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Alternative Observation Models

9

p0005 In previous chapters we considered various models of *encounter probability*, both in terms of parametric functions of distance and also a ~~myriad~~ of covariate models (Chapter 7 and elsewhere). However, we have so far only considered a specific probability model for the observations (we'll call this the “observation model”)—the Bernoulli ~~encounter process~~ model which, in `secr`, is the *proximity detector* model. This assumes that individual- and trap-specific encounters are independent Bernoulli trials.

p0010 In this chapter, we focus on developing additional observation models. The observation model could be thought of as being determined by the type of device—or the type of “detector” using the terminology of `secr` (Efford, 2011a). We consider models that apply when observations are not binary and, in some cases, that do not require independence of the observations. ~~We present models when the data are encounter frequencies, based on the Poisson distribution, and observation models based on the multinomial distribution.~~ For example, if sampling devices can detect an individual some arbitrary number of times during an interval, then it is natural to consider observation models for encounter frequencies, such as the Poisson model. Another type of encounter device is the “multi-catch” device (Efford et al., 2009a) which is a physical device that can capture and hold an arbitrary number of individuals. A typical example is a mist net for birds (Borchers and Efford, 2008). It is natural to regard observations from these kinds of studies as independent multinomial observations. A related type of device that produces *dependent* multinomial observations are the so-called *single-catch* traps (Efford, 2004; Efford et al., 2009a). The canonical example are small-mammal live traps which catch and hold a single individual. Competition among individuals for traps induces a complex dependence structure among individual encounters. To date, no formal inference framework has been devised for this method although it stands to reason that the independent multinomial model should be a good approximation in some situations (Efford et al., 2009a). We analyze a number of examples of these different observation models using **JAGS** and also the **R** package `secr` (Efford, 2011a).

9.1 Poisson observation model

s0005

The models we analyze in Chapter 5 assumed binary observations—i.e., standard encounter history data—so that individuals are captured at most one time in a trap on any given sample occasion. This makes sense for many types of DNA sampling (e.g., based on hair snares) because distinct visits to sampled locations or devices cannot be differentiated. However, for some encounter devices, or methods, the potential number of encounters is *not* fixed, and so it is possible to encounter an individual some arbitrary number of times during any particular sampling episode. That is, we might observe encounter frequencies $y_{ijk} > 1$ for individual i , trap j , and sampling interval k . As an example, if a camera device is functioning properly it may be programmed to take photos every few seconds if triggered. For a second example, suppose we are searching a quadrat or length of trail for scat, we may find multiple samples from the same individual. Therefore, we seek observation models that accommodate such encounter frequency data. In general, any discrete probability mass function could be used for this purpose, including the standard models for count data used throughout ecology, the Poisson, and negative binomial. Here we focus on using the Poisson model only although other count frequency models are possible for SCR models (Efford et al., 2009b).

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Let y_{ijk} be the frequency of encounter for individual i , in trap j , during occasion k , then assume:

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$$y_{ijk} \sim \text{Poisson}(\lambda_{ij}),$$

where the expected encounter frequency λ_{ij} depends on both individual and trap. As we did in the binary model of Chapter 5, we now seek to model the expected value of the observation (which was p_{ij} in Chapter 5) as a function of the individual activity center \mathbf{s}_i . We propose

$$\lambda_{ij} = \lambda_0 k(\mathbf{x}_j, \mathbf{s}_i),$$

where $k(\mathbf{x}, \mathbf{s})$ is any positive valued function, such as the negative exponential or the bivariate Gaussian kernel, and λ_0 is the baseline encounter rate—the expected number of encounters if a trap is placed precisely at an individual's home-range center (note: in secr the notation for this is g_0). Then, $\lambda_0 k(\mathbf{x}_j, \mathbf{s}_i)$ is the expected encounter rate in trap \mathbf{x}_j for an individual having activity center \mathbf{s}_i . Note that

$$\log(\lambda_{ij}) = \log(\lambda_0) + \log(k(\mathbf{x}_j, \mathbf{s}_i)).$$

Equating $\alpha_0 \equiv \log(\lambda_0)$, and, if $k(\mathbf{x}, \mathbf{s}) \equiv \exp(-d(\mathbf{x}, \mathbf{s})^2/(2\sigma^2))$ (i.e., the Gaussian model), then:

$$\log(\lambda_{ij}) = \alpha_0 - \alpha_1 d(\mathbf{x}_j, \mathbf{s}_i)^2, \quad (9.1.1)$$

where $\alpha_1 = 1/(2\sigma^2)$, which is the same linear predictor as we have seen for the Bernoulli model in Chapter 5. This Poisson SCR model is therefore a type of Poisson generalized linear mixed model (GLMM).

We can accommodate covariates at the level of individual-, trap-, or sample-occasion by including them on the baseline encounter rate parameter λ_0 . For example,

p0025

if C_j is some covariate that depends on trap only, then we express the relationship between λ_0 and C_j as:

$$\log(\lambda_{0,ijk}) = \alpha_0 + \alpha_2 C_j$$

and therefore covariates on the logarithm of baseline encounter probability appear also as linear effects on λ_{ij} . In general, covariates might also affect the coefficient on the distance term (α_1) (e.g., sex of individual). We don't get into too much discussion of general covariate models here, ~~but we covered them in some detail in both Chapters 7 and 8.~~

p0030 For models in which we do not have covariates that vary across the sample occasions k , we can aggregate the observed data by the property of compound additivity of the Poisson distribution (if x and y are *iid* Poisson with mean λ then $x + y$ is Poisson with mean 2λ). Therefore,

$$y_{ij} = \left(\sum_{k=1}^K y_{ijk} \right) = \text{Poisson}(K \lambda_{0k}(\mathbf{x}_j, \mathbf{s}_i)).$$

We see that K and λ_0 serve the same role as affecting the base encounter rate. Since the observation model is the same, probabilistically speaking, for all values of K , evidently we need only $K = 1$ “survey” from which to estimate model parameters (Efford et al., 2009b). We know this intuitively, as sampling by multiple traps serves as replication in SCR models. This has great practical relevance to the conduct of capture-recapture studies and the use of SCR models. For example, if individuality is obtained by genetic information from scat sampling, one should only have to carry out a single spatial sampling of the study area. However, one must be certain that sufficient spatial recaptures will be obtained so that effective estimation is possible.

s0010 9.1.1 Poisson model of space usage

p0035 It is natural to interpret the Poisson encounter model as a model of space usage resulting from movement of individuals about their home range (Section 5.4). Imagine we have perfect samplers in every pixel of the landscape so that whenever an individual moves from one pixel to another, we can record it. Let m_{ij} be the number of times individual i was recorded in pixel j (i.e., it selected or used pixel j). Then, we might think of the Poisson model for the observed *use* frequencies:

$$m_{ij} \sim \text{Poisson}(\lambda_{0k}(\mathbf{x}_j, \mathbf{s}_i)),$$

where λ_0 is related to the baseline movement rate of the animal (how often it moves). This model of space usage gives rise to the standard resource selection function (RSF) models (see Chapter 13). But now suppose our samplers are not perfect but, rather, record only a fraction of the resulting visits. A sensible model is

$$y_{ij} | m_{ij} \sim \text{Binomial}(m_{ij}, p).$$

The marginal distribution of y_{ij} is:

$$y_{ij} \sim \text{Poisson}(p \lambda_{0k}(\mathbf{x}_j, \mathbf{s}_i)).$$

where p_0 is a composite of the movement rate and conditional detection probability p . Therefore, we see that encounters accumulate in proportion to the frequency of outcomes of an individual using space (or “selecting resources”).

We introduced an interpretation of SCR models in terms of movement and space usage in Section 5.4, and it is one of the main underlying concepts of SCR models that is not present in ordinary capture-recapture models. As we noted there, the underlying model of space usage is only as complex as the encounter probability model which has been, so far in this book, only symmetric and stationary (does not vary in space). We generalize this model of space usage substantially in Chapter 13.

9.1.2 Poisson relationship to the Bernoulli model

There is a sense in which the Poisson and Bernoulli models can be viewed as consistent with one another. Note that under the Poisson model, the relationship between the expected count and the probability of counting “at least 1” is given by

$$\Pr(y > 0) = 1 - \exp(-\lambda), \quad (9.1.2)$$

where $\mathbb{E}(y) = \lambda$. Therefore, if we equate the event “encountered” with the event that the individual was captured at least 1 time under the Poisson model, i.e., $y > 0$, then it would be natural to set $p_{ij} = \Pr(y > 0)$ according to Eq. (9.1.2). That is, we can use Eq. (9.1.2) as the model for encounter probability for binary observations. This is the “hazard rate” model in distance sampling.

In fact, as λ gets small, the Poisson model is a close approximation to the Bernoulli model in the sense that outcomes concentrate on $\{0, 1\}$, i.e., $\Pr(y \in \{0, 1\}) \rightarrow 1$ as $\lambda \rightarrow 0$. Indeed, under the Poisson model, $\Pr(y > 0) \rightarrow \lambda$ for small values of λ . This phenomenon is shown in Figure 9.1 where the left panel shows a plot of $\lambda_{ij} = \lambda_0 k(\mathbf{x}_j, \mathbf{s}_i)$ vs. distance and superimposed on that is a plot of $p_{ij} = 1 - \exp(-\lambda_{ij})$ vs. distance, for values $\lambda_0 = 0.1$ and $\sigma = 1$, and the right panel shows a plot of $\Pr(y > 0)$ vs. $\mathbb{E}(y)$. We see that the two quantities are practically indistinguishable. This is

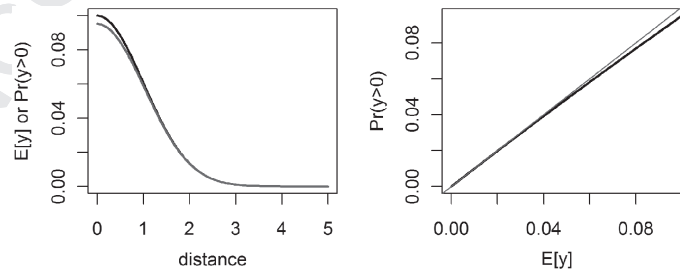


FIGURE 9.1

Poisson approximation to the binomial. As the Poisson mean approaches 0, then $\Pr(y > 0)$ under the Poisson model approaches λ and therefore $y \sim \text{Poisson}(\lambda)$ is well approximated by a Bernoulli model with parameter λ .

