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CHAPTER

Fully Spatial Capture-Recapture Models

p0005 In the previous chapter, we discussed models that could be viewed as primitive spatial capture-recapture models. We looked at a basic distance sampling model, and we also considered a lossical individual covariate modeling approach in which we defined a covariate to be the distance from the (estimated) home range center to the center of the trap array. The individual covariate model that we conjured up was "spatial" in the sense that it included some characterization of where individuals live but, on the other CAN hand, only a primitive or no characterization of trap location. That said, there is only a small step from this model to spatial capture-recapture models that we consider in this chapter, which fully recognize the spatial attribution of both individual animals and the locations of encounter devices.

Capture-recapture models must accommodate the spatial organization of individuals and the encounter devices because the encounter process occurs at the level of Ceruma individual traps. Failure to consider the trap-specific data is one of the key deficiencies with classical ad hoc approaches which aggregate encounter information to the resolution of the entire trap array. We have previously addressed some problems that counce this causes including induced heterogeneity in encounter probability, imprecise notation of "sample area," and not being able to accommodate trap-specific effects or trap-specific missing values. In this chapter we resolve these issues by developing our first fully spatial capture-recapture model. This model is not too different from counce that considered in Section 4.5 but instead of defining the individual covariate to be Commo distance to the centroid of the array we define J individual covariates—the distance to each trap. And, instead of using estimates of individual locations s, we consider a fully hierarchical model in which we regard s as a latent variable and impose a prior distribution on it

In this chapter we investigate the basic spatial capture-recapture model, which we refer to as "model SCR0," and address some important considerations related to its analysis in BUGS. We demonstrate how to summarize posterior output for the purposes of producing density maps or spatial predictions of density. The key aspect of the SCR models considered in this chapter is the formulation of a model for encounter probability that is a function of distance between individual home range center and trap locations. We also discuss how encounter probability models are related to explicit models of space usage or "home range area," Understanding this allows us to compute, for example, the area used by an individual during some

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CHAPTER 5 Fully Spatial Capture-Recapture Models

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prescribed time. While it is intuitive that SCR models should be related to some model of space usage, this has not been discussed much in the literature (but see Royle et at. (2012a) which we address further in Chapter 13).

Sampling design and data structure

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In our development here, we will assume a standard sampling design in which an array of J traps is operated for K sample occasions (say, nights) producing encounters of n individuals. Because sampling occurs by traps and over time, the most general data structure yields temporally and spatially indexed encounter histories for each individual. Thus a typical data set will include an encounter history matrix for each individual indicating which trap the individual was captured during each sample occasion. For example, suppose we sample at 4 traps over 3 nights. A plausible data set for a single individual captured one time in trap 1 on the first night and one time

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in trap 3 on the third night is:

	night1	night2	night3
trap1	1.	0	O
trap2	0	0	Ŏ
trap3	0	0	1
trap4	0	G.	0

This data structure would be obtained for each of the i = 1, 2, ..., n captured individuals.

We develop models in this chapter for passive detection devices such as "hair poors snares" or other DNA sampling methods (Kéry et al., 2010; Gardner et al., 2010b) and related types of sampling devices in which (i) devices ("traps") may capture any number of individuals (i.e., they don't fill up); (ii) an individual may be captured in more than one trap during each occasion but (iii) individuals can be encountered at most 1-time by each trap during any occasion. Hair snares for sampling DNA from bears and other species function according to these rules. An individual bear wandering about its territory might come into contact with >1 devices; a device may encounter multiple bears; however, in practice, it will often not be possible to attribute multiple visits of the same individual during a single occasion (e.g., night) to distinct encounter events. Thus, an individual may be captured at most 1 time in each trap during any occasion. While this model, which we refer to as SCRO, is most directly relevant to hair snares and other DNA sampling methods for which multiple detections of an individual are not distinguishable, we will also make use of the model for data that arise from camera trapping studies. In practice, with camera trapping, individuals might be photographed several times in a night but it is common to distill such data into a single binary encounter event for reasons discussed later in Chapter 9.

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The statistical assumptions we make to build a model for these data are that individual encounters within and among traps are independent, and this allows us to

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regard individual and trap-specific encounters as independent Bernoulli trials (see next section). These basic (but admittedly at this point somewhat imprecise) assumptions define the basic spatial capture-recapture model, SCRO. We will make things more precise as we develop a formal statistical definition of the model shortly.

5.2 The binomial observation model

We begin by considering the simple model in which there are no time-varying covariates that influence encounter, there are no explicit individual-specific covariates, and there are no covariates that influence density. In this case, we can aggregate the binary encounters over the K sample occasions and record the total number of encounters out of K. We will denote these individual and trap-specific encounter frequencies by y_{ij} for i = 1, 2, ..., n captured individuals and j = 1, 2, ..., J traps. For example, suppose we observe six individuals in sampling at 4 traps over 3 nights of sampling then a plausible data set is the 6 × 4 matrix of encounters (out of 3 sampling occasions) shown in Table 5.1. We assume that y_{ij} are mutually independent outcomes of ('emma a binomial random variable, which we express as.

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$$y_{ij} \sim \text{Binomial}(K, p_{ij}).$$
 (5.2.1)

This is the basic model underlying standard closed population models (Chapter 4) except that, in the present case, the encounter frequencies are individual and trapspecific, and encounter probability p_{ij} depends on both individual and trap.

As we did in Section 4.5, we will make explicit the notion that p_{ij} is defined conditional on where individual i lives. Naturally, we think about defining an individual home range and then relating pij explicitly to a summary of its location relative to each trap. For example, the centroid of the individual's home range, or its center of activity (Efford, 2004; Borchers and Efford, 2008; Royle and Young, 2008). In what follows, we define si, a two-dimensional spatial coordinate, to be the home range or activity center of individual i. Then, the SCR model postulates that encounter probability, p_{ij} , is a decreasing function of distance between s_i and the location of trap f, x_i

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Table 5.1 Hypothetical spatial capture-recapture data set showing 6 individuals captured in 4 traps. Each entry is the number of captures out of K=3nights of sampling

individual: 1	1	^	THE HE TOTAL THE SECURITY SE	Carrieran Alegaria
2	ò	9	0	Ü
3	ő	ō	0	1
ļ	0	1	ō	ó
j	0	0	1	í
,	,1 (. 0 ,	1	0

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(also a two-dimensional spatial coordinate). A standard model for modeling binomial counts is the logistic regression, where we model the dependence of p_{ij} on distance according to: express

$$logit(p_{ij}) = \alpha_0 + \alpha_1 \|\mathbf{x}_j - \mathbf{s}_i\|, \qquad (5.2.2)$$

where there $\|\mathbf{x}_j - \mathbf{s}_i\|$ is the distance between \mathbf{s}_i and \mathbf{x}_j . We sometimes write $\|\mathbf{x}_j - \mathbf{s}_i\|$ $|\mathbf{s}_i|| = \operatorname{dist}(\mathbf{x}_j, \mathbf{s}_i) = d_{ij}$. Alternatively, a popular model is

$$p_{ij} = p_0 \exp\left(-\frac{1}{2\sigma^2} \|\mathbf{x}_j - \mathbf{s}_i\|^2\right),$$
 (5.2.3)

which is similar to the "half-normal" model in distance sampling, except with an country intercept $p_0 \le 1$ which can be estimated in SCR studies. Because it is the kernel of a bivariate normal, or Gaussian, probability density function for the random variable "individual location" we will refer to it as the "(bivariate) normal" or "Gaussian" model although the distance sampling term "half-normal" is widely used. In the context of two-dimensional space, the model is clearly interpretable as a primitive model of movement outcomes or space usage (we discuss this in Section 5.4).

There are a large number of standard detection models commonly used (see Chapter 7). All other standard models that relate encounter probability to s will also have a parameter that multiplies distance in some non-linear function. To be consistent with parameter naming across models, we will sometimes parameterize any encounter probability model so that the coefficient on distance (or distance squared) is α_1 . So, for the Gaussian model, $\alpha_1 = 1/(2\sigma^2)$. A characteristic of the common parametric forms is they are monotone decreasing with distance, but vary in their characteristicbehavior as they approach distance = 0. We show the standard Gaussian, Gaussian hazard, negative exponential, and logistic models in Figure 5.1. The negative exponential model has $p_{ij} = p_0 \exp(-\alpha_1 ||\mathbf{x}_j - \mathbf{s}_i||)$ and the Gaussian hazard model has $p_{ij} = 1 - \exp(-\lambda_0 k(\mathbf{x}_j, \mathbf{s}_i))$ where $k(\mathbf{x}_j, \mathbf{s}_i)$ is the Gaussian kernel. Whatever model we choose for encounter probability, we should always keep in mind that the activity center for individual i, s_i , is an unobserved random variable. To be precise about this in the model, we should express the observation model as

 $y_{ij}|\mathbf{s}_i \sim \text{Binomial}(K, p(\mathbf{s}_i; \alpha_1))$

but sometimes, for notational simplicity, we abbreviate this by omitting some of the arguments to p.

5.2.1 Definition of home range center

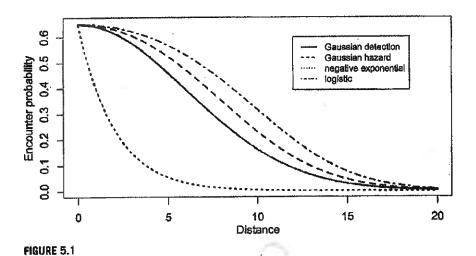
We define an individual's home range as the area used by an organism during some time period which has a clear meaning for most species regardless of their biology. We therefore define the home range center (or activity center) to be the center of the space that individual was occupying (or using) during the period in which traps were active. Thinking about it in that way, it could even be observable (almost) as the centroid of a very large number of radio fixes over the course of a survey period

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Some common encounter probability models showing the characteristic monotone decrease of encounter probability with distance between activity center and trap location.

or a season. Thus, this practical version of a home range center in terms of space usage is a well-defined construct regardless of whether one thinks the home range itself is a meaningful concept. We use the terms home range center and activity center interchangeably, and we recognize that this is a transient thing which applies only to a well-defined period of study.

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5.2.2 Distance as a latent variable

If we knew precisely every s_i in the population (and population size N), then the model specified by Eqs. (5.2.1) and (5.2.2) would be just an ordinary logistic regression type of a model (with covariate d_{ij}) which we learned how to fit using WinBUGS previously (Chapter 3). However, the activity centers are unobservable even in the best possible circumstances. In that case, d_{ij} is an unobserved variable, analogous to the situation in classical random effects models. We need to therefore extend the model to accommodate these random variables with an additional model component—the random effects distribution. The customary assumption is the so-called "uniformity assumption," which is to assume that the s_i are uniformly distributed over space (the obvious next question: "which space?" is addressed below). This uniformity assumption amounts to a uniform prior distribution on s_i , i.e., the pdf of s_i is constant, which we may express

 $Pr(s_i) \propto constant.$ (5.2.4)

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As it turns out, this assumption is usually not precise enough to fit SCR models in practice for reasons we discuss shortly. We will give another way to represent this

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prior distribution that is more concrete, but depends on specifying the "state-space" of the random variable s_i . The term state-space is a technical way of saying "the space of all possible outcomes" of the random variable.

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5.3 The binomial point process model

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In the SCR model, the individual activity centers are unobserved and thus we treat them as random effects. Specifically, the collection of individual activity centers s_1, \ldots, s_N represents a realization of a binomial point process (filian et al., 2008, p. 61). The binomial point process (BPP) is analogous to a Poisson point process in the sense that it represents a "random scatter" of points in space—except that the total number of points is fixed, whereas, in a Poisson point process, it is random (having a Poisson distribution). As an example, we show in Figure 5.2 locations of 20 individual activity centers (black dots) in relation to a grid of 25 traps. For a Poisson point process the number of such points in the prescribed state-space would be random whereas often we will simulate fixed numbers of points, e.g., for evaluating the performance of procedures, e.g., how well does our estimator perform when N = 50?

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It is natural to consider a binomial point process in the context of capture-recapture models because it preserves N in the model and thus preserves the linkage directly with closed population models. In fact, under the binomial point process model, model

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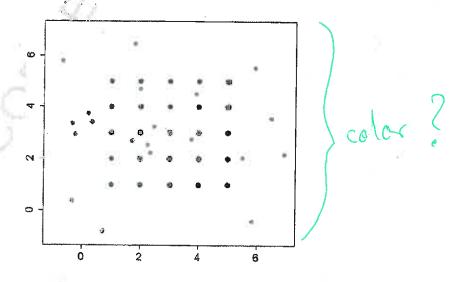


FIGURE 5.2

Realization (small dots) of a binomial point process with N = 20. The large dots represent trap locations.

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5.3 The Binomial Point Process Model

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M₀ and other closed models are simple limiting cases of SCR models, i.e., they arise as the coefficient on distance (α_1 above) tends to 0.

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While we often will express SCR models "conditional-on-N," it will sometimes be convenient to impose specific prior distributions on N. By assuming N has a binomial distribution, we can make use of data augmentation, our preferred tool, for Bayesian analysis of the models as in Chapter 4, thus yielding a methodologically coherent approach to analyzing the different classes of models. We might also assume that N has a Poisson distribution in some cases (see Chapter 14). Of course, the two assumptions are closely related in the usual limiting sense.

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One consequence of having fixed N in the BPP model is that the model is not strictly a model of "complete spatial randomness." This is because, if one forms counts $n(A_1), \ldots, n(A_k)$ in any set of disjoint regions of the state-space, say A_1, \ldots, A_k , then these counts are not independent. In fact, they have a multinomial distribution (see Illian et al., 2008, p. 61). Thus, the BPP model introduces a slight bit of dependence in the distribution of points. However, in most situations this will have no practical effect on any inference or analysis and, as a practical matter, we will usually regard the BPP model as one of spatial independence among individual activity centers, because each activity center is distributed independently of each other activity center. Despite this independence we see in Figure 5.2 that realizations of randomly distributed points will typically exhibit distinct non-uniformity. Thus, independent, uniformly distributed points will almost never appear regularly, uniformly, or systematically distributed. For this reason, the basic binomial (or Poisson) point process models are enormously useful in practical settings since they allow for a range of distribution are wellpatterns without violating the assumption of spatial randomness. More relevant for SCR models is that we actually have a little bit of data for some individuals and thus the resulting posterior point pattern can deviate strongly from uniformity, a point we come back to repeatedly in this book. The uniformity hypothesis is only a prior distribution which is directly affected by the quantity and quality of the observed data to produce a posterior distribution which may appear distinctly non-uniform. In addition, we can build more flexible models for the point process, which we take up in Chapter 11.

