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Chapter: 5 Capture-Recapture Book: Spatial

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CHAPTER



125

Capture-Recapture Models Fully Spatial

this chapter, which fully recognize the spatial attribution of both individual animals a-small step from this model to spatial capture-recapture models that we consider in hand, only a primitive or no characterization of trap location. That said, there is only sense that it included some characterization of where individuals live but, on the other the trap array. The individual covariate model that we conjured up was "spatial" in the covariate to be the distance from the (estimated) home range center to the center of considered a classical individual covariate modeling approach in which we defined a capture-recapture models. We looked at a basic distance sampling model, and we also poose In the previous chapter, we discussed models that could be viewed as primitive spatial

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uals and the encounter devices because the encounter process occurs at the level of Capture-recapture models must accommodate the spatial organization of individand the locations of encounter devices

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this allows us to compute, for example, the area used by an individual during some are related to explicit models of space usage or "home range area." Understanding range center and trap locations. We also discuss how encounter probability models for encounter probability that is a function of distance between individual home aspect of the SCR models considered in this chapter is the formulation of a model the purposes of producing density maps or spatial predictions of density. The key to its analysis in BUGS. We demonstrate how to summarize posterior output for we refer to as "model SCR0," and address some important considerations related In this chapter we investigate the basic spatial capture-recapture model, which

fully hierarchical model in which we regard s as a latent variable and impose a prior to each trap. And, instead of using estimates of individual locations s, we consider a distance to the centroid of the array we define J individual covariates—the distance that considered in Section 4.5 but, instead of defining the individual covariate to be our first fully spatial capture-recapture model. This model is not too different from trap-specific missing values. In this chapter we resolve these issues by developing tion of "sample area," and not being able to accommodate trap-specific effects or this causes including induced heterogeneity in encounter probability, imprecise notaresolution of the entire trap array. We have previously addressed some problems that cies with classical ad hoc approaches which aggregate encounter information to the individual traps. Failure to consider the trap-specific data is one of the key deficien-

Spatial Capture-Recapture. http://dx.doi.org/10.1016/B978-0-12-405939-9.00005-0

156

CHAPTER 5 Fully Spatial Capture-Recapture Models

al. (2012a) which we address further in Chapter 13). of space usage, this has not been discussed much in the literature (but see Royle et prescribed time. While it is intuitive that SCR models should be related to some model

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5.1 Sampling design and data structure

in trap 3 on the third night is: set for a single individual captured one time in trap I on the first night and one time occasion. For example, suppose we sample at 4 traps over 3 nights. A plausible data individual indicating which trap the individual was captured, during each sample individual. Thus a typical data set will include an encounter history matrix for each data structure yields temporally and spatially indexed encounter histories for each n individuals. Because sampling occurs by traps and over time, the most general of J traps is operated for K sample occasions (say nights) producing encounters of In our development here, we will assume a standard sampling design in which an array

trap2 trapl nighta taubtu εμμδτα

trap4 trap3

Chapter 9.

viduals. This data structure would be obtained for each of the i = 1, 2, ..., n captured indi-

to distill such data into a single binary encounter event for reasons discussed later in trapping, individuals might be photographed several times in a night but it is common the model for data that arise from camera trapping studies. In practice, with camera mültiple detections of an individual are not distinguishable, we will also make use of most directly relevant to hair snares and other DNA sampling methods for which in each trap during any occasion. While this model, which we refer to as SCRO, is to distinct encounter events. Thus, an individual may be captured at most I time attribute multiple visits of the same individual during a single occasion (e.g., night) may encounter multiple bears; however, in practice, it will often not be possible to wandering about its territory might come into contact with >1 devices; a device from bears and other species function according to these rules. An individual bear at most I fime by each trap during any occasion. Hair snares for sampling DNA in more than one trap during each occasion but (iii) individuals can be encountered number of individuals (i.e., they don't fill up); (ii) an individual may be captured and related types of sampling devices in which (i) devices ("traps") may capture any snares" or other DNA sampling methods (Kéry et al., 2010; Gardner et al., 2010b) We develop models in this chapter for passive detection devices such as "hair

vidual encounters within and among traps are independent, and this allows us to The statistical assumptions we make to build a model for these data are that indi-D0030

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more precise as we develop a formal statistical definition of the model shortly. tions define the basic spatial capture-recapture model, SCRO. We will make things next section). These basic (but admittedly at this point somewhat imprecise) assumpregard individual- and trap-specific encounters as independent Bernoulli trials (see

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a binomial random variable which we express as: sions) shown in Table 5.1. We assume that y_{ij} are mutually independent outcomes of then a plausible data set is the 6×4 matrix of encounters (out of 3 sampling occasuppose we observe six individuals in sampling at 4 traps over 3 nights of sampling Wy for $i=1,2,\ldots,n$ captured individuals and $j=\lfloor 1,2,\ldots,J$ traps. For example, out of K. We will denote these individual- and trap-specific encounter frequencies by encounters over the K sample occasions and record the total number of encounters there are no covariates that influence density. In this case, we can aggregate the binary ates that influence encounter, there are no explicit individual-specific covariates, and We begin by considering the simple model in which there are no time-varying covari-

(5.2.1)
$$\text{(2.2.1)} \qquad \text{(5.2.1)}$$

specific, and encounter probability py depends on both individual and trap. except that, in the present case, the encounter frequencies are individual- and trap-This is the basic model underlying standard closed population models (Chapter 4)

activity center of individual i. Then, the SCR model postulates that encounter probafollows, we define s_i , a two-dimensional spatial coordinate, to be the home range or activity (Efford, 2004; Borehers and Efford, 2008; Royle and Young, 2008). In what home range and then relating projectly to a summary of its location relative to ditional on where individual i lives. Naturally, we think about defining an individual As we did in Section 4.5, we will make explicit the notion that p_{ij} is defined con-

Table 5.1 Hypothetical spatial capture-recapture data set showing 6 individbility, p_{ij} , is a decreasing function of distance between s_i and the location of trap j, x_j each trap. For example, the centroid of the individual's home range, or its center of

Royle 978-0-12-405939-9 Perper all 0 0 Ż Trap 4 E gerT Trap 1 Individual .gnildmss to strigin uals captured in 4 traps. Each entry is the number of captures out of K=3

according to: counts is the logistic regression, where we model the dependence of p_{ij} on distance (also a two-dimensional spatial coordinate). A standard model for modeling binomial

(2.2.2)
$$||\mathbf{s} - \mathbf{k}|| ||\mathbf{s}|| + \alpha \mathbf{n} = (\sqrt{\eta}) \text{ ligol}$$

 $\mathbf{s}_i \| = \operatorname{dist}(\mathbf{x}_j, \mathbf{s}_i) = d_{ij}$. Alternatively, a popular model is where, here, $\|x_j - s_j\|$ is the distance between s_i and x_j . We sometimes write $\|x_j - s_j\|$

$$(5.2.3) v_0 \exp\left(-\frac{1}{2\sigma^2} \|\mathbf{x}\|^2 - \mathbf{s}_i\|^2\right),$$

model of movement outcomes or space usage (we discuss this in Section 5.4). context of two-dimensional space, the model is clearly interpretable as a primitive model although the distance sampling term "half-normal" is widely used. In the "individual location" we will refer to it as the "(bivariate) normal" or "Gaussian" a bivariate normal, or Gaussian, probability density function for the random variable intercept $p_0 \le 1$ which can be estimated in SCR studies. Because it is the kernel of which is similar to the "half-normal" model in distance sampling, except with an

There are a large number of standard detection models commonly used (see

in the model, we should express the observation model as center for individual i, si, is an unobserved random variable. To be precise about this we choose for encounter probability, we should always keep in mind that the activity $p_{ij} = 1 - \exp(-\lambda_0 k(x_j, s_i))$ where $k(x_j, s_i)$ is the Gaussian kernel. Whatever model nential model has $p_{ij} = p_0 \exp(-\alpha_1 ||\mathbf{x}_j - \mathbf{s}_i||)$ and the Gaussian hazard model has hazard, negative exponential, and logistic models in Figure 5.1. The negative expobehavior as they approach distance = 0. We show the standard Gaussian, Gaussian forms is they are monologic decreasing with distance, but vary in their characteristic for the Gaussian model $\alpha I = I \setminus (2\sigma^2)$. A characteristic of the common parametric probability model so that the coefficient on distance (or distance squared) is \$\alpha_1\$. So, with parameter naming across models, we will sometimes parameterize any encounter have a parameter that multiplies distance in some non-linear function. To be consistent Chapter 7). All other standard models that relate encounter probability to s will also

$$\langle ((1s; is)q, \lambda) | \text{Binomial} \langle k, p(s; \alpha_1) \rangle$$

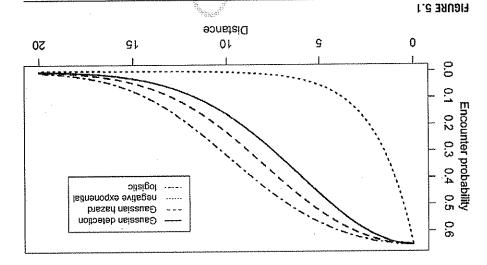
arguments to p. but sometimes, for notational simplicity, we abbreviate this by omitting some of the

Definition of home range center

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the centroid of a very large number of radio fixes over the course of a survey period were active. Thinking about it in that way, it could even be observable (almost) as the space that individual was occupying (or using) during the period in which traps We therefore define the home range center (or activity center) to be the center of time period which has a clear meaning for most species regardless of their biology. We define an individual's home range as the area used by an organism during some

5.2 The Binomial Observation Model



decrease of encounter probability with distance between activity center and trap location. Some common encounter probability models showing the characteristic monotone

a well-defined period of study: interchangeably, and we recognize that this is a transient thing which applies only to itself is a meaningful concept. We use the terms home range center and activity center usage is a well-defined construct regardless of whether one thinks the home range or a season. Thus, this practical version of a home range center in terms of space

5.2.2 Distance as a latent variable

which we may express assumption amounts to a uniform prior distribution on si, i.e., the pdf of si is constant, (the obvious next question: "which space?" is addressed below). This uniformity assumption." which is to assume that the s, are uniformly distributed over space random effects distribution. The customary assumption is the so-called "uniformity to accommodate these random variables with an additional model component—the situation in classical random effects models. We need to therefore extend the model possible circumstances. In that case, d_{ij} is an unobserved variable, analogous to the previously (Chapter 3). However, the activity centers are unobservable even in the best type of a model (with covariate d_{ij}) which we learned how to fit using WinBUGS specified by Eqs. (§.2.1) and (5.2.2) would be just an ordinary logistic regression pooss If we knew precisely every sin the population (and population size N), then the model

 $Pr(s_i) \propto constant.$ (4.2.2)

practice for reasons we discuss shortly. We will give another way to represent this As it turns out, this assumption is usually not precise enough to fit SCR models in

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prior distribution that is more concrete, but depends on specifying the "state-space" of the random variable s₁. The term state-space is a technical way of saying "the space of all possible outcomes" of the random variable.

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5.3 The binomial point process model

In the SCR model, the individual activity centers are unobserved and thus we treat them as random effects. Specifically, the collection of individual activity centers $\mathbf{s}_1, \ldots, \mathbf{s}_N$ represents a realization of a *binomial point process* (Illian et al., 2008, p. 61). The binomial point process (BPP) is analogous to a Poisson point process in the sense that it represents a "random scatter" of points in space—except that the total number of points is fixed, whereas, in a Poisson point process, it is random (having a Poisson of points is fixed, whereas, in a Poisson point process the distribution). As an example, we show in Figure 5.2 locations of 20 individual activity centers (black dots) in relation to a grid of 25 traps. For a Poisson point process the number of such points in the prescribed state-space would be random whereas often we will simulate fixed numbers of points, e.g., for evaluating the performance of procedures, e.g., how well does our estimator perform when N = 50?

It is natural to consider a binomial point process in the context of capture-recapture models because it preserves W in the model and thus preserves the linkage directly with closed population models. In fact, under the binomial point process model, model with closed population models. In fact, under the binomial point process model, model

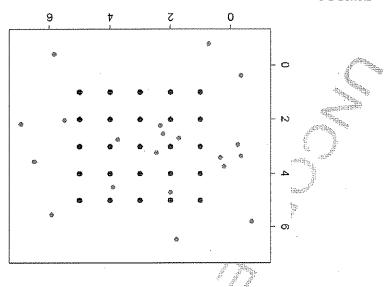


FIGURE 5.2

Realization (small dots) of a binomial point process with N=20. The large dots represent trap locations.