convenient in some cases because the Poisson model might be more tractable to fit (or even vice versa). For an example, see the models described in Chapter 18, and we also consider another case in Section 20.1.5 below. To evaluate the closeness of the approximation, you can use the following R commands which we used to produce Figure 9.1:

```
o0005 > x <- seq(0.001, 5, , 200)
o0010 > lam0 <- .1
o0015 > sigma <- 1
o0020 > lam <- lam0*exp(-x*x/(2*sigma*sigma))

o0025 > par(mfrow=c(1,2))
o0030 > p1 <- 1-exp(-lam)
o0035 > plot(x, lam, ylab="E[y] or Pr(y>0)", xlab="distance", type="l", lwd=2)
o0040 > lines(x, p1, lwd=2, col="red")
o0045 > plot(lam, p1, xlab="E[y]", ylab="Pr(y>0)", type="l", lwd=2)
o0050 > abline(0,1, col="red")
```

p0055 To summarize, if y is Poisson then, as λ gets small,

$$\begin{aligned} \Pr(y > 0) &\approx \mathbb{E}(y), \\ 1 - \exp(-\lambda_0 k(\mathbf{x}, \mathbf{s})) &\approx \lambda_0 k(\mathbf{x}, \mathbf{s}). \end{aligned} \quad (9.1.3)$$

What all of this suggests is that if we have very few observations > 1 in our SCR data set, then we won't lose much information by using the Bernoulli model. On the other hand, the Poisson model may have some advantages in terms of analytic or numerical tractability in some cases. Further, this approximation explains the close correspondence we have found between these two versions of the Gaussian encounter probability model (Section 5.4). Namely, the Gaussian hazard model and the Gaussian encounter probability model are close approximations because $1 - \exp(-\lambda) \approx \lambda$ if λ is small.

p0060 Even in such cases where the Poisson and Bernoulli models are not quite equivalent, we might choose to truncate individual encounter frequencies to binary observations anyhow (transforming counts to 0/1 is called “quantizing”). We might do this intentionally in some cases, such as when the distinct encounter events are highly dependent as often happens in camera trap studies when the same individual moves back and forth in front of a camera during a short period of time. But sometimes, truncation is a feature of the sampling. For example, in the case of bear hair snares, the number of encounters might be well approximated by a Poisson distribution but we cannot determine unique visits and so only get to observe the binary event “ $y > 0$.” In this case, we might choose to model the encounter probability for the binary encounter using Eq. (9.1.3). This is equivalent to the complementary log-log link model, or the “Gaussian hazard” as we called it in Chapter 5:

$$\text{cloglog}(p_{ij}) = \log(\lambda_0) + \log(k(\mathbf{x}, \mathbf{s})),$$

where $\text{cloglog}(u) = \log(-\log(1 - u))$.

9.1.3 A cautionary note on modeling encounter frequencies

s0020

Other models for counts might be appropriate. For example, ecologists are especially fond of negative binomial models for count data (Ver Hoef and Boveng, 2007; White and Bennetts, 1996; Kéry et al., 2005) but other models for excess-Poisson variation are possible. For example, we might add a normally distributed random effect to the linear predictor (Coull and Agresti, 1999).

p0065

As a general rule we favor the Bernoulli observation model even if our sampling scheme produces encounter frequencies. The main reason is that, with frequency data, we are forced to confront a model choice problem (i.e., Poisson, negative binomial, log-normal mixture) that is wholly unrelated to the fundamental space usage process that underlies the genesis of many types of SCR data. Repeated encounters over short time intervals are not likely to be the result of independent encounter events. E.g., an individual moving back and forth in front of a camera yields a cluster of observations that is not informative about the underlying spatial structure of the population. Similarly in scat surveys dogs are used to locate scats which are processed in the laboratory for individuality (Kohn et al., 1999; MacKay et al., 2008; Thompson et al., 2012). The process of local scat deposition is not strictly the outcome of movement or space usage but rather the outcome of complex behavioral considerations as well as dependence in detection of scat by dogs. For example, dogs find (or smell) one scat and then are more likely to find one or more nearby ones, if present, or they get into a den or latrine area and find many scats. The additional assumption required to model variation in observed frequencies (i.e., conditional on location) provides relatively no information about space usage and density, and we feel that the model selection issue should therefore be avoided.

p0070

~~To elaborate on this, we suppose that an individual with activity center \mathbf{s} visits a particular pixel \mathbf{x} with some probability $p(\mathbf{x}, \mathbf{s})$, and then, once there, deposits a number of scat, or visits a camera some number of times with frequency $y(\mathbf{x}, \mathbf{s}) \geq 0$. We describe the outcome of this movement/usage process with a two-level hierarchical model of the form: $[y|w][w|p(\mathbf{x}, \mathbf{s})]$ where $w(\mathbf{x}, \mathbf{s})$ is a binary variable that indicates whether the individual with activity center \mathbf{s} used pixel \mathbf{x} during some interval, and let $w(\mathbf{x}, \mathbf{s}) \sim \text{Bernoulli}(p(\mathbf{x}, \mathbf{s}))$. If we suppose encounter frequency y is independent of \mathbf{x} and \mathbf{s} conditional on the use variable w , then we see that the model for y (amount of use) does not depend on \mathbf{s} .~~

p0075

9.1.4 Analysis of the Poisson SCR model in BUGS

s0025

We consider the simplest possible model here in which we have no covariates that vary over sample occasions $k = 1, 2, \dots, K$ so that we work with the aggregated individual- and trap-specific encounters:

p0080

$$y_{ij} = \left(\sum_{k=1}^K y_{ijk} \right) \sim \text{Poisson}(K \lambda_0 k(\mathbf{x}_j, \mathbf{s}_i))$$

and we consider the bivariate normal form of $k(\mathbf{x}, \mathbf{s})$:

$$k(\mathbf{x}, \mathbf{s}) = \exp(-d(\mathbf{x}, \mathbf{s})^2 / (2\sigma^2))$$

so that

$$\log(\lambda_{ij}) = \alpha_0 - \alpha_1 d(\mathbf{x}_j, \mathbf{s}_i)^2,$$

where $\alpha_0 = \log(\lambda_0)$ and $\alpha_1 = 1/(2\sigma^2)$.

p0085 As usual, we approach Bayesian analysis of these models using data augmentation (Section 4.2). Under data augmentation, we introduce a collection of all-zero encounter histories to bring the total size of the data set up to M , and a corresponding set of data augmentation variables $z_i \sim \text{Bern}(\psi)$. Then the observation model is specified conditional on z according to:

$$y_{ij} \sim \text{Poisson}(z_i K \lambda_{ij}),$$

which evaluates to a point mass at $y = 0$ if $z = 0$. In other words, the observation model under data augmentation is a zero-inflated Poisson model which is easily analyzed by Bayesian methods, e.g., in one of the **BUGS** dialects or, alternatively, using likelihood methods, which we neglect here although the same principles as in Chapter 6 apply.

s0030 9.1.5 Simulating data and fitting the model

p0090 Simulating a sample SCR data set under the Poisson model requires only a couple of minor modifications to the procedure we used in Chapter 5 (see the function `simSCR0`). In particular, we modify the block of code which defines the model to be that of $\mathbb{E}(y)$ and not $\text{Pr}(y = 1)$, and we change the random variable generator from `rbinom` to `rpois`:

```
o0055 ##
o0060 ## S =activity centers and traplocs defined as in simSCR0()
o0065 ##
o0070 ## Compute distance between activity centers and traps:
o0075 > D <- e2dist(S,traplocs)

o0080 ## Define parameter values:
o0085 > alpha0 <- -2.5
o0090 > sigma <- 0.5
o0095 > alpha1 <- 1/(2*sigma*sigma)

o0100 ## Encounter probability model:
o0105 > muy <- exp(alpha0)*exp(-alpha1*D*D)

o0110 ## Now generate the encounters of every individual in every trap
o0115 > Y <-matrix(NA,nrow=N,ncol=ntraps)
o0120 > for(i in 1:nrow(Y)){
o0125   Y[i,] <- rpois(ntraps,K*muy[i,])
o0130 }
```

p0095 We modified our simulation code from Chapter 5 to simulate Poisson encounter frequencies for each trap, and then we analyze an ideal data set using **BUGS**.

256 CHAPTER 9 Alternative Observation Models

This Poisson simulator function `simPoissonSCR` is available in the `scrbook` package (it can produce 3-d encounter history data too, although we don't do that here). Here is an example of simulating a data set and harvesting the required data objects, and doing the data augmentation:

```
## Simulate data and extract data elements o0135
## o0140
> data <- simPoissonSCR(discard0=TRUE, rnd=2013) o0145
> y <- data$Y o0150
> nind <- nrow(y) o0155
> X <- data$traplocs o0160
> K <- data$K o0165
> J <- nrow(X) o0170
> xlim <- data$xlim o0175
> ylim <- data$ylim o0180

## Data augmentation o0185
> M <- 200 o0190
> y <- rbind(y, matrix(0, nrow=M-nind, ncol=ncol(y))) o0195
> z <- c(rep(1, nind), rep(0, M-nind)) o0200
```

The process for fitting the model in **WinBUGS** or **JAGS** is identical to what we've done previously in Chapter 5. In particular, we `setup` some starting values, package the data and inits, identify the parameters to be monitored, and then send everything off to our MCMC engine. Here it all is for fitting the Poisson observation model (these commands are shown in the help file for `simPoissonSCR`):

```
## Starting values for activity centers o0205
## o0210
> sst <- X[sample(1:J, M, replace=TRUE), ] o0215
> for(i in 1:nind){ o0220
  if(sum(y[i,])==0) next o0225
  sst[i,1] <- mean( X[y[i,]>0,1] ) o0230
  sst[i,2] <- mean( X[y[i,]>0,2] ) o0235
} o0240
## Dithered a little bit from trap locations o0245
> sst <- sst + runif(nrow(sst)*2, 0, 1)/8 o0250
> data <- list (y=y, X=X, K=K, M=M, J=J, xlim=xlim, ylim=ylim) o0255
> inits <- function(){ o0260
  list (alpha0=rnorm(1, -2, .4), alphas=runif(1, 1, 2), s=sst, z=z, psi=.5) o0265
} o0270
> parameters <- c("alpha0", "alpha1", "N", "D") o0275
```

