# Integrating Resource Selection with Spatial Capture-Recapture Models

# 13

In Chapter 5 we briefly discussed the notion of how SCR encounter probability models relate to models of space usage. When using symmetric and stationary encounter probability models, SCR models imply that space usage is a decreasing function of distance from an individual's home range center. This is not a very realistic model in most applications. In this chapter, we extend SCR models to incorporate models of resource selection, such as when one or more explicit landscape covariates are available which the investigator believes might affect how individual animals use space within their home range. This is what Johnson (1980) called *third-order* selection—a term emphasizing the hierarchical nature of resource selection.

An appealing feature of SCR models is that they provide a mechanism for modeling multiple levels of the resource selection hierarchy. For instance, Johnson (1980) defined *second-order* selection as the process determining the location of home ranges on a landscape, which is exactly the process being modeled using the methods presented in Chapter 11. Thus, SCR provides a way of studying the density and distribution of home range centers, while at the same time allowing for inferences about the use of resources within home ranges.

Our treatment follows Royle et al. (2013b) who integrated a standard family of resource selection models based on auxiliary telemetry data into the capture-recapture model for encounter probability. They argued that SCR models and resource selection models (Manly et al., 2002) are based on the same basic underlying model of space usage. The important distinction between SCR and RSF studies is that, in SCR studies, encounter of individuals is imperfect (i.e., "$p < 1$"); whereas, with RSF data obtained by telemetry, encounter is perfect. SCR and telemetry data can therefore be combined in the same likelihood by formally recognizing this distinction in the model.

There are two important motives for considering a formal integration of RSF models with capture-recapture. The first is to integrate models of resource use by individuals with models of population size or density. There is relatively little in the literature on this topic, although Boyce and McDonald (1999) describe a procedure where (an estimate of) population size is used to scale resource selection functions to produce a population density surface. The second reason is to allow for the integration of auxiliary data from telemetry studies with capture-recapture data. Telemetry data has been widely used in conjunction with capture-recapture data using standard non-spatial models. For example, White and Shenk (2001) and Ivan (2012) suggested using

telemetry data to estimate the probability that an individual is exposed to capture-recapture sampling. However, their estimator requires that individuals are telemetry-tagged in proportion to this unknown quantity, which seems impossible to achieve in many studies. In addition, they do not directly integrate the telemetry data with the capture-recapture model so that common parameters are jointly estimated.

Formal integration of capture-recapture with telemetry data for the purposes of modeling resource selection has a number of immediate benefits. For one, telemetry data provide direct information about $\sigma$ (Sollmann et al., 2013a, c). As a result, model parameter estimates are improved which, as we see in Section 10.7, also has important implications for the design of SCR studies. In addition, active resource selection by animals induces a type of heterogeneity in encounter probability, which is misspecified by standard SCR encounter probability models. Animals that use more space due to the configuration of habitat or landscape features stand to be exposed to more traps than animals that use less space. Ignoring the heterogeneity in encounter probability resulting from resource selection can lead to bias in estimates of population size or density (Royle et al., 2013b). Finally, because the resource selection model translates directly to a model for encounter probability for spatial capture-recapture data, the implication of this is that it allows us to estimate resource selection model parameters directly from SCR data, i.e., *absent* telemetry data. This fact should broaden the practical relevance of spatial capture-recapture not just for estimating density, but also for directly studying movement and resource selection.

## 13.1  A model of space usage

Assume that the landscape is defined in terms of a discrete raster of one or more covariates, having the same dimensions and extent. Let $\mathbf{x}_1, \ldots, \mathbf{x}_G$ identify the center coordinates of $G$ pixels that define a landscape, organized in the matrix $\mathbf{X}_{G \times 2}$. Let $C(\mathbf{x})$ denote a covariate defined for every pixel $\mathbf{x}$. We suppose that individual members of a population utilize space in some manner related to the covariate $C(\mathbf{x})$.

As a biological matter, space use is the outcome of individuals moving around their home range (Hooten et al., 2010), i.e., where an individual is at any point in time is the result of some movement process. However, to understand space usage, it is not necessary to entertain explicit models of movement, just to observe the outcomes, and so we don't elaborate further on what could be sensible or useful models of movement, but we imagine existing methods of hierarchical or state-space models are suitable for this purpose (Ovaskainen, 2004; Jonsen et al., 2005; Forester et al., 2007; Ovaskainen et al., 2008; Hooten et al., 2010; McClintock et al., 2012). We consider explicit movement models in the context of SCR models in the later chapters of this book (Chapters 15 and 16). Here we adopt more of a phenomenological formulation of space usage as follows: If an individual appears in pixel $\mathbf{x}$ at some instant, this is defined as a decision to "use" pixel $\mathbf{x}$. Over any prescribed time interval, if we sample some number of points times say $R$, then let $m_{ij}$ be the use frequency of pixel $j$ by individual $i$—i.e., the number of times individual $i$ used pixel $j$. We assume the