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The state-space of the point process

Shortly we will focus on Bayesian analysis of model SCR0 with N known so that we can gain some basic experience with important elements of the model, and its analysis. To do this, we note that the individual activity centers s_i, ..., s_N are unknown quantities and we will need to be able to simulate each si in the population from the posterior distribution. In order to simulate the s_i , it is necessary to describe precisely the region over which they are distributed. This is the quantity referred to above as the state-space, which is sometimes called the observation window in the point process literature. We denote the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (throughout this book) by S, which is the state-space henceforth (through this book) by S, which is the state-sp a region or a set of points comprising the potential values (the support) of the random

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variable s. Thus, an equivalent explicit statement of the "uniformity assumption" is

 $\mathbf{s}_i \sim \text{Uniform}(\mathcal{S}),$

where S is a precisely defined region, e.g., in Figure 5.2, S is the square defined by $[-1, 7] \times [-1, 7]$. Thus each of the N = 20 points was generated by randomly selecting each coordinate on the line [-1, 7]. When points are distributed uniformly over some region, the point process is usually called a homogeneous point process.

5.3.1.1 Prescribing the state-space

Evidently, to define the model, we need to define the state-space, S. How can we possibly do this objectively? Prescribing any particular S seems like the equivalent of specifying a "buffer" which we have criticized as being ad hoc. How is it, then, that the choice of a state-space is not ad hoc? As we observed in Chapter 4, it is true that N increases with \mathcal{S} , but only at the same rate as the area of \mathcal{S} increases under the prior assumption of constant density. As a result, we say that density is invariant to S as long as S is sufficiently large. Thus, while choice of S is (or can be) essentially arbitrary, once ${\cal S}$ is chosen, it defines the population being exposed to sampling, which scales appropriately with the size of the state-space.

For our simulated system developed previously in this chapter, we defined the statespace to be a square within which our trap array was centered. For many practical situations this might be an acceptable approach to defining the state-space, i.e., just a rectangle around the trap array. Although defining the state-space to be a regular polygon has computational advantages (e.g., we can implement this more efficiently in BUGS and cannot for irregular polygons), a regular polygon induces an apparent problem of admitting into the state-space regions that are distinctly non-habitat (e.g., oceans, large lakes, ice fields, etc.). It is difficult to describe complex regions in mathematical terms that can be used in BUGS. As an alternative, we can provide a representation of the state-space as a discrete set of points which the R package secr (Efford, 2011a) permits (secruses the term "mask" for what we call the state-space). Defining the state-space by a discrete set of points is handy because it allows specific points to be deleted or not, depending on whether they represent available or suitable habitat (see Section 5.10). We can also define the state-space as an arbitrary collection of polygons stored as a GIS shapefile which can be analyzed easily by MCMC in R (see Section 17.7), but not so easily in the BUGS engines. In Section 5.10, we provide an analysis of the wolverine camera trapping data, in which we define the state-space

5.3.1.2 Invariance to the state-space

to be a regular continuous polygon (a rectangle).

We will assert for all models we consider in this book that density is invariant to p0095 the size and extent of S, if S is sufficiently large, and as long as our model relating p_{ij} to s_i is a decreasing function of distance. We can prove this easily by drawing an analogy with a 1-d case involving distance sampling. Let y_j be the number of individuals captured in some interval $[d_{j-1}, d_j)$, and define $d_J = B$ for some large

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value of B. The observations from a survey are y_1, \ldots, y_{J_1} and the likelihood is a multinomial likelihood, so the log-likelihood is of the form

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$$\log L(y_1, ..., y_J) = \sum_{j=1}^J y_j \log(\pi_j),$$

where π_j is the probability of detecting an individual in distance class j, which depends on parameters of the detection function (the manner of which is not relevant for the present discussion). Choosing B sufficiently large guarantees that $\mathbb{E}(y_J) = 0$ and therefore the observed frequency in the "last cell" contributes nothing to the likelihood, in regular situations in which the detection function decays monotonically with distance and prior density is constant. We can think of B as being related to the state-space in an SCR model, as the width of a rectangular state-space with area $B \times L$, L being the length of the transect. Thus, if we choose B large enough, then we ensure that the expected trap frequencies beyond B will be 0, and thus contribute nothing to the likelihood.

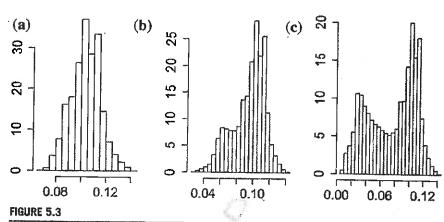
Sometimes our estimate of density can be affected by choosing S too small. However, this might be sensible if S is naturally well defined. As we discussed in Chapter 1, S is part of the model, and thus it is sensible that estimates of density might be sensitive to its definition in problems where it is natural to restrict S. One could imagine, however, in specific cases e.g., a small population with well-defined habitat preferences, that a problem could arise because changing the state-space based on differing opinions, and GIS layers, might have substantial affects on the density estimate. But this is a real biological problem, and a natural consequence of the spatial formalization of capture-recapture models—a feature, not a bug or some statistical artifact—and it should be resolved with better information, research, and thinking. For situations where there is not a natural choice of S, we should default to choosing S to be very large in order to achieve invariance or, otherwise, evaluate sensitivity of density estimates by trying a couple of different choices of S. This is a standard "sensitivity to prior" argument that Bayesians always have to be conscious of. We demonstrate this in our analysis of Section 5.9 below. As an additional practical consideration, we note that the area of the state-space S affects data augmentation. If you increase the size of S, then there are more individuals to account for and therefore the size of the augmented data set M must increase. This has computational 1 whelh implications.

5.3.2 Connection to model M_h and distance sampling

SCR models are closely related to "model M_h " and distance sampling. In SCR models, heterogeneity in encounter probability is induced by both the effect of distance in the model for detection probability and from specification of the state-space. Hence, the state-space is an explicit element of the model. To understand this, suppose activity centers have the uniform distribution:

 $\mathbf{s} \sim \text{Uniform}(\mathcal{S})$

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Implied distribution of p_i for a population of individuals as a function of the size of the state-space buffer around the trap array. The state-space buffer is 0.2, 0.5, and 1.0 for panels (a), (b), (c), respectively. In each case, the trap array is fixed and centered within a square state-space.

and encounter probability is a function of s, denoted by p(s) = p(y = 1|s). For example, under Eq. (5.2.2) we have that

$$p(\mathbf{s}) = \operatorname{logit}^{-1}(\alpha_0 - \alpha_1 \|\mathbf{x}_j - \mathbf{s}_I\|)$$

and we can work out, either analytically or empirically, what is the implied distribution of p for a population of individuals. Figure 5.3 shows a histogram of p for a hypothetical population of 100,000 individuals on a state-space enclosing our 5×5 trap array above, under the logistic model for distance given by Eq. (5.2.2) with buffers of 0.2, 0.5, and 1.0. We see the mass shifts to the left as the buffer increases, implying more individuals with lower encounter probabilities, as their home range centers increase in distance from the trap array.

Another way to understand this is by representing S as a set of discrete points on pollo a grid. In the coarsest possible case where S is a single arbitrary point, then every individual has exactly the same p. As we increase the number of points in S, more distinct values of p are possible. Indeed, when S is characterized by discrete points, then SCR models are precisely a type of finite-mixture model (Norris and Pollock, 1996; Pledger, 2004), except, in the case of SCR models, we have some information about which group an individual belongs to (i.e., where their activity center is), as a result of which traps it is captured in.

It is also worth reemphasizing that the basic SCR encounter model is a binomial polls encounter model in which distance is a covariate. As such, it is strikingly similar to classical distance sampling models (Buckland et al., 2001). Both have distance as a covariate but, in classical distance sampling problems, the focus is on the distance between the observer and the animal at an instant in time, not the distance between a

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5.4 The Implied Model of Space Usage

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trap and an animal's home range center. As a practical matter, in distance sampling, "distance" is observed for those individuals that appear in the sample. Conversely, in SCR problems, it is only imperfectly observed (we have partial information in the form of trap observations). Clearly, it is preferable to observe distance if possible, but distance sampling requires field methods that are not practical in many situations, e.g., when studying carnivores such as bears or large cats. Furthermore, SCR models allow us to relax many of the assumptions made in classical distance sampling, such as perfect detection at distance zero, and SCR models allow for estimates of quantities other than density, such as home range size, and space usage (See Chapters 12 and 13).

5.4 The implied model of space usage

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We developed the basic SCR model in terms of a latent variable, s, the home range center or activity center. Surely the encounter probability model, which relates encounter of individuals in specific traps to s, must somehow imply a certain model for home range geometry and size. Here we explore the nature of that relationship and we argue that any given detection model implies a model of space usage—i.e., the amount and extent of area used some prescribed percentage of the time. So we might say, for example, 95% of animal movements are within some distance from an individual's activity center. While we have used the term "home range" or similar, what we really mean to imply is something that would be more clearly identified as resource selection or space usage (the latter term meaning resource selection, when the resource is only homogeneous space).

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Intuitively, the detection function of SCR models is related to space usage by individuals. Indeed; it is natural to interpret the detection model as the composite of two processes: movement of an individual about its home range, i.e., how it uses space within its home range ("space usage"), and detection conditional on use in the vicinity of a trapping device. It is natural to decompose encounter probability according to:

Pr(encounter at x|s) = Pr(encounter|usage of x, s) Pr(usage of x|s).

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In practice it might make sense to think about the first component, i.e., Pr(encounter| usage of x, s) as being a constant (e.g., if traps are located within arbitrarily small grid cells) and then in that case, the encounter probability model is directly proportional to this model for individual movements about their home range center determining the use frequency of each x. This is a sensible heuristic model for what ecologists would call a central place forager, although, as we have stated previously, it may be meaningful as a description of transient space usage as well (that is, the space usage during the period of sampling).

p0130

To motivate a specific model for space usage, imagine the area we are interested in consists of some large number of small pixels (i.e., we're looking at a discrete representation of space), and that we have some kind of perfect observation device (e.g., continuous telemetry) so that we observe every time an individual moves into a

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values of x

pixel. After a long period of time, we observe an enormous sample size of x values. We tally those up into each pixel, producing the frequency $m(\mathbf{x}, \mathbf{s})$, which is something like the "true" usage of pixel x by individual with activity center s. So, then, the usage model should be regarded as a probability mass function for these counts and, naturally, we regard the counts $m(\mathbf{x}, \mathbf{s})$ as a multinomial observation with probabilities $\pi(\mathbf{x}|\mathbf{s})$, and prescribe a suitable model for $\pi(\mathbf{x}|\mathbf{s})$ that describes how use events should accumulate in space. A natural null model for $\pi(\mathbf{x}|\mathbf{s})$ has a decreasing probability of use as x gets far away from s; i.e., animals spend more time close to their activity centers than far away. We can regard points used by the individual with activity center s as the realization of a point process with conditional intensity:

$$\pi(\mathbf{x}|\mathbf{s}) = \frac{k(\mathbf{x},\mathbf{s})}{\sum_{i} k(\mathbf{x},\mathbf{s})},$$
 (5.4.1)

where k(x, s) is any positive function. In continuous space, the equivalent representation we stake:

 $\pi(\mathbf{x}|\mathbf{s}) = \frac{k(\mathbf{x},\mathbf{s})}{\int k(\mathbf{x},\mathbf{s})dx}.$

Clearly the space used by an individual will be proportional to whatever kernel, $k(\mathbf{x}, \mathbf{s})$, we plug in here. If we use a negative exponential function, then this produces a standard resource selection function (RSF) model (e.g., Manly et al., 2002, Chapter 8). But, here we use a Gaussian kernel, i.e.,

$$k(\mathbf{x}, \mathbf{s}) = \exp(-d(\mathbf{x}, \mathbf{s})^2/(2\sigma^2))$$

so that contours of the probability of space usage resemble a bivariate normal or Gaussian probability distribution function.

To apply this model of space usage to SCR problems we allow for imperfect detection by introducing a non-uniform "thinning rate" of the true counts m(x, s). This yields, precisely, our Gaussian encounter probability model where the thinning rate is our baseline encounter probability p_0 for each pixel where we place a trap, and p = 0 in each pixel where we don't place a trap.

The main take-away point here is that underlying most SCR models is some kind of model of space usage, implied by the specific choice of k(x, s). Whether or not we have perfect sampling devices, the function we use in the encounter probability model equates to some conditional distribution of points, a utilization distribution, as in Eq. (5.4.1), from which we can compute effective home range area, i.e., the area that contains some percent of the mass of a probability distribution proportional to k(x, s); e.g., 95% of all space used by an individual with activity center s.

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5.4.1 Bivariate normal case

s0045

One encounter model that allows direct analytic computation of home range area is p0145 the Gaussian encounter probability model

Subscripts (1) ? $p(\mathbf{x}, \mathbf{s}) = p_0 \exp\left(-\frac{1}{2\sigma^2} \|\mathbf{x} - \mathbf{s}\|^2\right).$

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5.4 The Implied Model of Space Usage

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For this model, encounter probability is proportional to the kernel of a bivariate normal (Gaussian) pdf and so the natural interpretation is that in which movement outcomes (or successive locations of an individual) are draws from a bivariate normal distribution with standard deviation \u03c3. We say that use of this model implies a bivariate normal model of space usage. Under this model we can compute precisely the effective home range area. In particular, if use outcomes are bivariate normal, then $\|\mathbf{x} - \mathbf{s}\|^2$ has a chi-square distribution with 2 df and the quantity $B(\alpha)$ that encloses $(1-\alpha)\%$ of all realized distances, i.e., $\Pr(d \le B(\alpha)) = 1 - \alpha$, is $B(\alpha) = \sigma(*\sqrt{g(\alpha, 2)})$, where $q(\alpha, 2)$ is the 0.05 chi-square critical value on 2 df. For example, to compute q(.05, 2)in R we execute the command qchisq (.95,2), which is $q(2,\alpha) = 5.99$. Then, for $\sigma = 1$, $B(\alpha) = 1 \times \sqrt{5.99} = 2.447$. Therefore 95% of the points used will be within 2.447 (standard deviation) units of the home range center. So, in practice, we can estimate σ by fitting the bivariate normal encounter probability model to some SCR data, and then use the estimated σ to compute the "95% radius," say $r_{.95} = \sigma \sqrt{5.99}$, and convert this to the 95% use area—the area around s which contains 95% of the movement outcomes—according to $A_{.95} = \pi r_{.95}^2$.