Next, we write the **BUGS** model to an external file: p0105

```
> cat(" o0280
model{ o0285
  alpha0 ~ dnorm(0, .1) o0290
```

```

o0295 alpha1 ~ dnorm(0,.1)
o0300 psi ~ dunif(0,1)

o0305 for (i in 1:M){
o0310   z[i] ~ dbern(psi)
o0315   s[i,1] ~ dunif(xlim[1],xlim[2])
o0320   s[i,2] ~ dunif(ylim[1],ylim[2])
o0325   for(j in 1:J){
o0330     d[i,j] <- pow(pow(s[i,1]-X[j,1],2) + pow(s[i,2]-X[j,2],2),0.5)
o0335     y[i,j] ~ dpois(lam[i,j])
o0340     lam[i,j] <- z[i]*K*exp(alpha0)*exp(- alpha1*d[i,j]*d[i,j])
o0345   }
o0350 }
o0355 N <- sum(z[])
o0360 D <- N/64
o0365 }
o0370 ",file = "SCR-Poisson.txt")

```

p0110 To fit the model we execute bugs in the usual way:

```

o0375 > library(R2WinBUGS)
o0380 > out1 <- bugs (data, inits, parameters, "SCR-Poisson.txt", n.thin=1,
o0385   n.chains=3,n.burnin=1000,n.iter=2000,working.dir=getwd(),
o0390   debug=TRUE)

```

Or, using **JAGS** via `rjags`, we would do something like this:

```

o0395 > library(rjags)
o0400 > jm <- jags.model("SCR-Poisson.txt", data=data, inits=inits,
o0405   n.chains=3, n.adapt=1000)
o0410 > out2 <- coda.samples(jm, parameters, n.iter=1000, thin=1)

```

Summarizing the output from the **WinBUGS** run produces the following:

```

> print(out1,digits=2)
Inference for Bugs model at "SCR-Poisson.txt", fit using WinBUGS,
3 chains, each with 2000 iterations (first 1000 discarded)
n.sims = 3000 iterations saved

```

	mean	sd	2.5%	25%	50%	75%	97.5%	Rhat	n.eff
alpha0	-2.57	0.19	-2.95	-2.69	-2.57	-2.44	-2.19	1.00	2600
alpha1	2.34	0.36	1.69	2.08	2.32	2.57	3.12	1.00	3000
N	114.13	15.25	87.97	103.00	113.00	124.00	147.00	1.01	370
D	1.78	0.24	1.37	1.61	1.77	1.94	2.30	1.01	370
deviance	329.95	21.92	290.00	314.20	329.50	344.40	375.80	1.00	1700
...									

```

[...some output deleted...]
...

```

s0035 9.1.6 Analysis of the wolverine study data

p0115 We reanalyzed the data from the wolverine camera trapping study that were first introduced in Section 5.9. We modified the **R** script from the function `wolvSCR0` to fit the Poisson model (see the help file for `wolvSCR0pois`). Executing this function

Table 9.1 Results of fitting the SCR model with Poisson encounter frequencies to the wolverine camera trapping data. Posterior summaries were obtained using **WinBUGS** with 3 chains, each with 6000 iterations, discarding the first 1000 as burn-in, to yield a total of 15000 posterior samples.

Parameter	Mean	SD	2.5%	50%	97.5%	Rhat	n.eff
N	60.12	11.91	40.00	59.00	87.00	1	630
D	5.80	1.15	3.86	5.69	8.39	1	630
$\log(p_0)$	-2.89	0.17	-3.22	-2.89	-2.57	1	5000
λ_0	0.06	0.01	0.04	0.06	0.08	1	5000
σ	0.64	0.06	0.54	0.64	0.76	1	730
ψ	0.30	0.07	0.19	0.30	0.45	1	650

sp025

produces the results shown in Table 9.1. The results are almost indistinguishable from the Bernoulli model fitted previously, where we had a posterior mean for N of 59.84 and σ was 0.64. You can edit the script `wolvSCR0pois` to obtain more posterior samples, or modify the model in some way.

9.1.7 Count detector models in the `secr` package

s0040

The **R** package `secr` will fit Poisson or negative binomial encounter frequency models. The formatting of data and structure of the analysis proceeds in a similar fashion to the Bernoulli model described in Section 6.5, except that we specify the `detector="count"` option when the `traps` object is created. The setup proceeds as follows:

p0120

```
> library(secr)
> library(scrbook)
> data(wolverine)

> traps <- as.matrix(wolverine$wtraps)
> dimnames(traps) <- list(NULL, c("trapID", "x", "y", paste("day", 1:165, sep="")))
> traps1 <- as.data.frame(traps[, 1:3])
> trapfile1 <- read.traps(data=traps1, detector="count")
```

o0415

o0420

o0425

o0430

o0435

o0440

o0445

You can proceed with analysis of these data and compare/contrast with the Bayesian analysis given above, or the results of the Bernoulli model fitted in Chapter 6.

p0125

9.2 Independent multinomial observations

s0045

Several types of encounter devices yield multinomial observations in which an individual can be caught in a single trap during a particular encounter occasion, but traps might catch any number of individuals. Mist netting is the canonical example of such a “multi-catch” device (Efford et al., 2009a). Also some kinds of bird or mammal cage-traps hold multiple animals, as do pit-fall traps which are commonly used for

p0130

many species of herptiles. Another type of sample method that might be viewed (in some cases) as a multi-catch device are area-searches of, for example, reptiles where we think of a small polygon as the “trap”—we could get multiple individuals (turtles, lizards) in the same plot but not, in the same sample occasion, at different plots. The key features of this independent multinomial or multi-catch model are: (1) capture of an individual in a trap is *not* independent of its capture in other traps, because initial capture precludes capture in any other trap and (2) individuals behave independently of one another, so whether a trap captures some individual doesn’t have an affect on whether it captures another. A type of model in which the second assumption is violated are the “single-catch” trap systems which we address in Section 20.1.5 below.

p0135 In this case we assume the observation \mathbf{y}_{ik} for individual i during sample occasion k is a multinomial observation which consists of a sequence of 0’s and a single 1 indicating the trap of capture, or “not captured”. For the “not captured” event we define an additional outcome, by convention element $J + 1$ of the vector. As an example, if we capture an individual in trap 2 during some occasion of a study involving $J = 6$ traps. Then, the multinomial observation has length $J + 1 = 7$, and the observation is $\mathbf{y}_i = (0, 1, 0, 0, 0, 0, 0)$. An individual not captured at all would have the observation vector $(0, 0, 0, 0, 0, 0, 1)$. If we sample for five occasions in all and the individual is also caught in trap 4 during occasion 3, but otherwise uncaptured, then the five encounter observations for that individual are as follows:

occasion	trap						"not captured"
	1	2	3	4	5	6	7
1	0	1	0	0	0	0	0
2	0	0	0	0	0	0	1
3	0	0	0	1	0	0	0
4	0	0	0	0	0	0	1
5	0	0	0	0	0	0	1

Statistically we regard the rows of this data matrix as *independent* multinomial trials.

p0140 Analogous to our previous Bernoulli and Poisson models, we seek to construct the multinomial cell probabilities for each individual, as a function of where that individual lives, through its center of activity \mathbf{s} . Thus we suppose that

$$\mathbf{y}_{ik} | \mathbf{s}_i \sim \text{Multinomial}(1, \boldsymbol{\pi}(\mathbf{s}_i)), \quad (9.2.1)$$

where $\boldsymbol{\pi}(\mathbf{s}_i)$ is a vector of length $J + 1$, where $\pi_{i,J+1}$, the last cell, corresponds to the probability of the event “not captured”. Now we have to construct these cell probabilities in some meaningful way that depends on each individual’s \mathbf{s} . We use the standard multinomial logit with distance as a covariate:

$$\pi_{ij} = \frac{\exp(\alpha_0 - \alpha_1 d_{ij})}{1 + \sum_j \exp(\alpha_0 - \alpha_1 d_{ij})}$$

260 CHAPTER 9 Alternative Observation Models

for $j = 1, 2, \dots, J$ and, for $J + 1$, i.e., “not captured”,

$$\pi_{i,(J+1)} = \frac{\exp(0)}{1 + \sum_j \exp(\alpha_0 - \alpha_1 d_{ij}^2)}$$

or, more commonly, we use d_{ij}^2 to correspond to our Gaussian kernel model for encounter probability. Whatever function of distance we use in the construction of multinomial probabilities will have a direct correspondence to the standard encounter probability models we used in the Bernoulli or Poisson models as well (see Section 5.4).

It is convenient to express these multinomial models short-hand as follows, e.g., p0145 for the Gaussian encounter probability model:

$$\text{mlogit}(\pi_{ij}) = \alpha_0 - \alpha_1 d_{ij}^2.$$

In this way we can refer to models with covariates in a more concise way. For example, a model with a trap-specific covariate, say C_j , is:

$$\text{mlogit}(\pi_{ij}) = \alpha_0 - \alpha_1 d_{ij}^2 + \alpha_2 C_j$$

or we could include occasion-specific covariates too, such as behavioral response.

A statistically equivalent distribution to the multinomial is the *categorical* distribution. If \mathbf{y} is a multinomial trial with probabilities $\boldsymbol{\pi}$ then the *position* of the non-zero element of \mathbf{y} is a categorical random variable with probabilities $\boldsymbol{\pi}$. We express this for SCR models as p0150

$$\mathbf{y}|\mathbf{s} \sim \text{Categorical}(\boldsymbol{\pi}(\mathbf{s})).$$

In the SCR context, the categorical version of the multinomial trial corresponds to the *trap of capture*. Using our example above with six traps then we could as well say y_{ik} is a categorical random variable with possible outcomes (1, 2, 3, 4, 5, 6, 7) where outcome $y = 7$ corresponds to “not captured.” Obviously, how this is organized or labeled is completely irrelevant, although it is convenient to use the integers 1 to $(J + 1)$ where $J + 1$ is the event not captured. Therefore, for our illustration in the previous table, $y_{i1} = 2$, $y_{i2} = 7$, $y_{i3} = 4$, and so on.