5.3 The Binomial Point Process Model

131

Mo and other closed models are simple limiting cases of SCR models, i.e., they arise

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assumptions are closely related in the usual limiting sense. that M has a Poisson distribution in some cases (see Chapter 14): Of course, the two coherent approach to analyzing the different classes of models. We might also assume Bayesian analysis of the models as in Chapter 4, thus yielding a methodologically binomial distribution, we can make use of data augmentation, our preferred tool, for be convenient to impose specific prior distributions on M. By assuming M has a While we often will express SCR models 'conditional-on-N," it will sometimes

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in Chapter II. addition, we can build more flexible models for the point process, which we take up data, to produce a posterior distribution which may appear distinctly non-uniform. In distribution which is directly affected by the quantity and quality of the observed we come back to repeatedly in this book. The uniformity hypothesis is only a prior the resulting posterior point pattern can deviate strongly from uniformity, a point SCR models is that we actually have a little bit of data for some individuals and thus patterns without violating the assumption of spatial randomness. More relevant for enormously useful in practical settings since they allow for a range of distribution distributed. For this reason, the basic binomial (or Poisson) point process models are distributed points will almost never appear regularly, uniformly, or systematically points will typically exhibit distinct non-uniformity. Thus, independent, uniformly this independence we see in Figure 5.2 that realizations of randomly distributed each activity center is distributed independently of each other activity center. Despite BPP model as one of spatial independence among individual activity centers because effect on any inference or analysis and, as a practical matter, we will usually regard the in the distribution of points. However, in most situations this will have no practical Illian et al., 2008, p. 61). Thus, the BPP model introduces a slight bit of dependence then these counts are not independent. In fact, they have a multinomial distribution (see $n(A_1), \ldots, n(A_k)$ in any set of disjoint regions of the state-space, say A_1, \ldots, A_k , strictly a model of "complete spatial randomness." This is because, if one forms counta One consequence of having fixed N in the BPP modelizathat the model is not

5.3.1 The state-space of the point process

a region or a set of points comprising the potential values (the support) of the random literature. We denote the state-space henceforth (throughout this book) by S, which is state-space, which is sometimes called the observation window in the point process the region over which they are distributed. This is the quantity referred to above as the posterior distribution. In order to simulate the s₁, it is necessary to describe precisely quantities and we will need to be able to simulate each s; in the population from the analysis. To do this, we note that the individual activity centers s_1, \ldots, s_N are unknown we can gain some basic experience with important elements of the model, and its Shortly we will focus on Bayesian analysis of model SCR0 with N known so that

variable s. Thus, an equivalent explicit statement of the "uniformity assumption" is

(S)mrofinU $\sim i$ s

over some region, the point process is usually called a homogeneous point process. selecting each coordinate on the line [-1, 7]. When points are distributed uniformly by $[-1,7] \times [-1,7]$. Thus each of the N=20 points was generated by randomly where S is a precisely defined region, e.g., in Figure 5.2 S is the square defined

5.3.1.1 Prescribing the state-space

arbitrary, once S is chosen, it defines the population being exposed to sampling, which S as long as S is sufficiently large. Thus, while choice of S is (or can be) essentially prior assumption of constant density. As a result, we say that density is invariant to that M increases with S, but only at the same rate as the area of S increases under the that the choice of a state-space is not ad hock As we observed in Chapter 4, it is true of specifying a "buffer" which we have cuttored as being ad hoc. How is it, then, possibly do this objectively? Prescribing any particular S seems like the equivalent Evidently, to define the model, we need to define the state-space, S. How can we

For our simulated system developed previously in this chapter, we defined the statescales appropriately with the size of the state-space.

to be a regular continuous polygon (a rectangle). an analysis of the wolverine camera trapping data, in which we define the state-space (see Section 17.7), but not so easily in the BUGS engines. In Section 5.10, we provide of polygons stored as a GIS shapefile which can be analyzed easily by MCMC in R habitat(see Section 5.10). We can also define the state-space as an arbitrary collection points to be deleted or not, depending on whether they represent available or suitable Defining the state-space by a discrete set of points is handy because it allows specific (Efford, 2011a) permits (secr uses the term "mask" for what we call the state-space). representation of the state-space as a discrete set of points which the R package sect mathematical terms that can be used in BUGS. As an alternative, we can provide a oceans, large lakes, ice fields, etc.). It is difficult to describe complex regions in problem of admitting into the state-space regions that are distinctly non-habitat (e.g., in BUCS and cannot for irregular polygons), a regular polygon induces an apparent polygon has computațional advantages (e.g., we can implement this more efficiently a rectangle around the trappartay. Although defining the state-space to be a regular situations this might be an acceptable approach to defining the state-space, i.e., just space to be a square within which our trap array was centered. For many practical

5.3.1.2. Invariance to the state-space

individuals captured in some interval $[d_{j-1}, d_j)$, and define $d_j = B$ for some large an analogy with a 1-d case involving distance sampling. Let y be the number of p_{ij} to s_i is a decreasing function of distance. We can prove this easily by drawing the size and extent of S, if S is sufficiently large, and as long as our model relating We will assert for all models we consider in this book that density is invariant to

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5.3 The Binomial Point Process Model 133

value of B. The observations from a survey are y_1, \ldots, y_J and the likelihood is a multinomial likelihood, so the log-likelihood is of the form

$$\log L(\gamma_1, \ldots, \gamma_l) \le \sum_{i=l}^{l} = (\gamma_i, \ldots, \gamma_l) \log L(\gamma_i)$$

where π_J is the probability of detecting an individual in distance class J, which depends on parameters of the detection function (the manner of which is not relevant for the present discussion). Choosing B sufficiently large guarantees that $\mathbb{E}(y_J) = 0$ and therefore the observed frequency in the "last cell" contributes nothing to the likelihood, in regular situations in which the detection function decays monotonically with distance and prior density is constant. We can think of B as being related to the state-space in an SCR model, as the width of a rectangular state-space with area $B \times L$, L being the length of the transect. Thus, if we choose B large enough, then we ensure that the expected trap frequencies beyond B will be 0, and thus contribute nothing to the likelihood

nothing to the likelihood.

Sometimes our estima

znonsoilqmi therefore the size of the augmented data set M must increase. This has computational If you increase the size of S, then there are more individuals to account for and consideration, we note that the area of the state-space S affects data augmentation. demonstrate this in our analysis of Section 5.9 below. As an additional practical "sensitivity to priog" argument that Bayesians always have to be conscious of. We of density estimates by trying a couple of different choices of S. This is a standard S to be very large in order to achieve invariance or, otherwise, evaluate sensitivity For situations where there is not a natural choice of S, we should default to choosing artifact—and it should be resolved with better information, research, and thinking. formalization of capture-recapture models—a feature, not a bug or some statistical estimate. But this is a real biological problem, and a natural consequence of the spatial on differing opinions, and GIS layers, might have substantial affects on the density habitat preferences, that a problem could arise because changing the state-space based could imagine, however, in specific gases, e.g., a small population with well-defined might be sensitive to its definition in problems where it is natural to restrict S. One Chapter 1, S is part of the model, and thus it is sensible that estimates of density However, this might be sensible if S is naturally well defined. As we discussed in Sometimes our estimate of density can be affected by choosing S too small.

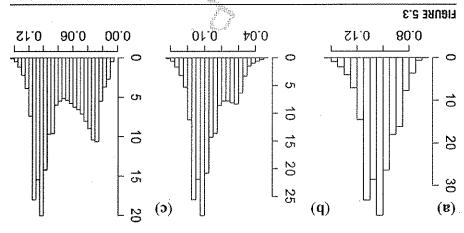
5.3.2 Connection to model M_h and distance sampling

SCR models are closely related to "model M_h " and distance sampling. In SCR models, heterogeneity in encounter probability is induced by both the effect of distance in the model for detection probability and from specification of the state-space. Hence, the state-space is an explicit element of the model. To understand this, suppose activity seater-space is an explicit element of the model. To understand this, suppose activity centers have the uniform distribution:

centers have the unitorm distribution:

 (\mathcal{S}) mnolin $U \sim \mathbf{z}$

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Implied distribution of p_i for a population of individuals as a function of the size of the state-space buffer around the trap array. The state-space buffer is 0.2, 0.5, and 1.0 for panels (a), (b), (c), respectively. In each case, the trap array is fixed and centered within a square state-space.

and encounter probability is a function of s, denoted by p(s) = p(y = 1|s). For example, under Eq. (5.2.2) we have that

$$\|\mathbf{r}_{\mathbf{k}}(\mathbf{s})\|_{\mathbf{k}} = \|\mathbf{r}_{\mathbf{k}}\|_{\mathbf{k}} = \|\mathbf{r}_{\mathbf{k}}\|_{\mathbf{k}} = \|\mathbf{r}_{\mathbf{k}}\|_{\mathbf{k}}$$

and we can work out, either analytically or empirically, what is the implied distribution of p for a population of individuals. Figure 5.3 shows a histogram of p for a hypothetical population of 100,000 individuals on a state-space enclosing our 5×5 trap array above, under the logistic model for distance given by Eq. (5.2.2) with buffers of 0.2, 0.5, and 1.0. We see the mass shifts to the left as the buffer increases, implying more individuals with lower encounter probabilities, as their home range centers increase in distance from the trap array.

Another way to understand this is by representing S as a set of discrete points on a grid. In the coarsest possible case where S is a single arbitrary point, then every individual has exactly the same p. As we increase the number of points in S, more distinct values of p are possible. Indeed, when S is characterized by discrete points, then SCR models are precisely a type of finite-mixture model (Norris and Pollock, 1996; Pledger, 2004), except, in the case of SCR models, we have some information about which group an individual belongs to (i.e., where their activity center is), as a result of which traps it is captured in.

It is also worth reemphasizing that the basic SCR encounter model is a pinomial encounter model in which distance is a covariate. As such, it is attained a similar to classical distance sampling models (Buckland et al., 2001). Both have distance as a covariate but, in classical distance sampling problems, the focus is on the distance between the observer and the animal at an instant in time, not the distance between a

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5.4 The Implied Model of Space Usage

132

tities other than density, such as home range size, and space usage () ded Chapters 12 as perfect detection at distance zero, and SCR models allow for estimates of quanallow us to relax many of the assumptions made in classical disfance sampling, such e.g., when studying carnivores such as bears or large cats. Furthermore SCR models but distance sampling requires field methods that are not practical in many situations, form of trap observations). Clearly, it is preferable to observe distance if possible, in SCR problems, it is only imperfectly observed (we have partial information in the "distance" is observed for those individuals that appear in the sample. Conversely, trap and an animal's home range center. As a practical matter, in distance sampling,

S.A The implied model of space usage

homogeneous space). or space usage (the latter term meaning resource selection, when the resource is only mean to imply is something that would be more clearly identified as resource selection activity center. While we have used the term "home range" or similar, what we really example, 95% of animal movements are within some distance from an individual's extent of area used some prescribed percentage of the time. So we might say, for that any given detection model implies a model of space usage—i.e., the amount and range geometry and size. Here we explore the natifie of that relationship and we argue of individuals in specific traps to s, must somehow imply a certain model for home ter or activity center. Surely the encounter probability model, which relates encounter We developed the basic SCR model in terms of a latent variable, s, the home range cen-

of a trapping device it is natural to decompose encounter probability according to: within its home range ("space usage"), and detection conditional on use in the vicinity two processes: movement of an individual about its home range, i.e., how it uses space individuals Indeed; it is natural to interpret the detection model as the composite of Intuitively, the detection function of SCR models is related to space usage by

Pr(encounter at x | s) = Pr(encounter usage of x, s) Pr(usage of x | s).

during the period of sampling). meaningful as a description of transient space usage as well (that is, the space usage would call a central place forager although, as we have stated previously, it may be the use frequency of each x. This is a sensible heuristic model for what ecologists to this model for individual movements about their home range center determining cells) and then, in that case, the encounter probability model is directly proportional usage of x, s) as being a constant (e.g., it traps are located within arbitrarily small grid In practice it might make sense to think about the first component, i.e., Pr (encounter)

(e.g., continuous telemetry) so that we observe every time an individual moves into a representation of space), and that we have some kind of perfect observation device in consists of some large number of small pixels (i.e., we're looking at a discrete To motivate a specific model for space usage, imagine the area we are interested

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pixel. After a long period of time, we observe an enormous sample size of x values. We tally those up into each pixel, producing the frequency m(x, s), which is something like the "true" usage of pixel x by individual with activity center s. So, then, the usage model should be regarded as a probability mass function for these counts and, naturally, we regard the counts m(x, s) as a multinomial observation with probabilities accumulate in space. A natural null model for $\pi(x|s)$ that describes how use events should accumulate in space. A natural null model for $\pi(x|s)$ that describes how use events should accumulate in space. A natural null model for $\pi(x|s)$ that describes how use events should use as x gets far away from s; i.e., animals spend more time close to their activity of centers than far away. We can regard points used by the individual with activity centers than far away. So a point process with conditional intensity:

(1.4.2)
$$\frac{(\mathbf{g}(\mathbf{x}))\lambda}{(\mathbf{g}(\mathbf{x}))\lambda_{\mathbf{x}}} = (\mathbf{g}|\mathbf{x})\pi$$

where k(x, s) is any positive function. In continuous space, the equivalent represent

$$\frac{(\mathbf{s}, \mathbf{x})\lambda}{\mathbf{s}} = (\mathbf{s}|\mathbf{x})\pi \qquad \qquad \begin{pmatrix} \mathbf{s} & \mathbf{s} \\ \mathbf{s} & \mathbf{s} \end{pmatrix}$$

Clearly the space used by an individual will be proportional to whatever kernel, k(x, s), we plug in these Lf we use a negative exponential function, then this produces a standard resource selection function (RSE) model (e.g., Manly et al., 2002, Chapter 8). But, here we use a Gaussian kernel, i.e.,

$$k(\mathbf{x}, \mathbf{s}) = \exp(-d(\mathbf{x}, \mathbf{s})^2/(2\sigma^2))$$

so that contours of the probability of space usage resemble a bivariate normal or Gaussian probability-distribution function.

To apply this model of space usage to SCR problems we allow for imperfect points detection by introducing a non-uniform "thinning rate" of the true counts $m(\mathbf{x}, \mathbf{s})$. This yields, precisely, our Gaussian encounter probability model where the thinning rate is our baseline encounter probability p_0 for each pixel where we place a trap, and the is our baseline encounter probability p_0 for each pixel where we place a trap, and

p = 0 in each pixel where we don't place a trap. The main take-away point here is that underlying most SCR models is some kind potent of model of space usage, implied by the specific choice of k(x, s). Whether or not

of model of space usage, implied by the specific choice of $k(\mathbf{x}, \mathbf{s})$. Whether or not we have perfect sampling devices, the function we use in the encounter probability model equates to some conditional distribution of points, a utilization distribution, as in Eq. (5.4.1), from which we can compute effective home range area, i.e., the area that contains some percent of the mass of a probability distribution proportional to that contains some percent of the mass of a probability distribution proportional to

5.4.1 Bivariate normal case

One encounter model that allows direct analytic computation of home range area is potes

$$p(\mathbf{x}, \mathbf{s}) = p_0 \exp\left(-\frac{1}{2\sigma^2} \|\mathbf{x} - \mathbf{s}\|^2\right).$$

5.4 The Implied Model of Space Usage

For this model, encounter probability is proportional to the kernel of a bivariate normal (Gaussian) pdf and so the natural interpretation is that in which movement outcomes (or successive locations of an individual) are draws from a bivariate normal distribution with standard deviation σ . We say that use of this model implies a bivariate normal model of space usage. Under this model we can compute precisely the effective home range area. In particular, if use outcomes are bivariate normal, then $\|\mathbf{x} - \mathbf{s}\|^2$ has a chi-square distribution with Σ df and the quantity $B(\alpha)$ that encloses $(1-\alpha)$ % of all realized distances, i.e., $\Pr(d \le B(\alpha)) = 1 - \alpha$, is $B(\alpha) = \infty \sqrt{q(\alpha, \Sigma)}$ where $q(\alpha, \Sigma)$ is the 0.05 chi-square critical value on Σ df. For example, to compute $q(.05, \Sigma)$ where σ is the 0.05 chi-square critical value on Σ df. For example, to compute $q(.05, \Sigma)$ in \mathbf{R} we execute the command qchi sql σ (0.05) which is σ (2.01) at σ (2.02) in practice, we can σ 1, σ (3) and then use the bivariate normal encounter probability model to some σ 2.447 (standard deviation) units of the home range center. So, in practice, we can σ 1, σ 2.447 (standard deviation) units of the home range center. So, in practice, we can also and then use the estimated σ to compute the "95% radius," say σ 2.95. σ 4.579.

movement outcomes—according to $A_{.95} = \pi v_{.95}^{-95}$. An alternative bivariate normal model is the bivariate normal hazard rate model:

 $(5.4.2) \qquad \int \left(-\lambda_0 |\mathbf{s} - \mathbf{x}| \left\| \frac{1}{2_0 2} \right\| \mathbf{x} - \mathbf{s} \right) d\mathbf{x} d\mathbf{x} = 1 - \exp\left(-\lambda_0 |\mathbf{s} - \mathbf{x}| \right)$

We use λ_0 here because this parameter, the baseline encounter vate, can be > 1. This arises by assuming the latent "use frequency" $m(\mathbf{x}, \mathbf{s})$ is a Poisson random variable with intensity $\lambda_0 k(\mathbf{x}, \mathbf{s})$. The model is distinct from our Gaussian encounter model partially in terms of estimates of density or 95% use area, as long as baseline encounter probability is low. We discuss these two formulations of the bivariate normal model further in Chapter 9.