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An alternative bivariate normal model is the bivariate normal hazard rate model:

$$p(\mathbf{x}, \mathbf{s}) = 1 - \exp\left(-\lambda_0 + \exp\left(-\frac{1}{2\sigma^2} \|\mathbf{x} - \mathbf{s}\|^2\right)\right). \tag{5.4.2}$$

We use λ_0 here because this parameter, the baseline encounter *rate*, can be >1. This arises by assuming the latent "use frequency" m(x, s) is a Poisson random variable with intensity $\lambda_0 k(x, s)$. The model is distinct from our Gaussian encounter model $p(x, s) = p_0 k(x, s)$ used previously, although we find that they produce similar results in terms of estimates of density or 95% use area, as long as baseline encounter probability is low. We discuss these two formulations of the bivariate normal model further in Chapter 9.

s0050

5.4.2 Empirical analysis

of

p0155

For any encounter model we can compute space usage quantiles empirically by taking a fine grid of points and either simulating movement outcomes with probabilities proportional to $p(\mathbf{x}, \mathbf{s})$ and accumulating area around \mathbf{s} , or else we can do this precisely by varying $B(\alpha)$ to find that value within which 95% of all movements are concentrated, i.e., the set of all \mathbf{x} such that $\|\mathbf{x} - \mathbf{s}\| \le B(q)$. Under any detection model, movement outcomes will occur in proportion to $p(\mathbf{x}, \mathbf{s})$, as long as the probability of encounter is constant, conditional on use, and so we can define our space usage distribution according to:

 $\pi(\mathbf{x}|\mathbf{s}) = \frac{p(\mathbf{x},\mathbf{s})}{\sum_{\mathbf{x}} p(\mathbf{x},\mathbf{s})}$

Given the probabilities $\pi(x, s)$ for all x we can find the value of B(q), for any q, such that

 $\sum_{\mathbf{x} \ni \|\mathbf{x} - \mathbf{s}\| \le B(q)} \pi(\mathbf{x}, \mathbf{s}) \le 1 - q \qquad \text{before } \mathbf{y} + \mathbf{s} \cdot \mathbf{B}(\mathbf{x})$

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(here, we use ∋ to mean "such that"). We have a function called hra in the scrbook package that computes the home range area for any encounter model and prescribed parameter values. The help file for hra has an example of simulating some data. The following commands illustrate this calculation for two different bivariate normal models of space usage:

lene?

```
00005
## Define encounter probability model as R function
                                                                             00010
                                                                             00015
> pGauss2 <- function(parms,Dmat){</pre>
                                                                             00020
    a0 <- parms[1]
                                                                             00025
    sigma <- parms[2]
                                                                             00030
    1p <- parms[1] -(1/(2*parms[2]*parms[2]))*Dmat*Dmat</pre>
                                                                             o0035
    p <- 1-exp(-exp(lp))
                                                                             o0040
                                                                             00045
}
                                                                             00050
> pGauss1 <- function(parms,Lmat)</pre>
                                                                             00055
    a0 <- parms[1]
                                                                             a0060
    sigma <- parms[2]
                                                                             00065
    p <- plogis(parms[1])**exp(-(1/(2*parms[2]*parms[2]))*Dmat*Dmat)</pre>
                                                                             o0070
                                                                             00075
}
                                                                             00080
                                                                             00085
## Execute hra with sigma = .3993
                                                                             00090
##
                                                                             00095
> hra(pGauss1,parms=c(-2,.3993),plot=FALSE,xlim=c(0,6),ylim=c(0,6)
                                                                            00100
      ng=500, tol=:0005)
                                                                             o0105
[1] 0.9784019
                                                                             o0110
radius to achieve 95% of area: 0.9784019
                                                                             00115
home range area: 3.007353
                                                                             o0120
[1] 3.007353
                                                                             00125
## Analytic solution:
                                                                             00130
      true sigma that produces area of 3
                                                                             00135
> sqrt(3/pi)/sqrt(5.99)
                                                                            00140
[1] 0.3992751
                                                                            00145
```

X & Herres C What this means is that B(q) = 0.978 is the radius that encloses about 95% of all movements under the standard bivariate normal encounter model. Therefore, the area is about $\pi * .978^2 = 3.007$ spatial units. You can change the intercept of the model and find that it has no effect. The true (analytic) value of σ that produces a home range area of 3.0 is 0.3993 which is the value we initially plugged in to the hra function. We can improve on the numerical approximation to home range area (get it closer to 3.0) by increasing the resolution of our spatial grid (increase the no argument) along with the tol argument.

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5.4 The Implied Model of Space Usage

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We can also reverse this process, and find, for any detection model, the parameter values that produce a certain (1-q)% home range area, which we imagine would be useful for doing simulation studies. The function hra will compute the value of the scale parameter that achieves a certain target (1-q)% home range area, by simply providing a non-null value of the variable target area. Here we use target area = 3.00735 (from above) to obtain a close approximation to the value σ we started with (the parameter argument is meaningless here):

X ?

00150

> hra(pGauss1,parms=c(-2,.3993),plot=FALSE,xlim,ylim,ng=500,target.area=3.00735,tol=.0005)

o0155 Value of parm[2] to achieve 95% home range area of 3.00735: 0.3993674

55 5.4.3 Relevance of understanding space usage

One important reason that we need to be able to deduce "home range area" from a detection model is so that we can compare different models with respect to a common biological currency. Many encounter probability models have some scale parameter, which we might call σ no matter the model, but this relates to 95% area in a different manner under each model. Therefore, we want to be able to convert different models to the same currency. Another reason to understand the relationship between models of encounter probability and space usage is that it opens the door to combining traditional resource selection data from telemetry with spatial capture-recapture data. In Chapter 13 we consider this problem, for the case in which a sample of individuals produces encounter history data suitable for SCR models and, in addition, we have telemetry relocations on a sample of individuals. This is achieved by regarding the two sources of data as resulting from the same underlying process of space usage but telemetry data produce "perfect" observations like always-on camera traps blanketing a landscape. We use this idea to model the effect of a measured covariate at each pixel, say C(X), on home range size and geometry and, hence, the probability

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5.4.4 Contamination due to behavioral response

of encounter in traps.

points Interpretation of encounter probability models as models of animal home range and space usage can be complicated by a number of factors, including whether traps are baited or not. In the case of baited traps, this might lead to a behavioral response (Section 7.2.3) which could affect animal space usage. For example, if traps attract animals from a long distance, it could make typical home ranges appear larger than normal. More likely, in our view, it wouldn't change the typical size of a range but would change how individuals use their range, e.g., by moving from baited trap to baited trap, so that observed movement distances of individuals are typically larger than normal.

p0180

In other cases, the reliance on Euclidean distance in models for encounter probability might be unrealistic and can lead to biased estimates of density (Royle et al., 2013). For example, animals might concentrate their movements along trails, roads,

or other landscape features. In this case, models that accommodate other distance metrics can be considered. We present models based on least-cost path in Chapter 12.

5.5 Simulating SCR data

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It is always useful to simulate data because it allows you to understand the system that poiss you're modeling and calibrate your understanding with specific values of the model parameters. That is, you can simulate data using different parameter values until you obtain data that "look right" based on your knowledge of the specific situation that you're interested in. Here we provide a simple script to illustrate how to simulate spatial encounter history data. In this exercise we simulate data for 100 individuals and a 25-trap array laid out in a 5×5 grid of unit spacing. The specific encounter model is the Gaussian model given above and we used this code to simulate data used in subsequent analyses. The 100 activity centers were simulated on a state-space defined by an 8 × 8 square within which the trap array was centered (thus the trap

array is buffered by 2 units). Therefore, the density of individuals in this system is

```
> set.seed(2013)
                                                                                   00160
  # Create 5 x 5 grid of trap locations with unit spacing
                                                                                   o0165
  > traplocs <- cbind(sort(rep(1:5,5)),rep(1:5,5))
                                                                                   o0170
  > ntraps <- nrow(traplogs)
                                                                                   00175
  # Compute distance matrix:
                                                                                   00180
  > Dmat :- e2dist(traplocs,traplocs)
                                                                                   o0185
 # Define state-space of point process. (i.e., where animals live).
                                                                                   o0190
   "buffer" just adds a fixed buffer to the outer extent of the traps.
                                                                                   00195
                                                                                   00200
                                                                                   00205
 > xlim <- c(min(traplocs[,1] - buffer), max(traplocs[,1] + buffer))
                                                                                   00210
 > ylim <- c(min(traplocs[,2] - buffer),max(traplocs[,2] + buffer))</pre>
                                                                                   00215
 > N <- 100
                 # population size
                                                                                   00220
 > K <-
         20
                 # number nights of effort
                                                                                   00225
 > sx < runif(N,xlim[1],xlim[2])
                                         # simulate activity centers
                                                                                   00230
 > sy <- runif(N,ylim[1],ylim[2])
                                                                                  00235
 > 8 <- cbind(sx,sy)
                                                                                   00240
 # Compute distance matrix:
                                                                                  00245
 > D <- e2dist(S,traplocs)
                                 # distance of each individual from each trap
                                                                                  00250
> alpha0 <- -2.5
                         # define parameters of encounter probability
                                                                                  00255
 > sigma <- 0.5
                         # scale parameter of half-normal
                                                                                  00260
 > alpha1 <- 1/(2*sigma*sigma) # convert to coefficient on distance
                                                                                  00265
 # Compute Probability of encounter:
                                                                                  00270
                                                                                  o0275
 > probcap <- plogis(-2.5)*exp(- alpha1*D*D)</pre>
                                                                                  o0280
 # Generate the encounters of every individual in every trap
                                                                                  00285
```

```
o0290
          Y <- matrix (NA, nrow=N, ncol=ntraps)
  o0295
          for(i in 1:nrow(Y)){
  00300
             Y[i,] <- rbinom(ntraps,K,probcap[i,])
  o0305
            We remind the reader that, in presenting R or other code snippets throughout the
   p0190
        book, we will deviate from our standard variable expressions for some quantities. In
        particular, we sometimes substitute words for integer variable designations: nind
        (for n), ntraps (for J), and nocc (for K). In our opinion this leaves less to be
        inferred by the reader in trying to understand code snippets.
            Subsequently we will generate data using this code packaged in an R function
  p0195
        called simSCRO in the package scrbook which takes a number of arguments
        including discardo which, if TRUE, will return only the encounter histories for
         captured individuals. A second argument is array3d which, if TRUE, returns the
                                                                                         I Pagir Put
         three-dimensional encounter history array instead of the aggregated nind x ntraps
                                                                                                    Map-specfic
Common frequencies (see below). Finally we provide a random number seed, rnd
         = 2013, to ensure repeatability of the analysis here. We obtain a data set as above
         using the following command:
   0310 > data <- simSCR0(discard0=TRUE, array3d=FALSE, rnd=2013)
                                                                                              Fourt size?
         The R object data is a list, so let's take a look at what's in the list and then harvest
         some of its elements for further analysis below:
   00315
        > names (data)
                        "traplocs" "xlim"
                                              "ylim"
   00320
         [1] "Y"
                                                                   'aloha0'
                                                                                "beta
   00325
             "sigma"
         [8]
         ## Grab encounter histories from simulated data list
   00330
   o0335
         > Y <- data$Y
         ## Grab the trap locations
   o()340
         > traplocs <- data$tfaplocs
   o0345
         We'll use this sinunared doto set shortly
         5.5.1 Formatting and manipulating real data sets
   s0070
   p0205
         Conventional capture-recapture data are easily stored and manipulated as a two-
         dimensional array, an nind x K (individuals by sample occasions) matrix, which
         is maximally informative for any conventional capture-recapture model, but not for
         spatial capture-recapture models. For SCR models we must preserve the spatial infor-
         mation in the encounter history information. We will routinely analyze data from three
                                                 and grand thered
         standard formats:
   oll65 (1) The basic two-dimensional data format, which is an nind x ntraps encounter
```

frequency matrix such as that simulated previously. These are the total number of encounters in each trap, summed over the K sample occasions.

o1170 (2) The maximally informative three-dimensional array, for which we establish here

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the convention that it has dimensions nind \times ntraps \times K.

(3) We use a compact format—the "encounter data file" which we describe below o1175 in Section 5.9.