For simulating and fitting data in the **BUGS** engines we will typically use the categorical representation of the model because it is somewhat more convenient. We have found that fitting multinomial models in **WinBUGS** is less efficient than **JAGS** (Royle and Converse, in review), which we use in the subsequent examples involving multinomial observation models. p0155

9.2.1 Multinomial resource selection models

s0050

The multinomial probabilities in Eq. (9.2.2) look similar to the multinomial resource selection function (RSF) model for telemetry data (Manly et al., 2002; Lele and Keim, 2006). This suggests how we might model landscape or habitat covariates using such methods—i.e., by including them as explicit covariates in a larger multinomial model for “use”—which, if we take the product of use with encounter, produces a model for the observable encounter data. This leads naturally to the development of p0160

models that integrate RSF data from telemetry studies with SCR data (Royle et al., 2012a), which is the topic of Chapter 13.

9.2.2 Simulating data and analysis using JAGS

We're going to show the nugget of a simulation function which is used in the function `simMnSCR` found in the **R** package `scrbook`. The first lines of the following **R** code make use of some things that you need to define, but we omit them here (e.g., `xlim`, `ylim` are the boundaries of the state-space, `N` is the population size, etc.):

```
##
## Simulate random activity centers:
##      (first define N, xlim, ylim, etc.)
##
> S <- cbind(runif(N,xlim[1],xlim[2]),runif(N,ylim[1],ylim[2]))
## Distance from each individual to each trap
> D <- e2dist(S,traplocs)

## Set paramter values
> sigma <- 0.5
> alpha0 <- -1
> alpha1 <- -1/(2*sigma*sigma)

## make an empty data matrix and fill it up with data
> Ycat <- matrix(NA,nrow=N,ncol=K)
> for(i in 1:N){
  for(k in 1:K){
    lp <- alpha0 + alpha1*D[i,]*D[i,]
    cp <- exp(c(lp,0))
    cp <- cp/sum(cp)
    Ycat[i,k] <- sample(1:(ntraps+1),1,prob=cp)
  }
}
```

We save the data in the matrix `Ycat` to clarify that it is the categorical observation representing “trap of capture”. The matrix `Ycat` here has ~~the maximal dimension N~~ and ~~so~~, to do an analysis that mimics a real situation, we would have to discard the uncaptured individuals. The function `simMnSCR` ~~in the package `scrbook`~~ will also simulate data that includes a behavioral response which will be the typical situation in small-mammal trapping problems (see Converse and Royle, 2012, for details).

Here we use our function `simMnSCR` to simulate a data set with $K = 7$ occasions. We'll run the model using **JAGS** which we have found is much more effective for this class of models. We get the data ~~setup~~ for analysis by augmenting the size of the data set to $M = 200$. In addition we choose starting values for \mathbf{s} and the data augmentation variables \mathbf{z} . For starting values of \mathbf{s} we cheat a little bit here and use the true values for the observed individuals and then augment the $M \times 2$ matrix \mathbf{S} with $M - n$ randomly selected activity centers. Our function `spiderplot` returns the mean

262 CHAPTER 9 Alternative Observation Models

observed location of ~~individuals for use as starting values for~~ the n_{ind} encountered individuals. The parameters input to `simMnSCR` are the intercept α_0 , $\sigma = \sqrt{1/(2\alpha_1)}$ for the Gaussian encounter probability model, and α_2 is the behavioral response parameter. The data simulation and setup proceeds as follows:

```
> set.seed(2013) o0555
> parms <- list(N=100,alpha0= -.40, sigma=0.5, alpha2= 0) o0560
> data <- simMnSCR(parms, K=7, sbuffer=2) o0565
> nind <- nrow(data$Ycat) o0570

> M <- 200 o0575
> Ycat <- rbind(data$Ycat,matrix(nrow(data$X)+1,nrow=(M-nind),ncol=data$K)) o0580
> Sst <- rbind(data$S,cbind(runif(M-nind,data$xlim[1],data$xlim[2]), o0585
                           runif(M-nind,data$ylim[1],data$ylim[2]))) o0590
> zst <- c(rep(1,160),rep(0,40)) o0595
```

The model specification is not much more complicated than the binomial or Poisson models given previously. The main consideration is that we define the cell probabilities for each trap $j = 1, 2, \dots, J$ and then define the last cell probability, $J + 1$, for “not captured”, to be the complement of the sum of the others. The code is shown in Panel 9.1. In the last lines of code ~~here~~ we specify N and density, D , as derived parameters. p0180

To fit the model, we need to package everything up (~~inits~~, parameters, data) and send it off to **JAGS** to build an MCMC simulator for us (these commands are ~~executed~~ in the help file for `simMnSCR`). In addition to the usual data objects, we also pass the limits of the assumed rectangular state-space (`ylim`, `xlim`, both 1×2 vectors) and the scale of the standardized units, called `trap.space` here because we typically will define the trap coordinates to be an integer grid. If the trap spacing is 10 m and we want units of density ~~computed~~ in terms of individuals per ~~meter-squared~~, then we input `trap.space=10`. The analysis is carried out as follows:

```
> inits <- function(){ list (z=zst,sigma=runif(1,.5,1) ,S=Sst) } o0600
# Parameters to monitor o0605
> parameters <- c("psi","alpha0","alpha1","sigma","N","D") o0610

# Bundle the data. Note this reuses "data" o0615
> data <- list (X=data$X,K=data$K, trap.space=1,Ycat=Ycat,M=M, o0620
              ntraps=nrow(data$X),ylim=data$ylim,xlim=data$xlim) o0625

> library(R2jags) o0630
> out <- jags (data, inits, parameters, "model.txt", n.thin=1, o0635
              n.chains=3, n.burnin=1000, n.iter=2000) o0640
```

The posterior summaries are provided in the following **R** output (recall that $N = 100$, $\alpha_0 = -.40$, and $\sigma = 0.5$): p0190

```
> out
Inference for Bugs model at "model.txt", fit using jags,
 3 chains, each with 2000 iterations (first 1000 discarded)
n.sims = 3000 iterations saved
```

	mu.vect	sd.vect	2.5%	25%	50%	75%	97.5%	Rhat	n.eff
D	1.873	0.189	1.531	1.750	1.859	2.000	2.250	1.006	1300
N	119.867	12.107	98.000	112.000	119.000	128.000	144.000	1.006	1300
alpha0	-0.435	0.151	-0.738	-0.535	-0.439	-0.331	-0.146	1.004	580
alpha1	2.195	0.286	1.658	2.004	2.180	2.372	2.785	1.003	2400
psi	0.599	0.069	0.465	0.552	0.599	0.645	0.739	1.006	1400
sigma	0.480	0.032	0.424	0.459	0.479	0.500	0.549	1.003	2400
deviance	892.164	21.988	850.922	877.417	891.561	906.246	937.728	1.003	950

[... output deleted ...]

s0060 9.2.3 Multinomial relationship to the Poisson

p0195 The multinomial is related to the Poisson encounter rate model by a conditioning argument. Let y_{ij} be the number of encounters for individual i in trap j .

```
model{
  psi ~ dunif(0,1)
  alpha0 ~ dnorm(0,10)
  sigma ~ dunif(0,10)
  alpha1 <- 1/(2*sigma*sigma)

  for(i in 1:M){
    z[i] ~ dbern(psi)
    S[i,1] ~ dunif(xlim[1],xlim[2])
    S[i,2] ~ dunif(ylim[1],ylim[2])
    for(j in 1:ntraps){
      #distance from capture to the center of the home range
      d[i,j] <- pow(pow(S[i,1]-X[j,1],2) + pow(S[i,2]-X[j,2],2),1)
    }
    for(k in 1:K){
      for(j in 1:ntraps){
        lp[i,k,j] <- exp(alpha0 - alpha1*d[i,j])*z[i]
        cp[i,k,j] <- lp[i,k,j]/(1+sum(lp[i,k,]))
      }
      cp[i,k,ntraps+1] <- 1-sum(cp[i,k,1:ntraps]) # last cell = not captured
      Ycat[i,k] ~ dcat(cp[i,k,])
    }
  }

  N <- sum(z[1:M])
  A <- ((xlim[2]-xlim[1])*trap.space)*((ylim[2]-ylim[1])*trap.space)
  D <- N/A
}
```

PANEL 9.1

BUGS model specification for the independent multinomial observation model. For data simulation and model fitting see the help file `?simMnSCR` in the **R** package `scrbook`.

264 CHAPTER 9 Alternative Observation Models

If $y_{ij} \sim \text{Poisson}(\lambda_{ij})$, then, conditional on the *total* number of captures (i.e., across all traps), $y_i = \sum_j y_{ij}$, the trap encounter frequencies are multinomial with probabilities

$$\pi_{ij} = \frac{\lambda_{ij}}{\sum_j \lambda_{ij}}$$

for $j = 1, 2, \dots, J$. Or equivalently the *trap of capture* is categorical with probabilities π_{ij} as given above. Under the Gaussian kernel model, these probabilities are:

$$\pi_{ij} = \frac{\exp(-\alpha_1 d(\mathbf{x}_i, \mathbf{s}_j)^2)}{\sum_j \exp(-\alpha_1 d(\mathbf{x}_i, \mathbf{s}_j)^2)}, \quad (9.2.2)$$

where, we note, the intercept α_0 has been canceled from both the numerator and denominator. This makes sense because, here, these probabilities describe the trap-specific capture probabilities *conditional on capture*. Therefore, the model is not completely specified, absent a model for the “overall” probability of encounter or the expected frequency of captures, say ϕ_i . Depending on how we specify a model for this quantity ϕ_i , we can reconcile it directly with the Poisson model. Let y_i be the total number of encounters for individual i and suppose y_i has a Poisson distribution with mean ϕ_i . Then, marginalizing Eq. (9.2.1) over the Poisson distribution for y_i , produces the original set of *iid* Poisson frequencies with probabilities:

$$\lambda_{ij} = \phi_i \pi_{ij}$$

for $j = 1, 2, \dots, J$. In particular, if we suppose that $\phi_i = \sum_j \exp(\alpha_0 - \alpha_1 d(\mathbf{x}, \mathbf{s})^2)$ then the marginal distribution of y_{ij} is Poisson with mean $\exp(\alpha_0 - \alpha_1 d(\mathbf{x}, \mathbf{s})^2)$, equivalent to Eq. (9.1.1).

In summary, the Poisson and multinomial models are equivalent in how they model the distribution of captures among traps. It stands to reason that, if the encounter rate of individuals is low, we could use the Poisson and multinomial models interchangeably. In fact, based on our discussion in Section 9.1.2 above we could use any of the binomial/Poisson/multinomial models with little ill effect when encounter rate is low.