5.4.2 Empirical analysis

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Por any encounter model we can compute space usage quantiles empirically by taking a fine grid of points and either simulating movement outcomes with probabilities proportional to $p(\mathbf{x}, \mathbf{s})$ and accumulating area around \mathbf{s} , or else we can do this precisely by varying $B(\alpha)$ to find that value within which 95% of all movements are concentrated, i.e., the set of all \mathbf{x} such that $\|\mathbf{x} - \mathbf{s}\| \le B(q)$. Under any detection modelymovement outcomes will occur in proportion to $p(\mathbf{x}, \mathbf{s})$, as long as the probability of encounter is constant, conditioned on that $\|\mathbf{x} - \mathbf{s}\| \le B(q)$. As the probability of encounter is constant, conditioned on the probability of encounter is constant, conditioned on the proportion of encounter is constant.

distribution according to: $\pi(\mathbf{x}, \mathbf{x}) = \frac{(\mathbf{x}, \mathbf{x})_{q}}{\sqrt{2}} = (\mathbf{x} | \mathbf{x})_{\pi}$

Given the probabilities $\pi(x,s)$ for all x we can find the value of B(q), for any q, such

$$p-1 \ge \left((\mathbf{s}, \mathbf{x}) \pi \sum_{(p) \, d \ge \|\mathbf{s} - \mathbf{x}\| \in \mathbf{x}} \right)$$

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CHAPTER 5 Fully Spatial Capture-Recapture Models

(here, we use ∋ to mean "such that"). We have a function called hra in the scrbook package that computes the home range area for any encounter model and prescribed parameter values. The help file for hra has an example of simulating some data. The following commands illustrate this calculation for two different bivariate normal models of space usage:

```
IS7266E.0 [I]
54100
                                                     00140
                                 trule sigms that produces area of 3
26100
                                                       ## Analytic solution:
00130
                                                                 εεένοο.ε [τ]
00125
                                                   home range area: 3.007353
00100
                                   radius to adhieve 95% of area: 0.9784019
SILOO
                                                                6104876.0 [I]
01100
                                                     (S000)=[04'00S=Bu
90100
     (0,0) D=milY,(0,0) D=milx, AZLAY=Jolq,(8998.,S-) D=smrsq, LasusDq) srd <
00100
$600°
                                          ## Execute hra with sigma = .3993
06000
₹8000
0800o
$700o
     p \leftarrow plogis(parms[1]) * exp(1)(2*parms[2]*parms[2])) * Dmat*Dmat*Dmat)
00000
                                                        sigma <- parms[2]
59000
                                                           90 <- parms[1]
09000
                                          > pGauss1 <- function(parms,Dmat)
55000
05000
54000
                                                    D <- J-exp(-exp(Jp))
000040
                  Lp <- parms[1] -(1/(2*parms[2]*parms[2])*Dmat*Dmat</pre>
90000
                                                        sigma <- parms[2]
06000
                                                           a0 <- parms[1]
00052
                                         } (Jemas, Dmat) on (parms, Dmat) {
02000
$1000
                      ## Define encounter probability model as R function
01000
$0000
```

What this means is that B(q) = 0.978 is the radius that encloses about 95% of all movements under the standard bivariate normal encounter model. Therefore, the area is about $\pi * .978^2 = 3.007$ spatial units. You can change the intercept of the model and find that it has no effect. The true (analytic) value of σ that produces a home range area of 3.0 is 0.3993 which is the value we initially plugged in to the hrz function. We can improve on the numerical approximation to home range area (get it closer to 3.0) by increasing the resolution of our spatial grid (increase the negacinative of the total argument.

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target. area = 3.00735 (from above) to obtain a close approximation to the by simply providing a non-null value of the variable target. areas Here we use of the scale parameter that achieves a certain target (1-q)% home range area, be useful for doing simulation studies. The function has will compute the value values that produce a certain (1-q)% home range area, which we imagine would We can also reverse this process, and find, for any detection model, the parameter

target.area=3.00735,tol=.0005) . hra (pGausal, parms=c(.2,.3993), plot=TALSE, xlim, ylim, ng=500, value σ we started with (the parameter argument is meaningless here):

00155 Value of parm[2] to achieve 95% home range area of the convact 0.3993674

5.4.3 Relevance of understanding space usage

each pixel say C(x), on home range size and geometry and, hence, the probability keting a landscape. We use this idea to model the effect of a measured covariate at but telemetry data produce "perfect" observations, like always-on camera traps blantwo sources of data as resulting from the same underlying process of space usage telemetry relocations on a sample of individuals. This is achieved by regarding the produces encounter history data suitable for SCR models and, in addition, we have In Chapter 13 we consider this problem, for the case in which a sample of individuals traditional resource selection data from telemetry with spatial capture-recapture data. models of encounter probability and space usage is that it opens the door to combining models to the same currency. Another reason to understand the relationship between different manner under each model. Therefore, we want to be able to convert different ter, which we might call o no matter the model, but this relates to 95% area in a biological currency. Many encounter probability models have some scale paramedetection model is so that we can compare different models with respect to a common Orion One important reason that we need to be able to deduce "home range area" from a

5.4.4 Contamination due to behavioral response

paited trap, so that observed movement distances of individuals are typically larger would change how individuals use their range, e.g., by moving from baited trap to normal. More likely, in our view, it wouldn't change the typical size of a range but animals from a long distance, it could make typical home ranges appear larger than (Section 7.2.3) which could affect animal space usage. For example, if traps attract baited or not. In the case of baited traps, this might lead to a behavioral response space usage can be complicated by a number of factors, including whether traps are poiss Interpretation of engounter probability models as models of animal home range and

2013). For example, animals might concentrate their movements along trails, roads, ability might be unrealistic and can lead to biased estimates of density (Royle et al., In other cases, the reliance on Euclidean distance in models for encounter prob-

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of encounter in traps

5.5 Simulating SCR data

or other landscape features. In this case, models that accommodate other distance metrics can be considered. We present models based on least-cost path in Chapter 12.

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It is always useful to simulate data because it allows you're understand the system that you're modeling and calibrate your understanding with specific values of the model parameters. That is, you can simulate data using different parameter values until you obtain data that "look right" based on your knowledge of the specific situation that you're interested in. Here we provide a simple script to illustrate how to simulate spatial encounter history data. In this exercise we simulate data for 100 individuals and a 25 trap array laid out in a 5×5 grid of unit spacing. The specific encounter model is the Gaussian model given above and we used this code to simulate data used in subsequent analyses. The 100 activity centers were simulated on a state-space defined by an 8×8 square within which the trap array use centered (thus the trap array is buffered by 2 units). Therefore, the density of individuals in this system is fixed at 100/64:

```
# Generate the encounters of every individual in every trap
$8200
                                       \Ox0*isApta -) qxe*(2.2-) sigoid -> qsodoxq <</pre>
00280
SLZ00
                                                # Compute Probability of encounter:
00270
               > alphal <- l/(2*sigma*sigma) # convert to coefficient on distance
9700
                           # scale parameter of half-normal
                                                                     2.0 -> smpis <
09700
                                                                    2.5- -> 0shqls
              # define parameters of encounter probability
90255
                                                          > D <- eSqiat (S) craploca)
      # distance of each individual from each trap
05200
                                                         Compute distance matrix:
2000
                                                                 (ya,xa)bnido==> 2 <
00240
                                                                             ->≞Ya <
                                                   ((S)milx,[1]milx,N)limux >> xs
([S]mily,[1]mily,N)limux >> \quad \text{y}a
SEZOO
                 # simulate activity centers
00230
                                                                       > K <- 30
                                          # number nights of effort
90525
                                                   ezts uotaeindod #
00220
               > ylim <- c(min(traplocs[,2] - buffer), max(traplocs[,2] + buffer))
51200
               > xJim <- c(min(craplocs[,1] - buffer), max(traplocs[,1] + buffer))
01200
$0200
00200
            "buffer" just adds a lixed buffer to the outer extent of the traps.
S6100
               # Define state-space of point process. (i.e., where animals live).
06100
                                                > Dmat <- e2dist(traplogs,traplocs)
28100
                                                         # Compute distance matrix:
08100
                                                        > vrxsbs <- vxow(rxsbjogs)
$2100
                                  0/100
                           # Create 5 x 5 grid of trap locations with unit spacing
$9100
                                                                    > set,seed(2013)
09100
```

5.5 Simulating SCR Data

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1110NB 108

```
0610d
                                              50500
Y[i,] <- rbinom(ntraps, K, probcap[i,])
                                               00500
                    > tor(t in 1:nrow(X)){
                                              $6700
     > Y <- matrix(NA, nrow=N, ncol=ntraps)
```

inferred by the reader in trying to understand code snippets (for n), ntraps (for J), and noce (for K). In our opinion this leaves less to be particular, we sometimes substitute words for integer variable designations: nind book, we will deviate from our standard variable expressions for some quantities. In We remind the reader that, in presenting R or other code snippets throughout the

encounter frequencies (see below). Finally we provide a random number seed, rnd three-dimensional encounter history array instead of the aggregated $n \pm n d \times n \cot apa$ captured individuals. A second argument is array3d which, if TRUE, returns the including discardo which, if TRUE, will return only the encounter histories for called aimSCRO in the package scrbook which takes a number of arguments Subsequently we will generate data using this code packaged in an R function

using the following command: = 2013, to ensure repeatability of the analysis here. We obtain a data set as above

> data <- simSCR0(discard0=TRUE; array3d=FALSE, rnd=2013)

some of its elements for further analysis below: The R object data is a list, so let's take a look at what's in the list and then harvest

```
52500
                                                                пКи
                                                  "traploca" "xlim"
                                                                                  [T]
                                                                                        00320
            "alphao"
"ретаб"
                                                                       > names(data)
                                                                                        $1500
```

Grab the trap locations Y <- data\$Y ## Grab encounter histories from simulated data list 06500

> fxsbloca <- datagrzaploca

Stadleted SIN 200 77,0M

5.5.1 Formatting and manipulating real data sets

standard formats: mation/intille encounter history information. We will routinely analyze data from three spatial capting-recapture models. For SCR models we must preserve the spatial inforis maximally informative for any conventional capture-recapture model, but not for dimensional array, an nind × K (individuals by sample occasions) matrix, which Conventional capture-recapture data are easily stored and manipulated as a two-

of encounters in each trap, summed over the K sample occasions. frequency matrix such as that simulated previously. These are the total number oli65 (1) The basic two-dimensional data format, which is an nind \times ntraps encounter

the convention that it has dimensions nand \times nersps \times K. olive (2) The maximally informative three-dimensional array, for which we establish here

> SOZOO (S WD) DD 02008

\$610d

678-0-12-405939-9

(3) We use a compact format—the "encounter data file" which we describe below of in Section 5.9.

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To simulate data in the most informative format—the "3-d agray"—we can use the R commands given previously but replace the last four lines with the following:

We see that a collection of K binary encounter events are generated for each individual and for each trap. The probabilities of those Bernoulli trials are computed based on the distance from each individual's home range center and the trap (see calculation above), and those are housed in the matrix probcap. Our data simulator function simspecto will return the full 3-d array if array3d=TRUE is specified in the function call. To recover the 2-d matrix from the 3-d array, and subset the 3-d array to individuals that were captured, we do this:

```
# Keep those individuals that were captured

# Keep those individuals that were captured

# Keep those individuals that were captured

# Y2d <- Y2d x - Y[ncaps 0, 7]

# Y2d <- Y[ncaps 0, 7]

# Xeep those individuals that were captured

# Xeep those individuals that were captured

# Xeep those individuals that were captured
```

SaU8 ni OAO2 labom gnitti 8.8

scoos Mosaile februa sid, 48 kines am 14 % 3 % in 10 %

Clearly if we somehow knew the value of N then we could fit this model directly because, in that case, it is a special kind of logistic regression model, one with a random effect (s) that enters into the model in a peculiar fashion and also with a distribution (uniform) which we don't usually think of as standard for random effects. So our aim here is to analyze the known-N problem, using our simulated data, as an incremental step in our progress toward fitting more generally useful models. To begin, we use our simulator to grab a data set and then harvest the elements of the

resulting object for further analysis: > data <- aimSCR0 (discardo=FALSE, rnd=2013) > traplocs <- data\$traplocs