To simulate data in the most informative format—the "3-d array"—we can use the R commands given previously but replace the last four lines with the following:

```
> Y <- array(NA, dim=c(N, ntraps, K))

> for(i in 1:nrow(Y)){
    for(j in 1:ntraps){
        Y[i,j,1:K] <- rbinom(K,1, probcap[i,j])
    }
}
```

We see that a collection of K binary encounter events are generated for each individual and for each trap. The probabilities of those Bernoulli trials are computed based on the distance from each individual's home range center and the trap (see calculation above), and those are housed in the matrix probcap. Our data simulator function simsRCO will return the full 3-d array if array3d=TRUE is specified in the function call. To recover the 2-d matrix from the 3-d array, and subset the 3-d array to individuals that were captured, we do this:

```
# Sum over the "sample occasions" dimension (3rd margin of the array) 00380
> Y2d <- apply(Y,c(1,2),sum) 00385

# Compute how many times each individual was captured 00395
> ncaps <- apply(Y2d,1,sum) 00395

# Keep those individuals that were captured 00400
> Y <- Y[ncaps=0,.]
```

5.6 Fitting model SCRO in BUGS

s0075 p0220

o0425

Clearly if we somehow knew the value of N then we could fit this model directly because, in that case, it is a special kind of logistic regression model, one with a random effect (s) that enters into the model in a peculiar fashion, and also with a distribution (uniform) which we don't usually think of as standard for random effects models. So our aim here is to analyze the known-N problem, using our simulated data, as an incremental step in our progress toward fitting more generally useful models. To begin, we use our simulator to grab a data set and then harvest the elements of the resulting object for further analysis:

```
> data <- simSCR0(discard0=FALSE,rnd=2013) 00410
> y <- data$Y 00415
> traplocs <- data$traplocs 00420
```

In this case mind=N because we're doing the known-N problem

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5.6 Fitting Model SCRO in BUGS

```
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```

```
00430
       nind <- nrow(y)
00435
00440
       X <- data$traplocs
                            # number of traps
o0445
        J \leftarrow nrow(X)
       K <- data$K
o0450
     > xlim <- data$xlim
n0455
     > ylim <- data$ylim
o0460
        Note that we specify discard0 = FALSE so that we have a complete data
p0225
     model using the following commands:
```

set, i.e., one with the all-zero encounter histories corresponding to uncaptured individuals. Now, within an R session, we can create the BUGS model file and fit the

```
cat("
o0465
o0470
      model (.
      alpha0 ~ dnorm(0,.1)
o0475
      logit(p0) <- alpha0
o0480
o0485
      alphal "dnorm(0,.1)
      sigma <- sqrt(1/(2*alphal))
o0490
                          # note N here - N is KNOWN in this example
      for(i in 1:N) {
00495
       s[i,1] ~ dunif(xlim[1],xlim[2])
00500
       s[i,2] ~ dunif(ylim[1],ylim[2])
o0505
00510
       for(j in 1:3){
         d(i,j) \leftarrow pow(pow(s[i,1]-X[j,1],2) + pow(s[i,2]-X[j,2],2),0.5)
o0515
         y[i,j] ~ dbin(p[i,j],K)
o0520
         p[i,j] <- p0*exp(- alpha1*d[i,j]*d[i,j])
00525
00530
o0535
00540
      ",file = "SCROa.txt").
o0545
```

p0230

This model describes the Gaussian encounter probability model, but it would be trivial to modify that to various others including the logistic described above. One consequence of using the half-normal is that we have to constrain the encounter probability to be in [0, 1] which we do here by defining alphao to be the logit of the intercept parameter p0. Note that the distance covariate is computed within the BUGS model specification given the matrix of trap locations, X, which is provided to WinBUGS as data.

Next we do a number of organizational activities including bundling the data for WinBEGS, defining some initial values, the parameters to monitor and some basic MCMC settings. We choose initial values for the activity centers s by generating uniform random numbers in the state-space but, for the observed individuals, we

```
replace those values by each individual's mean trap coordinate for aftencounters:
      ### Starting values for activity centers, s
00550
     > ost <- cbind(runif(nind,xlim[1],xlim[2]),runif(nind,ylim[1],ylim[2]))
00555
o0560
     > for(i in 1:nind) {
00565
            if(sum(y[i,])==0) next
```

(p0235

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```
sst[i,1] \leftarrow mean(X(y[i,]>0,1))
                                                                                   00570
      sst[i,2] \leftarrow mean(X[y[i,]>0,2])
                                                                                   00575
  }
                                                                                   o0580
> data <- list (y=y, X=X, K=K, N=nind, J=J, xlim=xlim ylim=ylim)
                                                                                   o0585
> inits <- function() {
                                                                                   o0590
      list (alpha0=rnorm(1,-4,.4), alpha1=runif(1,1,2), s=sst)
                                                                                   00595
                                                                                   00600
> library(R2WinBUGS)
                                                                                   00605
> parameters <- c("alpha0", "alpha1", "sigma")
                                                                                   00610
> out <- bugs (data, inits, parameters, "SCRQa.txt", n.thin=1, n.chains=3,
                                                                                   a0615
                n.burnin=1000,n.iter=2000,debug=TRUE,working.dir=getwd())
```

There is little to say about the preceding operations other than to suggest that you might explore the output and investigate additional analyses by running the simSCRO script provided in the R package scrbook.

For purposes here, we ran 1,000 burn-in and 1,000 post-burn-in iterations, and 3 chains, to obtain 3,000 posterior samples. Because we know N for this particular data set we only have two parameters of the detection model to summarize (alpha0 and alpha1), along with the derived parameter σ , the scale parameter of the Gaussian kernel, i.e., $\sigma = \sqrt{1/(2\alpha_1)}$. When the object out is produced we print a summary of the results as follows:

```
> print(out,digits=2)
Inference for Bugs model at "SCROa.tot", fit using WinBugs.
 3 chains, each with 2000 iderations (first 1000 discarded)
 n.sims = 3000 iterations saved
             mean
                        bd
                                2.5%
                                          25%
                                                    50%
                                                              75%
                                                                                       n.eff
alphao
             -2.50
                      0.22
                               -2.95
                                         -2.65
                                                   -2.48
                                                             -2.34
                                                                      -2.09
                                                                               1.01
                                                                                         190
alpha1
             2.44
                      42
                                1.64
                                          2.15
                                                   2.44
                                                             2.72
                                                                       3.30
                                                                               1,00
                                                                                         530
sioma
              0.46
                      0 04
                                0.39
                                          0.43
                                                             0.48
                                                                       0.55
                                                                               1.00
                                                                                         530
deviance
           292.80
                     21.16
                             255.60
                                        277.50
                                                 291.90
                                                           306.00
                                                                     339.30
                                                                               1.01
                                                                                         380
[ ... some output deleted ...]
```

We know the data were generated with alpha 0 = -2.5 and alpha 1 = 2. The estimates look reasonably close to those data-generating values and we probably feel pretty good about the performance of the Bayesian analysis and MCMC algorithm that WinBUGS cooked up based on our sample size of 1 data set. It is worth noting that the Rhat statistics indicate reasonable convergence but, as a practical matter, we might choose to run the MCMC algorithm for additional time to bring these closer to 1.0 and to increase the effective posterior sample size (n.eff). Other summary output includes "deviance" and related things including the deviance information criterion (DIC). We discuss general issues of convergence and other MCMC considerations in Chapter 17, and DIC and model selection in Chapter 8.

5.7 Unknown N

In all real applications N is unknown. We handled this important issue in Chapter 4 using the method of data augmentation (DA), which we apply here to achieve a realistic

between each chat.

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analysis of model SCRO. As with the basic closed population models considered previously, we formulate the problem by augmenting our observed data set with a number of "all-zero" encounter histories—what we referred to in Chapter 4 as potential individuals. If n is the number of observed individuals, then let M-n be the number of potential individuals in the data set. For the two-dimensional y_{ij} data structure (n individual $\times J$ traps encounter frequencies) we simply add additional rows of all-zero observations to that data set. Because such "individuals" are unobserved, they therefore necessarily have $y_{ij} = 0$ for all j. A data set say with 4 traps and 6 individuals, augmented with 4 pseuda-individuals therefore might look like this:

	trap1	trap2	trap3	trap4	0
[1,]	1	0	0	0	Potential
[2,]	0	2	0	0	14
[3,]	0	0	0	1	4/
[4,]	0	1	0	0	40
[5,]	0	0	1	1."	
[6,]	1	0	1	0	
[7,]	0	0	0	0	
[8,]	0	0	0	-0	
[9,]	0	0	0	0	
[10,]	0	0	0	0	

We typically have more than 4 traps and, if we're fortunate, many more individuals in our data set.

p0255

For the augmented data set, we introduce a set of binary latent variables (the data augmentation variables), z_i , and the model is extended to describe $\Pr(z_i = 1)$ which is, in the context of this problem) the probability that an individual in the augmented data set is a member of the population of size N that was exposed to sampling. In other words, if $z_i = 1$ for one of the all-zero encounter histories, this is implied to be a sampling zero whereas observations for which $z_i = 0$ are "structural zeros" under the model. Under DA, we also express the binomial observation model conditional on z_i as follows:

$$y_{ij}|z_i \sim \text{Binomial}(K, z_i p_{ij}),$$

where we see that the binomial probability evaluates to 0 if $z_i = 0$ (so y_{ij} is a fixed 0 in that case) and evaluates to p_{ij} if $z_i = 1$.

0260

How brg does the augmented data set have to be? We discussed this issue in Chapter 4 where we noted that the size of the data set is equivalent to the upper limit of a uniform prior distribution on N. Practically speaking, it should be sufficiently large so that the posterior distribution for N is not truncated. On the other hand, if it is too large then unnecessary calculations are being done. An approach to choosing M by trial-and-error is indicated. Do a short MCMC run and then consider whether you need to increase M. See Chapter 17 for an example of this. Kéry and Schaub (2012, Chapter 6) provide an assessment of choosing M in closed population models. The useful thing about DA is that it removes N as an explicit parameter of the model.

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Instead, N is a derived parameter, computed by $N = \sum_{i=1}^{M} z_i$. Similarly, density, D, is also a derived parameter, computed as D = N/area(S).

5.7.1 Analysis using data augmentation in WinBUGS

s0085

We provide a complete R script for simulating and organizing a data set, and analyzing the data in WinBUGS. As before we begin by obtaining a data set using our simSCRO function and then harvesting the required data objects from the resulting data list. Note that we use the discardo=TRUE option this time so that we get a "real looking" data set with no all-zero encounter histories:

p0265

Make Make

```
00620
## Simulate the data and extract the required objects
                                                                     00625
                                                                     00630
> data <- simSCRO(discardO=TRUE,rnd=2013)
                                                                     00635
 y <- data$Y
                                                                     00640
> nind <- nrow(y)</pre>
                                                                     00645
 X <- data$traplocs
                                                                     c0650
  K <- data$K
                                                                     00655
  J \leftarrow nrow(X)
                                                                     00660
 xlim <- data$xlim
                                                                     00665
  ylim <- data$ylim
                                                                     00670
```

After harvesting the data we augment the data matrix y with M-n all-zero encounter histories, and create starting values for the variables z_i and also the activity centers s_i of which, for each, we require M values. One thing to take care of in using the BUGS engines is the starting values for the activity centers. It is usually helpful to start the s_i for each observed individual at or near the trap(s) it was captured. All of this happens as follows:

```
## Data augmentation
                                                                            e0675
> M <- 200
                                                                            00680
    < rbind(y,matrix(0,nrow=M-nind,ncol=ncol(y)))</pre>
                                                                            00685
    <- c(rep(1, nind), rep(0, M-nind))
                                                                            00690
## Starting values for s
                                                                            00695
> sst <- cbind(runif(M, xlim[1], xlim[2]), runif(M, ylim[1], ylim[2]))
                                                                            00700
> for(i in 1:nind){
                                                                            00705
    sst[i,1] <- mean( X{y[i,]>0,1} )
                                                                            o0710
    sst[i,2] <- mean( X[y[i,]>0,2] )
                                                                            00715
                                                                            00720
```

Next, we write out the BUGS model specification and save it to an external file called SCROb.txt. The model specification now includes M encounter histories including the augmented potential individuals, the data augmentation parameters z_i , and the data augmentation parameter ψ :