vector of use frequencies $\mathbf{m}_i = (m_{i1}, \ldots, m_{iG})$ has a multinomial distribution:

$$\mathbf{m}_i \sim \text{Multinomial}(R, \boldsymbol{\pi}_i),$$

where $R = \sum_j m_{ij}$ is the total number of "use decisions" made by individual $i$ and

$$\pi_{ij} = \frac{\exp(\alpha_2 C(\mathbf{x}_j))}{\sum_{\mathbf{x}} \exp(\alpha_2 C(\mathbf{x}))},$$

for each $j = 1, 2, \ldots, G$ pixels. This is a standard RSF model used to model telemetry data. In particular, this is "protocol A" of Manly et al. (2002) where all available landscape pixels are censused (i.e., known without error), and used pixels are sampled randomly for each individual. The parameter $\alpha_2$ is the effect of the landscape covariate $C(\mathbf{x})$ on the relative probability of use. Thus, if $\alpha_2$ is positive, the relative probability of use increases as the covariate increases.

In practice, we don't observe $m_{ij}$ for all individuals but, instead, only for a small subset which we capture and telemeter. For the telemetered individuals, we assume they use resources according to the same RSF model as the population as a whole.

To extend this model to make it more realistic, and consistent with the formulation of SCR models, let $\mathbf{s}$ denote the center of an individual's home range and let $d_{ij} = ||\mathbf{x}_j - \mathbf{s}_i||$ be the distance from the home range center of individual $i$, $\mathbf{s}_i$, to pixel $j$, $\mathbf{x}_j$. We modify the space usage model to accommodate that space use will be concentrated around an individual's home range center:

$$\pi_{ij} = \frac{\exp\left(-\alpha_1 d_{ij}^2 + \alpha_2 C(\mathbf{x}_j)\right)}{\sum_x \exp\left(-\alpha_1 d_{ij}^2 + \alpha_2 C(\mathbf{x})\right)}. \tag{13.1.1}$$

The parameters $\alpha_1$, $\alpha_2$ and the activity centers $\mathbf{s}$ can be estimated directly from telemetry data, using standard likelihood methods based on the multinomial likelihood (Johnson et al., 2008b). Normally this model is expressed in terms of the scale parameter $\sigma$, where $\alpha_1 = 1/(2\sigma^2)$, and the multinomial model Eq. (13.1.1) can be understood as a compound model of space usage governed by distance-based "availability" according to a Gaussian kernel, and "use," conditional on availability (Johnson et al., 2008b; Forester et al., 2009). In other words, the model suggests a kind of distance-based availability in which a pixel is less available to an individual if it is located further away from $\mathbf{s}_i$.

Equation (13.1.1) resembles standard SCR encounter probability models that we have used previously, but here the model includes an additional covariate $C(\mathbf{x})$ (see Chapter 9). In particular, under this model for space usage or resource selection, if we have no covariates at all, or if $\alpha_2 = 0$, then the probabilities $\pi_{ij}$ are directly proportional to the SCR model for encounter probability, if there is trap in every pixel. In other words, setting $\alpha_2 = 0$, the probability of use for pixel $j$ is:

$$p_{ij} \propto \exp\left(-\alpha_1 d_{ij}^2\right).$$

Clearly, whatever function of distance we use in the RSF model implies an equivalent SCR model for encounter probability. In particular, for whatever encounter probability

model we choose for $p_{ij}$ in an ordinary SCR model, we can modify the distance component in the RSF function in Eq. (13.1.1) to be consistent with that model by setting:

$$\pi_{ij} \propto \exp(\log(p_{ij}) + \alpha_2 C(\mathbf{x}_j))$$

(see Forester et al., 2009). Therefore, to contemplate integrating RSFs based on telemetry data with SCR data, we think of SCR data as representing a thinning (or sampling) of the potentially observable ("perfect") use frequencies $m_{ij}$ obtainable by telemetry. The above expression identifies the manner in which parameters of the SCR encounter probability model are shared by the parameters of the RSF model.