In this case nind=N because we're doing the known-N problem 00425

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5.6 Fitting Model SCRO in BUGS

```
06500
                           p[i,j] \leftarrow p0*exp(-alghall*d[i,j])*([i,i])
                                                                             90225
                                             λ[t,j] ~ dbin(p[i,j],K),
                                                                             002500
 (2.0,(S,[S,t]X-[S,t]a) woq + (S,[\frac{r}{L},t]\frac{x}{R}-[L,t]a) woq) woq -> [t,t]b
                                                                             $1500
                                                          {(T: I ni [) rol
                                                                             01500
                                    [2,1] ~ dunif(ylim[l],ylim[2])
                                                                             50500
                                      ([[S]milx,[I]milx)linub ~ [I,i]e
                                                                             00200
     in is KNOWN in this example
                                       # note N here
                                                           for(f in 1:N){
                                                                             $6$00
                                             sigma <- sqrt(1/(2*alphal))
                                                                             06400
                                                     (f.,0)mxonb ~ Lanqia
                                                                             $840a
                                                     logit(p0) <- alpha0
                                                     (1.,0) mronb ~ 0shqls
                                                                     model {
                                                                             07400
                                                                       cat ("
                                                                             29400
                                         model using the following commands:
viduals. Now, within an R session, we can create the BUGS model file and fit the
set, i.e., one with the all-zero encounter histories corresponding to uncaptured indi-
Note that we specify discardo = FALSE so that we have a "complete" data
                                                                              $220q
                                                     > ylim <- data$ylim
                                                                             09400
                                                     milx$stab -> milx <
                                                            > K <- data$K
                                                           > 1 <- uxow(X)
                                # unmper of traps
                                                   > X <- data$traplocs
                                                        00432 > ujuq <- uxom(X)
                                                                             06430
```

the intercept parameter p.o. Note that the distance covariate is computed within the probability to be in [0, 1] which we do here by defining alpha0 to be the logit of consequence of using the half-normal is that we have to constrain the encounter trivial to modify that to various others including the logistic described above. One This model describes the Gaussian encounter probability model, but it would be

WinBUGS as data. BUGS model specification given the matrix of trap locations, X, which is provided to

replace those values by each individual's mean trap coordinate for all encounters: uniform random numbers in the state-space but, for the observed individuals, we MCMC settings. We choose initial values for the activity centers s by generating WinBUGS, defining some initial values, the parameters to monitor and some basic Next we do a number of organizational activities including bundling the data for

5,21 10

 $j_{\chi}(y[i,j]) = ([i,j])$ cocno } (putu: t ut t) xot <</pre> 09500 (([S]mify,[1]mify,bnin)linux,([S]mifx,[i]mifx,bnin)linux)bnido -> dee < cccoo ### Starting values for activity centers, s

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p0230

54500 09500 26500

```
n.burnin=1000, n.iter=2000, debug=TRUE, working.dir=getwd())
       > out -> buga (data, inits, parameters, "SCROa.txg", n.thin=1, n.chain=3,
$1900
                                       > parameters <- c("alpha0", "alpha1", "sigma")
01900
                                                                 > library(R2WinBUGS)
$0900
00900
                    (Jes=s____(S_L,I)linu=IsAqIs ,(4.,4-,I)mxonr=0sAqIs) Jail
96900
                                                              }()uotabung -> satut <</pre>
06500
                 > data <- list (y=y, X=X, K=K, N=nind, J=J, xlim=ylim) >
$8500
08500
                                              ast[i,2] <- mean( X[y[i,]>0,2] )
STZOO
                                               [1,0<[1,1] <- mean ( X[y[1,] dean ->
02500
```

script provided in the R package scrbook might explore the output and investigate addiffonal analyses by running the aimsCRO There is little to say about the preceding operations other than to suggest that you

kernel, i.e., $\sigma = \sqrt{1/(2\alpha_1)}$. When the object out is produced we print a summary alphal), along with the derived parameter of the scale parameter of the Gaussian set we only have two parameters of the defection model to summarize (alphao and chains, to obtain 3000 posterior samples. Because we know M for this particular data For purposes here, we ran 1000 burn-in and 1000 post-burn-in iterations, and 3

> print (out, digits=2) of the results as follows:

```
[...some output deleted...]
                                                                91.15
                                                       09'552
                                                                         08:262
                05.655
                          306,00
                                   391.90
                                             377.50
        TO'E
                                                               ₽0 °0
                                                                                      engrs
                                             EF.0
                                                       68.0
                                                                         97.0
        00'T
                55.0
                          81.0
                                    55.0
        00'T
                0ε.ε
                                             ST'Z
                                                                25.0
                                                                                     alphal
                          27.5
089
                                                       56'7-3
                                                                22.0
                                                                                     аддрао
                                    84.2-
                                             59.5.
061
        TO'T
                60.5~
                          PE. S-
                                                       $5.5°
                                                                ps
lle.a
        Rust
                85.76
                                             $57
                                                         n.sims = 3000 iterations saved
                             3 chains, each with 2000 iterations (first 1000 discarded)
                             Inference for Bugs model at "SCROa.txt", fit using WinBUGS,
```

We know the data were generated with alpha 0 = -2.5 and alpha 1 = 2. The

Chapter 17, and DIC and model selection in Chapter 8. (DIC). We discuss general issues of convergence and other MCMC considerations in includes "deviance" and related things including the deviance information criterion and to increase the effective posterior sample size (n.eff). Other summary output 0.1 of resolutions to bring these closer to additional time to bring these closer to 1.0 Rhat statistics indicate reasonable convergence but, as a practical matter, we might WinBUGS gooked up based on our sample size of 1 data set. It is worth noting that the pretty good about the performance of the Bayesian analysis and MCMC algorithm that estimates look reasonably close to those data-generating values and we probably feel

5.7 Unknown N

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using the method of data augmentation (DA) which we apply here to achieve a realistic In all real applications IV is unknown. We handled this important issue in Chapter 4

Royle 6-656504-21-0-876

analysis of model SCR0. As with the basic closed population models considered previously, we formulate the problem by sugmenting our observed data set with a number of "all-zero" encounter histories—what we referred to in Chapter 4 as potential individuals. If n is the number of observed individuals, then let M-n be structure (n individuals. If n is the number of potential individuals in the data set. For the two-dimensional y_{ij} data structure (n individuals x) traps encounter frequencies) we simply add additional rows of all-zero observations to that data set. Because such "individuals" are unobserved, of all-zero observations to that data set. Because such "individuals" are unobserved, they therefore necessarily have $y_{ij} = 0$ for all j. A data set, say with 4 traps and 6 individuals, augmented with 4 premain individuals therefore might look like this:

			. (4)			
		0 %	0	0	0	['OT]
		0	0	0	0	['6]
		0	0	0	0	['8]
			0	0	0	['L]
		0 *>	T	0	Ţ	['9]
	13. 10.	J	Ť	0	0	['s]
	AL.	0	0	T	0	['Þ]
		Ţ	0	0	0	['٤]
		0	0	7	0	[5]
Potential	/^	0	0	0	τ	['t]
U		trap4	£xap3	trap2	frapl	

We typically have more than 4 traps and, if we're fortunate, many more individuals

our data se

For the augmented data set, we introduce a set of binary latent variables (the data augmentation variables), z_i , and the model is extended to describe $\Pr(z_i = 1)$ which is, in the context of this problem, the probability that an individual in the augmented data set is a member of the population of size N that was exposed to sampling. In other words, if $z_i = 1$ for one of the all-zero encounter histories, this is implied to be a sampling zero whereas observations for which $z_i = 0$ are "structural zeros" under the model. Under $\mathbb{D} A$, we also express the binomial observation model conditional on z_i as follows:

 $|\chi_{ij}|_{Z_i} \sim \text{Binomial}(K, z_i p_{ij}),$

where we see that the binomial probability evaluates to 0 if $z_i=0$ (so y_{ij} is a fixed 0 in that case, and evaluates to p_{ij} if $z_i=1$.

How big does the augmented data set have to be? We discussed this issue in Chapter where we noted that the size of the data set is equivalent to the upper limit of a uniform prior distribution on W. Practically speaking, it should be sufficiently large so that the posterior distribution for W is not truncated. On the other hand, if it is too large then unnecessary calculations are being done. An approach to choosing M by trial-and-error is indicated. Do a short MCMC run and then consider whether you need to increase M. See Chapter 17 for an example of this. Kéry and Schaub (2012, need to increase M. See Chapter 17 for an example of this. Kéry and Schaub (2012, need to increase M. See Chapter I7 for an example of this. The models. The useful thing about DA is that it removes M as an explicit parameter of the model.

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Instead, N is a derived parameter, computed by $N=\sum_{i=1}^M z_i$. Similarly, density, D, is also a derived parameter computed as D=N area (S).

SAUAniW ni noitstnemgus stsb gnisu sisylsnA 1.7.3

We provide a complete R script for simulating and organizing a data set, and analyzing poses the data in WinBUGS. As before we begin by obtaining a data set using our simsCRO function and then harvesting the required data objects from the resulting data list. Note that we use the discardo=TRUE option this time so that we get a "real looking" data set with no all-zero encounter histories:

> ylim <- data\$ylim 04900 milx\$etab -> milx < 59900 > 1 <- uxow(X) 09900 > K <- data\$K 55900 spolgstraplocs < datastraplocs 05900 $\langle \lambda \rangle = - \nu = -$ 54900 х\$едер -> Х < 01/900 > data <- simSCRO(discard0=TRUE,rnd=2013)</pre> \$6900 06900 ## Simulate the data and extraget the required objects \$2900 00900

After harvesting the data we augment the data matrix Y with M-n all-zero encounter histories, and create starting values for the variables z_i and also the activity centers s_i of which, for each, we require M values. One thing to take care of in using the BUGS engines is the starting values for the activity centers. It is usually helpful to start the s_i for each observed individual at or near the trap(s) it was captured. All

of this happens as follows:

```
02700
                                      set[i,2] <- mean (X[y[i,] Jes
$1700
                                      ([I,0<[i,1]] <- mean(X[y[i,]])
01/.00
                                                        } (bnin:1 ni i) *ef <</pre>
$0700
      (([2]miLY,[1]mity,M)linux,([2]milx,[1]milx,M)linux)bnido -> Jee
00700
                                                  ## Starting values for s
$6900
                                       ((bnin-M,0)qex,(bnin,L)qex,p > z <
06900
                       rbind(y, matrix(0, nrow=M-nind, ncol=ncol(y)))
28900
                                                                ~ 002 -> M <
08900
                                                       ## Data augmentation
ST300
```

Next, we write out the BUGS model specification and save it to an external file called SCROD. Ext . The model specification now includes M encounter histories including the augmentation parameters z_i , and the data augmentation parameter ψ :

\$7.20q

£8008

B978-0-12-405939-9.00005-0

141

MCHOURS

```
N nwonan V. 5.7 Unknown W
```

```
0820d
                                                             file = "SCROD.txt")
                                                                                           52800
                                                                                           00820
                                                                             79/N -> a
                                                                                           $1800
                                                                        ([]z)wns -> N
                                                                                           01800
                                                                                           20800
                                                                                           00800
                       ([\dot{\iota},\dot{\iota}]b^*[\dot{\iota},\dot{\iota}]b^*ladqla -)qx9^*0q^*[\dot{\iota}]z -> [\dot{\iota},\dot{\iota}]q
                                                                                           S6400
                                                     \lambda[i,j] dbin(p[i,j],K)
                                                                                           06400
(2.0,(S,[S,L]X-[S,L]S) \text{ woq}_{\perp} + (S,[L,L]X-[L,L]S) \text{ woq}) \text{ woq -> } [L,L]b
                                                                                           $8700
                                                                    }(r: t ur f) aoj
                                                                                           08700
                                             ([Z]wttk'[t]wttk) ltnub ~ [Z,t]s
                                                                                           SLL00
                                             ([S]milx,[I]milx)linub ~ [f,i]a
                                                                                           07700
                                                               z[i] _ qpexu(bsi)
                                                                                           59700
                                                                      ) (M: L ni i) 101 00700
                                                                    (1,0)linub ~ izq 22700
                                                     sigma <- sqrt(1/(2*alphal))
                                                              alphal ~ dnorm(0,.1)
                                                                                          S4700
                                                             logit (p0) <- alpha0
                                                                                           00740
                                                            alpha0 ~ dnorm(0,.1)
                                                                                           SE700
                                                                                 00730 model{
                                                                                00725 > Cat("
```

cuting WinBUCS, looks much the same as before except with more or differently The remainder of the code for bundling the data, creating initial values and exe-

named arguments:

```
n.chains=3, an.burnin=1000, n.iter=2000, debug=TRUE, working.dir=getwd())
                                                                                 59800
               00800 > out <- bugs (data inite, parameters, "SCROb.txt", n.thin=l,
                          00855 > parameters <- c@alpha0", "alpha1", "sigma", "N", "D")
                                                        > library(R2WinBUGg)
                                                                                00820
                                                                                 54800
            (z=z , jez=e , (2,1,1) limur=langla , (4,4,4) mnonr=0angla) jeil
                                                        00835 > inits <- function() {
               06800 sata <- list (y=y, X=X, X=X , X=X , y=im, y=im, y=im, y=im)
```

and there is a model component for the DA variables z. We are also computing some known-N version-there are not many! The loop over individuals goes up to M now, Note the differences in this new WinBUCS model with that appearing in the

know N, but think that N = 200 is a good upper bound. This analysis can be run histories. Previously we knew that N = 100 but in this analysis we pretend not to too, as the augmented data set has more rows to include excess all-zero encounter also a derived parameter, being a function of W. The input data has changed slightly augmentation variables z; (as we've done previously in Chapter 4) and density, D, is derived parameters: population size N(S) is computed by summing up all of the data

directly using the SCRObayes function once the scrbook package is loaded, by

issuing the following commands:

> print (outl, digits=2)

CHAPTER 5 Fully Spatial Capture-Recapture Models

Summarizing the output from WinBUGS produces:

	er en			
08800	SCR0bayes (data, M=200, engine="winbugs", ni=2000, nb=1000)	>	Tino	<
57800	simSCR0(discard0=TRUE, rnd=2013)			
07800	ecrpook)	ιπλ	Tipra	<

de!

28108

DUMM | 212120 [...some output deleted...] 16.45E (06.71E 302,60 05'T0E 61'192 00#T 08.2 ₽€'I 84°T TO'T 092 113.62 N 00,511 124.00 390 TO'T 00'LFT 510 ຂມວິເຣ 65.0 65.0 1.02 55.0 85.0 reugie 2.73 24.0 94.2 5 4 e 91.2 1'63 75O 72.57 0 sagis 98.5 21.2. ₽0.E. 22.0 350 mean 85.76 n.sims = 3000 testions saved 3 chains, each with 2000 iterations (first 1000 discarded) Inference for Bugs model at "\$CROb.txt", fit using Win BUGS,

The Rhat statistic (discussed in Sections 3.5.2 and 17.6.4) for this analysis indicates satisfactory convergence. We see that the estimated parameters (α_0 and α_1) are comparable to the previous results obtained for the known-N case, and also not too different from the data-generating values. The posterior of N overlaps the data-generating value substantially.

