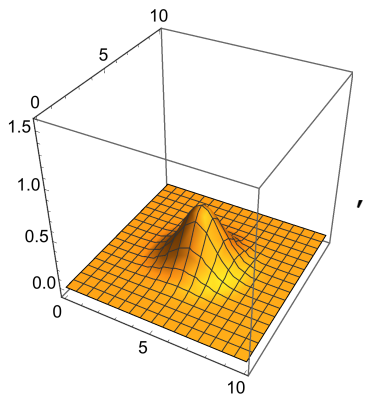
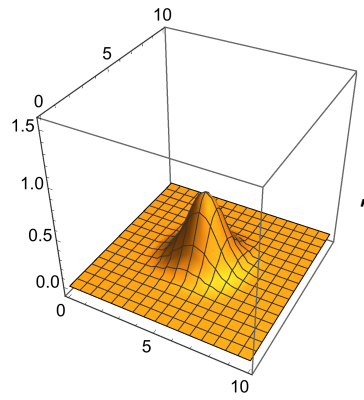
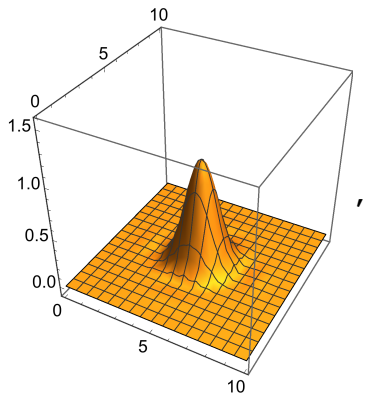
```
Manipulate[Plot3D[z[x, y, t], {x, 0, L}, {y, 0, H},
  BoxRatios -> {1, 1, 1}, PlotRange -> {-0.1, 1.6}], {t, 0, 10, .5}]
```