### 13.1.1 A simulated example

For a simulated landscape (shown in Figure 13.1), Royle et al. (2013b) depicted some typical space usage patterns under the model described above, which we reproduce here in Figure 13.2. The covariate in this case was simulated using a kriging model of correlated random noise with the following **R** commands:

```
> set.seed(1234)
> gr <- expand.grid(1:40,1:40)
> Dmat <- as.matrix(dist(gr))
> V <- exp(-Dmat/5)
> C <- t(chol(V))%*%rnorm(1600)
```
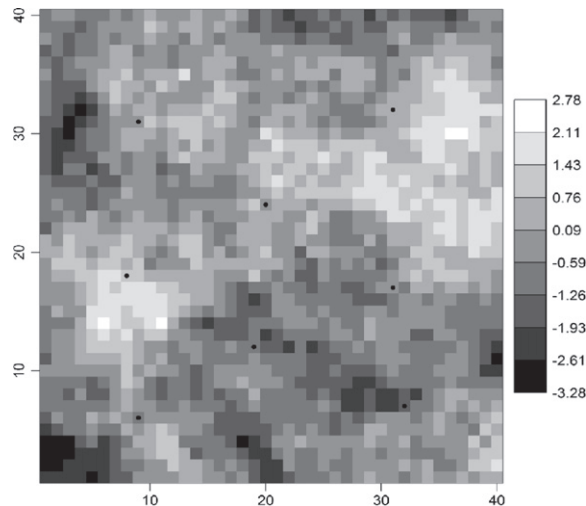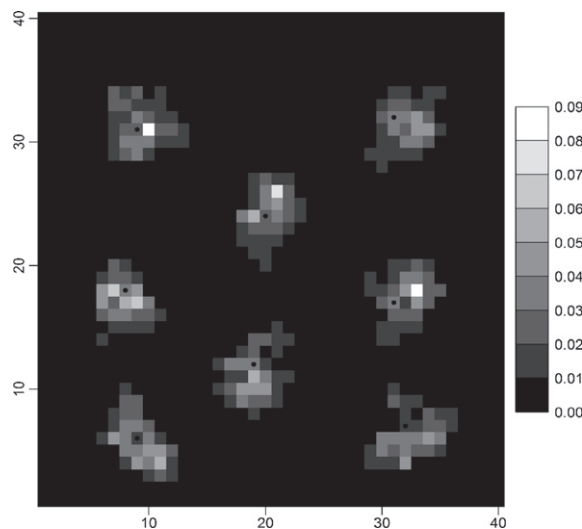


**FIGURE 13.1**

A typical habitat covariate reflecting habitat quality or hypothetical utility of the landscape to a species under study. Home range centers for 8 individuals are shown with black dots.

**FIGURE 13.2**

Space usage patterns of 8 individuals under a space usage model that contains a single covariate which is shown in Figure 13.1. The plotted value is the multinomial probability $\pi_{ij}$ for pixel $j$ under the model in Eq. (13.1.1).

The resulting covariate vector $\mathbf{C}$ is multivariate normal with mean 0 and variance-covariate matrix $\mathbf{V}$ which, here, has pairwise correlations that decay exponentially with distance. The use densities shown in Figure 13.2 were simulated with $\alpha_1 = 1/(2\sigma^2)$, $\sigma = 2$, and the coefficient on $C(\mathbf{x})$ set to $\alpha_2 = 1$. The resulting space usage densities—or "home ranges"—exhibit clear non-stationarity in response to the structure of the underlying covariate, and they are distinctly asymmetrical. We note that if $\alpha_2$ were set to 0, the 8 home ranges shown here would be proportional to a bivariate normal kernel with $\sigma = 2$.[1] The commands for generating the covariate, and producing Figure 13.1 are in the package `scrbook` (see `?RSF_example`).

### 13.1.2 Poisson model of space use

A natural way to motivate the multinomial model of space usage is to assume that individuals make a sequence of resource selection decisions so that the outcomes $m_{ij}$ are *independent* Poisson random variables:

$$m_{ij} \sim \text{Poisson}(\lambda_{ij}),$$

where

$$\log(\lambda_{ij}) = a_0 - \alpha_1 d_{ij}^2 + \alpha_2 C(\mathbf{x}_j).$$

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[1]This is why we have always referred to the similar-looking model for encounter probability as the Gaussian or bivariate normal model, instead of half-normal.

In this case, the number of visits to any particular cell is affected by the covariate $C(\mathbf{x})$ but has a baseline rate, $\exp(a_0)$, related to the amount (in an expected value sense) of movement occurring over some time interval. This is an equivalent model to the multinomial model given previously in the sense that, if we condition on the total sample size $R = \sum_j m_{ij}$, then the vector $\mathbf{m}_i$ has a multinomial distribution with probabilities given by Eq. (13.1.1).

In practice, we never observe "truth," i.e., the actual use frequencies $m_{ij}$. Instead, we observe a sample of the actual use outcomes by an individual. As formulated in Section 5.4, we assume a binomial ("random") sampling model:

$$y_{ij} \sim \text{Binomial}(m_{ij}, p_0).$$

We can think of these counts as arising by thinning the underlying point process (here, aggregated into pixels) where $p_0$ is the thinning rate of the point process. In this case, the marginal distribution of the observed counts $y_{ij}$ is also Poisson but with mean

$$\log(\mathbb{E}(y_{ij})) = \log(p_0) + a_0 - \alpha_1 d_{ij}^2 + \alpha_2 C(\mathbf{x}_i).$$

Thus, the space-usage model (RSF) for the thinned counts $y_{ij}$ is the same as the space usage model for the original variables $m_{ij}$. This is because if we remove $m_{ij}$ from the conditional model by summing over its possible values, then the vector $\mathbf{y}_i$ is *also* multinomial with cell probabilities

$$\pi_{ij} = \frac{\lambda_{ij}}{\sum_j \lambda_{ij}},$$

where any constant (the intercept term $a_0$ and thinning rate $p_0$) cancels from the numerator and denominator. Thus, the underlying multinomial RSF model applies to the frequencies $\mathbf{m}_i$ and those produced from thinning or sampling, $\mathbf{y}_i$.

