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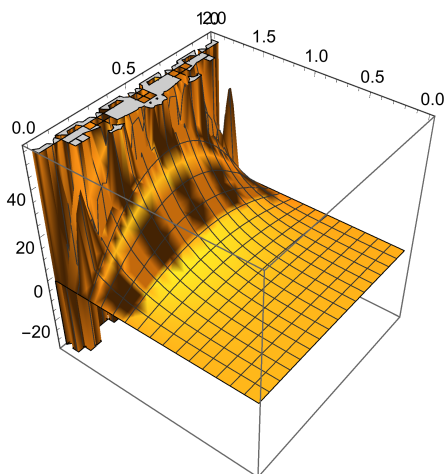
In[331]:= Clear[u, phi, psi, z, y, a, b, c, d, n, x, L, f, g]
L := 1
H := 2
nTerms := 10
f[x_] := x (1 - x)
g[x_] := 100
c[n_] := 
$$\frac{2 \int_0^L f[x] \sin\left[\frac{\pi n x}{L}\right] dx}{L}$$

d[n_] := 
$$\frac{\frac{2 \int_0^L g[x] \sin\left[\frac{\pi n x}{L}\right] dx}{L} - c[n] \cosh\left[\frac{\pi H n}{L}\right]}{\sinh\left[\frac{\pi H n}{L}\right]}$$

phi[x_, n_] :=  $\sin\left[\frac{\pi n x}{L}\right]$ 
psi[y_, n_] := c[n]  $\cosh\left[\frac{\pi n y}{L}\right]$  + d[n]  $\sinh\left[\frac{\pi n y}{L}\right]$ 
u[x_, y_, M_] :=  $\sum_{n=1}^M (\phi[x, n] \psi[y, n])$ 
z[x_, y_] := Evaluate[u[x, y, nTerms]]
z[x, y];
Plot3D[z[x, y], {x, 0, L}, {y, 0, H}, BoxRatios -> {1, 1, 1}]

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Out[344]=



$$\begin{aligned}
 & \sin[\pi x] \left( \frac{8 \cosh[\pi y]}{\pi^3} + \left( \frac{400}{\pi} - \frac{8 \cosh[2\pi]}{\pi^3} \right) \operatorname{csch}[2\pi] \sinh[\pi y] \right) + \\
 & \sin[3\pi x] \left( \frac{8 \cosh[3\pi y]}{27\pi^3} + \left( \frac{400}{3\pi} - \frac{8 \cosh[6\pi]}{27\pi^3} \right) \operatorname{csch}[6\pi] \sinh[3\pi y] \right) + \\
 & \sin[5\pi x] \left( \frac{8 \cosh[5\pi y]}{125\pi^3} + \left( \frac{80}{\pi} - \frac{8 \cosh[10\pi]}{125\pi^3} \right) \operatorname{csch}[10\pi] \sinh[5\pi y] \right) + \\
 & \sin[7\pi x] \left( \frac{8 \cosh[7\pi y]}{343\pi^3} + \left( \frac{400}{7\pi} - \frac{8 \cosh[14\pi]}{343\pi^3} \right) \operatorname{csch}[14\pi] \sinh[7\pi y] \right)
 \end{aligned}$$