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```
00725 > cat("
o0730
     model{
        alpha0 ~ dnorm(0,.1)
o0735
00740
        logit(p0) <- alpha0
o0745
      alphal '
              dnorm(0,.1)
     sigma <- sqrt(1/(2*alpha1))
00750
     psi ~ dunif(0,1)
o0755
o0760
      for(i in 1:M) {
        z[i] ~ dbern(psi)
00765
        s[i,1] ~ dunif(xlim[1],xlim[2])
60770
        s[i,2] ~ dunif(ylim[1],ylim[2])
00775
                                                                                         mate some
00780
        for(j in 1:J){
          d[i,j] \leftarrow pow(pow(s[i,1]-X[j,1],2) + pow(s[i,2]-X[j,2],2),0.5
00785
          y[i,j] \sim dbin(p[i,j],K)
a0790
          p[i,j] <- z[i]*p0*exp(- alpha1*d[i,j]*d[i,j])
o0795
00800
00805
00810
     N <- sum(z[])
     D <- N/64
00815
o0820
o0825
      ",file = "SCROb.txt")
         The remainder of the code for bundling the data, creating initial values and exe-
p0280
      cuting WinBUGS, looks much the same as before except with more or differently
      named arguments:
     > data <- list (y=y, X=X, k=K, M=M, J=J, xlim=xlim, ylim=ylim)
00830
      > inits <- function(){
o0835
         list (alpha0=rnorm(1 -4, 4), alpha1=runif(1,1,2), s=sst, z=2)
00840
00845
```

Note the differences in this new WinBUGS model with that appearing in the known-N version—there are not many! The loop over individuals goes up to M now, and there is a model component for the DA variables Z. We are also computing some derived parameters: population size N(S) is computed by summing up all of the data augmentation variables z_i (as we've done previously in Chapter 4) and density, D, is also a derived parameter, being a function of N. The input data has changed slightly too, as the augmented data set has more rows to include excess all-zero encounter histories. Previously we knew that N = 100 but in this analysis we pretend not to know N, but think that N = 200 is a good upper bound. This analysis can be run directly using the SCRObayes function once the scrbook package is loaded, by issuing the following commands:

n.chains=3, n.burnin=1000, n.iter=2000, debug=TRUE, working.dir=getwd())

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o0855 o0860

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D0285

> library(R2WinBUGS)

> parameters <- c."alpha0", "alpha1", "sigma", "N", "D")

> out <- bugs (data, inits, parameters, "SCROb.txt", n.thin=1,

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> library(scrbook)
> data <- simSCR0(discard0=TRUE,rnd=2013)
> out1 <- SCR0bayes(data,M=200,engine="winbugs",ni=2000,nb=1000)
00880</pre>

Summarizing the output from WinBUGS produces:

> print(o	ut1 digit	s=2)								_
Inference	for Bugs	model a	t "SCROb.	ext", fit	using Win	BUGS.			15	
	s, each w							100	, 6	
	= 3000 it							100		
	mean	ad	2.5%	25€	50%	75%	97.5%	Rhat	n.eff ! T	
alpha0	-2.57	0.23	-3.04	-2.72	-2.56	-2.41	-2.15	¥1.01	320 V	
alphal	2.46	0.42	1,63	2.16	2 44	2.73	3,33	1.02	120	1
#1gma	0.46	0.04	0.39	0.43	0 15	0.48	0.55	1.02	120	1
N	113.62	15.73	86.00	102.00	112 00	124.00	147.00	1.01	260	.
a	1.78	0.25	1.34	1.59	1.77	1.94	2.30	1.01	260	1
deviance	302.00	23,67	261.19	285.4	301.50	317,90	354.91	1.00	1400	1
				6	ا د		٠, ١			1
(some d	ontbit de	ecea	l	246	Deser	e IW	wire			7

The Rhat statistic (discussed in Sections 3.5.2 and 17.6.4) for this analysis indicates satisfactory convergence. We see that the estimated parameters (α_0 and α_1) are comparable to the previous results obtained for the known-N case, and also not too different from the data-generating values. The posterior of N overlaps the data-generating value substantially.

5.7.1.1 Use of other BUGS engines; JAGS

There are two other popular BUGS engines in widespread use: OpenBUGS (Thomas et al., 2006) and JAGS (Plummer, 2003). Both of these are easily called from R. OpenBUGS can be used instead of WinBUGS by changing the package option in the bugs call to package = "OpenBUGS". JAGS can be called using the function jags M in package R2 jags which has nearly the same arguments as bugs M. Or, it can be executed from the R package rjags (Plummer, 2011) which has a slightly different implementation that we demonstrate here as we reanalyze the simulated data set in the previous section (note: the same R commands are used to generate the data and package the data, inits and parameters to monitor). The function jags model is used to initialize the model and run the MCMC algorithm for an adaptive period during which tuning of the MCMC algorithm might take place. These samples cannot be used for inference. Then the Markov chains are updated using coda. samples to obtain posterior samples for analysis, as follows:

These commands can be executed using the function SCR0bayes provided with p0300 the R package scrbook! Hobbs (2011) provides a good introduction to ecological modeling with JAGS which we recommend.

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by setting the a engine argument

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5.7 Unknown N

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(Using The Function hea)

5.7.2 Implied home range area

Here we apply the method described in Section 5.4 to compute the effective home range area under different encounter probability models fit to simulated data. We simulated a data set from the Gaussian kernel model as in Section 5.7 and then we fitted four models to it: (1) the true data-generating Gaussian encounter probability model; (2) the "hazard" or complementary log-log link model (Eq. (5.4.2)); (3) the negative exponential model; and (4) the logit model (Eq. (5.2.2)). We modified the function SCRObayes for this purpose which you should be able to do with little difficulty. We fit each model to the same simulated data set using WinBUGS, based only on 1000 post-burn-in samples and 3 chains, which produced the posterior summaries given in Table 5.2. The main thing we see is that, while the implied home range area can vary substantially, there are smaller differences in the estimated N and hence D.

5.7.3 Realized and expected density

In Bayesian analysis of the SCR model, we estimate a parameter N which is the size of the population for the prescribed state-space (presumably the state-space is defined so as to be relevant to where our traps were located, so N can be thought of as the size of the sampled population). In the context of Efford and Fewster (2012) this is the *realized* population size. Conversely, sometimes we see estimates of expected population size reported, which are estimates of $\mathbb{E}(N)$, the expected size of some hypothetical, unspecified population. Usually the distinction between realized and expected population size is not made in SCR models, because almost everyone only cares about actual populations—and their realized population size.

If you do likelihood analysis of SCR models, then the distinction between realized and expected is often discussed by whether the estimator is "conditional-on-N" (realized) or not (expected). The naming arises because in obtaining the MLE of N, its properties are evaluated *conditional* on N—in particular, if the estimator is unbiased then $\mathbb{E}(\hat{N}|N) = N$ and $\text{Var}(\hat{N}|N) = \tilde{\sigma}_{\hat{N}}^2$ is the sampling variance. This does not conform to any concept or quantity that is relevant to Bayesian inference. If we care

course

- encounter probability

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Table 5.2 Posterior mean of model parameters for four different models fitted to a single simulated data set, and the effective home range area under each detection model. Compared 19149 The Function William

	. Gauesian	Cloglog	Exponentia	Logic ?
N	113.62	114.16	119.69	. 118.29
D	1.78	1.78	1.87	1.85
αο	2.57	2.60	-1.51	-0.47
α1	2.46	2.56	3.59	3.86
hra	3.85	3.78	5.51	2.64

about N for the population that we sampled it is understood to be a realization of a random variable, but the relevance of "conditional-on-N" is hard to see. Bayesian analysis will provide a prediction of N that is based on the posterior $[N|y, \theta]$ —which is certainly not conditional on N.

There is a third type of inference objective that is relevant in practice and that p0320 is prediction of N for a population that was not sampled -i.e., a "new" population. To elaborate on this, consider a situation in which we are concerned about the tiger population in two distinct reserves in India. We do a camera trapping study on one of the reserves to estimate N_1 and we think the reserves are similar and homogeneous so we're willing to apply a density estimate based on N1 to the second reserve. For the second reserve, do we want a prediction of the realized population size, N_2 , or do we want an estimate of its expected value? We believe the former is the proper quantity for inference about the population size in the second reserve. An estimate of N_2 should include the uncertainty with which the mean is estimated (from reserve 1) and it should also include "process variation" for making the prediction of the latent

As a practical matter, to do a Bayesian analysis of this you could just define the p0325 state-space to be the union of the two state-spaces, increase M so that the posterior of the total population size is not truncated, and then have MCMC generate a posterior sample of individuals on the joint state-space. You can tally up the ones that are on S_2 as an estimate of N_2 . Alternatively, we can define $\mu = \psi M/A_1$ and then simulate posterior samples of N Binomial $(M, \mu A_2/M)$ for the new state-space area, A_2 .

To carry out a classical likelihood analysis of this second type of problem, what p0330 should we do? The argument for making a prediction of a new value of N would go something like this: If you obtain an MLE of N, say N, then the inference procedure tells us the variance of this conditional on N, i.e., $Var(\hat{N}|N)$. This is fine, if we care about the specific value of N that generated our data set. However, if we don't care about the specific one in question then we want to "uncondition" on N to introduce a new variance component. Law of total variance says:

$$Var(\hat{N}) = \mathbb{E}[Var(\hat{N}|N)] + Var[\mathbb{E}(\hat{N}|N)].$$

If \hat{N} is unbiased then we say the unconditional variance is

$$Var(\hat{N}) = \sigma_{\hat{N}}^2 + Var(N).$$

The first part is estimation error and the second component is the "process variance." If you do Bayesian analysis, then you don't have to worry too much about how to compute variances properly. You decide if you care about N, or its expected value, or predictions of some "new" N, and you tabulate the correct posterior distribution from your MCMC output.

The considerations for estimating density are the same. Density can-be N/A_{p0335} where N is the realized population, which we understand it to be unless we put an expectation operator around the N_i like $\mathbb{E}(N)/A$. Classically, density is thought of as

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5.8 The Core SCR Assumptions

being defined as the expected value of N but this might not always be meaningful because the context of whether we mean realized density, of an actual population, or expected density for some hypothetical unspecified population, should matter. The formula for obtaining "expected density" is slightly different depending on whether we assume N has a Poisson distribution or whether we assume a binomial distribution (under data augmentation). In the latter case ψ is related to the point process intensity (see Chapter 11) in the sense that, under the binomial prior:

$$\mathbb{E}(N) = M \times \psi$$

so, what we think of as "density," D, is $D = M\psi/A$. Under the Poisson point process model we have:

$$\mathbb{E}(N) = D \times A.$$

In summary, there are three basic inference problems that relate to estimating ρ0340 population size (or density):

oilso (1) What is the value of N for some population that was sampled. This is what Efford and Fewster call "realized N" In general, we want the uncertainty to reflect having to estimate n_0 , the part of the population not seen.

01185 (2) We need to estimate N for some population that we didn't sample but it is "similar" to the population that we have information on. In this case, we have to account for both variation in having to estimate parameters of the distribution of N and we have to account for process variation in N (i.e., due to the stochastic Comma model of N).

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In some extremely limited cases we might care about estimating the expected value of N, $\mathbb{E}(N)$ This is only useful as a hypothetical statement that we might use, e.g., if we were to establish a new million ha refuge somewhere; then we might say its expected population size is 200 tigers.

5.8 The core SCR assumptions

or exit from the sampled population.

It's always a good idea to sit down and reflect on the meaning of any particular model, its various assumptions, and what they mean in a specific context. From the statistician's point of view, the basic assumption, the omnibus assumption, as in all of statistics, and for every statistical model, is that "the model is correctly specified." So, naturally, that precludes everything that isn't explicitly addressed by the model. To

point this out to someone seems to cause a lot of anxiety, so we enumerate here what we think are the most important statistical assumptions of the basic SCR0 model: Demographic closure. The model does not allow for demographic processes. There is no recruitment or entry into the sampled population. There is no mortality

Geographic closure. We assume no permanent emigration or immigration from the state-space. However, we allow for "temporary" movements around the statespace and variable exposure to encounter as a result. The whole point of SCR

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models is to accommodate this dynamic. In ordinary capture-recapture models we have to assume geographic closure to interpret N in a meaningful way.

Activity centers are randomly distributed. That is, uniformity and independence u0015 of the underlying point process s_1, \ldots, s_N (see next section).

Detection is a function of distance. A detection model that describes how encounter 40020 probability declines as a function of distance from an individual's home range

Independence of encounters among individuals. Encounter of any individual is 10025 independent of encounter of each other individual.

Independence of encounters of the same individual. Encounter of an individual in u0030 any trap is independent of its encounter in any other trap, and subsequent sample occasion.

It's easy to get worried and question the whole SCR enterprise just on the grounds that these assumptions combine to form such a simplistic model, one that surely can't describe the complexity of real gopulations. On this sentiment, a few points are worth making. First, you don't have inherently fewer assumptions by using an ordinary capture-recapture model but, rather, the SCR model relaxes a number of important assumptions compared to the non-spatial counterpart. For one, here, we're not assuming that p is constant for all individuals but rather that p varies substantially as a matter of the spatial juxtaposition of individuals with traps. So maybe the manner in which p varies isn't quite right, but that's not an argument that supports doing less modeling. Fundamentally a distance-based model for p has some basic biological justification in virtually every capture-recapture study. Secondly, for some of these core assumptions such as uniformity, and independence of individuals and of encounters, we expect a fair amount of robustness to departures. They function primarily to allow us to build a model and an estimation scheme and we don't usually think they represent real populations (of course, no model does!). Third, we can extend these assumptions in many different ways and we do that to varying extents in this book, and more work remains to be done in this regard. Fourth, we can also evaluate the reasonableness of the assumptions formally in some cases using standard methods of assessing model fit (Chapter 8).

Finally, we return back to our sentiment about the omnibus assumptions, which is that the model is properly specified. This precludes everything that isn't in the model. Sometimes you see in capture recapture literature statements like "we assume no marks are lost," "marks are correctly identified," and similar things. We might as well also assume that, a shopping mall is not built, or a meteor does not crash down into our study area, the sun does not go super-nova, and so forth. Our point is that we should separate statistical assumptions about model parameters or aspects of the probability model from what are essentially logistical or operational assumptions about how we interpret our data, or based on our ability to conduct the study. It is pointless to enumerate all of the possible explanations for apparent departures, because there are an infinity of such cases.

Entende number of



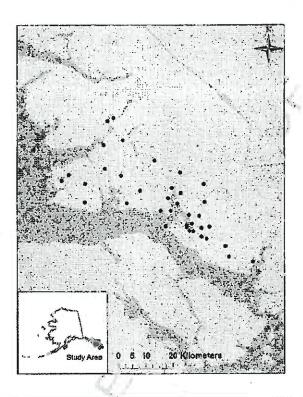


FIGURE 5.4

Wolverine camera trap locations (black dots) from a study that took place in SE Alaska. See Magoun et al. (2011) for details.

EXample:

5.9 Wolverine camera trapping study

We provide an illustration of some of the concepts we've introduced previously in this chapter by analyzing data from a camera trapping data from study of wolverines Gulo gulo (Magoun et al., 2011; Royle et al., 2011b). The study took place in SE Alaska (Figure 5 4) where 37 cameras were operational for variable periods of time (min = 5 days, max = 108 days, median = 45 days). A consequence of this is that the number of sampling occasions, K, is variable for each camera. Thus, we must provide a vector of sample sizes as data to BUGS and modify the model specification in Section 5.7 accordingly.

50110 5.9.1 Practical data organization

p0360 To carry out an analysis of these data, we require the matrix of trap coordinates and the encounter history data. We usually store data in two distinct data files which contain all the information needed for an analysis. These files are:

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The encounter data file (EDF) containing a record of which traps and when each 10035 individual encounter occurred.

The trap deployment file (TDF), which contains the coordinates of each trap, along u6040 with information indicating which sample occasions each trap was operating.

Encounter Data File (EDF)—We store the encounter data in an efficient file format posts which is easily manipulated in R and easy to create in Excel and other spreadsheets which are widely used for data managemen. The file structure is a simple matrix with four columns those being: (1) session ID: the trap session which usually corresponds to a year or a primary period in the context of a Robust Design situation. but it could also correspond to a distinct spatial unit (see Section 6.5.4 and Chapter 14). For a single-year study (as considered here) this should be an integer that is the same for all records; (2) individual ID: the individual identity, being an integer from 1 to n (repeated for multiple captures of the same individual) indicating which individual the record (row) of the matrix belongs to; (3) occasion ID, the integer sample occasion which generated the record; and (4) trap ID: the trap identity, an integer from 1 to J, the number of traps. The structure of the EDF is the same as used in the secr package (Efford, 2011a) and similar to that used in the SPACECAP (Gopalaswamy et al., 2012a), and SCRbayes (Russell et al., 2012) packages, both of which have a 3-column format (trapID, indID, sampID). We note that the naming of the columns is irrelevant as far as anything we do in this book, although secr and other software may have requirements on variable naming.

To illustrate this format, the wolverine data are available in the package scrbook posto by typing:

> data(wolverine)

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which contains a list having elements weaps (the EDF) and wtraps (the TDF). We see that wcaps has 115 rows, each representing a unique encounter event including the trap identity, the individual identity, and the sample occasion index (sample). The first five rows of wcaps are:

> wolverine\$wcaps[1:5,]

	year	individual	day	trap							
[1,]	1	2	127	1							
[2,]	1	2	128	1							
[3.,]		2	129	1							
[4,]	1	18	130	1							
[5,]	1	3	106	2							

The first column here, labeled year, is in integer indicating the year or session of posts the encounter. All these data come from a single year (2008) and so year is set to 1. The Variable individual is an integer identity of each individual captured, day is the sample occasion of capture (in this case, the sample occasions correspond to days), and trap is the integer trap identity. The variable trap d will have to correspond to the row of a matrix containing the trap coordinates—in this case the TDF file wtraps; which we describe further below.

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5.9 Wolverine Camera Trapping Study

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Note that the information provided in this encounter data file wcaps does not represent a completely informative summary of the data. For example, if no individuals were captured in a certain trap or during a certain period, then this compact data format will have no record. Thus we will need to know J, the number of traps, and K, the number of sample occasions when reformatting this SCR data format into a 2-d encounter frequency matrix or 3-d array. In addition, the encounter data file does not provide information about which periods each trap was operated. This additional information is also necessary as the trap-specific sample sizes must be passed to BUGS as data. We provide this information along with trap coordinates, in the "trap deployment file" (TDF) which is described below.

p0385

For our purposes, we need to convert the wcaps file into the $n \times J$ array of binomial encounter frequencies, although more general models might require an encounter-history formulation of the model which requires a full 3-d array. To obtain our encounter frequency matrix, we do this the hard way by first converting the encounter data file into a 3-d array and then summarize to trap totals. We have a handy function, SCR23darray which takes the compact encounter data file and converts it to a 3-d array, and then we use the R function apply to summarize over the sample occasion dimension (by convention here, this is the 2nd dimension). To apply this to the wolverine data in order to compute the 3-d array we do this:

Comma