SAAL: sanigna Saug natho to asu 1.1.7.3

There are two other popular BUGS engines in widespread use: **OpenBUGS** (Thomas et al., 2006) and **JAGS** (Plummer, 2003). Both of these are easily called from **R. OpenBUGS** can be used instead of **WinBUGS** by changing the package option in the buge call to package = "OpenBUGS". **JAGS** can be called using the function jage () in package R2jage which has nearly the same arguments as buge (). Or, it can be executed from the **R** package xjage (Plummer, 2011) which has a slightly different implementation that we demonstrate here as we reanalyze the simulated data and package the data, inits and parameters to monitor). The function jage. model is used to initialize the model and run the MCMC algorithm for an adaptive period during which tuning of the MCMC algorithm might take place. These samples cannot be used for inference. Then the Markov chains are updated using coda. eamples () be used for inference. Then the Markov chains are updated using coda. eamples () to obtain posterior samples for analysis, as follows:

28800 ("SCROD.txt", data=data, inita=inita, n.chaina=3, n.adapt=1000) > jout <- coda.samples(jinit, parameters, n.iter=1000, thin=1)

These commands can be executed using the function SCR0bayes provided with the ${f R}$ package serbook. Hobbs (2011) provides a good introduction to ecological modeling with ${f JAGS}$ which we recommend.

5.7 Unknown V 149

- (Uging The Function bla)

5.7.2 Implied home range area

Here we apply the method described in Section 5.4 to compute the effective home range area, ander different encounter probability models fit to simulated data. We simulated a data set from the Gaussian kernel model as in Section 5.7 and then we fitted four models to it: (1) the true data-generating Gaussian encounter probability model; (2) the "hazard" or complementary log-log link model (Eq. (5.4.2)); (3) the negative exponential model; and (4) the logit model (Eq. (5.2.2)). We modified the function exponential model; and (4) the logit model (Eq. (5.2.2)). We modified the function fit each model to the same simulated data set using WinBUGS, based only on 1000 post-burn-in samples and 3 chains, which produced the posterior summaries given in Table 5.2. The main thing we see is that, while the implied home range area can vary substantially, there are smaller differences in the estimated. Vand hence D.

5.7.3 Realized and expected density

one by the population for the SCR model, we estimate a parameter W which is the size of the population for the prescribed state-space (presumably the state-space is defined so as to be relevant to where our traps were located, so N can be thought of as the size of the sampled population). In the context of Efford and Fewster (2012) this is the realized population size. Conversely, sometimes we see estimates of expected population size reported, which are estimates of E(N), the expected size of some hypothetical, unspecified population. Usually the distinction between realized and expected population size is not made in SCR models, because almost everyone only earlies about actual populations—and their realized population size.

If you do likelihood analysis of SCR models, then the distinction between realized and expected is often discussed by whether the estimator is "conditional-on- \mathcal{N} " (realized) or not (expected). The naming arises because in obtaining the MLE of \mathcal{N} , its properties are evaluated conditional on \mathcal{N} —in particular, if the estimator is unbiased then $\mathbb{E}(\mathring{\mathcal{N}}|\mathcal{N})=\mathring{\mathcal{N}}$ is the sampling variance. This does not conform to any concept or quantity that is relevant to Bayesian inference. If we care conform to any concept or quantity that is relevant to Bayesian inference. If we care

020qs

3	
1	detection model Confitted of 5209 the Function NICLO
	to a single simulated data set, and the effective home range area under each
	Table 5.2 Posterior mean of model parameters for four different models fitted
Ų	441 141

2.64	ľð.ð	87.E	38.6	pra
38.6	69.8	2.56	2,46	ιx
74.0-	19.1-	-2.60	73.5-	0,0
38.1	78.1	87.1	87.1	а
62,811	69.611	91,411	113.62	N
	Exponential	Ciodiod	nsiseusə	
fino I	leitnengaya	Clodio		

about N for the population that we sampled it is understood to be a realization of a random variable, but the relevance of "conditional-on-N" is hard to see. Bayesian analysis will provide a prediction of N that is based on the posterior $[N|y,\theta]$ —which is certainly not conditional on N.

There is a third type of inference objective that is relevant in practice and that is prediction of M for a population that was not sampled—i.e., a "new" population. To elaborate on this, consider a situation in which we are concerned about the tiger population in two distinct reserves in India. We do a camera trapping study on one of the reserves to estimate M; and we think the reserves are similar and homogeneous so we're willing to apply a density estimate based on M; to the second reserve. For the second reserve, do we want a prediction of the realized population size, M2, or do we want an estimate of its expected value? We believe the former is the proper do we want an estimate of its expected value? We believe the former is the proper quantity for inference about the population size in the second reserve. An estimate of M2 should include the uncertainty with which the mean is estimated (from reserve I) and it should also include "process variation" for making the prediction of the latent variable M2.

As a practical matter, to do a Bayesian analysis of this you could just define the state-space to be the union of the two state-spaces, increase M so that the posterior of the total population size is not truncated, and then have MCMC generate a posterior sample of individuals on the joint state-space. You can tally up the ones that are on S_2 as an estimate of N_2 . Alternatively, we can define $\mu = \psi M/\Lambda_1$ and then simulate posterior samples of M_2 . Binomial $(M, \mu \Lambda_2/M)$ for the new state-space area, Λ_2 . To the new state-space area, Λ_2 .

To carry out a classical likelihood analysis of this second type of problem, what should we do? The argument for making a prediction of a new value of N would go something like this: If you obtain an MLE of N, say \hat{N} , then the inference procedure tells us the variance of this conditional on N, i.e., $Var(\hat{N}|N)$. This is fine, if we care about the specific value of N that generated out data set. However, if we don't care about the specific one in question then we want to "uncondition" on N to introduce a new variance component. Law of total variance says:

 $V_{ar}(\hat{N}) = \mathbb{E}[V_{ar}(\hat{N}|N)] + V_{ar}[\mathbb{E}(\hat{N}|N)].$

If \hat{N} is in the second that we say the unconditional variance is

$$Var(\hat{N}) = o^{\frac{2}{N}} + Var(N)$$

The first part is estimation error and the second component is the "process variance."

If you do Bayesian analysis, then you don't have to worry too much about how to compute variances properly. You decide if you care about M, or its expected value, or predictions of some "new" M, and you tabulate the correct posterior distribution or predictions of some "new" M, and you tabulate the correct posterior distribution

from your MCMC output. The considerations for estimating density are the same. Density can be N/Λ where N is the realized population, which we understand it to be unless we put an expectation operator around the N like $\mathbb{E}(N)/\Lambda$. Classically, density is thought of as

Koyle

There of any particular N.

5.8 The Core SCR Assumptions 191

(see Chapter 11) in the sense that, under the binomial prior: (under data augmentation). In the latter case ψ is related to the point process intensity we assume N has a Poisson distribution or whether we assume a binomial distribution formula for obtaining "expected density" is slightly different depending on whether expected density for some hypothetical unspecified population, should matter. The because the context of whether we mean realized density, of an actual population, or being defined as the expected value of N but this might not always be meaningful

$$\mathbb{E}(N) = M \times \psi$$

so, what we think of as "density," D, is $D = M\psi/A$. Under the Poisson point process

model we have:
$$\mathbb{E}(\mathcal{N}) = D \times \Lambda.$$

population size (or density): 0460q In summary, there are three basic inference problems that relate to estimating

Efford and Fewster call "realized N." In general, we want the uncertainty to oil80 (1) What is the value of M for some population that was sampled. This is what

oilss (2) We need to estimate N for some population that we didn't sample but it is reflect having to estimate no, the part of the population not seen.

PI TI TOM PWA 1800 AL model of N). N and we have to account for process variation in N (i.e., due to the stochastic account for both variation in having to estimate parameters of the distribution of "similar" to the population that we have information on. In this case, we have to

use, e.g., if we were to establish a new million ha refuge somewhere, then we value of M, E(M)/This is only useful as a hypothetical statement that we might oli o (3) In some extremely infitted cases we might care about estimating the expected

might say its expected population size is 200 tigers:

soloo 5.8 The core SCR assumptions

we think are the most important statistical assumptions of the basic SCR0 model: point this out to someone seems to cause a lot of anxiety, so we enumerate here what naturally, that precludes everything that isn't explicitly addressed by the model. To statistics, and for every statistical model, is that "the model is correctly specified." So, statistician's point of view, the basic assumption, the omnibus assumption, as in all of model, its various assumptions, and what they mean in a specific context. From the It's always a good idea to sit down and reflect on the meaning of any particular

There is no recruitment or entry into the sampled population. There is no mortality Demographic closure. The model does not allow for demographic processes. • \$000n

space and variable exposure to encounter as a result. The whole point of SCR the state-space. However, we allow for "temporary" movements around the state-Geographic closure. We assume no permanent emigration or immigration from or exit from the sampled population.

Koyle 678-0-12-405939-9

models is to accommodate this dynamic. In ordinary capture-recapture models we have to assume geographic closure to interpret N in a meaningful way. Activity centers are randomly distributed. That is, uniformity and independence

of the underlying point process \$1, ..., \$N (see next section).

Detection is a function of distance. A detection model that describes how encounter woode probability declines as a function of distance from an individual's home range

center.

Independence of encounters among individuals. Encounter of any individual is 10025

independent of encounter of each other individual. Encounter of an individual in 60030 any trap is independent of its encounter in any other trap, and subsequent sample any trap is independent of its encounter in any other trap, and subsequent sample

occasion.

reasongbleness of the assumptions formally in some cases using standard methods of and more work remains to be done in this regard. Fourth, we can also evaluate the assumptions in many different ways and we do that to varying extents in this book, represent real populations (of course, no model does!). Third, we can extend these allow us to build a model and an estimation scheme and we don't usually think they ters, we expect a fair amount of robustness to departures. They function primarily to core assumptions such as uniformity, and independence of individuals and of encounjustification in virtually every capture-recapture study. Secondly, for some of these modeling. Fundamentally a distance-based model for p has some basic biological in which p varies isn't quite right, but that's not an argument that supports doing less as a matter of the spatial juxtaposition of individuals with traps. So maybe the manner not assuming that p is constant for all individuals but rather that p varies substantially important assumptions compared to the non-spatial counterpart. For one, here, we're ordinary capture-recapture model but rather, the SCR model relaxes a number of are worth making. First, you don't have inherently fewer assumptions by using an can't describe the complexity of real populations. On this sentiment, a few points that these assumptions combine to form such a simplistic model, one that surely It's easy to get worried and question the whole SCR enterprise just on the grounds

Finally, we return back to our sentiment about the omnibus assumptions which is that the model is properly specified. This precludes everything that isn't in the model. Sometimes you see in capture-recapture literature statements like "we assume no also assume that, a shopping mall is not built, or a meteor does not crash down into our study area, the sun does not go super-nova, and so forth. Our point is that we should separate statistical assumptions about model from what are essentially logistical or operational assumptions about how we interpret our data, or based on our ability to conduct the study. It is pointless to enumerate all of the possible explanations for apparent departures, because there are enumerate all of the possible explanations for apparent departures, because there are an infinity of such cases.

5.9 Wolverine Camera Trapping Study

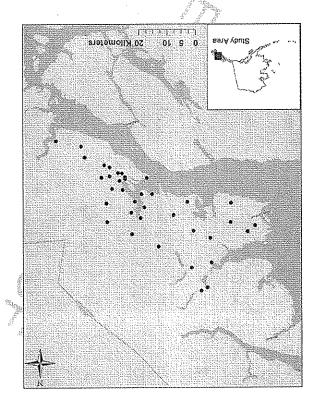


FIGURE 5.4

Wolverine camera trap locations (black dots) from a study that took place in SE Alaska.

See Magoun et al. (2011) for details.

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Section 5.7 accordingly. a vector of sample sizes as data to BUCS and modify the model specification in number of sampling occasions, K, is variable for each camera. Thus, we must provide (min = 5 days, median = 45 days). A consequence of this is that the Alaska (Figure 34) where 37 cameras were operational for variable periods of time Gulo gulo (Magoun et al., 2011; Royle et al., 2011b). The study took place in SE chapter by analyzing data from a camera trapping thata frofts of wolverines posss We provide an illustration of some of the concepts we've introduced previously in this

noitezinegro etab lactical data organization

all the information needed for an analysis. These files are: encounter history data. We usually store data in two distinct data files which contain poseo To carry out an analysis of these data, we require the matrix of trap coordinates and the

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Royle

- The encounter data file (EDF) containing a record of which traps and when each 40035
- with information indicating which sample occasions each trap was operating. The trap deployment file (TDF) which contains the coordinates of each trap, along individual encounter occurred.

naming of the columns is irrelevant as far as anything we do in this book, although of which have a 3-column format (eraplD, indlD, samplD). We note that the (Gopalaswamy et al., 2012a), and SCRbayes (Russell et al., 2012) packages, both in the secr package (Efford, 2011a) and similar to that used in the SPACECAP from 1 to J, the number of traps. The structure of the EDF is the same as used occasion which generated the record; and (4) trap ID: the trap identity, an integer the record (row) of the matrix belongs to; (3) cocasion ID: the integer sample to n (repeated for multiple captures of the same individual) indicating which individual for all records; (2) individual ID: the individual identity, being an integer from I For a single-year study (as considered here) this should be an integer that is the same but it could also correspond to a distinct spatial unit (see Section 6.5.4 and Chapter 14). corresponds to a year or a primary period in the context of a Robust Design situation, with four columns, those being: (1) session ID: the trap session which usually which are widely used for data management. The file structure is a simple matrix which is easily manipulated in R and easy to create in Excel and other spreadsheets Encounter Data File (EDF)—We store the encounter datain an efficient file format poses

To illustrate this format, the wolverine data are available in the package acrbook secr and other software may have requirements on variable naming.