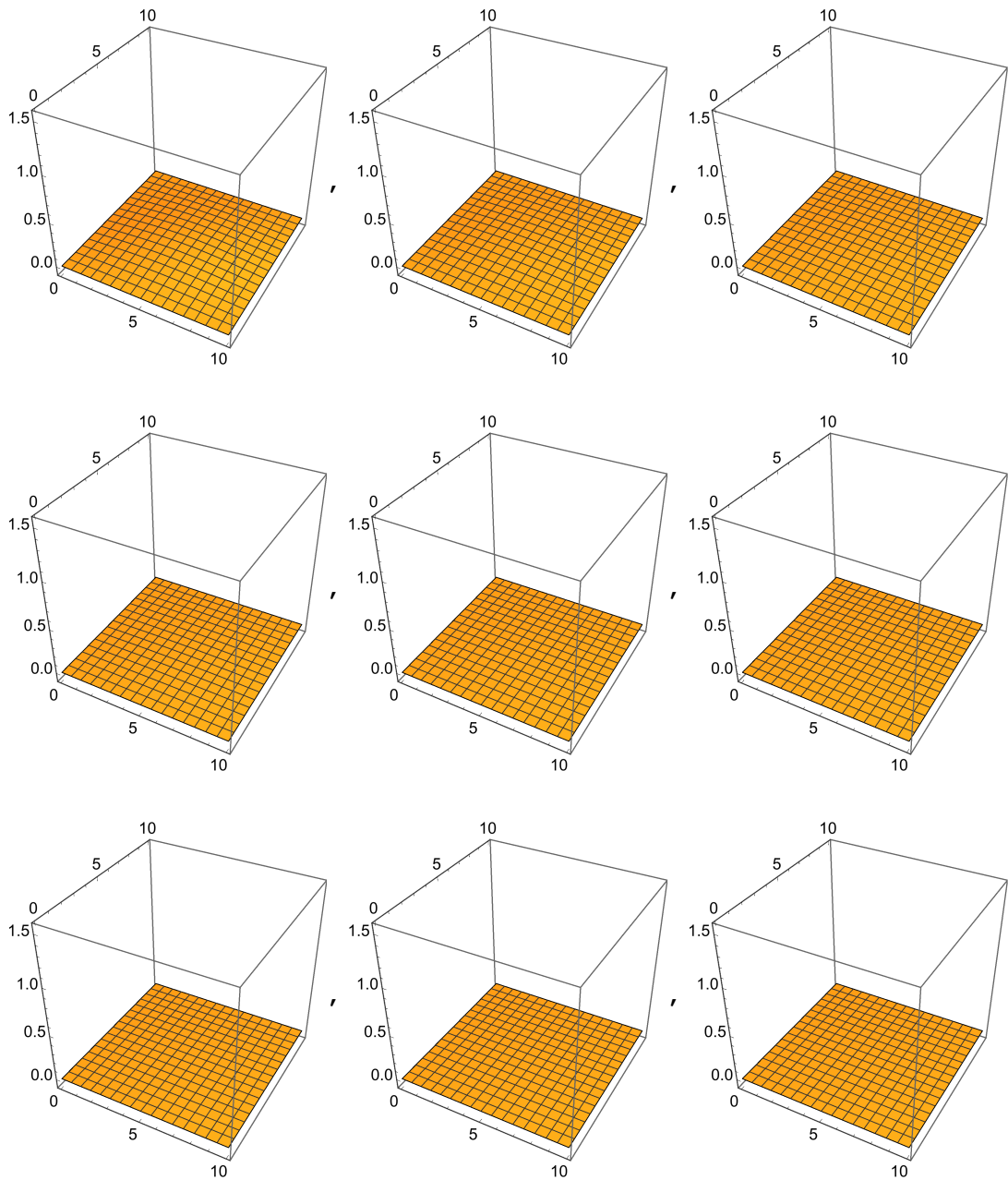


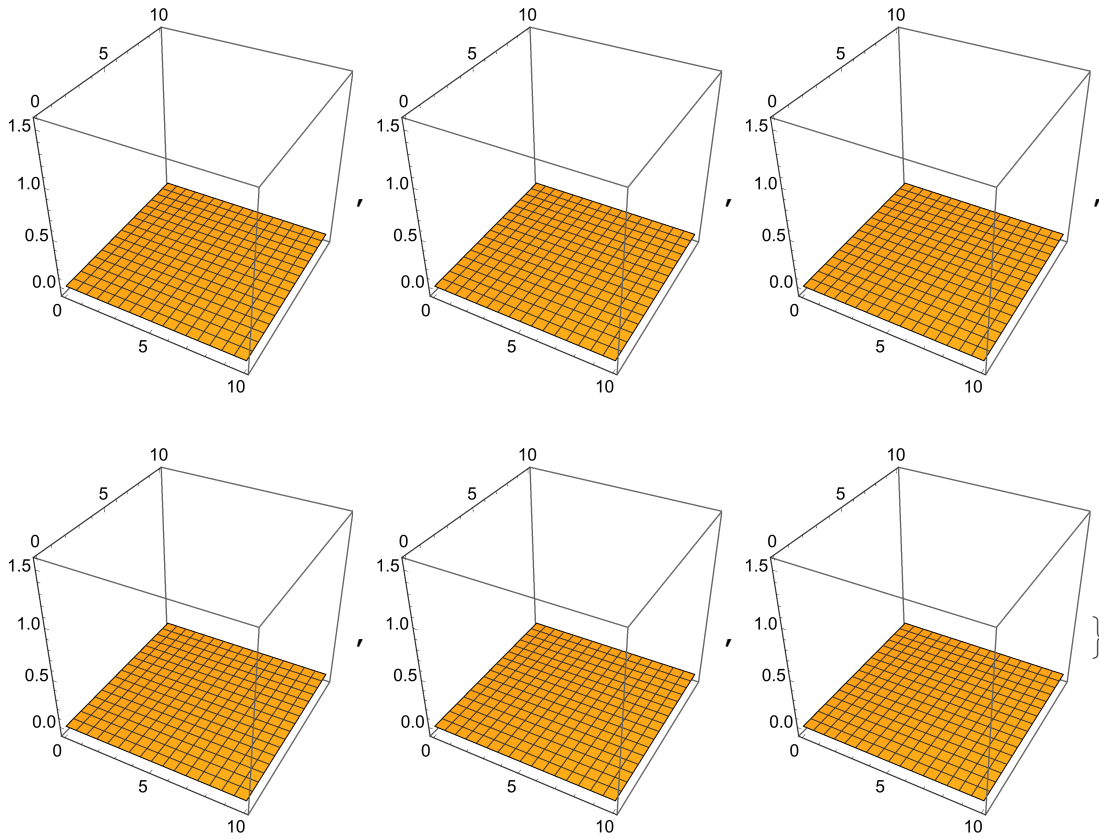
```
In[359]:= tplot := Table[Plot3D[z[x, y, t], {x, 0, L}, {y, 0, H}, BoxRatios -> {1, 1, 1},
  PlotRange -> {-0.1, 1.6}], {t, {0, 0.1, 0.2, 0.5, 0.7, 0.8, 1, 2, 5,
  8, 10, 15, 20, 25, 30, 35, 40, 45, 50, 60, 70, 80, 90, 100, 500}}]
```

tplot









```
In[361]:= Manipulate[ContourPlot[z[x, y, t], {x, 0, L},
  {y, 0, H}, BoxRatios -> {1, 1, 1}, PlotRange -> {-0.1, 1.6},
  ColorFunction -> "TemperatureMap", PlotPoints -> 20], {t, 0, 10, .1}]
```

Out[361]=