```
o0900 > y3d <- SCR23darray(wolverine$wcaps,wolverine$wtraps)
o0905 > y <- apply(y3d,c(1,2),sum)</pre>
```

See the help file for more information on SCR23darray. The 3-d array is necessary to fit certain types of models (e.g., behavioral response) and this is why we sometimes will require this maximally informative 3-d data format but, here, we analyze the summarized data.

Trap Deployment File (TDF)—The other important information needed to fit SCR models is the "trap deployment file" (TDF) which provides additional information not contained in the encounter data file. The traps file has K+3 columns. The first column is assumed to be a trap identifier, columns 2 and 3 are the easting and northing coordinates (assumed to be in a Euclidean coordinate system), and columns 4 to K+3 are binary indicators of whether each trap was operational during each sample occasion. The first 10 rows (out of 37) and 10 columns (out of 167) of the trap deployment file for the wolverine data are shown as follows:

```
> wolverine$wtraps[1:10,1:10]
```

	Easting	Northing	1	2	3	4	5	6	7	8
1	632538	6316012	0	0	0	0	0	0	0	0
2	634822	6316568	1	1	1	1	1	1	1	1
3	638455	6309781	0	0	0	0	0	0	0	0
4	634649	6320016	0	0	0	0	0	0	0	0
5	637738	6313994	0	0	0	0	0	0	0	0

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6	625278	6318386	0	0	0	0	0	0	0	0
7	631690	6325157	0	0	0	0	0	0	0	0
8	632631	6316609	0	0	0	0	0	0	0	0
		6331273								
		6328575								

This tells us that trap 2 was operated during occasions (days) 1-7, but the other possible tells us that trap 2 was operated during occasions (days) 1-7, but the other traps were not operational during those periods. It is extremely important to recognize that each trap was operated for a variable period of time and thus the binomial "sample size" is different for each, and this needs to be accounted for in the BUGS model specification. To compute the vector of sample sizes K, and extract the trap locations, we do this:

```
> traps <- wolverine$wtraps
> traplocs <- traps[,1:2]
> K <- apply(traps[,3:ncol(traps)],1,sum)</pre>
                                                                00920
```

This results in a matrix traplocs which contains the coordinates of each trap and a vector K containing the number of days that each trap was operational. We now have all the information required to fit a basic SCR model in BUGS.

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Summarizing the data for the wolverine study, we see that 21 unique individuals p0400 were captured a total of 115 times. Most individuals were captured 1-6 times, with 4, 1, 4, 3, 1, and 2 individuals captured 1-6 times, respectively. In addition, 1 individual was captured each 8 and 14 times and 2 individuals each were captured 10 and 13 times. The number of unique traps that captured a particular individual ranged from 1 to 6, with 5, 10, 3, 1, 1, and 1 individual captured in each of 1-6 different traps, respectively, for a total of 50 unique wolverine-trap encounters. These numbers might be hard to get your mind around whereas some tabular summary is often more convenient. For that it seems natural to tabulate individuals by trap and total encounter frequencies. The spatial information in SCR data is based on multi-trap captures, and so, it is informative to understand how many unique traps each individual is captured in, and the total number of encounters. For the wolverine data, we reproduce Table 5.1 from Royle et al. (2011b) as Table 5.3.

5.9.2 Fitting the model in WinBUGS

Here we fit the simplest SCR model with the Gaussian encounter probability model, although we revisit these data and fit additional models in later chapters. Model SCRO is summarized by the following four elements:

s0115 p0405