> data(wolverine)

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the trap identity, the individual identity, and the sample occasion index (sample). see that weape has 115 rows, each representing a unique encounter event including which contains a list having elements weaps (the EDF) and wtraps (the TDF). We

The first five rows of weaps are:

[['9] τ τ 128 τ ISL Τ дяХ individual crap

which we describe further below. the row of a matrix containing the trap coordinates—in this/case the TDF file werraps and trap is the integer trap identity. The variable trap 4 will have to correspond to sample occasion of capture (in this case, the sample occasions correspond to days), Variable individual is an integer identity of each individual captured, day is the the encounter. All these data come from a single year (2008) and so year is set to I. The first column here, labeled year, is in integer indicating the year or session of

678-0-12-405939-9

Koyle

5.9 Wolverine Camera Trapping Study 122

BUGS as data. We provide this information along with trap coordinates, in the "trap information is also necessary as the trap-specific sample sizes must be passed to not provide information about which periods each trap was operated. This additional 2-d encounter frequency matrix or 3-d array. In addition, the encounter data file does K, the number of sample occasions when reformatting this SCR data format into a format will have no record. Thus we will need to know J, the number of traps, and were captured in a certain trap or during a certain period, then this compact data represent a completely informative summary of the data. For example, if no individuals Note that the information provided in this encounter data file weaps does not

the sample occasion dimension (by convention here, this is the 2nd dimension). To converts it to a 3-d array, and then we use the Relunction apply to summarize over handy function SCR23darray which takes the compact encounter data file, and encounter data file into a 3-d array and then summarize to trap totals. We have a our encounter frequency matrix, we do this the hard way by first converting the encounter-history formulation of the model which requires a full 3-d array. To obtain binomial encounter frequencies, although more general models might require an For our purposes, we need to convert the weaps flight into the $n \times J$ array of deployment file" (TDF) which is described below.

apply this to the wolverine data in order to compute the 3-d array we do this:

> y3d <- SCR23darray(wolyerine\$wcaps,wolverine\$wtraps)

summarized data. will require this maximally informative 3-d data format but, here, we analyze the to fit certain types of models (e.g., behavioral response) and this is why we sometimes See the help file for more information on SCR23 darray. The 3-d array is necessary

sample occasion. The first 10 rows (out of 37) and 10 columns (out of 167) of the trap 4 to K + 3 are binary indicators of whether each trap was operational during each northing coordinates (assumed to be in a Euclidean coordinate system), and columns first column is assumed to be a trap identifier, columns 2 and 3 are the easting and not contained in the encounter data file. The traps file has K + 3 columns. The models is the "trap deployment file" (TDF) which provides additional information Trap Deployment File (TDF)—The other important information needed to fit SCR

deployment file for the wolverine data are shown as follows:

 $> \lambda < - \text{abbJ}\lambda(\lambda_3q)c(\gamma)$ and

06£0q

08£0q

```
₱66ETE9
                               S
                    857759
         9100ZE9
                               ₹
                    679789
                               ٤
         T8760E3
                    938459
                               z
                    228759
         2109129
                    852559
                               T
         Northing
                    Easting
> wolyerine$wtraps[1:10,1:10]
```

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0	0	0	0	0	0	0	0	6331273	7 75759	6
0	0	0	0	0	0	0	0	6099TE9	TE9ZE9	8
0	0	0	0	0	0	0	0	4325157	069189	L
0	0	0	0	0	0	0	0	9888189	872229	9

CHAPTER 5 Fully Spatial Capture-Recapture Models

This tells us that trap Δ was operated during occasions (dâys) 1-7 but the other traps were not operational during those periods. It is extremely important to recognize that each trap was operated for a variable period of time and thus the binomial "sample size" is different for each, and this needs to be accounted for in the **BUGS** model specification. To compute the vector of sample sizes K, and extract the trap locations, we do this:

This results in a matrix traploca which contains the coordinates of each trap and a vector K containing the number of days that each trap was operational. We now have all the information required to fit a basic SCR model in BUGS.

Summarizing the data for the wolverine study, we see that 21 unique individuals were captured a total of 115 times. Most individuals were captured 1–6 times, with 4, 1, 4, 3, 1, and 2 individuals captured 1–6 times, respectively. In addition, 1 individual was captured each 8 and 14 times and 2 individuals each were captured 10 and 13 times. The number of unique traps that captured a particular individual ranged from 1 to 6, with 5, 10, 3, 1, 1, and 1 individual captured in each of 1–6 different traps, respectively, for a total of 50 unique wolverine-trap encounters. These numbers might be hard to get your mind around whereas some tabular summary is often more convenient. For that it seems natural to tabulate individuals by trap and total encounter frequencies. The spatial information in SCR data is based on multi-trap captures, and so, it is informative to understand how many unique traps each individual is captured so, it is informative to understand how many unique traps each individual is captured

in, and the total number of encounters. For the wolverine data, we reproduce Table

5.3 from Royle et al. (2011b) as Table 5.3. **2.9.2 6.5**

Here we fit the simplest SCR model with the Gaussian encounter probability model, posos although we revisit these data and fit additional models in later chapters. Model SCR0

```
is summarized by the following four elements:

(1) y_{i,j}|\mathbf{s}_i \sim \text{Binomial}(K, z_i p_{i,j});
(2) p_{i,j} = p_0 \exp(-\alpha_1 \|\mathbf{x}_j - \mathbf{s}_i\|^2);
(3) \mathbf{s}_i \sim \text{Uniform}(S);
(4) \mathbf{s}_i \sim \text{Bernoulli}(\Psi).
```

We assume customary flat priors on the structural (hyper-) parameters of the model,

 $\alpha_0 = \log it(p_0)$, α_1 and ψ .

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5.9 Wolverine Camera Trapping Study

Table 5.3 Individual frequencies of capture for wolverines captured in camera traps in SE Alaska in 2008. Rows index unique traps of capture for each individual and columns represent total number of captures (e.g., we captured 4 individuals 1 time, necessarily in only 1 trap; we captured 3 individuals 3 times have in 2 different traps.

times but in 2 different traps).

									17	INDÍ	7
				ile.							$\sim \downarrow \downarrow$
0	l l	0	0	0	0	0	0	0	0	1	. 9
0	0	0	0,,,	0	L	0	0	0	0		9
0	l	0	0	0	0	0	0	0	0		t l
	0	0	0	0	0	L	-	0	0		3
0	0	ٿي	N. P.	7	0	7	ε	0	0		7
0	0	O.	0	0	0	0	0	L	Þ		l I
Kanera and S					endos i crestos 100 milios			-		edou i	o redmuN
71	£1.	Ok	8	9	S	ν	L	G	· ·	anest i	o aoguante
			ptures	eo Jo .	ıəqwi	าท					
					itteritten.				motivationing 4	s had you be the second of the second	STATUS DELL'ARCO COSTO DELL'ARCO DE COSTO

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It remains to define the state-space S For this, we nested the trap array (Figure 5.4) in a rectangular state-space extending 20 km beyond the traps in each cardinal direction. We scaled the coordinate system so that a unit distance was equal to 10 km, producing a rectangular state-space of dimension 9.88 \times 10.5 units (avea = 10, 374 km²) within which the trap array was nested. As a general rule, we recommend scaling the state-space so that it is defined near the origin (x, y) = (0, 0). While the scaling of the coordinate system is theoretically irrelevant, a poorly scaled state-space should be large enough so that individuals beyond the state-space boundary are not likely to be encountered (Section 5.3.1). To evaluate this, we fit models for various choices of a rectangular state-space based on buffers from 1.0 to 5.0 units for various choices of a rectangular state-space based on buffers from 1.0 to 5.0 units when the model SCR0. For example, to fit the model in WinbUGS using data sugmentation with M = 300 potential individuals, using three Markov chains each of mentation with M = 300 potential individuals, using three Markov chains each of 12,000 total iterations, discarding the first 2000 as burn-in, we execute the following

R commands:

```
00955 > library(scrbook)
00930 > data(Wolverine)
00940 > y3d <- scR23darray(wolverine$wcaps,wolverine$wtraps)
00945 > wolv <- wolvsCR0(y3d,traps,nb=2000,ni=l2000,buffer=1,M=300)
```

The argument buffer determines the buffer size of the state-space in the scaled units (i.e., 10 km). Note that this analysis takes between 1 and 2 h on many machines (in 2013) so we recommend testing it with lower values of M and fewer iterations. The posterior summaries are shown in Table 5.4.

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CHAPTER 5 Fully Spatial Capture-Recapture Models

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Table 5.4 Posterior summaries of SCR model parameters for the wolverine camera trapping data from SE Alaska, using state-space buffers from 10 up to 50 km. Each analysis was based on 3 chains, 12,000 iterations, 2000 burn-in, for a total of 30,000 posterior samples.

							Pa	TAD C)
3400	12,1	67.3	3400	39.16	19.131	0074	90.0	£9.0	1 05
3300	1.24	58.3	3300	89 82	134.43	10,000	90.0	49.0	97
091	1.30	78.3	014	71.92	30.811	014	90.0	79 '0	01
30,000	1,24	38.3	30,000	79°12	67.101	0097	60.0	£9.0	36
3900	12.1	5.82	3900	86,71	24.88	0099	60.0	69.0	30
2700	81.1	6Z.3	2700	27.41	72.40	3600	30.0	49.0	52
20,000	31.1	77.3	20,000	68.11	48.65	1200	90.0	49.0	20
3300	1.09	87.3	3300	61.6	77.84	013	90.0	79.0	91
0017	1,00	76.3	001Z	0Ľ9	89.68	1800	90.0	99'0	10
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***	45			U.					
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5.9.3 Summary of the wolvering analysis

We see that the estimated density is roughly consistent as we increase the state-space buffer from 15 to 55 km. We do note that the data augmentation parameter ψ (and, correspondingly, N) increases with the state-space in accordance with the increase the size of the state-space beyond a certain point. For the 10 km state-space buffer, we see a slight effect on the posterior distribution of D because the state-space is not sufficiently large. The full results from the analysis based on 20 km state-space is not sufficiently large. The full results from the analysis based on 20 km state-space

Our point estimate of wolverine density from this study, using the posterior mean from the state-space based on the 20 km buffer, is approximately 5.77 individuals/ 1000 km² with a 95% posterior interval of [3.86, 8.29]. Density is estimated

Table 5.5 Posterior summaries of SCR model parameters for the wolverine camera trapping data from SE Alaska. The model was run with the trap array centiered in a state-space with a 20 km rectangular buffer.

ij	05.0	62.0	02.0	71.0	21.0	90.0	02.0	/ .
ľ	97.0	79.0	69.0	09.0	46.0	90.0	49.0	
l	80.0	90.0	90.0	90.0	40.0	10.0	90.0	0
l	17.1	04.1	1.25	11.1	78.0	12.0	1.26	Ļ
ŀ	62.8	94.9	69.3	76.⊅	3.86	91.1	77.3	(
L	00.88	00.78	00.68	00.13	40.00	68.11	148.65	. /

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buffer are given in Table 5.5.

5.9 Wolverine Camera Trapping Study

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imprecisely which might not be surprising given the low sample size (n=21 individuals!). This seems to be a basic feature of carnivore studies although it should not (in our view) preclude the study of their populations by capture-recapture nor attempts

It is worth thinking about this model, and these estimates, computed under a rectangular state-space, roughly centered over the trapping array (Higure 5.4). Does it make sense to define the state-space to include, for example, ocean? What are the possible consequences of this? What can we do about it? There's no reason at all that the state-space has to be a regular polygon—we defined it as such here strictly for convenience and for ease of implementation in WinBUGS where it enables us to specify the prior for the activity centers as uniform priors for each coordinate. While it would be possible to define a more realistic state-space using some general polygon of Soverage, it might take some effort to implement that in the BUGS language but it is not difficult to devise custom MCMC algorithms to do that (see Chapter 17). Alternatively, we recommend using a discrete representation of the state-space—i.e., approximate S by a grid of G points. We discuss this in Section 5.10.

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solz5 5.9.4 Wolverine space usage

to estimate density or vital rates.

The parameter α_1 is related to the home range radius (Section 5.4). For the Gaussian model we interpret the scale parameter σ , related to α_1 by $\alpha_1 = 1/(2\sigma^2)$, as the radius of a bivariate normal model of space usage. In this case $\sigma = 0.64$ standardized units (10 km), which corresponds to $0.64 \times 10 = 6.4$ km. It can be argued then that 95% of space used by an individual is within $6.4 \times \sqrt{5.99} = 15.66$ km of the home range center. The effective "home range area" is then the area of this circle, which is $\pi \times 15.66^2 = 770.4$ km². Using our handy function has we do this:

00000 hra(pdaussl,parms=c(2,1)(2*.64*.64)),xlim=c(1,7),ylim=c(-1,7))
80915 [1] 7.731408

which is in units of $100 \, \mathrm{km}^2$ from the difference in this case is due to numerical approximation of our all-purpose tool hrea. This home range size is relatively huge for measured home ranges which range between $100 \, \mathrm{and} \, 535 \, \mathrm{km}^2$ (Whitman et al., 1986).

Royle et al. (2011b) reported estimates for σ in the range 6.3–9.8 km depending on the model, which isn't too different than here. ¹ However, these estimates are larger than the typical home range sizes suggested in the literature. One possible explanation is that if a wolverine is using traps as a way to get yummy chicken, so it's moving from trap to trap instead of adhering to "normal" space usage patterns, then the from trap to trap instead of adhering to "normal" space usage patterns, then the

¹Royle et al. (2011b) expressed the model as cloglog(p_{ij}) = $α_0 - (1/σ^2) * d_{ij}^2$, but the estimates of σ reported in their Table 5.2 are actually based on the model according to cloglog(p_{ij}) = $α_0 - \frac{1}{2σ^2} * d_{ij}^2$, and so the estimates of σ they report in units of km are consistent to what we report here except based on the complementary log-log (Gaussian hazard) model, instead of the Gaussian encounter probability model.

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patterns of space usage See Chapters 12 and 13/18 on σ , although SCR models can be extended to handle more general, non-Euclidean, such, we caution against direct biological interpretations of home range area based or assumptions, such as that traps don't effect individual space usage patterns. As of detection models in terms of home range area depends on some additional context implied home range size might not be worth much biologically. Thus, interpretation

for individuals beyond the prescribed state-space. For the wolverine data, with σ in prescribed state-space. Essentially, by specifying a state-space, we're setting p=0order that the probability of encountering an individual is very close to 0 beyond the home range radius of the species. We should target a buffer of width 2 to $3 \times \sigma$ in We can calibrate the desired size of the state-space by looking at the estimated

the range of 6-9 km, a state-space buffer of 20 km is sufficiently large.