9.2.4 Avian mist-netting example

We analyze data from a mist-netting study of ovenbirds, conducted at the Patuxent Wildlife Research Center, Laurel MD, by D.K. Dawson and M.G. Efford. The data from this study are available in the `secr` package and have been analyzed previously by Efford et al. (2004), see also Borchers and Efford (2008). Forty-four mist-nets spaced 30 m apart on the perimeter of a 600-m \times 100-m rectangle were operated on 9 or 10 non-consecutive days in late May and June for 5 years from 2005 to 2009. The ovenbird data can be loaded as follows:

```
> library(secr)
> data(ovenbird)
```

The data set consists of adult ovenbirds caught during sampling in each of 5 years, 2005–2009. (one ovenbird was killed in 2009 indicated by a negative net number in

the encounter data file). As with most mist-netting studies, nets are checked multiple times during a day (e.g., every hour during a morning session). However, for this data set, the within-day recaptures are not included so each bird has at most a single capture per day. Therefore, the multinomial model (detector type “multi” in `secr`) is appropriate. Although several individuals were captured in more than 1 year, this information is not used in the models presently offered in `secr`, but we do make use of it in the development of open models in Chapter 16.

s0070 9.2.4.1 Multiple sample sessions

p0210 Up to this point we have only dealt with a basic closed population sampling situation consisting of repeated sample occasions on a single population of individuals using a single array of traps. In practice, many studies produce repeated samples over longer periods of time over which demographic closure isn’t valid, or at different locations where the populations are completely distinct. We adopt the `secr` terminology of *session* for such replication by groups of time or space, and the models are *multi-session* models, although we think of such models as being relevant to any stratified population (see Chapter 14). We introduced `secr`’s multi-session models in Section 6.5.4. In the case of the ovenbird data, sampling was carried out in multiple years, with a number of sample occasions within each year (9 or 10), a type of data structure commonly referred to as “the robust design” (Pollock, 1982). In this context, it stands to reason that there is recruitment and mortality happening across years. In Chapter 16 we model these processes explicitly but, here, we provide an analysis of the data that does not require explicit models for recruitment and survival, regarding the yearly populations as independent strata, and fitting a multi-session model.

p0215 When the sessions represent explicit time periods, the multi-session model of `secr` can be thought of as a type of open population model. In particular, a special case of open models arises when we assume N_t (time-specific population sizes) are independent from one time period or session to the next—this can be thought of as a “random temporary emigration” model of the Kendall et al. (1997) variety, and this is the multi-session model implemented in `secr`. In particular, by assuming that N_t is Poisson with mean Λ_t , one can model variation in abundance among sessions based on the Poisson-integrated likelihood in which parameters of Λ_t appear directly in the likelihood as we noted in Section 6.5.4. We provide an analysis (below) of the ovenbird data here using the multi-session models in `secr`. We formalize the multi-session model approach from a Bayesian perspective using data augmentation in Chapter 14 (Converse and Royle, 2012; Royle and Converse, in review).

p0220 A third way to develop models for stratified or grouped populations, not based on multi-session models, but that is convenient in **BUGS**, is to regard the data from each session as an independent data set with its own N_t parameter, and do T distinct data augmentations. Because each N_t is regarded as a free parameter, independent of the other parameters, we’ll call this the non-parametric multi-session model to distinguish it from the multi-session model which assumes the N_t are related to one another by having been generated from a common Poisson distribution. We can analyze this model in the normal context of data augmentation by augmenting each

year separately in the same **BUGS** model specification. This approach avoids making explicit model assumptions about the N_t parameters. This is distinct from the model implemented in `secr` in that `secr` is removing the N_t parameters by integrating the conditional on N_t likelihood over the Poisson prior for N_t .¹

We demonstrate these three approaches to analyzing grouped/stratified data using the ovenbird data: (1) In the following section, we provide the non-parametric multi-session model with unconstrained N_t ; (2) we demonstrate the Poisson model-based multi-session models from `secr` both here (following section) and in Chapter 14 from a Bayesian standpoint; (3) later, in Chapter 16, we provide a fully dynamic “spatial Jolly-Seber” model and apply it to the ovenbird data.

9.2.4.2 Analysis in JAGS

The ovenbird data are provided as a multi-session `capthist` object `ovenCH` which, by regarding years as independent strata, or sessions, allows for the fitting of the multi-session model. For doing a Bayesian analysis in one of the **BUGS** engines (we use **JAGS** here) there are a number of ways to structure the data and describe the model. We can analyze either a 2-d data set with all years (data augmented) “stacked” into a data set of dimension $(5 * M) \times 10$ (5 years, M = size of the augmented data set, $K = 10$ replicate sample occasions). Or, we could produce a three-d array ($M \times J \times K$). We adopted the former approach, analyzing the data as a 2-d array and creating an additional categorical variable for “year” to indicate which stratum (year) each record goes with.

Data on individual sex is included with `secr`, but we provide an analysis of a single model for all adults, constant σ across years, constant p_0 , and year-specific values of N_t (and hence D_t). There is a habitat mask provided with the data but the mask appears to just be a modified rectangle around the net locations, clipped to have rounded corners, and so we don’t use it here. Instead, we used a rectangular state-space buffer of 200 meters for our analysis. There was a single loss-on-capture which we accounted for by fixing $p = 0$ for all subsequent encounters of that individual (indicated by the binary variable `dead`, as shown in Panel 9.2). We have an **R** script in `scrbook` package called `SCRovenbird`, so you can see how to setup the data and run the model. Executing the script `SCRovenbird` produces the posterior summaries given in Table 9.2. Here, density is in units of birds per ha. The posterior mean of σ is about 76 m, and there is considerable variability in density over the 5-year period with density peaking at 1.2 birds/ha in year 3, although there is considerable posterior uncertainty. The \hat{R} -hat’s look a little bit peaked and so we might consider running the MCMC analysis longer.

9.2.4.3 Analysis in secr

Included with the ovenbird data are a number of models fitted as examples. Those include:

¹We do not know of `secr` documentation that states this (or contradicts it). We think this is what is being done, based partially on conversations or emails with M.G. Efford, D.L. Borchers, the various publications on `secr`, and our own thinking about it.

```
ovenbird.model.1 fitted secr model -- null
ovenbird.model.1b fitted secr model -- g0 net shyness
ovenbird.model.1T fitted secr model -- g0 time trend within years
ovenbird.model.h2 fitted secr model -- g0 finite mixture
ovenbird.model.D fitted secr model -- trend in density across years
```

p0245 The model fit objects provided in `secr` are based on the use of the habitat mask. To make the analyses consistent with our previous analysis in **JAGS**, we refit all of the

```
model{
  alpha0 ~ dnorm(0,.1)
  sigma ~ dunif(0,200)
  alpha1 <- 1/(2*sigma*sigma)

  A <- ((xlim[2]-xlim[1]))*((ylim[2]-ylim[1]))
  for(t in 1:5){
    N[t] <- inprod(z[1:bigM],yrdummy[,t])
    D[t] <- (N[t]/A)*10000 # Put in units of per ha
    psi[t] ~ dunif(0,1)
  }

  for(i in 1:bigM){ # bigM = total size of jointly augmented data set
    z[i] ~ dbern(psi[year[i]])
    S[i,1] ~ dunif(xlim[1],xlim[2])
    S[i,2] ~ dunif(ylim[1],ylim[2])

    for(j in 1:ntraps){ # X = trap locations, S = activity centers
      d2[i,j] <- pow(pow(S[i,1]-X[j,1],2) + pow(S[i,2]-X[j,2],2),.5)
    }
    for(k in 1:K){
      Ycat[i,k] ~ dcat(cp[i,k,])
      for(j in 1:ntraps){
        lp[i,k,j] <- exp(alpha0 - alpha1*d2[i,j])*z[i]*(1-dead[i,k])
        cp[i,k,j] <- lp[i,k,j]/(1+sum(lp[i,k,1:ntraps]))
      }
      cp[i,k,ntraps+1] <- 1-sum(cp[i,k,1:ntraps]) # Last cell = not captured
    }
  }
}
```

PANEL 9.2

BUGS model specification for the non-parametric multi-session model in which each N_t is independent of the other. The implied prior (by data augmentation) is that $N_t \sim \text{Uniform}(0,100)$. To fit this model to the ovenbird data, see `?SCRovenbird` in the **R** package `scrbook`.

268 CHAPTER 9 Alternative Observation Models

Table 9.2 Posterior summary statistics for the ovenbird mist-netting data based on the independent multinomial (“multi-catch”) encounter process model. Parameters ψ , N , and D are indexed by year. MCMC was done using jags with 3 chains, each with 11,000 iterations, discarding the first 1,000, for a total of 30,000 posterior samples.

sp030

Parameter	Mean	SD	2.5%	50%	97.5%	Rhat	n.eff
D[1]	0.983	0.211	0.636	0.966	1.455	1.002	1900
D[2]	1.023	0.209	0.673	1.003	1.492	1.001	7100
D[3]	1.208	0.238	0.807	1.186	1.749	1.004	740
D[4]	0.896	0.195	0.575	0.880	1.333	1.002	3000
D[5]	0.753	0.177	0.465	0.734	1.149	1.001	4000
α_0	-3.479	0.160	-3.797	-3.477	-3.171	1.005	490
α_1	0.000	0.000	0.000	0.000	0.000	1.003	1100
σ	76.214	6.125	65.569	75.758	89.360	1.003	1100
N[1]	80.423	17.283	52.000	79.000	119.000	1.002	1900
N[2]	83.685	17.077	55.000	82.000	122.000	1.001	7100
N[3]	98.822	19.483	66.000	97.000	143.000	1.004	740
N[4]	73.288	15.962	47.000	72.000	109.000	1.002	3000
N[5]	61.589	14.468	38.000	60.000	94.000	1.001	4000
ψ [1]	0.403	0.092	0.246	0.395	0.606	1.002	1600
ψ [2]	0.419	0.091	0.260	0.412	0.620	1.001	6400
ψ [3]	0.494	0.102	0.315	0.486	0.723	1.004	760
ψ [4]	0.368	0.086	0.221	0.361	0.555	1.002	3200
ψ [5]	0.310	0.079	0.178	0.302	0.485	1.002	3500

models here without the habitat mask. The re-analysis proceeds as follows, changing the “trend in density across years” model to allow for year-specific density:

```
## Fit constant-density model
> ovenbird.model.l1 <- secr.fit(ovenCH)
## Fit net avoidance model
> ovenbird.model.lb <- secr.fit(ovenCH, model = list(g0 ~ b))
## Fit model with time trend in detection
> ovenbird.model.lT <- secr.fit(ovenCH, model = list(g0 ~ T))
## Fit model with 2-class mixture for g0
> ovenbird.model.h2 <- secr.fit(ovenCH, model = list(g0 ~ h2))
## Fit a model with session (year)-specific Density
> ovenbird.model.DT <- secr.fit(ovenCH, model = list(D ~ session))
```