## 13.2 Integrating capture-recapture data

The key to combining RSF data with SCR data is to note that the Poisson model of space usage given above is exactly our Poisson encounter probability model from Chapter 9, but with a spatial covariate $C(\mathbf{x})$, and some arbitrary intercept off-set related to the sampling rate of the telemetry device. We've used exactly this model for SCR data (Chapter 7), but with a different intercept, $\alpha_0$, unrelated to the intercept of the Poisson use model for telemetry described above, but, rather, to the efficiency of the capture-recapture encounter device. In other words, we view camera traps (or other devices) located in some pixel $\mathbf{x}$ (or multiple pixels) as being equivalent to being able to turn on a type of (less perfect) telemetry device, and only in some pixels. Therefore, data from camera trapping are Poisson random variables for every pixel $j$ where a trap is located:

$$y_{ij} | \mathbf{s}_i \sim \text{Poisson}(\lambda_{ij})$$

with

$$\log(\lambda_{ij}) = \alpha_0 - \alpha_1 d_{ij}^2 + \alpha_2 C(\mathbf{x}_j).$$

The parameters $\alpha_1$ and $\alpha_2$ are shared with the multinomial model for the telemetry data. A key point here is that if resource selection is happening, then it appears as a covariate on encounter rate (or encounter probability) in the same way as ordinary covariates which we discussed in Chapter 7.

Alternatively, the SCR study can produce binary encounters depending on the type of sampling being done, where $y_{ij} = 1$ if the individual $i$ visited the pixel containing a trap and was detected. In this case, we imagine that $y_{ij}$ is related to the latent variable $m_{ij}$ being the event $m_{ij} > 0$, which occurs with probability

$$p_{ij} = 1 - \exp(-\lambda_{ij}) \qquad (13.2.1)$$

and then the observed encounter frequencies for individual $i$ and trap $j$, from sampling over $K$ occasions, are binomial:

$$y_{ij}|\mathbf{s}_i \sim \text{Binomial}(K, p_{ij}).$$

To construct the likelihood for SCR data when we have direct information on space usage from telemetry data, we regard the two samples (SCR and RSF) as independent of one another, and we form the likelihood for each set of observations as a function of the same underlying parameters. The joint likelihood then is the product of the two components.

In particular, let $\mathcal{L}_{scr}(\alpha_0, \alpha_1, \alpha_2, N; \mathbf{y})$ be the likelihood for the SCR data in terms of the basic encounter probability parameters and the total (unknown) population size $N$, and let $\mathcal{L}_{rsf}(\alpha_1, \alpha_2; \mathbf{m})$ be the likelihood for the RSF data based on telemetry which, because the sample size of telemetered individuals is fixed, does not depend on $N$. Assuming independence of the two data sets, the joint likelihood is the product of these two pieces:

$$\mathcal{L}_{rsf+scr}(\alpha_0, \alpha_1, \alpha_2, N; \mathbf{y}, \mathbf{m}) = \mathcal{L}_{scr}(\alpha_0, \alpha_1, \alpha_2, N; \mathbf{y}) \times \mathcal{L}_{rsf}(\alpha_1, \alpha_2; \mathbf{m}),$$

where $\mathcal{L}_{scr}$ is the standard integrated likelihood (Chapter 6), and the RSF likelihood contribution is the multinomial ~~telemetry~~ likelihood having cell probabilities Eq. (13.1.1). The **R** code for maximizing the joint likelihood was given in the supplement to Royle et al. (2013b), and we include a version of this in the `scrbook` package, see `?intlik3rsf`, which also shows how to simulate data and fit the combined SCR + RSF model.

## 13.3  SW New York black bear study

Royle et al. (2013b) applied the integrated SCR + RSF model to data from a study of black bears[2] (*Ursus americanus*) in a region of approximately 4,600 km$^2$ in southwestern New York (Sun, in press). These data can be loaded from the `scrbook` package with the command `data(`~~nybears~~`)`.