5.10 Using a discrete habitat mask

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SCR model in Royle et al. (2009a) May Methodo bot 2 With RAW SPACECAP (Copalaswamy et al., 2012a) arose from the R implementation of the to perform the MCMC calculations in R (discussed in Chapter 17). The R package space can be computationally expensive in WinBUCS. That said, it isn't too difficult on using polygon operations to define an integular state-space. Use of a discrete stateof a discrete state-space butin Chapter 17 we demonstrate the latter approach based MCMC analysis. We focus here on the formulation of the basic SCR model in terms can use polygon clipping methods to enforce constraints on the state-space in the formulation of the state-space but attempt to describe constraints analytically, or we equal probabilities to each possible value. Alternatively, we can retain the continuous to represent the state-space, i.e., by the set of coordinates si, ..., so, and assign suitable habitat. There are several ways to approach this: We can use a grid of points assume uniformity of the activity centers over the remaining portions judged to be and non-habitat. In that case we can remove the non-habitat from the state-space and example, we might be able to classify the state-space into distinct blocks of habitat address here, is to modify the shape and organization of the state-space explicitly. For density. A simplistic method of affecting the distribution of activity centers, which we explicitly for non-uniformity of the activity centers by modeling covariate effects on always be a reasonable assumption. In Chapter 11, we develop models that allow centers are distributed uniformly over the prescribed state-space. Clearly this will not The SCR model developed previously in this chapter assumes that individual activity

differentiating the landscape by habitat or habitat quality must affect the geometry be known whether the animal being studied has the same understanding. Moreover, "habitat" vs. "non-habitat" based on their understanding of the system whereas it can't ocean, or river. But, having the capability to do this also causes people to start defining represents a clear-cut restriction on the state-space such as a reserve boundary or a lake, should go about this very cautiously. We might prefer to do it when non-habitat While clipping out non-habitat seems like a good idea, we think investigators

5.10 Using a Discrete Habitat Mask 161

and morphology of home ranges (see Chapter 13) much more so than the plausible locations of activity centers. That is, a home range centroid could, in actual fact, occur in a shopping mall parking lot if there is pretty good habitat around the shopping mall, so there is probably no sense preclude it as the location for an activity center. It would generally be better to include some definition of habitat quality in the model for the detection probability (Royle et al., 2013) which we address in Chapters-12 and 13.

soliss 5,10.1 Evaluation of coarseness of habitat mask

specifications as approximations to truth in the sense that they represent a component is, strictly speaking, an approximation to truth. That said, we regard all state-space activity centers as a continuous gandom variable and thus the discrete state-space the R package scrbook. We note that for this comparison we generated the actual different number of support points. We provide an R script called SCRObayesDas in demonstrate this here by reanalyzing simulated data using a state-space defined by a grid of support points to evaluate the integral to a reasonable level of accuracy. We numerical integration where we find (see Chapter 6) that we don't need a very fine state-space. We can also think about discretizing the state-space as being related to sizes. We therefore expect a similar effect in SCR models when we discretize the of heterogeneity and are adequate for most data sets of small to moderate sample find that a small number of groups (e.g., 2 or 3 at the most) can explain high levels being location of activity center). In the standard-finite-mixture models we typically be able to obtain direct information about which group individuals belong to (group finite mixture (Norris and Pollock, 1996; Pledger, 2004) where we are fortunate to M_h . As noted in Section 5.3.2 above, we can think about SOR models as a type of We have two analogies that can help us understand. First is the relationship to model if the grain is sufficiently fine relative to typical animal home range sizes. Why is this? poses The coarseness of the state-space should not really have much of an effect on estimates

of the SCK model.

As with our **R** function SCR obsyees, the modification SCR obsyeeDes will use either **WinBUGS** of **JAGS**. In addition, it requires a grid resolution argument (ng) which is the dimension of 1 side of a square state-space. To execute this function we

```
09600 > library(scribook)
09655 > data <- simsCR0(discard0=TRUE, rnd=2013) # Generate data set
00970 # Run with JAGS
00975 > outl <- sCR0bayesDss(data,ng=8,M=200,engine="jags",ni=2000,nb=1000)
00980 # Run with WinBUGS
00985 > outl <- sCR0bayesDss(data,ng=8,M=200,engine="winbugs",ni=2000,nb=1000)
```

We fit this model to the same simulated data set for 6×6 , 9×9 , 12×15 , 15×15 state-space grids. For WinBUGS, we used 3 chains of 5000 total length with 1000 burn-in, which yields 12,000 total posterior samples. Summary results are shown in

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do, for example:

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CHAPTER 5 Fully Spatial Capture-Recapture Models

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		13,010	JE842E8:0	0.1637436	12759.71	675.311	31 × 31		
		T'0011	987297.0	\$969891'0	5485.71	9086,311	12 × 15		
1961/2		4300	67828.0	0.1642355	47.99109	114.2294	6×6		
1017		2274	800289.0	7888131.0	16.61414	6699.111	9×9		
Ŭ		(s) əmitnufi	BSseltes-emiT	J S9visM	as:	Mean	Grid Size		
		CORPORA CARROLLO CONTRACTOR CONTRACTOR AND CONTRACT		un from R.ZW					
		ime are given.	maries and runt	osterior sumi	data set. P	betelumis a	of M for s		
	070q		ce grid coarsenes						

start the latent activity centers at values near where individuals were captured. The some problems, so be careful when using JACS. To improve its performance, always to starting values, producing MCMC algorithms that often simply do not work for our analysis of the wolverine (next section) that JAGS could be extremely sensitive this might suggest that one should always use JAGS for this analysis, we found in at a subset of values or perhaps using previous calculations more effectively. While possible values whereas it may be that JAGS is evaluating the full conditional only that WinBUCS is evaluating the full conditional for each activity center at all G faster and, furthermore, relatively constant as we increase the grid size. We suspect state-space grid points. We found (not shown here) that the runtime of JAGS is much we imagine it would be impractical to run models with more than a few hundred the runtime increases with the size of the state-space grid (not unexpected), such that Table 5.6. The results are broadly consistent except for the 6×6 case. We see that

5.10.2 Analysis of the wolverine camera trapping data

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the effectiveness of the MCMC algorithms, as measured by effective sample size slight differences depending on the resolution of the state-space grid. Interestingly, (Table 5.4) based on a rectangular, continuous state-space. We also see that there are We see that the density estimates are quite a bit larger than obtained in our analysis density. The posterior summaries for the three habitat grids are given in Table 5.7. so we would prefer to use them, but only if there is no strong influence on estimated because the coarser grids will be more efficient from a computational standpoint and doing this was to evaluate the relative influence of grid resolution on estimated density state-space, and deleting the points over water (see Royle et al., 2011b). Our interest in by 2, 🐇 and 8 km (see Figure 5.5). These were constructed from a 40 km buffered

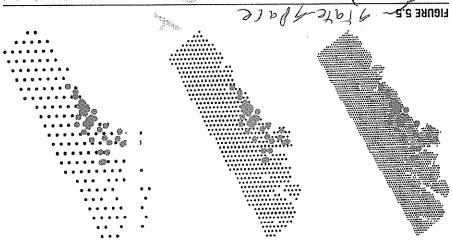
We reanalyzed the wolverine data using discrete state-space grids with points spaced

of BUCS and pass it as data, although we haven't fully evaluated this approach. performance of either should improve if we compute the full distance matrix outside

spacing) took about 6 days to run and thus it would not be practical for large problems $(n \cdot eff)$, is pretty remarkably different. Furthermore, the finest grid resolution (2 km

or with many models.

5.11 Summarizing Density and Activity Center Locations



Three flabitat mask grids used in the comparison of the effect of pixel size on the estimated density surface of wolverines. The three cases are 2 (left), 4 (center), and 8 (right) km spacing of state-space points, extending 40 km from the vicinity of the trap array.

5,11 Summarizing density and activity center locations

One of the most useful aspects of SCR models is that they are parameterized in terms of individual locations—i.e., where each individual lives—and, thus, we can compute many useful and interesting summaries of the activity centers using output from an MCMC simulation, including anaps of density (the number of activity centers per unit area), estimates of N for any well—defined polygon, or estimates of where the activity centers for specific individuals reside. In Bayesian analysis by MCMC, obtaining such summaries entails no added calculations, because we need only post-process the output for the individual activity centers to obtain the desired summaries. We demonstrate that in this section. Note that you have to be sure to retain the MCMC history for the systables and the data augmentation variables z in order to do the following analyses.

solso 5,11.1 Constructing density maps

Because SCR models are spatially explicit, it is natural to want to summarize the results of fitting a model by producing a map of density. Using Bayesian analysis by MCMC, this most easy to make a map of vealized density. We can do this by tallying up the number of activity centers s, in pixels of arbitrary size and then producing a nice multi-color spatial plot of the result. Specifically, let B(x) indicate a pixel centered

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$$N(\mathbf{x}) = \sum_{i=1}^{M} I(\mathbf{s}_i \in B(\mathbf{x}))$$

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Table 5.7 Posterior summaries for the wolverine camera trapping data, using model SCRO, with a Gaussian hazard encounter probability model, and a discrete habitat mask of three different resolutions: 2, 4, and 8 km. Parameters are λ_0 = baseline encounter rate, p_0 = $1 - \exp(-\lambda_0)$, σ is the scale parameter of the Gaussian kernel, ψ is the data augmentation parameter, N and D are population size and density, respectively. Models fitted using **WinBUGS**, 3 chains, each with 11,000 iterations (first 1000 discarded) producing 30,000 chains, each with 11,000 iterations (first 1000 discarded) producing 30,000 posterior samples.

									7 <u>34</u>	
ſ	076	1.00	19.0	74.0	۲Þ,0	98.0	92.0	60'0	24.0	Λ
	220	10.1	77.0	17.0	79.0	79.0	69.0	90.0	89.0	ø
	099	1.00	90.0	90.0	ħ0.0	40.0	60.0	10.0	30.0	0d
	099	00.1	90.0	90.0	30.0	40.0	60.03	10.0	90.0	γ0
	004	1.00	11.84	97.6	81.8	Tr.T	75.8	∍r8,r	82.8	а
	004	1.00	119.00	93'00	82.00	72.00	00.93	pl 91	81,58	Ν
								бі	ijoeds u	8 KI
		/A.	`\							
	1300	(/ <i>XV</i> :1	1 ,9,0	05.0	bb.0	86.0	8Z.0	60.0	9 1 .0	Λ
	1600	101	14.0	1 9,0	19.0	86.0	65.0	40.0	19.0	٥
	2200	10001	<i>4</i> 0.0	90.0	20.0	40.0	60.0	10.0	90.0	0d
	\S200	0001	20'0	90.0	90.0	90:0	⊅ 0.0	10.0	30.0	γ0
	1100	0011	12.82	10,10	88.8	TT.T	96.3	97.1	10.6	а
	0011	Ob 01 \	127.00	00.001	00.88	00:TT	00.69	<i>ት</i> ታ.۲۱	92.68	Ν
.	, ,	/						Бі	n sbacin	けか
ı					The state of the s			00.0	~	A.
	099	1,00	69.0	67'0	64.0	7E.0	7S.0	60.0	£4.0	η O
	160	10.1	£7.0	99'0	29.0	69.0	1 9'0	90.0	29.0	0d
	320	10.1	90.0	90.0	90.0	1 0.0	60.03	10.0	90.0	υυ 9γ
	320	10.1	70.0	90.0	90.0	40.0	40.0	10.0	30.0	
	919	1,00	12.57	68.6	29.8	09.7	87.3	27.1	87.8	a
	018	1.00	124.00	00.76	00.88	00.37	00.78	₽6.91	96.98	Ν
								6u	ijoeds w	N Z
										- Σ. - Σ. Ε.
	Hə.n	JedA .	%9'Z6	%9Z	%09	%97 <u>:</u>	5.5%	as	nseM	

(here, $I(\alpha_R g)$ is the indicator function which evaluates to 1 if $\alpha_R g$ is true, and 0 otherwise) is the population size of pixel B(x), and $D(x) = N(x)/\|B(x)\|$ is the local density. Note that these N(x) parameters are just "derived parameters" as we normally obtain from posterior output using the appropriate Monte Carlo average (see

Chapter 3). One thing to be careful about, in the context of models in which N is unknown, is that, for each MCMC iteration m, we only tabulate those activity centers which correspond to individuals in the sampled population, i.e., for which the data augmentation variable $z_i = 1$. In this case, we take all of the output for MCMC iterations

 $m=1,2,\ldots$, niter and compute this summary:

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5.11 Summarizing Density and Activity Center Locations

$$N(\mathbf{x}, \mathbf{m}) = \sum_{\mathbf{i} = m, i \ge i} I(\mathbf{s}_{i, m} \in B(\mathbf{x})).$$

Thus, $N(\mathbf{x}, 1)$, $N(\mathbf{x}, 2)$, ..., is the Markov chain for parameter $N(\mathbf{x})$, in what follows we will provide a set of \mathbf{R} commands for doing this calculation and making a basic image plot from the MCMC output:

oldie Step 1: Define the center points of each pixel B(x), or point at which local density will be estimated:

(02, ,[S]mifx,[L]mifx)per -> px < 00000 (02, ,[S]mify,[L]mify)per -> py < 20000

ol220 Step 2: Extract the MCMC histories for the activity centers and the data augmentation variables. Note that these are each $N \times niter$ matrices. Here we do this assuming

that WinBUGS was run producing the R object named out:

olds Step 3: We associate each coordinate with the proper pixel using the R command cut (). Note that we keep only the activity centers for which z=1 (i.e., individuals

that belong to the population of size N):

oszso Step 4: Use the table () command to tally up how many activity centers are in

orzas Step 5: Use the image (3) command to display the resulting matrix:

oloso > image(xg Vg, Dn/nrow(z), col=terrain.colors(l0))

Me'll wath the poet that density maps will not usually appear uniform to is worth emphasizing here that density maps will not usually appear uniform

despite that we have assumed that activity centers are uniformly distributed. This is because the observed encounters of individuals provide direct information about the location of the $i=1,2,\ldots,n$ activity centers and thus their "estimated" locations will be affected by the observations. In a limiting sense, were we to sample space intensely enough, every individual would be captured a number of times and we would have considerable information about all N point locations. Consequently, the uniform prior would have almost no influence at all on the estimated density surface in this limiting situation. Thus, in practice, the influence of the uniformity assumption decreases as the fraction of the population encountered, and the total number of encounters per the fraction of the population encountered, and the total number of encounters per

individual, increases.

```
Spatial dot plots—A cruder version of the density map can be made using our posoo
         looking at. You can always specify the x and y labels explicitly as we did above.
     you do image (rot (M)) then it puts it on the monitor as iffit was a map you were
     should be in the upper left corner. We have a function rot () which does that. If
     the lower left corner. If you want M[] to be plotted "as you look at it" then M[], 1]
      a matrix M by 1 mage (M), might not be very intuitive to some—it plots M[1, 1] in
On the non-intuitiveness of image ()—the R function image (), invoked for posso
```

function is as follows: as input, point locations and the value to be displayed. A simplified version of this "spatial dot map" function spatial. plot (in scrbook). This function requires,

```
SSIOS
                      ((z)woxn/nd ,(yy,yy), Dn/nrow(z) <
08010
$2019
                             # To execute the function do this:
01010
29010
09010
                        image.scale(V_ccol=togo:colors(20))
52010
           points(x,pch=20,col=topo.colors(20)[nc],cex=2)
02010
                                              broc(x'bcy=" ")
54010
                                nc <- as.numeric(cut(y,20))
01040
                              > yatial.plot -> tunction(x,Y)
25010
```