All of these can be fitted easily in **JAGS** but the model we fitted previously is roughly equivalent to the last model, `ovenbird.model.DT`, because we allowed for year-specific population sizes (and hence density). So, we’ll compare our results from **JAGS** to that model. The `secr` output is extensive and so we do not reproduce it completely here. By default, it summarizes the trap information for each year, encounter information, and then output for each year. Here is an abbreviated version for `ovenbird.model.DT`:

```
o0705 > print(ovenbird.model.DT,digits=2)

o0710 secr.fit( capthist = ovenCH, model = list(D ~ session), buffer = 300 )
o0715 secr 2.3.1, 14:46:52 23 Jan 2013

$`2005`
Object class      traps
Detector type     multi
Detector number   44
Average spacing   30.27273 m
x-range           -50 49 m
y-range           -285 285 m

[... deleted ...]

      2005 2006 2007 2008 2009
Occasions      9  10  10  10  10
Detections     35  42  52  30  33
Animals        20  22  26  19  16
Detectors      44  44  44  44  44

Model           : D~session g0~1 sigma~1
Fixed (real)    : none
Detection fn     : halfnormal
Distribution     : poisson
N parameters    : 7
Log likelihood  : -1119.845
AIC             : 2253.689
AICc            : 2254.868

[... deleted ...]
```

p0255 To do model selection we use the handy helper-function AIC as follows (output edited to fit on the page):

```
o0720 AIC (ovenbird.model.1, ovenbird.model.1b, ovenbird.model.1T,
o0725      ovenbird.model.h2, ovenbird.model.DT)

      model detectfn npar logLik      AIC      AICc      dAICc
ovenbird.model.1T[edited output] 4 -1111.850 2231.700 2232.109 0.000
ovenbird.model.1b      ....      4 -1117.615 2243.229 2243.637 11.528
ovenbird.model.h2      ....      3 -1121.164 2248.327 2248.570 16.461
ovenbird.model.1       ....      5 -1119.762 2249.524 2250.143 18.034
ovenbird.model.DT      ....      7 -1119.845 2253.689 2254.868 22.759
```

p0260 We see that our DT model is way down at the bottom of the list. Instead, the model with a time trend (within-season) in detection probability is preferred, followed by a behavioral response. We encourage you to adapt the **JAGS** model specification for such models which is easily done (see Chapter 7 for many examples). We provide the summary results for the model having $D \sim \text{session}$ as follows:

```
o0730 > print(ovenbird.model.DT,digits=2)
```

270 CHAPTER 9 Alternative Observation Models

```
secr.fit(capthist = ovenCH, model = list(D ~ session), buffer = 300) o0735
secr 2.3.1, 14:46:52 23 Jan 2013 o0740

[...deleted...] o0745

Fitted (real) parameters evaluated at base levels of covariates o0750

session = 2005
      link estimate SE.estimate      lcl      ucl
D      log      0.920      0.228    0.571    1.484
g0     logit      0.028      0.004    0.021    0.037
sigma   log     78.566      6.379   67.025   92.095

session = 2006
      link estimate SE.estimate      lcl      ucl
D      log      0.963      0.238    0.598    1.553
g0     logit      0.028      0.004    0.021    0.037
sigma   log     78.566      6.379   67.025   92.095

session = 2007
      link estimate SE.estimate      lcl      ucl
D      log      1.139      0.282    0.706    1.836
g0     logit      0.028      0.004    0.021    0.037
sigma   log     78.566      6.379   67.025   92.095

session = 2008
      link estimate SE.estimate      lcl      ucl
D      log      0.832      0.206    0.516    1.341
g0     logit      0.028      0.004    0.021    0.037
sigma   log     78.566      6.379   67.025   92.095

session = 2009
      link estimate SE.estimate      lcl      ucl
D      log      0.701      0.173    0.435    1.130
g0     logit      0.028      0.004    0.021    0.037
sigma   log     78.566      6.379   67.025   92.095
```

The point estimates (MLEs) of density are uniformly lower than the Bayesian estimates (posterior means) shown in Table 9.2. We expect some difference in this direction due to small-sample skew of the posterior. In addition, there may be slight differences due to the fact that `secr` multi-session model assumes that the N_t have a Poisson prior, but the implementation in **JAGS** using data augmentation is based on a binomial prior. The estimated σ is very similar between the **JAGS** analysis and `secr`. p0265

9.3 Single-catch traps

The classical animal trapping experiment is based on a physical trap which captures a single animal and holds that individual until subsequent molestation by a biologist. p0270

This type of observation model—the “single-catch” trap—was the original situation considered in the context of spatial capture-recapture by Efford (2004). Nowadays, capture-recapture data are more often obtained by other methods (DNA from hair snares, or scat sampling, camera traps, etc.) but nevertheless the single-catch traps are still widely used in small-mammal studies (Converse et al., 2006b; Converse and Royle, 2012) and other situations.

p0275 The single-catch model is basically a multinomial model but one in which the number of available traps is reduced as each individual is captured. As such, the constraints on the joint likelihood for the sample of n encounter histories are very complicated. As a result, at the time of this writing, there has not been a formal development of either likelihood or Bayesian analysis of this model, and applications of SCR models to single-catch systems have used the independent multinomial model as an approximation (see below).

p0280 Nevertheless, we can make some progress to describing the basic observation model formally. In particular, if we imagine that all of the individuals captured queued up at the beginning of the capture session to draw a number indicating their order of capture, then there is a nice conditional structure resulting from a “removal process” operating on the traps. The first individual captured has the multinomial observation model:

$$\mathbf{y}_1 \sim \text{Multinomial}(\boldsymbol{\pi}_1),$$

whereas the second individual captured also has a multinomial encounter probability model but with the trap which captured the first individual removed. We might express this as:

$$\mathbf{y}_2 \sim \text{Multinomial}(\boldsymbol{\pi}_2),$$

where

$$\pi_{2j} = \frac{(1 - y_{1j}) * \exp(\alpha_0 - \alpha_1 d_{ij}^2)}{\sum_j (1 - y_{1j}) * \exp(\alpha_0 - \alpha_1 d_{ij}^2)}$$

and so on for $i = 3, 4, \dots, n$. In a certain way, this model is a type of local behavioral response model but where the response is to other individuals being captured. Evidently, the **order of capture** is relevant to the construction of these multinomial cell probabilities. More generally, the *time* of capture of an individual in any trapping interval will affect the encounter probability of subsequently captured individuals, but we think that order of capture might lead to a practical approximation to the single-catch process (this is how we simulate the data in our function `simScSCR`). In the simulation of single-catch data, we randomly ordered the population of individuals for each sample occasion, and then cycled through them, turning off each trap if an individual was captured in it.

s0090 9.3.1 Inference for single-catch systems

p0285 For the single-catch model, we argued that the observations have a multinomial type of observation model, but the multinomial observations have a unique conditional dependence structure among them owing to the “removal” of traps as they fill up

with individuals. Thus, competition for single-catch traps renders the independence assumptions for the independent multinomial model invalid. However, as [Efford et al. \(2009a\)](#) noted, we expect “bias to be small when trap saturation (the proportion of traps occupied) is low. Trap saturation will be higher when population density is high...” relative to trap density, or when net encounter probability is high. [Efford et al. \(2009a\)](#) did a limited simulation study and found essentially no effective bias and concluded that estimators of density from the misspecified independent multinomial model are robust to the mild dependence induced when trap saturation is low. Naturally then, we expect that the Poisson model could also be an effective approximation under the same set of circumstances.

In the **R** package `scrbook` we provide a function for simulating data from a single-catch system (function `simScSCR`) and fitting the misspecified model (`example(simScSCR)`) in **JAGS** so that you can evaluate the effectiveness of this misspecified model for situations that interest you.

9.3.2 Analysis of Efford's possum trapping data

We provide an analysis here of data from a study of brushtail possums in New Zealand. The data are available with the **R** package `secr` ([Efford et al., 2009a](#)); see the help file `?possum` after loading the `secr` package. Originally the data were analyzed by [Efford et al. \(2005\)](#), and a detailed description of the data set is available in the help file, from which we summarize:

*Brushtail possums (*Trichosurus vulpecula*) are an unwanted invasive species in New Zealand. Although most abundant in forests, where they occasionally exceed densities of 15/ha, possums live wherever there are palatable food plants and shelter.*

To load the possum data, execute the following commands:

```
> library(secr)
> data(possum)
```

The study area encompasses approximately 300 ha, and 180 live traps were organized in five distinct grids, shown in Figure 9.2. Each square arrangement of traps consisted of 36 traps with a spacing of 20 m. Thus the squares are 180 m on a side. Individuals were captured, tagged, and released over 5 days during April, 2002. A noteworthy aspect of this study is that it involves replicated grids selected in some fashion from within a prescribed region. From an analysis standpoint, we could adopt the use of the multi-session models, which we used previously to analyze the ovenbird data. This would be useful if we had covariates at the trapping grid level that we wanted to model. Alternatively, we could pool the data from all of the grids and analyze them jointly as if they were based on a single trapping grid (with 180 traps), which is clearly a reasonable view in this case. ~~In doing this sort of pooling, there is an implicit assumption that N_i (i indexing trapping grid in this case) is Poisson~~



FIGURE 9.2

Trapping grids used in possum study from [Efford et al. \(2005\)](#), data are contained in the **R** package `secr` ([Efford, 2011a](#)), refer to the help file `?possum` for additional details of this study.