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[2]This is a different data set from the Fort Drum bear study which we've analyzed in previous chapters.
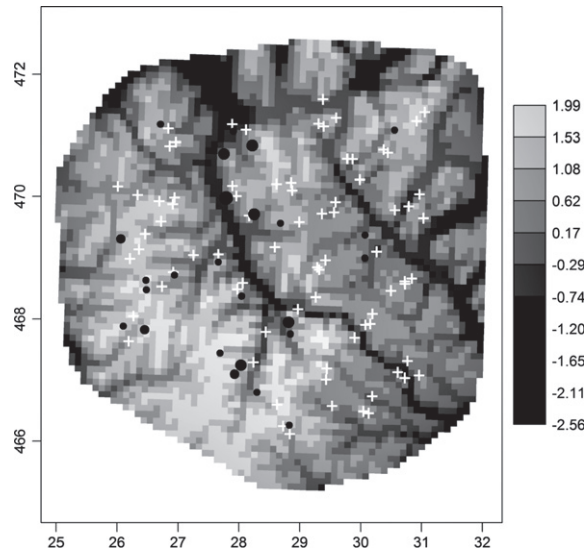
**FIGURE 13.3**

Elevation (standardized), and hair snare locations marked by the number of individuals captures at each site according to the size of the black circle. White crosses represent hair snare locations with no captures.

The data are based on a noninvasive genetic capture-recapture study using 103 hair snares in June and July, 2011. Hair snares were baited, scented and checked weekly (Sun, in press). The study yielded sparse encounter histories of 33 individuals with a total of 14 recaptures and 27 individuals captured 1 time only. Telemetry data were collected on three individuals, which produced locations for each bear approximately once per hour. Telemetry locations were thinned to once per 10 h to produce movement outcomes that might be more independent. This produced 195 telemetry locations used in the RSF component of the model. Elevation was used as a covariate for this model, a standardized version of which is shown in Figure 13.3 along with the number of individuals captured at each hair snare site.

There are a number of models that could be fitted to these data based on the combination of SCR and RSF data as well as the elevation covariate. The models fitted here are based on the Gaussian hazard encounter probability model, including an ordinary SCR model with no covariates or telemetry data, the SCR model with elevation affecting either baseline encounter probability or density $D(\mathbf{x})$ (Chapter 11), and models that use telemetry data. The six models and notation describing each are as follows:

Model 1, p(·): ordinary SCR model
Model 2, p(elev): ordinary SCR model with elevation as a covariate on baseline encounter probability.

**Table 13.1** Summary of model-fitting results for the black bear study. Parameter estimates are for the intercept ($\alpha_0$), logarithm of $\sigma$, the scale parameter of the Gaussian hazard encounter model, $\beta$ is the coefficient of elevation on density, $\alpha_2$ is the coefficient of elevation in the encounter probability/space-usage model, and the total population size of the state-space is $N$. Standard errors are in parentheses. The SCR data are based on $n = 33$ individuals, and the telemetry data are based on 3 individuals.

| Model | $\alpha_0$ | $\log(\sigma)$ | $\alpha_2$ | $N$ | $\beta$ | $-$loglik |
|---|---|---|---|---|---|---|
| p(elev) | −2.860 | −1.117 | 0.175 | 95.80 | | 122.738 |
| | (0.390) | (0.139) | (0.248) | (22.99) | | |
| p(·) | −2.729 | −1.122 | | 93.90 | | 122.990 |
| | (0.345) | (0.140) | | (22.06) | | |
| p(·) + D(elev) | −2.715 | −1.133 | | 94.20 | 1.247 | 118.007 |
| | (0.353) | (0.139) | | (21.90) | (0.408) | |
| p(elev) + D(elev) | −2.484 | −1.157 | −0.384 | 103.50 | 1.571 | 117.075 |
| | (0.391) | (0.142) | (0.276) | (26.56) | (0.463) | |
| p(elev) + RSF | −3.068 | −0.814 | −0.281 | 81.60 | | 1271.739 |
| | (0.272) | (0.036) | (0.118) | (17.65) | | |
| p(elev) + D(elev) + RSF | −3.070 | −0.810 | −0.371 | 89.10 | 1.273 | 1266.700 |
| | (0.272) | (0.037) | (0.124) | (20.55) | (0.411) | |

Model 3, p(·) + D(elev): ordinary SCR model with elevation as a covariate on density only.

Model 4, p(elev) + D(elev): ordinary SCR model with elevation as a covariate on both baseline encounter probability and density.

Model 5, p(elev) + RSF: SCR model including data from three telemetered individuals.

Model 6, p(elev) + D(elev) + RSF: SCR model including telemetered individuals and with elevation as a covariate on density.

Parameter estimates for the six models are given in Table 13.1 (reproduced from Royle et al. (2013b), see also the help file ?nybears). It is tempting to want to compare these different models by AIC but, because models 5 and 6 involve additional data, they cannot be compared with models 1–4.