```
(1) y_{ij}|s_i \sim \text{Binomial}(K, z_i|p_{ii});
                                                                                                                                                ol 195
(2) p_{ij} = p_0 \exp(-\alpha_1 \|\mathbf{x}_j - \mathbf{s}_i\|^2);
                                                                                                                                                01200
(3) \mathbf{s}_i \sim \text{Uniform}(\mathcal{S});
                                                                                                                                                01205
(4) z_i \sim \text{Bernoulli}(\psi).
                                                                                                                                                01210
```

We assume customary flat priors on the structural (hyper-) parameters of the model, $\alpha_0 = \operatorname{logit}(p_0), \alpha_1 \text{ and } \psi$.

photographed

sp055

Table 5.3 Individual frequencies of capture for wolverines captured in camera traps in SE Alaska in 2008. Rows index unique traps of capture for each individual and columns represent total number of captures (e.g., we captured 4 individuals 1 time, necessarily in only 1 trap; we captured 3 individuals 3 times but in 2 different traps).

	<u> </u>	rollin		meralah 2			*0	de		
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1	4	1	0	0	0	0	0	0	0	0
2	0	0	3	2	0	2	100	2	0	0
3	0	0	1	1	0	0 .	0.	0	0	1
4	0	0	0	0	0	0	.0	0	1	0
5	0	0	0	0	1	0	0	0	0	0
6 1	0	0	0	0	0	0 -	0	0	1	0

Center

p0410

It remains to define the state-space S. For this, we nested the trap array (Figure 5.4) in a rectangular state-space extending 20 km beyond the traps in each cardinal direction. We scaled the coordinate system so that a unit distance was equal to 10 km, producing a rectangular state-space of dimension 9.88 × 10.5 units $(area = 10, 374 \text{ km}^2)$ within which the trap array was nested. As a general rule, we recommend scaling the state-space so that it is defined near the origin (x, y) = (0, 0). While the scaling of the coordinate system is theoretically irrelevant, a poorly scaled coordinate system can produce Markov chains that mix poorly. The buffer of the state-space should be large enough so that individuals beyond the state-space boundary are not likely to be encountered (Section 5.3.1). To evaluate this, we fit models for various choices of a rectangular state-space based on buffers from 1.0 to 5.0 units (10-50 km). In the R package scrbook we provide a function wolvSCR0 which will fit model SCRO. For example, to fit the model in WinBUGS using data augmentation with M = 390 potential individuals, using three Markov chains each of 12,000 total iterations, discarding the first 2000 as burn-in, we execute the following R commands:

& wall activity centers

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augment

00925 > library(scrbook)

00930 > data(wolverine)

00935 > traps < wolverine\$wtraps

00940 > y3d <- SCR23darray(wolverine\$wcaps,wolverine\$wtraps)

o0945 > wolv <- wolvSCR0(y3d,traps,nb=2000,ni=12000,buffer=1,M=300)

The argument buffer determines the buffer size of the state-space in the scaled units (i.e., 10 km). Note that this analysis takes between 1 and 2 h on many machines (in 2013) so we recommend testing it with lower values of M and fewer iterations. The posterior summaries are shown in Table 5.4.

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Table 5.4 Posterior summaries of SCR model parameters for the wolverine camera trapping data from SE Alaska, using state-space buffers from 10 up to 50 km. Each analysis was based on 3 chains, 12,000 iterations, 2000 burn-in, for a total of 30,000 posterior samples.

Buffer		, 0			N			, p	
	Méan	ŚŌ	n.eff	Mean	SD	n.eff :	Mean	ŠĐ 1	n.eff
10	0.65	0.06	1800	39.63	6.70	7100	5.97	1.00	7100
15	0.64	0.06	510	48.77	9.19	3300	5.78	1.09	3300
20	0.64	0.06	1200	59.84	11.89	20,900	5.77	1.15	20,000
25	0.64	0.05	3600	72.40	14.72	2700	5.79	1.18	2700
30	0.63	0.05	5600	86.42	17.98	3900	5.82	1.21	3900
35	0.63	0.05	4500	101.79	21,54	30,000	5.85	1.24	30,000
40	0.64	0.05	410	118.05	26.17	410	5.87	1.30	450
45	0.64	0.05	10,000	134.43	28 68	3300	5.83	1.24	3300
50	0.63	0.05	4700	151.61	31.65	3400	5.79	1.21	3400
1	A - 1-								

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5.9.3 Summary of the wolverine analysis

s0120

We see that the estimated density is roughly consistent as we increase the state-space p0415 buffer from 15 to 55 km. We do note that the data augmentation parameter ψ (and, correspondingly, N) increases with the size of the state-space in accordance with the deterministic relationship (De 1. However, density is more or less constant as we increase the size of the state-space beyond a certain point. For the 10 km state-space buffer, we see a slight effect on the posterior distribution of D because the state-space is not sufficiently large. The full results from the analysis based on 20 km state-space buffer are given in Table 5.5.

Our point estimate of wolverine density from this study, using the posterior mean p0420 from the state-space based on the 20 km buffer, is approximately 5.77 individuals/ Coulcilla 1000 km² with a 95% posterior interval of [3.86, 8.29]. Density is estimated

Table 5.5 Posterior summaries of SCR model parameters for the wolverine camera trapping data from SE Alaska. The model was run with the trap array

	in a state-								
Paramet	er Mean	ŞD.	2.5%	25%	50%	75%	97.5%	l Real	
N	59.84	11.89	40.00	51.00	59.00	67.00	86.00	1	
D	5.77	1.15	3.86	4.92	5.69	6.46	8.29	1	
α_1	1.26	0.21	0.87	1.11	1.25	1.40	1.71	1	
<i>P</i> 0	0.06	0.01	0.04	0.05	0.06	0.06	0.08	1	
σ	0.64	0.06	0.54	0.60	0.63	0.67	0.76	1	

0.17

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0.23

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5.9 Wolverine Camera Trapping Study

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imprecisely which might not be surprising given the low sample size (n = 21 individuals!). This seems to be a basic feature of carnivore studies although it should not (in our view) preclude the study of their populations by capture-recapture nor attempts to estimate density or vital rates.

p0425

It is worth thinking about this model, and these estimates, computed under a rectangular state-space, roughly centered over the trapping array (Figure 5.4). Does it make sense to define the state-space to include, for example, ocean? What are the possible consequences of this? What can we do about it? There's no reason at all that the state-space has to be a regular polygon—we defined it as such here strictly for convenience and for ease of implementation in WinBUGS where it enables us to specify the prior for the activity centers as uniform priors for each coordinate. While it would be possible to define a more realistic state-space using some general polygon GIS coverage, it might take some effort to implement that in the BUGS language but at 1740196 it is not difficult to devise custom MCMC algorithms to do that (see Chapter 17). Alternatively, we recommend using a discrete representation of the state-space—i.e., approximate S by a grid of G points. We discuss this in Section 5.10.

5.9.4 Wolverine space usage

p0430 The parameter α_1 is related to the home range radius (Section 5.4). For the Gaussian model we interpret the scale parameter σ , related to α_1 by $\alpha_1 = 1/(2\sigma^2)$, as the radius of a bivariate normal model of space usage. In this case $\sigma = 0.64$ standardized units (10 km), which corresponds to $0.64 \times 10 = 6.4$ km. It can be argued then that 95% of space used by an individual is within $6.4 \times \sqrt{5.99} = 15.66$ km of the home range center. The effective "home range area" is then the area of this circle, which is $\pi \times 15.66^2 = 770.4 \text{ km}^2$. Using our handy function hra we do this:

hra(pGauss1, parms=c(-2, 1/(2*.64*.64)), xlim=c(-1, 7), ylim=c(-1, 7))

[1] 7.731408 c0955

> which is in units of 100 km². The difference in this case is due to numerical approximation of our all-purpose tool hra. This home range size is relatively huge for measured home ranges; which range between 100 and 535 km² (Whitman et al., l of wolverings

> Royle et al. (2011b) reported estimates for σ in the range 6.3-9.8 km depending on the model, which isn't too different than here. 1 However, these estimates are larger than the typical home range sizes suggested in the literature. One possible explanation is that if a wolverine is using traps as a way to get yummy chicken, so it's moving from trap to trap instead of adhering to "normal" space usage patterns, then the

¹Royle et al. (2011b) expressed the model as $\operatorname{cloglog}(p_{ij}) = \alpha_0 - (1/\sigma^2) * d_{ij}^2$, but the estimates of σ reported in their Table 5.2 are actually based on the model according to cloglog $(p_{ij}) = \alpha_0 - \frac{1}{2\alpha_0} * d_{ij}^2$ and so the estimates of o they report in units of km are consistent to what we report here except based on the complementary log-log (Gaussian hazard) model, instead of the Gaussian encounter probability

model.

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CHAPTER 5 Fully Spatial Capture-Recapture Models

let sure is work getting into the hear movements one more timear, the circular HP assumption will inflate & We had that proble with juguars too

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implied home range size might not be worth finish biologically. Thus, interpretation of detection models in terms of home range area depends on some additional context or assumptions, such as that traps don't effect individual space usage patterns. As such, we caution against direct biological interpretations of home range area based on σ , although SCR models can be extended to handle more general, non-Euclidean, patterns of space usage. See Chapters 12 and 13 σ

We can calibrate the describ size of the state-space by looking at the estimated home range radius of the species. We should target a buffer of width 2 to $3 \times \sigma$ in order that the probability of encountering an individual is very close to 0 beyond the prescribed state-space. Essentially, by specifying a state-space, we're setting p=0 for individuals beyond the prescribed state-space. For the wolverine data, with σ in the range of 6–9 km, a state-space buffer of 20 km is sufficiently large.

5.10 Using a discrete habitat mask

The SCR model developed previously in this chapter assumes that individual activity centers are distributed uniformly over the prescribed state-space. Clearly this will not always be a reasonable assumption. In Chapter 11, we develop models that allow explicitly for non-uniformity of the activity centers by modeling covariate effects on density. A simplistic method of affecting the distribution of activity centers, which we address here, is to modify the shape and organization of the state-space explicitly. For example, we might be able to classify the state-space into distinct blocks of habitat and non-habitat. In that case we can remove the non-habitat from the state-space and assume uniformity of the activity centers ever the remaining portions judged to be suitable habitat. There are several ways to approach this: We can use a grid of points to represent the state-space, i.e., by the set of coordinates s_1, \ldots, s_G , and assign equal probabilities to each possible value. Alternatively, we can retain the continuous formulation of the state-space but attempt to describe constraints analytically, or we can use polygon clipping methods to enforce constraints on the state-space in the MCMC analysis. We focus here on the formulation of the basic SCR model in terms of a discrete state-space but in Chapter 17, we demonstrate the latter approach based on using polygon operations to define an integular state-space. Use of a discrete statespace can be computationally expensive in WinBUGS. That said, it isn't too difficult to perform the MCMC calculations in R (discussed in Chapter 17). The R package SFACECAP (Gopalaswamy et al., 2012a) arose from the R implementation of the SCR model in Royle et al. (2009a) Was Meticated by This, 500 gm,

While clipping out non-habitat seems like a good idea, we think investigators should go about this very cautiously. We might prefer to do it when non-habitat represents a clear-cut restriction on the state-space such as a reserve boundary or a lake, ocean, or river. But, having the capability to do this also causes people to start defining "habitat" vs. "non-habitat" based on their understanding of the system whereas it can't be known whether the animal being studied has the same understanding. Moreover, differentiating the landscape by habitat or habitat quality must affect the geometry

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5.10 Using a Discrete Habitat Mask 161

and morphology of home ranges (see Chapter 13) much more so than the plausible locations of activity centers. That is, a home range centroid could, in actual fact, occurin a shopping mall parking lot if there is pretty good habitat around the shopping mall, so there is probably no sense preclude it as the location for an activity center. It would generally be better to include some definition of habitat quality in the model for the detection probability (Royle et al., 2013) which we address in Chapters 12 and 13.

5.10.1 Evaluation of coarseness of habitat mask

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The coarseness of the state-space should not really have much of an effect on estimates if the grain is sufficiently fine relative to typical animal home range sizes. Why is this? We have two analogies that can help us understand! First is the relationship to model M_h . As noted in Section 5.3.2 above, we can think about SCR models as a type of finite mixture (Norris and Pollock, 1996; Pledger, 2004) where we are fortunate to be able to obtain direct information about which group individuals belong to (group being location of activity center). In the standard finite-mixture models we typically find that a small number of groups (e.g., 2 or 3 at the most) can explain high levels of heterogeneity and are adequate for most data sets of small to moderate sample sizes. We therefore expect a similar effect in SCR models when we discretize the state-space. We can also think about discretizing the state-space as being related to numerical integration where we find (see Chapter 6) that we don't need a very fine grid of support points to evaluate the integral to a reasonable level of accuracy. We demonstrate this here by reanalyzing simulated data using a state-space defined by a different number of support points. We provide an R script called SCRObayesDss in the R package scrbook. We note that for this comparison we generated the actual activity centers as a continuous random variable and thus the discrete state-space is, strictly speaking, an approximation to truth. That said, we regard all state-space specifications as approximations to truth in the sense that they represent a component of the SCR model.

As with our \mathbf{R} function SCR0bayes, the modification SCR0bayesDss will use either WinBUGS or JAGS. In addition, it requires a grid resolution argument (ng) which is the dimension of 1 side of a square state-space. To execute this function we do, for example:

simSCRO (discard0=TRUE, rnd=2013) # Generate data set

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out1 < SCRObayesDss (data,ng=8,M=200,engine="jags",ni=2000,nb=1000)

Run with WinBUGS a0980

out2 <- SCRObayesDas (data,ng=8,M=200,engine="winbugs",ni=2000,nb=1000)

p0465

We fit this model to the same simulated data set for 6×6 , 9×9 , 12×12 , 15×15 state-space grids. For WinBUGS, we used 3 chains of 5000 total length with 1000 burn-in, which yields 12,000 total posterior samples. Summary results are shown in

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Table 5.6 Comparison of the effect of state-space grid coarseness on estimates of N for a simulated data set. Posterior summaries and runtime are given. Results obtained using WinBUGS run from R2WinBUGS.

Grid Size	Mean	SD	NaiveSE	Time seriesSI	: : : : : : : : : : : : : : : : : : :
6×6	111.6699	16.61414	0.1516657	0.682008	2274
9×9	114.2294	17.99109	0.1642355	0.833294	4300
12 × 12	115,9806	17.3843	0,1586964	0.762756	لر7100
15 × 15	115.379	17.93721	0.1637436	0.832483/	13,010

Table 5.6. The results are broadly consistent except for the 6×6 case. We see that the runtime increases with the size of the state-space grid (not unexpected), such that we imagine it would be impractical to run models with more than a few hundred state-space grid points. We found (not shown here) that the runtime of JAGS is much faster and, furthermore, relatively constant as we increase the grid size. We suspect that WinBUGS is evaluating the full conditional for each activity center at all G possible values whereas it may be that JAGS is evaluating the full conditional only at a subset of values or perhaps using previous calculations more effectively. While this might suggest that one should always use JAGS for this analysis, we found in our analysis of the wolverine (next section) that JAGS could be extremely sensitive to starting values, producing MCMC algorithms that often simply do not work for some problems, so be careful when using JAGS. To improve its performance, always start the latent activity centers at values near where individuals were captured. The performance of either should improve if we compute the full distance matrix outside of BUGS and pass it as data, although we haven't fully evaluated this approach.

5.10.2 Analysis of the wolverine camera trapping data

We reanalyzed the wolverine data using discrete state-space grids with points spaced by 2, 4, and 8 km (see Figure 5.5). These were constructed from a 40 km buffered state-space, and deleting the points over water (see Royle et al., 2011b). Our interest in doing this was to evaluate the relative influence of grid resolution on estimated density, 5 because the coarser grids will be more efficient from a computational standpoint and so we would prefer to use them, but only if there is no strong influence on estimated density. The posterior summaries for the three habitat grids are given in Table 5.7. We see that the density estimates are quite a bit larger than obtained in our analysis (Table 5.4) based on a rectangular, continuous state-space. We also see that there are slight differences depending on the resolution of the state-space grid. Interestingly, the effectiveness of the MCMC algorithms, as measured by effective sample size (n.eff), is pretty remarkably different. Furthermore, the finest grid resolution (2 km spacing) took about 6 days to run and thus it would not be practical for large problems or with many models.

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5.11 Summarizing Density and Activity Center Locations

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FIGURE 5,5~ 1 Tate Apale

Three habitat mask grids used in the comparison of the effect of pixel size on the estimated density surface of wolverines. The three cases are 2 (left), 4 (center), and 8 (right) km spacing of state-space points, extending 40 km from the vicinity of the trap array.

38-km (right)

5.11 Summarizing density and activity center locations

One of the most useful aspects of SCR models is that they are parameterized in terms of individual locations—i.e., where each individual lives—and, thus, we can compute many useful and interesting summaries of the activity centers using output from an MCMC simulation, including maps of density (the number of activity centers per unit area), estimates of N for any well-defined polygon, or estimates of where the activity centers for specific individuals reside. In Bayesian analysis by MCMC, obtaining such summaries entails no added calculations, because we need only post-process the output for the individual activity centers to obtain the desired summaries. We demonstrate that in this section. Note that you have to be sure to retain the MCMC history for the s variables and the data augmentation variables in order to do the following analyses.

Functions of ?

0150 5.11.1 Constructing density maps

Because SCR models are spatially explicit, it is natural to want to summarize the results of fitting a model by producing a map of density. Using Bayesian analysis by MCMC, it is most easy to make a map of realized density. We can do this by tallying up the number of activity centers s_i in pixels of arbitrary size and then producing a nice multi-color spatial plot of the result. Specifically, let B(x) indicate a pixel centered

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County at x then

$$N(\mathbf{x}) = \sum_{i=1}^{M} I(\mathbf{s}_i \in B(\mathbf{x}))$$

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Table 5.7 Posterior summaries for the wolverine camera trapping data, using model SCRO, with a Gaussian hazard encounter probability model, and a discrete habitat mask of three different resolutions: 2, 4, and 8 km. Parameters are $\lambda_0 = \text{baseline encounter rate}$, $p_0 = 1 - \exp(-\lambda_0)$, σ is the scale parameter of the Gaussian kernel, ψ is the data augmentation parameter, N and D are population size and density, respectively. Models fitted using WinBUGS, 3 chains, each with 11,000 iterations (first 1000 discarded) producing 30,000 posterior samples

posterior samples.									
	Mean .	SD ·	2.5%	25%	50%	75%	97.5%	Riat	n.eff
2 k	m spaçin	7						MA.	
N	86.56	16.94	57.00	75.00	85.00	97.00	124.00	1.00	510
D	8.78	1.72	5.78	7.60	8.62	9.83	12.57	1.00	510
λ_0	0.05	0.01	0.04	0.04	0.05	0.06	0.07	1.01	320
P ₀	0.05	0.01	0.03	0.04	0.05	0.05	0.06	1.01	320
σ	0.62	0.05	0.54	0.59	0.62	0.65	0.73	1.01	160
ψ	0.43	0.09	0.27	0.37	0.43	0.49	0.63	1.00	560
4 kn	n spacing						40. 40. 46	187	A COLUMN
N	89.25	17.44	59.00	77.00	88.00	100.00	127.00	10 00	1100
D	9.01	1.76	5.96	7.77	8.88	10.10	12.82/	1,00	1100
λ_0	0.05	0.01	0.04	0.05	0.05	0.06	0.07	1,00	2500
p_0	0.05	0.01	0.03	0.04	0.05	0.05	0.07	1,00	2500
σ	0.61	0.04	0.53	0.58	0.61	0.64	0.71	1.0	1600
Ψ	0.45	0.09	0.28	0.38	0.44	0.50	0.64	1.00/	1300
8 kn	n spacing		# 19 No. 1				25/24		
N	83,18	16.14	56.00	72.00	82.00	93.00	119.00	1.00	700
D	8.28	1.67	5.57	7.17	8.16	9.26	11.84	1.00	700
λο	0.05	0.01	0.03	0.04	0.05	0.05	0.06	1.00	560
$p_{\mathbb{Q}}$	0.05	.0.01	0.03	0.04	0.04	0.05	0.06	1.00	560
σ	0.68	0.05	0.59	0.64	0.67	0.71	0.77	1.01	220
	0.40	.0.00	0.00						~~~

(here, I(arg) is the indicator function which evaluates to 1 if arg is true, and 0 otherwise) is the population size of pixel B(x), and $D(x) = N(x)/\|B(x)\|$ is the local density. Note that these N(x) parameters are just "derived parameters" as we normally obtain from posterior output using the appropriate Monte Carlo average (see Chapter 3).

0.41

0.47

0.61

1.00

940

One thing to be careful about, in the context of models in which N is unknown, p0485 is that, for each MCMC iteration m, we only tabulate those activity centers which correspond to individuals in the sampled population, i.e., for which the data augmentation variable $z_i = 1$. In this case, we take all of the output for MCMC iterations m = 1, 2, ..., niter and compute this summary:

0.42

0.09

0.26

0.36

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5.11 Summarizing Density and Activity Center Locations

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$$N(\mathbf{x},m) = \sum_{i:\mathbf{z}_{i,m}=1} I(\mathbf{s}_{i,m} \in B(\mathbf{x})).$$

Thus, N(x, 1), N(x, 2), ..., is the Markov chain for parameter N(x). In what follows we will provide a set of R commands for doing this calculation and making a basic image plot from the MCMC output:

Step 1: Define the center points of each pixel B(x), or point at which local density p1215 will be estimated:

> xg <- seq(xlim[1],xlim[2],,,50) 00990

yg <- seq(ylim[1],ylim[2],,50)</pre> o0995

Step 2: Extract the MCMC histories for the activity centers and the data augmentation variables. Note that these are each $N \times \text{niter}$ matrices. Here we do this assuming that WinBUGS was run producing the R object named out:

> Sxout <- out\$sims.list\$s[, ,1] 01000

01005 > Syout <- out\$sims.list\$s[,.,2]</pre>

z <- out\$sims.list\$z 01010

Step 3: We associate each coordinate with the proper pixel using the R command cut M. Note that we keep only the activity centers for which z = 1 (i.e., individuals that belong to the population of size N):

> Sxout <- cut(Sxout[z==1], breaks=xg, include.lowest=TRUE) 01015

> Syout <- cut (Syout [z==1], breaks=yq, include.lowest=TRUE) 01020

Step 4: Use the table of command to tally up how many activity centers are in 01230 each B(x):

> Dn <- table(Sxout, Syout) 01025

p0490

Step 5: Use the image of command to display the resulting matrix: 01235

> image(xg, yg, Dn/nrow(z), col=terrain.colors(10)) 01030

We'll work Through Tit allis This and 145's To The It is worth emphasizing here that density maps will not usually appear uniform

despite that we have assumed that activity centers are uniformly distributed. This is because the observed encounters of individuals provide direct information about the location of the i = 1, 2, ..., n activity centers and thus their "estimated" locations will be affected by the observations. In a limiting sense, were we to sample space intensely enough, every individual would be captured a number of times and we would have considerable information about all N point locations. Consequently, the uniform prior would have almost no influence at all on the estimated density surface in this limiting situation. Thus, in practice, the influence of the uniformity assumption decreases as the fraction of the population encountered, and the total number of encounters per individual, increases.

On the non-intuitiveness of image M—the R function image M, invoked for a matrix M by image M, might not be very intuitive to some—it plots M[1,1] in the lower left corner. If you want M[] to be plotted "as you look at it" then M[1,1] should be in the upper left corner. We have a function rot M which does that. If you do image (rot M) then it puts it on the monitor as if it was a map you were looking at. You can always specify the M and M labels explicitly as we did above.

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Spatial dot plots—A cruder version of the density map can be made using our posson "spatial dot map" function spatial.plot (in scrbook). This function requires, as input, point locations and the value to be displayed. A simplified version of this function is as follows:

```
> spatial.plot <- function(x,y){</pre>
                                                                  01035
    nc <- as.numeric(cut(y,20))</pre>
                                                                  01040
    plot(x,pch=" ")
                                                                  o1045
    points(x,pch=20,col=topo.colors(20)[nc],cex=2)
                                                                  01050
    image.scale(y,col=topo.colors(20))
                                                                  o1055
                                                                  o1060
                                                                  01065
 To execute the function do this:
                                                                  01070
                                                                  01075
 spatial.plot(cbind(xg,yg), Dn/nrow(z))
                                                                  01080
```

5.11.2 Example: Wolverine density map

We return to the wolverine study which took place an 2005 in SE Alaska (Figure 5.4) and we produce a density map of wolverines from that analysis. We include the function SCRdensity which requires a specific data structure as shown below. In particular, we have to package up the MCMC history for the activity centers and the data augmentation variables into a list. This also requires that we add those variables to the parameters-to-be-monitored list when we pass things to BUGS.

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We used the posterior output from the wolverine model fitted previously to compute a relatively coarse version of a density map, using 100 pixels in a 10×10 grid (Figure 5.6 top panel) and using 900 pixels arranged in a 30×30 grid (Figure 5.6 lower panel) for a fine-scale map. The R commands for producing such a plot (for a short MCMC run) are as follows:

```
> library(scrbook)
                                                                             01085
> data(wolverine)
                                                                             01090
5. Sraps <- wolverine$wtraps</p>
                                                                             o1095
> y3d <- SCR23darray(wolverine$wcaps,wolverine$wtraps)
                                                                             o1100
# This takes 341 seconds on a standard CPU circa 2011
                                                                             01105
 out <- wolvSCR0(y3d,traps,nb=1000,ni=2000,buffer=1,M=100,keepz=TRUE)
                                                                            01110
> Sx <- out$sims.list$s[,,1]
                                                                             01115
> Sy <- out$sims.list$s[,,2]
                                                                             o1120
> 🌋 <- out$sims.list$z
                                                                             01125
```

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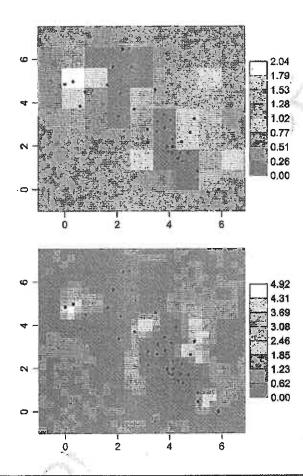


FIGURE 5.6

Density of wolverines (individuals per 100 km²) in SE Alaska in 2007 based on model SCRO. Map grid cells are about 103.7 km² (top panel) and 11.5 km² (bottom panel) in area. Dots are the trap locations.

```
oil30 > obj <- list(5x=Sx,Sy=Sy,z=z)
oil35 > tmp <- SCRdensity(obj,nx=10,ny=10,scalein=100,scalecut=100)
```

In these figures density is expressed in units of individuals per 100 km², while the area of the pixels is about 103.7 km² and 11.5 km², respectively. That calculation is based on:

```
oli40 > total.area <- (ylim[2]-ylim[1])*(xlim[2]-xlim[1])*100
oli45 > total.area/(10*10)
oli50 [1] 103.7427
oli55 > total.area/(30*30)
```

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ol160 [1] 11.52697

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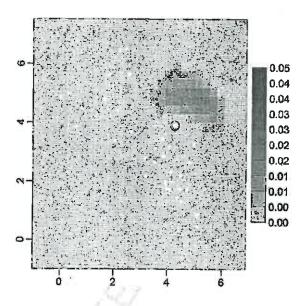


FIGURE 5.7

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Posterior probability distribution of s1, the activity center for individual 1 in the wolverine data set. This individual was captured a single time in one trap (trap 30) which is circled. White dots are trap locations.

A couple of things are worth noting: First is that as we move away from "where posis the data live" Haway from the trap array we see that the density approaches the mean density. This is a property of the estimator as long as the detection function decreases sufficiently rapidly as a function of distance. Relatedly, it is also a property of statistical smoothers such as splines, kernel smoothers, and regression smoothers predictions tend toward the global mean as the influence of data diminishes. Another way to think of it is that it is a consequence of the prior, which imposes uniformity, and as you get far away from the data, the predictions tend to the expected constant density under the prior. Another thing to note about this map is that density is not 0 over water (although the coastline is not shown). This might be perplexing to some who are fairly certain that wolverines do not like water. However, there is nothing about the model that recognizes water from non-water and so the model predicts over water as if it were habitat similar to that within which the array is nested. But, all of this is OK as far as estimating density goes and, furthermore, we can compute valid estimates of N over any well-defined region which presumably wouldn't include water if we so wished. Alternatively, areas covered by water could be masked out, which we discuss in the next section.

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5.12 Effective Sample Area

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s0160 5.11.3 Predicting where an individual lives

The density maps in the previous section show the expected number of individuals per unit area. A closely related problem is that of producing a map of the probable location of a specific individual's activity center. For any observed encounter history, we can easily generate a posterior distribution of s_i for individual. In addition, for an individual that is not captured, we can use the MCMC output to produce a corresponding plot of where such an individual might live, say s_{n+1} . Obviously, all such uncaptured individuals (for i = n + 1, ..., N) should have the same posterior distribution. To illustrate, we show the posterior distribution of s_1 , the activity center for the individual labeled 1 in the data set, in Figure 5.7. This individual was captured a single time at trap 30_i which is circled in Figure 5.7. We see that the posterior distribution is affected by traps of capture and traps of non-capture in fairly intuitive ways. In particular, because there are other traps in close proximity to trap 30_i in which individual 1 was not captured, the model pushes its activity center away from the trap array. The help file for SCRdensity shows how to calculate Figure 5.7.

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5.12 Effective sample area

One of the key issues in using ordinary capture recapture models which we've brought up over and over again is this issue that the area which is sampled by a trapping array is unknown—in other words, the N that is estimated by capture-recapture models does not have an explicit region of space associated with it. Classically, this has been addressed in the ad hoc way of prescribing an area that contains the trap array, usually by adding a buffer of some width, which is not estimated as part of the capture-recapture model. In SCR models we avoid the problem of not having an explicit linkage between N and "area," by prescribing explicitly the area within which the underlying point process is defined—the state-space of the point process. This state space is not the effective earnple (or sampled) area (ESA)—it is desirable that it be somewhat larger than the ESA, whatever that may be, in the sense that individuals at the edge of the state-space have no probability of being captured, but as part of the SCR model we don't need to try to estimate or otherwise characterize the ESA explicitly.

However, trispossible to provide a characterization of effective sampled area under any SCR model. This is directly analogous to the calculation of "effective strip width" in distance sampling (Buckland et al., 2001; Borchers et al., 2002). The conceptual definition of ESA follows from equating density to "apparent density"—ESA is the magic number that satisfies that equivalence:

D = N/A = n/ESA.

In other words, the ratio of N to the area of the state-space should be equal to the ratio of the observed sample size n to this number ESA. Both of these should equal density. So, to compute ESA for a model, we substitute $\mathbb{E}(n)$ for n into the above

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equation, and solve for ESA, to get:

$$ESA = \mathbb{E}(n)/D$$
.

Our following development assumes that D is constant, but these calculations can be generalized to allow for D to vary spatially. Imagine our habitat mask for the wolverine data, or the bins we just used to produce a density map, then we can write $\mathbb{E}(n)$ according to

$$\mathbb{E}(n) = \sum_{s} \Pr(\text{encounter}|s) \mathbb{E}(N(s)),$$

where if we prefer to think of this more conceptually we could replace the summation with an integration (which, in practice, we would just replace with a summation, and so we just begin there). In this expression note that $\mathbb{E}(N(s))$ is the expected population size at pixel s which is the density times the area of the pixel, i.e., $\mathbb{E}(N(s)) = D \times a$.

Therefore

$$\mathbb{E}(n) = D \times a \times \sum_{s} \Pr(\text{encounter}|\mathbf{s}) \qquad \text{Conv}$$

and (plugging this into the expression-above for ESA)

$$ESA = \frac{D \times a \times \sum_{s} Pr(\text{encounter}|\mathbf{s})}{D}.$$

We see that D cancels and we have ESA = $a \times \sum_{s} Pr(\text{encounter}|s)$. So what you have to do here is substitute in Pr(encounter|s) and just sum them up over all pixels. For the Bernoulli model of model SCR0

$$Pr(\text{encounter}|\mathbf{s}) = 1 - (1 - p(\mathbf{s}))^{K}$$

with slight modifications when encounter probability depends on covariates. Thus,

$$ESA = a \sum_{s} (1 - (1 - p(s))^{k})_{o}$$
 (5.12.1)

Clearly the calculation of ESA is affected by the use of a habitat mask, because the summation in Eq. (5.12.1) only occurs over pixels that define the state-space.

For the wolverine camera trapping data, we used the 2 x 2 km habitat mask and posss the posterior means of p_0 and σ (see Section 5.10.2) to compute the probability of encounter for each s of the mask points. The result is shown graphically in Figure 5.8. The ESA is the sum of the values plotted in that figure multiplied by 4, the area of each pixel. For the wolverine study, the result is 2507.152 km². We note that the probability of encounter declines rapidly to 0 as we move away from the periphery of the camera traps, indicating the state-space constructed from a 40 km buffered trap array was indeed sufficient for the analysis of these data. An R script for producing this figure is in the wolvESA function of the scrbook package.

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5.13 Summary and outlook

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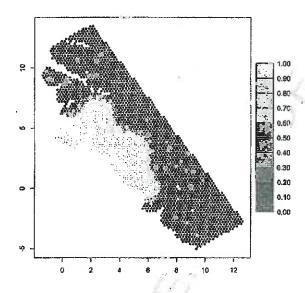


FIGURE 5.8

Probability of encounter used in computing effective sampled area for the wolverine camera trapping array, using the parameter estimates (posterior means) for the 2×2 km habitat mask.

5.13 Summary and outlook

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In this chapter, we introduced the simplest SCR model—"model SCR0"—which is an ordinary capture-recapture model like model M_0 , but augmented with a set of latent individual effects, s_i , which relate encounter probability to some sense of individual location using a covariate, "distance," from s_i to each trap location. Thus, individuals in close proximity to a trap will have a higher probability of encounter, and vice versa. The explicit modeling of individual locations and distance in this fashion resolves classical problems related to estimating density; unknown sample area, and heterogeneous encounter probability due to variable exposure to traps.

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SCR models are closely related to classical individual covariate models ("model M_x ," as introduced in Chapter 4), but with imperfect information about the individual covariate. Therefore, they are also not too dissimilar from standard GLMMs used throughout statistics and, as a result, we find that they are easy to analyze using standard MCMC methods encased in black boxes such as WinBUGS or JAGS. We will also see that they are easy to analyze using likelihood methods, which we address in Chapter 6.

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Formal consideration of the collection of individual locations (s_1, \ldots, s_N) is fundamental to all models considered in this book. In statistical terminology, we think of

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the collection of points (sc) as a realization of a point process. Because SCR models formally link individual encounter history data to an underlying point process, we can obtain formal inferences about the point process. For example, we showed how to produce a density map (Figure 5.6), or even a probability map for an individual's home range center (Figure 5.7). We can also use SCR models as the basis for doing more traditional point process analyses, such as testing for "complete spatial randomness" (CSR) (see Chapter 8), and computing other point process summaries (Illian et al., 2008).

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Part of the promise, and ongoing challenge, of SCR models is to develop models that reflect interesting biological processes, for example interactions among points or temporal dynamics in point locations. In this chapter we considered the simplest possible point process model in which points are independent and uniformly ("randomly") distributed over space. Despite the simplicity of this model, it should suffice in many applications of SCR models, although we do address generalizations in later chapters. Moreover, even though the prior distribution on the point locations is uniform, the realized pattern may deviate markedly from uniformity as the observed encounter data provide information to impart deviations from uniformity. Thus, estimated density maps will typically appear distinctly non-uniform (as we saw in the wolverine example). In applications of the basic SCR model, we find that this simple a priori model can effectively reflect or adapt to complex realizations of the underlying point process. For example, if individuals are highly territorial then the data should indicate this in the form of individuals not being encountered in the same trapy the resulting posterior distribution of point locations should therefore reflect non-independence. Obviously the complexity of posterior estimates of the point pattern will depend on the quantity of data, both number of individuals and captures per individual. Because the point process is such an integral component of SCR models, the state-space of the point process plays an important role in developing SCR models. As we emphasized in this chapter, the state-space is part of the model. It can have an influence on parameter estimates and other inferences, such as model selection (see Chapter 8).

One concept we introduced in this chapter, which has not been discussed much in the literature on SCR models, is the manner in which the encounter probability model relates to a model of space usage by individuals. The standard SCR models of encounter probability can all be motivated as simplistic models of space usage and movement, in which individuals make random use decisions from a probability distribution proportional to the encounter probability model. This both-clarifies the simplicity of the underlying model of space usage and suggests a direct extension to produce more realistic models, which we discuss in Chapter 13. We consider some other important extensions of the basic SCR model in later chapters. For example, we consider models that include covariates that vary by individual, trap, or over time (Chapter 7), spatial covariates on density (Chapter 11), open populations (Chapter 16) fund methods for model accessment and selection (Chapter 8) among other topics. We also consider technical details of maximum likelihood (Chapter 6) and Bayesian (Chapter 17) estimation, so that the interested reader can develop or extend methods to suit their own needs.

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Abstract: In this chapter we investigate the basic spatial capture-recapture model, which we refer to as "model SCR0." The model is a hierarchical model composed of two conditionally-related components: (1) a spatial point process describing the number and location of animal activity centers and (2) an observation model specifying capture or encounter probability as a function of the distance between individual activity centers and traps. As with all models, it includes several assumptions that must be understood and critically evaluated. We list the basic assumptions of SCR models and we provide some basic tools for simulating spatial capturerecapture data in R, so that the assumptions and properties of the model can be fully appreciated. The chapter also focuses on practical issues such as common sampling designs and how to format the resulting data. For inference, we focus on Bayesian methods using Markov chain Monte Carlo and data augmentation. Likelihood methods are covered in the next-chapter An example analysis is presented using wolverine data collected in southern Alaska, and this example demonstrates how to summarize posterior output for the purposes of producing posterior density maps and computing derived quantities such as the effective sample area.

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Keywords: Activity center, Bayesian inference, Data format, Observation model,

Sampling design, Spatial point process

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