~~distributed, with constant mean ([Royle, 2004a](#); [Royle et al., 2012c](#)), which we also address in Chapter 14.~~

p0315 The data file `possumCH` contains 112 encounter histories, and we analyze those here although the last eight of those are recaptures treated as new individuals.² The encounter process is not strictly a single-catch multinomial process because, as noted in the `possum` help file, “One female possum was twice captured at two sites on one day, having entered a second trap after being released; one record in each pair was selected arbitrarily and discarded.” which is a similar situation to what might happen in bird mist-net studies, as a bird might fly into a net upon release from another. By discarding the two extra-capture events, we can satisfactorily view these data as single-catch data, for which `secr` uses the independent multinomial likelihood (M. Efford, pers. comm.). If multiple, same-session captures were common, then it might be worth developing a model for $n_{ik} \equiv$ the number of captures of individual i during sample occasion k , in order to make use of all captures.

np010 ²M. Efford, personal communication

Table 9.3 Results of fitting the independent multinomial observation model to the possum trapping data. Strictly speaking, the trapping device is a “single-catch” trap, and the model represents an intentional misspecification. Density is reported in individuals per ha (Dha). Posterior summaries were obtained using **JAGS** with 3 chains, each with 2000 iterations, discarding the first 1000 as burn-in, to yield a total of 3000 posterior samples.

sp035

Parameter	Mean	SD	2.5%	50%	97.5%	Rhat	n.eff
N	235.407	17.435	204.000	235.000	270.000	1.009	340
Dha	1.549	0.115	1.343	1.547	1.777	1.009	340
α_0	-0.935	0.167	-1.270	-0.934	-0.605	1.007	870
α_1	0.000	0.000	0.000	0.000	0.000	1.001	2800
σ	52.020	2.675	47.067	51.933	57.585	1.001	2800
ψ	0.783	0.062	0.666	0.782	0.903	1.008	340

For our Bayesian analysis here, we used a rectangular state-space, which doesn’t account for any geographic boundaries of the survey region, but we note that a habitat mask is included in `secr` and it could be used in a Bayesian analysis. Whether or not we use the mask is probably immaterial as long as we understand the predictions of N or D over the water don’t mean anything biological and we probably wouldn’t report such predictions. The **JAGS** model specification is based on that of the ovenbird analysis given previously, and so we don’t reproduce the model here. The **R/JAGS** script is called `SCRpossum`, which is in the `scrbook` package. The results are summarized in Table 9.3.

p0320

The estimated density (posterior mean) is about 1.53 possums/ha. To obtain the `secr` results for the equivalent null model, we execute the following command.

p0325

```
> secr.fit(capthist = possumCH, trace = F)
```

o0765

which produces (edited) summary output:

```
[... some output deleted ...]
```

o0770

```
Fitted (real) parameters evaluated at base levels of covariates
      link estimateSE.estimate      lcl      ucl
D      log 1.6988930 0.17352645 1.3913904 2.0743547
g0     logit 0.1968542 0.02256272 0.1563319 0.2448321
sigma  log51.4689114 2.5998190546.6204139 56.8216500
```

```
[... some output deleted ...]
```

As we’ve discussed previously, there are many reasons for why there might be differences between Bayesian and likelihood estimates. ~~But even among likelihood estimates—any time you run a model there is some numerical integration going on which requires some specific choices of how to do the integration (see Chapter 6).~~

For now we just observe that the estimated density is certainly in the ballpark (compared to those in Table 9.3), and so $\hat{\sigma}$ is the estimated σ .

9.4 Acoustic sampling

s0100

p0335 The last decade has seen an explosion of technology that benefits the study of animal populations. This includes DNA sampling methods that allow for identification from hair or scat, camera trapping and identification software that allow efficient sampling of many mammals, and the resulting statistical technology that helps us to make sense of such data (Borchers and Efford, 2008; Royle and Young, 2008; Efford et al., 2009b; Gopalaswamy et al., 2012b; Sollmann et al., 2013a; Chandler and Royle, 2013). One other extremely promising technology area is that of acoustic sampling using microphones or recording devices. That is, instead of having cameras record encounters, or humans pick up scat, we can establish an array of (usually) electronic recording devices which, instead of establishing a visual identity of individuals, record a vocal expression of each individual. In this context, Efford et al. (2009b) referred to audio recorders as “signal strength proximity detectors” to distinguish them from other types of proximity detections, including camera traps, which are *visual* proximity detector. Using audio records, the spatial pattern of the *signal strength* at the different audio recorders or microphones can be used for inference about density (Dawson and Efford, 2009; Efford et al., 2009b) in the same way as the spatial pattern of detections is used in the types of SCR models we have discussed so far. The basic technical formulation of these models comes from Efford et al. (2009b), and it was applied to field study of birds by Dawson and Efford (2009). In that study, recording devices were organized in groups of 4 (in a square pattern), with an array of 5×15 such clusters of 4, separated by 100 m (300 total recorder locations). This data set, called `signalCH`, is provided with the `secr` package along with some sample analyses and help files. See Efford and Dawson (2010), a version of the document `secr-sound.pdf` (that also comes with the `secr` package) which you can access directly from the main help file (`?secr`).

p0340

Our development here mostly follows Efford et al. (2009b), but we change some notation to be consistent with our previous material. Let $S(\mathbf{x}, \mathbf{u})$ be the strength of a signal emanating from *signal* location \mathbf{u} , as recorded by a device at location \mathbf{x} . Just as ordinary SCR models represent a model of *encounter frequency* as a function of distance, ~~in acoustic models,~~ the acoustic SCR model is a model of sound attenuation as a function of distance. In particular, the acoustic models assumes that S (or a suitable transformation) declines with distance d from the origin of the sound, to the recording device. In the context of spatial sampling of animals, the origin is the actual location of some individual animal, and the recording device is something we nailed to a tree, or mounted on a post. For example, a model of sound attenuation used by Dawson and Efford (2009) is the following:

$$S(\mathbf{x}, \mathbf{u}) = \alpha_0 + \alpha_1 d(\mathbf{x}, \mathbf{u}) + \epsilon, \quad (9.4.1)$$

where $\epsilon \sim \text{Normal}(0, \sigma_s^2)$. In many standard situations, S will be measured in decibels, which can be any value on the real line. ~~In the conduct of acoustic sampling~~

~~and the development of custom models for your own situation, it would probably be helpful to know something about sound dynamics and signal processing.~~ In this model, the parameters α_0 , α_1 , and σ_s^2 are to be estimated. We abbreviate the set of parameters by θ for short.

The basic structure of an acoustic SCR study is not really much different from ordinary SCR studies. Just as ordinary SCR models require that individuals be encountered at >1 trap, these acoustic models require that individuals be heard at >1 recorder. Therefore, the acoustic signals (calls or vocalizations) must be reconcilable and, in fact, reconciled successfully by the investigator. In practice, this would require associating signals that occur at the same instant with the same individual (or making a decision one way or the other). Further, if individuals are actively moving during the sample period (that recorders are functioning) then individuals might be double-counted, thereby biasing estimates of density. In general, the models produce an estimate of density of *sources*, and how that is interpreted depends on whether individuals are stationary or mobile, and other things. In particular, if multiple survey occasions are used (e.g., on different days), then modeling movement of individuals would be essential in order to interpret estimates of density meaningfully. Models that allow some movement should be possible (see Section 9.4.3 below, and Chapters 15 and 16).

9.4.1 The signal strength model

We assert that an individual is detected if S exceeds a threshold, c . The reason for introducing this threshold c is that sound recorders will always record some background sound, and so effective use of the acoustic SCR models requires specification of the threshold of measured signal below which the record is censored (non-detection occurs) because the recorded sound is assumed to be background noise. So we assert that an individual is detected if $S > c$ which occurs with probability $\Pr(S > c)$, the encounter probability. To expand on and formalize this, let S_{ij} be the observed value of S for animal i at detector j . The encounter probability is $\Pr(S_{ij} > c)$ which is $\Pr(S_{ij} > c) = 1 - \Pr(S_{ij} < c)$; so that, if we standardize the variate we have

$$1 - \Pr\left(\frac{(S_{ij} - \mathbb{E}(S))}{\sigma_s} < \frac{(c - \mathbb{E}(S))}{\sigma_s}\right).$$

~~This probability calculation~~ requires evaluation of the CDF of a standard normal variate say, $\eta = (S_{ij} - \mathbb{E}(S))/\sigma_s$, being less than $\gamma(\theta) = (c - \mathbb{E}(S))/\sigma_s$, which is a function of all the parameters α_0 , α_1 , σ_s^2 and the individual location \mathbf{u} and trap location \mathbf{x} . We'll identify it by $\gamma(\theta, \mathbf{x}, \mathbf{u})$ when we need to be explicit about those things. We can compute $\Pr(S_{ij} > c) = 1 - \Pr(\eta < \gamma(\theta, \mathbf{x}, \mathbf{u}))$ easily using any software package including **R** which has a standard function, `pnorm`, for computing the normal cdf. To be more precise, we'll use the $\Phi()$ to represent the normal cdf. Therefore, an individual is encountered whenever $S_{ij} > c$ which happens with probability $\Pr(S_{ij} > c) = 1 - \Phi(\gamma(\theta, \mathbf{x}, \mathbf{u}))$.