By looking at Table 13.1, it is clear based on the negative log-likelihood of Models 1–4, that those containing an elevation effect on density (parameter $\beta$) are preferred (Models 3 and 4). The parameter estimates indicate a positive effect of elevation on density, which seems to be consistent with the raw capture data shown in Figure 13.3. Despite this strong effect of elevation, the estimates of $N$ under each of these models only ranged from 93 to 103 bears for the 4,600 km$^2$ state-space, and so estimated density is pretty consistent across models. If we consider not just density, but space usage (i.e., looking at the parameter $\alpha_2$), the effect of elevation is negative. Thus, elevation appears to affect density and space usage differently. It was

suggested that density operates at the second-order scale of resource selection and "…. is largely related to the spacing of individuals and their associated home ranges across the landscape. On the other hand, our RSF was defined based on selection of resources within the home range (third-order)" (Royle et al., 2013b). The positive effect of elevation on density is consistent with some other studies on black bears (e.g., Frary et al., 2011), and the negative effect of elevation on space usage can be attributed to seasonal variation in food availability, usage of corridors, or environmental conditions.

Models 5 and 6 include the additional telemetry data, thus the negative log-likelihoods are not directly comparable to the first four models, but we can still make a few important observations. First is that the parameter estimates under these two models are consistent with Model 4 in that elevation had a strong effect on both density and space usage. In comparing Models 5 and 6, the latter model which includes elevation as an effect on density reduces the negative log-likelihood by 5 units. Additionally, including the telemetry data reduces the standard errors (SE) of the density and space usage parameters and as we would expect, the incorporation of telemetry data also reduces the SE for $\sigma$. Model 6 (p(elev) + D(elev) + RSF) was used to produce maps of density (Figure 13.4) and space usage (Figure 13.5) showing the effect of elevation on both components of the model. The map of space usage shows the
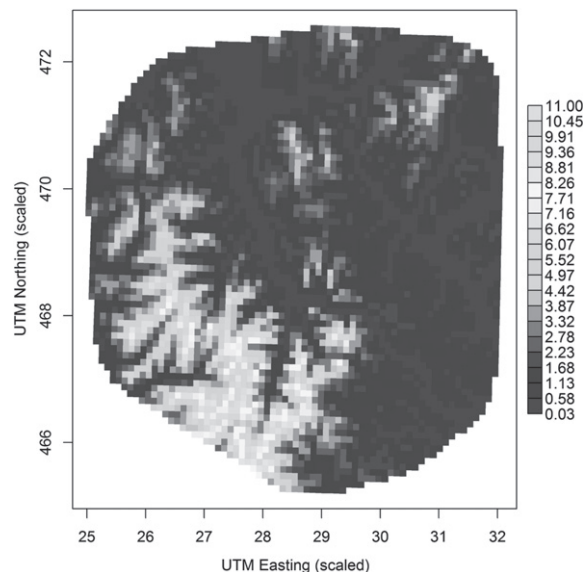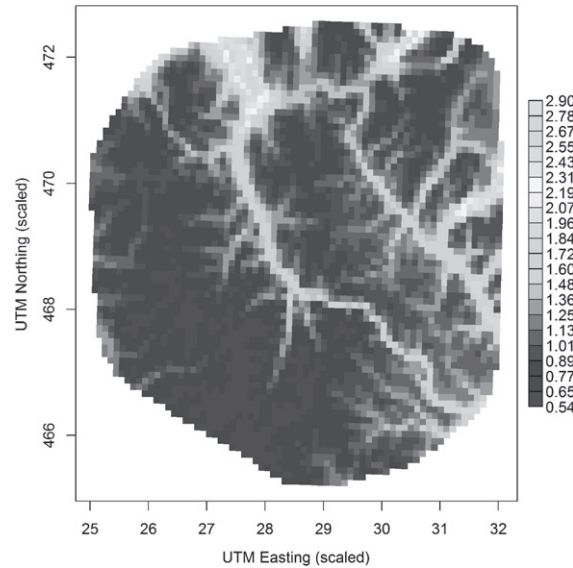


**FIGURE 13.4**

Predicted density of black bears (per 100 km$^2$) in southwestern New York study area.

**FIGURE 13.5**

Relative probability of use of pixel **x** compared to a pixel of mean elevation, at a constant distance from the activity center.

relative probability of using a pixel **x** relative to one having the mean elevation, given a constant distance to the individual's activity center.

## 13.4 Simulation study

Using the simulated landscape shown in Figure 13.1, Royle et al. (2013b) presented results of a simulation study considering populations of $N = 100$ and $N = 200$ individuals exposed to encounter by a $7 \times 7$ array of trapping devices, with $K = 10$ sampling occasions, using the Gaussian hazard model (Eq. (13.2.1)) with

$$\log(\lambda_{ij}) = -2 - \frac{1}{2\sigma^2}d_{ij}^2 + 1 \times C(\mathbf{x}_{ij}),$$

where $\sigma = 2, \alpha_0 = -2$ and $\alpha_2 = 1$. They investigated the effect of misspecification of the resource selection model with an ordinary model SCR0 (i.e., no habitat covariates affecting the trap encounter model), and the performance of the MLEs, under SCR + telemetry designs having 2, 4, 8, 12, and 16 telemetered individuals (with 20 independent telemetry fixes *per* individual). Three models were fitted: (i) the SCR only model, in which the telemetry data were not used; (ii) the integrated SCR/RSF model which combined all of the data for jointly estimating model parameters; and (iii) the RSF only model which just used the telemetry data alone (and therefore