5.11.2 Example: Wolverine density map

data augmentation variables z into a list. This also requires that we add those variables particular, we have to package up the MCMC history for the activity centers and the function SCRdensify which requires a specific data structure as shown below. In and we produce a density map of wolverines from that analysis. We include the We return to the wolverine study which took place an 2008 in SE Alaska (Figure 5.4)

to the parameters to-be-monitored list when we pass things to BUGS.

short MCMC run) are as follows: lower panel) for a fine-scale map. The R commands for producing such a plot (for a 6.2 straigiff) birg 05 × 05 a ni beginstra slexiq 000 gnisu bin (lenaq qof 6.2 straigiff) pute a relatively coarse version of a density map, using 100 pixels in a 10 imes 10 grid We used the posterior output from the wolverine model fitted previously to com-

```
z$deil.emie$duo -> z <
01152
                                                  [S,,]s$Jail.amia$Juo -> Y2 <
07110
                                                  | T' ']s$qsi['swis$qno -> x8 <</pre>
SILIO
     > out <- wolvsCR0(y3d,traps,nb=1000,ni=2000,buffer=1,M=100,keepz=TRUE)
01110
                        # This takes 341 seconds on a standard CPU circa 2011
$0110
                       > 13d <- SCR23darray (wolverine$wcaps, wolverine$wcraps)
00110
                                                    Successor -- wolverine$wtraps
$601°
                                                               > qqfq(wojnerine)
06010
                                                              Tiprary(scrbook)
28010
```

5.11 Summarizing Density and Activity Center Locations **L91**

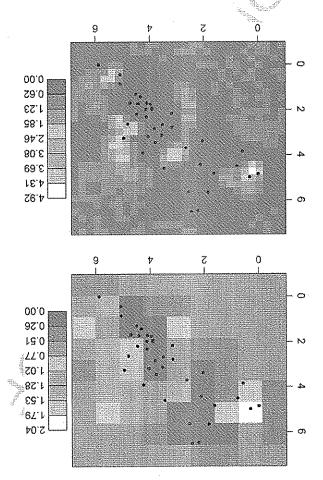


FIGURE 5.6

area. Dots are the trap locations. SCRO. Map grid cells are about 103.7 km2 (top panel) and 11.5 km2 (bottom panel) in Density of wolverines (individuals per $100~\mathrm{km}^2$) in SE Alaska in 2007 based on model

oll35 > tmp < SCRdensity(obj,nx=10,ny=10,scalein=100,scaleout=100) (z=z, y2=y2, x2=x2) dat_ -> tdo < 08110

area of the pixels is about 103.7 $\rm km^2$ and 11.5 $\rm km^2$, respectively. That calculation is In these figures density is expressed in units of individuals per $100~\mathrm{km}^2$, while the

> total.area (30*30)

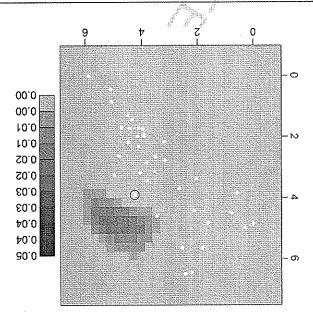
76922.II [I] 00110

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50001

FIGURE 5.7

CHAPTER 5 Fully Spatial Capture-Recapture Models



Posterior probability distribution of s₁, the activity center for individual 1 in the wolverine data set. This individual was captured a single time in one trap (trap 30) which is circled. White dots are trap locations.

water if we so wished. Alternatively, areas covered by water could be masked out, estimates of N over any well-defined region which presumably wouldn't include this is OK as far as estimating density goes and, furthermore, we can compute valid water as if it were habitat similar to that within which the array is nested. But, all of about the model that recognizes water from non-water and so the model predicts over who see fairly certain that wolverines do not like water. However, there is nothing over water (although the coastline is not shown). This might be perplexing to some density under the prior. Another thing to note about this map is that density is not 0 and as you get far away from the data, the predictions tend to the expected constant way to think of it is that it is a consequence of the prior, which imposes uniformity, predictions tend toward the global mean as the influence of data diminishes. Another of statistical smoothers such as splines, kernel smoothers, and regression smoothers decreases sufficiently rapidly as a function of distance. Relatedly, it is also a property mean density. This is a property of the estimator as long as the detection function the data live" Asway from the trap array we see that the density approaches the A couple of things are worth noting: First is that as we move away from "where

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which we discuss in the next section.

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5.12 Effective Sample Area

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5.11.3 Predicting where an individual lives

the trap array. The help file for SCRdenaity shows how to calculate Figure 5.7. which individual I was not captured, the model pushesaits activity center away from ways. In particular, because there are other traps in close proximity to trap 30, in distribution is affected by traps of capture and traps of non-capture in fairly intuitive a single time at trap 30 which is circled in Figure 5. We see that the posterior for the individual labeled 1 in the data set, in Figure 5.7. This individual was captured distribution. To illustrate, we show the posterior distribution of seather activity center such uncaptured individuals (for i = n + 1, ..., N) should have the same posterior corresponding plot of where such an individual might live, sayis_{n+1} Obviously, all for an individual that is not captured, we can use the MCMC output to produce a we can easily generate a posterior distribution of si for individual. In addition, location of a specific individual's activity center. For any observed encounter history, per unit area. A closely related problem is that of producing a map of the probable posso The density maps in the previous section show the expected number of individuals

5.12 Effective sample area

the SCR model we don't need to try to estimate or otherwise characterize the ESA at the edge of the state-space have no probability of being captured, but as part of be somewhat larger than the ESA, whatever that may be, in the sense that individuals state space is it (ASA) some (bolymes ample (or sampled) were (BAA) it is desirable that it the underlying point process is defined—the state-space of the point process. This explicit linkage between Mand "area," by prescribing explicitly the area within which capture-recapture model. In SCR models we avoid the problem of not having an usually by adding a buffer of some width, which is not estimated as part of the been addressed in the ad hoc way of prescribing an area that contains the trap array, does not have an explicit region of space associated with it. Classically this has is unknown—in other words, the M that is estimated by capture-recapture models up over and over again is this issue that the area which is sampled by a trapping array posss One of the key issues in using ordinary capture recapture models which we've brought

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magic number that satisfies that equivalence: definition of ESA follows from equating density to "apparent density"—ESA is the in distance sampling (Buckland et al., 2001; Borchers et al., 2002). The conceptual any SCR model. This is directly analogous to the calculation of "effective strip width" However, It is possible to provide a characterization of effective sampled area under

 $D = N/\Lambda = n/ES\Lambda.$

density. So, to compute ESA for a model, we substitute $\mathbb{E}(n)$ for n into the above ratio of the observed sample size n to this number ESA. Both of these should equal In other words, the ratio of N to the area of the state-space should be equal to the

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CHAPTER 5 Fully Spatial Capture-Recapture Models

equation, and solve for ESA, to get:

$$ESA = \mathbb{E}(n)/D$$
.

Our following development assumes that D is constant, but these calculations can be generalized to allow for D to vary spatially. Imagine our habitat mask for the wolverine data, or the bins we just used to produce a density map, then we can write $\mathbb{E}(n)$ according to

$$\mathbb{E}(n) = \sum_{s} \Pr(\text{encounter}|s) \mathbb{E}(N(s)),$$

where if we prefer to think of this more conceptually we could replace the summation, with an integration (which, in practice, we would just replace with a summation, and so we just begin there). In this expression note that $\mathbb{E}(N(\mathbf{s}))$ is the expected population size at pixel \mathbf{s} which is the density times the area of the pixel, i.e., $\mathbb{E}(N(\mathbf{s})) = D \times a$. Therefore

$$\mathbb{E}(n) = D \times a \times \sum_{s} \Pr(\text{encounter}|s)$$

and (plugging this into the expression above for ESA)

$$ESA = \frac{D \times a \times \sum_{s} Pr(encounter|s)}{D}.$$

We see that D cancels and we have $ESA = \alpha \times \sum_s Pr(encounter|s)$. So what you have to do here is substitute in Pr(encounter|s) and just sum them up over all pixels.

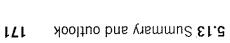
$$\Pr(\text{encounter}|\mathbf{s}) = 1 - (1 - p(\mathbf{s}))^K$$

with slight modifications when encounter probability depends on covariates. Thus,

Clearly the calculation of ESA is affected by the use of a habitat mask, because the summation in Eq. (5.12.1) only occurs over pixels that define the state-space.

For the wolverine camera trapping data, we used the 2×2 km habitat mask and the posterior means of p_0 and σ (see Section 5.10.2) to compute the probability of encounter for each s of the mask points. The result is shown graphically in Figure 5.8. The ESA is the sum of the values plotted in that figure multiplied by 4, the area of each pixel. For the wolverine study, the result is 2507.152 km². We note that the probability of encounter declines rapidly to 0 as we move away from the periphery of the camera traps, indicating the state-space constructed from a 40 km buffered trap array was indeed sufficient for the analysis of these data. An **R** script for producing this figure is in the wolvest function of the scrbook package.

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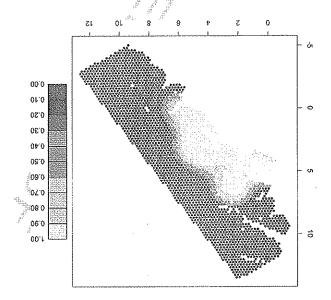


FIGURE 5.8

Probability of encounter used in computing effective sampled area for the wolverine camera trapping array, using the parameter estimates (posterior means) for the 2×2 km habitat mask.

5.13 Summary and outlook

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poseo In this chapter, we introduced the simplest SCR model—"model SCR0"—which is an ordinary capture-recapture model like model M₀, but augmented with a set of latent individual effects, s_i, which relate encounter probability to some sense of individual location using a covariate, "distance," from s_i to each trap location. Thus, individuals in close proximity to a trap will have a higher probability of encounter, and vice versa. The explicit modeling of individual locations and distance in this fashion resolves classical problems related to estimating density: unknown sample area, and resolves classical problems related to estimating density: unknown sample area, and resolves classical problems related to estimating density: unknown sample area, and

SCR models are closely related to classical individual covariate models ("model M_x," as introduced in Chapter 4), but with imperfect information about the individual covariate. Therefore, they are also not too dissimilar from standard GLMMs used throughout statistics and, as a result, we find that they are easy to analyze using standard MCMC methods encased in black boxes such as WinBUGS or JAGS. We will also see that they are easy to analyze using likelihood methods, which we address

in Chapter 6. Formal consideration of the collection of individual locations (s_1, \ldots, s_N) is fundamental to all models considered in this book. In statistical terminology, we think of

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ness" (CSR) (see Chapter 8), and computing other point process summaries (Illian more traditional point process analyses, such as testing for complete spatial randomhome range center (Figure 5.7). We can also use SCR models as the basis for doing to produce a density map (Figure 5.6), or even a probability map for an individual's can obtain formal inferences about the point process. For example, we showed how formally link individual encounter history data to an underlying point process, we the collection of points {s_i} as a realization of a point process. Because SCR models

Part of the promise, and ongoing challenge, of SCR models is to develop models et al., 2008).

parameter estimates and other inferences, such as model selection (see Chapter 8). sized in this chapter, the state-space is part of the model. It can have an influence on the point process plays an important role in developing SCR models. As we emphathe point process is such an integral component of SCR models, the state-space of the quantity of data, both number of individuals and captures per individual. Because Obviously the complexity of posterior estimates of the point pattern will depend on posterior distribution of point locations should therefore reflect non Independence. this in the form of individuals not being encountered in the same trap. The resulting process. For example, if individuals are highly territorial then the data should indicate model can effectively reflect or adapt to complex realizations of the underlying point example). In applications of the basic SCR model, we find that this simple a priori sity maps will typically appear distinctly non-uniform (as we saw in the wolverine data provide information to impart deviations from uniformity. Thus, estimated denrealized pattern may deviate markedly from uniformity as the observed encounter Moreover, even though the prior distribution on the point locations is uniform, the applications of SCR models, although we do address generalizations in later chapters. distributed over space. Despite the simplicity of this model, it should suffice in many ble point process model in which points are independent and uniformly ("randomly") temporal dynamics in point locations. In this chapter we considered the simplest possithat reflect interesting biological processes, for example interactions among points or

(Chapter 17) estimation, so that the interested reader can develop or extend methods We also consider technical details of maximum likelihood (Chapter 6) and Bayesian 16) (and methods for model assessment and selection (Chapter & among other topics. (Chapter 7), spatial covariates on density (Chapter 11), open populations (Chapter we consider models that include covariates that vary by individual, trap, or over time offict important extensions of the basic SCR model in later chapters. For example, produce more realistic models, which we discuss in Chapter 13. We consider some simplicity of the underlying model of space usage and suggests a direct extension to distribution proportional to the encounter probability model. This both clarifies the and movement, in which individuals make random use decisions from a probability of encounter probability can all be motivated as simplistic models of space usage model relates to a model of space usage by individuals. The standard SCR models in the literature on SCR models, is the manner in which the encounter probability One concept we introduced in this chapter, which has not been discussed much

to suit their own needs.

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maps and computing derived quantities such as the effective sample area. how to summarize posterior output for the purposes of producing posterior density using wolverine data collected in southern Alaska, and this example demonstrates lihood methods are covered in the next chapter. An example analysis is presented Bayesian methods using Markov chain Monte Carlo and data augmentation. Likesampling designs and how to format the resulting data. For inference, we focus on fully appreciated. The chapter also focuses on practical issues such as common recapture data in R, so that the assumptions and properties of the model can be of SCR models and we provide some basic tools for simulating spatial capturetions that must be understood and critically evaluated. We list the basic assumptions individual activity centers and traps. As with all models, it includes several assumpspecifying capture or encounter probability as a function of the distance between the number and location of animal activity centers and (2) an observation model of two conditionally-related components: (1) a spatial point process describing which we refer to as "model SCRO." The model is a hierarchical model composed Abstract: In this chapter we investigate the basic spatial capture-recapture model,

Sampling design, Spatial point process

Keywords: Activity center, Bayesian inference, Data format, Observation model,

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