Naturally this quantity should depend on *where* an individual is located at the time of recording—what we call its instantaneous location, say \mathbf{u} , to distinguish it from

its home range center \mathbf{s} (but we outline a model below that contains both \mathbf{u} and \mathbf{s}), and the trap \mathbf{x}_j so we index the quantity γ by those two quantities, in addition to the parameters α_0 , α_1 , and σ_s . The probability of detection is therefore

$$p_{ij} = p(\alpha_0, \alpha_1, \sigma | \mathbf{x}_j, \mathbf{u}_i) = 1 - \Phi(\gamma(\cdot)),$$

where \mathbf{u}_i is the instantaneous location of individual i and \mathbf{x}_j is the location of trap j . We'll suppose here that the random variables \mathbf{u}_i have state-space \mathcal{U} .³

p0360 How do we interpret this probability? Well, two things have to happen for an individual to be encountered by a trap: (1) it has to vocalize; (2) the microphone has to record a signal $> c$. These two things together are a product of biological and environmental factors which could include time of day, wind direction, and speed, or maybe rain, humidity, and other things. The bottom line is a lot of factors are balled up in whether or not the microphone records a sound greater than the threshold.

p0365 The observations from an acoustic survey are the signal strength measurements, and the likelihood of the observed signal strength from individual i at detection device j can be specified by noting that the likelihood is the normal pdf for the observed signal if the signal strength is $> c$ and, otherwise, the contribution to the likelihood is $\Phi(\gamma(\cdot))$ (see Eq. 8 of Efford et al. (2009b)):

$$\Pr(S_{ij} | \mathbf{u}_i) = \Phi(\gamma(\cdot))^{1-I(S_{ij}>c)} \text{Normal}(S_{ij}; \alpha_0, \alpha_1, \sigma_s, \mathbf{x}_j, \mathbf{u}_i)^{I(S_{ij}>c)}.$$

p0370 We can use this as the basis for constructing the binomial form of the likelihood as we did in Chapter 6, which involves the number of individuals not encountered, n_0 . The probability that an individual is *not* captured is equal to the probability that its signal strength doesn't exceed c at any microphone. The probability of not being captured at a microphone \mathbf{x}_j is:

$$1 - p_{\mathbf{u},j} = \Phi(\gamma(\cdot))$$

and therefore the probability of not being captured at any microphone is:

$$\Pr(\text{all } S_{\mathbf{u},j} < c | \mathbf{u}) = \prod_{j=1}^J (1 - p_{\mathbf{u},j}) = \prod_{j=1}^J \Phi(\gamma(\cdot, \mathbf{x}_j, \mathbf{u}))$$

and therefore the marginal probability of not being captured is

$$\pi_0 = [\text{all } S_{\mathbf{u},j} < c | \boldsymbol{\alpha}] = \int_{\mathcal{U}} \left\{ \prod_{j=1}^J \Phi(\gamma(\boldsymbol{\theta}, \mathbf{x}_j, \mathbf{u})) \right\} d\mathbf{u},$$

which can be used to construct the binomial form of the likelihood as we did in Chapter 6 (see Eq. 6.2.1).

np015 ³We use \mathcal{U} here to avoid confusion with definition of signal strength, S . However, \mathcal{U} is the same state-space as S in the rest of the book.

9.4.2 Implementation in secr

s0110

Fitting acoustic encounter models in `secr` is no more difficult than other SCR models. There is a handy manual (`secr-sound.pdf`) with examples (Efford and Dawson, 2010) which come with the `secr` package. The basic process is that `make.capthist` will make a `capthist` object from a three-dimensional encounter array—which is a binary array indicating whether each individual was detected or not at each recorder/microphone. In the case of signal strength data, `secr` handles the case where `# occasions = 1`, i.e., the recorders obtained data for a single sample occasion, but this is not a general requirement of the model for signal strength data (see next section). The “signal” attribute of the `capthist` object contains the signal strength in decibels. The best way to include the signal attribute is to use `make.capthist` in the usual way, providing it with the encounter data and trap data and, in addition, the variable “cutval” (which is c in our notation above) and then provide the signal strength data as an extra column of the `capthist` object. See `?make.capthist` for details.

p0375

9.4.3 Implementation in BUGS

s0115

We don’t know of any Bayesian applications of acoustic SCR models, although we imagine that implementation of such models in the **BUGS** engines should be achievable. It seems easy enough to write down a general hierarchical model that would accommodate sampling on repeated occasions. Let \mathbf{s}_i be the home-range center, and let \mathbf{u}_{ik} the instantaneous location of individual i during sample occasion k (see Chapter 15 for similar models). The model for \mathbf{u}_{ik} can be specified conditional on \mathbf{s}_i . For example, we could assume that \mathbf{u}_{ik} are bivariate normal draws with mean \mathbf{s}_i and some variance σ_u^2 . Then, conditional on \mathbf{u}_{ik} an individual produces a signal according to the signal attenuation model (Eq. (9.4.1)), or perhaps some other model. Then we generate the binary encounter data by truncating the observed signal at c . This general model then is an example of an SCR model in which parameters of a movement model are identifiable (see Section 2.6) because there is direct information about movement outcomes from the sampling method, unlike other types of encounter methods (e.g., camera traps) for which animal locations are restricted to a set of fixed, pre-determined points where traps are located. Other types of SCR methods allow for movement information too, including some of the search-encounter models (Chapter 15).

p0380

Instead of developing a Bayesian version of this model here, we leave it to the reader to explore simulating data and devising a Bayesian implementation of the acoustic model in one of the **BUGS** engines. Note that for a single occasion, you can simulate the data using the two-stage model (having both \mathbf{s} and \mathbf{u}) or you can simulate \mathbf{u} uniformly without dealing with \mathbf{s} in the model. The kernel of the **BUGS** model specification should resemble the following snippet:

p0385

```
model {
  # Ignoring loops and data augmentation
  u[i,1] ~ dunif(xlim[1], xlim[2])
  u[i,2] ~ dunif(ylim[1], ylim[2])
  mu[i,j] <- alpha0 + alpha1*d[i,j]
```

o0775

o0780

o0785

o0790

o0795


```
o0800   ###
o0805   ### JAGS has this T() truncation feature
o0810   S[i,j] ~ dnorm(mu[i,j], 1/sigma^2)T(c,Inf)
o0815   ###
o0835   gamma[i,j] <- (c - mu[i,j])/sigma
o0820   p[i,j] <- 1 - pnorm(gamma[i,j], 0, 1) # JAGS has pnorm() function
o0825   y[i,j] ~ dbern(p[i,j])
o0830 }
```

s0120 9.4.4 Other types of acoustic data

p0390 [Efford and Dawson \(2010\)](#) noted that various other types of acoustic data might arise for which SCR-like models would be useful.⁴ For example, we could measure the *time of arrival* of a vocal *queue* of some sort at multiple recorders to estimate the number and origin of N queues. Another example is that where we measure *direction* to a queue from multiple devices and do, effectively, a type of statistical triangulation to the multiple but unknown number of sources. This has direct relevance to types of double or multiple-observer sampling that ~~people do~~ in field studies of birds. Normally, two observers stand in close proximity and record birds, reconciling their detections after data collection. An SCR-based formulation of the double-observer method has two observers (or more) standing some distance apart, e.g., 50 or 100 m, and marking individual birds on a map (or at least a direction) and a time of detection. The SCR/double-observer method could be applied to such data.

s0125 9.5 Summary and outlook

p0395 In this chapter we extended SCR models to accommodate alternative models for the observation process, including Poisson and multinomial models. Along with the binomial model described in Chapter 5, this sequence of models will accommodate a substantial majority of contemporary spatial capture-recapture problems, including the four main types of encounter data: binary encounters, multinomial trials from “multi-catch” and “single-catch” ([Efford, 2004, 2011a](#); [Royle and Gardner, 2011](#)) trap systems, and Poisson encounter frequency data from devices that can record multiple encounters of the same individual at a device. We summarize the standard observation models and the corresponding `secr` terminology in Table 9.4. What we refer to as search-encounter (or area-search) models (see Chapter 15) are distinct from most of the other classes in that the observation location can also be random (in contrast to traps, where the location is fixed by design). This auxiliary data is informative about an intermediate process related to movement ([Royle and Young, 2008](#)).

p0400 There is a need for other types of encounter models that arise in practice. We identify a few of them here, although we neglect a detailed development of them at the present time or, in some cases, put that off until later chapters: (1) Removal

np020 ⁴Some of the following is also related to material presented by D.L. Borchers at the ISEC 2012 conference in Norway.

Table 9.4 Different observation models, where we discuss them in this book, and what the corresponding secr terminology is. sp040

observation Model	Where in This Book?	secr Name
Bernoulli	Chapter 5	proximity
Poisson	Section 9.1	count
Multinomial (ind)	Section 9.2	multi-catch
Multinomial (dep)	Section 20.4.5	single-catch
Acoustic	Section 9.4	signal
Search-encounter	Chapter 15	polygon (in part)

systems—Sometimes traps kill individuals and SCR models can handle that. This can be viewed as a kind of open model, with mortality only, and we handle such models (in part) in Chapter 16; (2) There are models for which only specific summary statistics are observable (Chandler and Royle, 2013; Sollmann et al., 2013a) which we cover in Chapters 18 and 19; (3) We can have multiple observation methods working together as in Gopalaswamy et al. (2012b).

There remains much research to be done to formalize models for certain observation systems. For example, while we think one will usually be able to analyze single-catch systems using the multi-catch model, or even the Bernoulli model if encounter probability is sufficiently low, a formalization of the single-catch model would be a useful development and, we believe, it should be achievable using one or another of the BUGS engines. In addition, classical “trapping webs” (Anderson et al., 1983; Wilson and Anderson, 1985a; Jett and Nichols, 1987; Parmenter and MacMahon, 1989; Link and Barker, 1994) have been around for quite some time and it seems like they are amenable to formulation as a type of SCR model although we have not pursued that development simply because trapping webs are rarely used in practice. p0405

Non Print Items

Abstract: In previous chapters we considered various models of encounter probability, both in terms of parametric functions of distance and ~~also a myriad of~~ covariate models. However, we have so far only considered a specific probability model for the observations (we'll call this the "observation model")—the Bernoulli encounter process model, which in secr is the proximity detector model. This assumes that individual and trap-specific encounters are independent Bernoulli trials. In this chapter, we focus on developing additional observation models. The observation model could be thought of as being determined by the type of device—or, in secr terminology, the type of "detector." We consider models that apply when observations are not binary and, in some cases, that do not require independence of the observations. For example, if sampling devices can detect an individual some arbitrary number of times during an interval, then it is natural to consider observation models for encounter frequencies, such as the Poisson model. Another type of encounter device is the "multi-catch" device, which is a physical device that can capture and hold an arbitrary number of individuals. A typical example is a mist-net for birds. It is natural to regard observations from these kinds of studies as independent multinomial observations. A related group of devices that produces dependent multinomial observations are the so-called single-catch traps. The canonical examples are small-mammal live traps which catch and hold a single individual. Competition among individuals for traps induces a complex dependence structure among individual encounters. To date, no formal inference framework has been devised for this method although the independent multinomial model can be a good approximation. The final sampling method covered in this chapter involves acoustic recording devices, and we explain how to analyze the resulting data. Throughout, several worked examples are presented using ~~using~~ JAGS and secr.

Keywords: Acoustic sampling, Encounter probability, Detection function, Observation model, Poisson model, Multinomial model, Proximity detector, Count detector, Multi-catch detector, Single-catch detector