**Table 13.2**  This table summaries the sampling distribution of the MLE of model parameters for models fitted to data generated under a resource selection model. The models fitted include the misspecified model, which is a basic model SCR0 (with no covariate), the SCR model with the covariate on encounter probability (SCR + C(x)), and the SCR model including the covariate and a sample of telemetered individuals (SCR/RSF; $n$ is the number of individuals telemetered). Data were simulated with $N = 200$ individuals, $\alpha_2 = 1$ and $\sigma = 2$.

| | $\hat{N}$ | RMSE | $\hat{\alpha}_2$ | RMSE | $\hat{\sigma}$ | RMSE |
|---|---|---|---|---|---|---|
| **$n = 2$** | | | | | | |
| SCR + C(x) | 199.11 | 14.28 | 0.99 | 0.09 | 2.00 | 0.090 |
| ~~SCR + RSF~~ | 199.11 | 13.80 | 0.99 | 0.09 | 2.00 | 0.079 |
| SCR0 | 161.48 | 39.98 | – | – | 1.84 | 0.180 |
| **$n = 4$** | | | | | | |
| SCR + C(x) | 199.67 | 13.87 | 1.00 | 0.09 | 2.00 | 0.090 |
| SCR/RSF | 199.65 | 13.59 | 1.00 | 0.09 | 2.00 | 0.072 |
| SCR0 | 161.32 | 40.00 | – | – | 1.83 | 0.191 |
| **$n = 8$** | | | | | | |
| SCR + C(x) | 199.24 | 15.49 | 0.99 | 0.10 | 2.01 | 0.093 |
| SCR/RSF | 199.55 | 14.17 | 0.99 | 0.08 | 2.00 | 0.063 |
| SCR0 | 161.46 | 40.06 | – | – | 1.84 | 0.184 |
| **$n = 12$** | | | | | | |
| SCR + C(x) | 200.41 | 15.16 | 0.99 | 0.10 | 2.00 | 0.086 |
| SCR/RSF | 200.95 | 13.04 | 1.00 | 0.08 | 2.00 | 0.051 |
| SCR0 | 162.40 | 38.95 | – | – | 1.84 | 0.185 |
| **$n = 16$** | | | | | | |
| SCR + C(x) | 199.16 | 15.62 | 1.00 | 0.09 | 2.00 | 0.095 |
| SCR/RSF | 199.63 | 13.38 | 1.00 | 0.07 | 2.00 | 0.052 |
| SCR0 | 160.93 | 40.44 | – | – | 1.84 | 0.190 |

the parameters $\alpha_0$ and $N$ are not estimable). An abbreviated version of the results from Royle et al. (2013b) are summarized in Table 13.2. We provide an **R** script (see `?RSFsim`) that can be modified for further analysis and exploration.

One thing we see is a ~~pretty~~ dramatic negative bias in estimating $N$ if the model SCR0 is fitted (interestingly, there is much less bias in estimating $\sigma$). Overall, though, when either the SCR model with covariate or the joint SCR + RSF model is fitted, the MLEs exhibit little bias for the parameter values simulated here. In terms of RMSE, there is only a slight $\approx$5–10% reduction in RMSE of the estimator of $N$ when we have at least 2 telemetered individuals. Thus, estimating $N$ benefits only slightly from the addition of telemetry data. This may be reasonable when we consider that information about the intercept, $\alpha_0$, comes only from the capture-recapture data. However, there

is a large improvement in precision (50–60%) for estimating the scale parameter $\sigma$. While this doesn't translate into improved estimation of $N$, it suggests that telemetry data should be relevant to the design of SCR studies for which trap spacing is one of the main considerations (Chapter 10). It is conceivable even that spatial recaptures are not needed if some telemetry data are available (in Chapter 19, in the context of mark-resight models, we show a case study of raccoons where additional telemetry data allows estimating model parameters in spite of a very low number of spatial recaptures (Sollmann et al., 2013a)). The resource selection parameter $\alpha_2$ is well estimated even *without* telemetry data. The fact that parameters of resource selection can be estimated from spatial capture-recapture data alone should have considerable practical relevance in the study of animal populations and landscape ecology. For the highest sample size of telemetered individuals ($n = 16$), the RMSE for estimating this parameter only decreases from about 0.09 to 0.07 compared to SCR alone.

## 13.5  **Relevance and relaxation of assumptions**

In constructing the combined likelihood for RSF and SCR data, we assumed the data from capture-recapture and telemetry studies were independent of one another. This may be reasonably satisfied if the two samples are random samples from the population of individuals with activity centers on the state-space (see Chapter 19 for additional discussion of this). We cannot foresee situations in which violation of this assumption should be problematic or invalidate the estimator under the independence assumption.

Our model pretends that we do not know anything about the telemetered individuals in terms of their encounter history in traps. In principle it should not be difficult to admit a formal reconciliation of individuals between the two lists. In that case, we just combine the two conditional likelihoods before we integrate **s** from the product likelihood. This would be almost trivial to do if *all* individuals were reconcilable between the SCR and telemetry samples (or none, as in the case we have covered here). But, in general, we think you will often have an intermediate case, i.e., only a subset of telemetered animals will be known and there will be some individuals encountered by traps or devices whose telemetry marking status cannot be determined. In that case, basically a type of marking uncertainty or misclassification is clearly more difficult to deal with (see Chapter 19 for some additional context).

We presented the model in a discrete landscape which regarded potential trap locations and the covariate $C(\mathbf{x})$ as being defined on the same set of points. In practice, trap locations may be chosen independently of the definition of the raster and this does not pose any challenge or novelty to the model as it stands. In that case, the covariate(s) need to be defined at each trap location. The model should be applicable also to covariates that are naturally continuous (e.g., distance-based covariates) although, in practice, it will usually be sufficient to work with a discrete representation of such covariates.

The multinomial RSF model for telemetry data assumes independent observations of resource selection. This would certainty be reasonable if telemetry fixes are

made far apart in time (or thinned). However, as noted by Royle et al. (2013b), the independence assumption is *not* an assumption of spatially independent movement outcomes in geographic space. Active resource selection should probably lead to the appearance of spatially dependent outcomes, regardless of how far apart in time the telemetry locations are. Even if resource selection observations are dependent, use of the independence model probably yields unbiased estimators while understating the variance. Continued development of integrated SCR + RSF models that accommodate more general models of movement is needed.

## 13.6   Summary and outlook

How animals use space is of fundamental interest to ecologists and is important in the conservation and management of many species. Investigating space use is normally done using telemetry and associated models referred to as resource selection functions (Manly et al., 2002), but in all of human history, animal resource selection has *never* been studied using capture-recapture models. Instead, essentially all applications of SCR models have focused on density estimation. It is intuitive, however, that space usage or resource selection should affect encounter probability and thus it should be highly relevant to density estimation in SCR applications, and, vice versa, SCR applications should yield data relevant to resource selection questions. The development in this chapter shows clearly that these two ideas can be unified within the SCR methodological framework so that classical notions of resource selection modeling can be addressed simultaneous to modeling of animal density. What we find is that if animal resource selection is occurring, this can be modeled as one or more covariates on encounter probability, with or without the availability of auxiliary telemetry data. If telemetry data do exist, we can estimate parameters jointly by combining the two likelihood components—that of the SCR data and that of the telemetry data.

Active resource selection by individuals induces a type of heterogeneous encounter probability, and this induces (possibly severe) bias in the estimated population size for a state-space when default symmetric encounter probability models are used. As such, it is important to account for resource selection when relevant covariates are known to influence resource selection patterns. Aside from properly modeling this selection-induced heterogeneity, integration of RSF data from telemetry with SCR models achieves a number of useful advances: First, it leads to an improvement in our ability to estimate density, and an improvement in our ability to estimate parameters of the RSF function. As many animal population studies have auxiliary telemetry information, the incorporation of such information into SCR studies has broad applicability. Secondly, the integrated model allows for the estimation of RSF model parameters directly from SCR data *alone*. Therefore, SCR models *are* explicit models of resource selection. In our view, this greatly broadens the utility and importance of capture-recapture studies beyond their primary historical use of estimating density or population size. Finally, we note that telemetry information provide direct information about the home range shape parameter, $\sigma$, in our analyzes above, and its estimation is greatly improved

with even moderate amounts of telemetry data (see also Sollmann et al. (2013a) and Sollmann et al. (2013c)). This should have some consequences in terms of the design of capture-recapture studies (Chapter 10), especially as it relates to trap spacing.

Simultaneously conducting telemetry studies with capture-recapture is extremely common in field studies of animal populations. However, the simultaneous, integrated analysis of the two sources of data is uncommon. The new class of integrated SCR/RSF models allows researchers to model how the landscape and habitat influence the movement and space use of individuals around their home range, using capture-recapture data that can be augmented with telemetry data. This should improve our ability to understand, and study, aspects of space usage and it might, ultimately, aid in addressing conservation-related problems such as reserve or corridor design.

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**Non Print Items**

**Abstract:** In this chapter, we extend SCR models to incorporate models of resource selection, such as when one or more explicit landscape covariates are available which the investigator believes might affect how individual animals use space within their home range. We present a method that integrates a standard family of resource selection models based on auxiliary telemetry data into the capture-recapture model for encounter probability. The important distinction between SCR and resource selection function (RSF) studies is that, in SCR studies, encounter of individuals is imperfect (i.e., "$p < 1$"); whereas, with RSF data obtained by telemetry, encounter is perfect. Thus, in this chapter, we argue that SCR and telemetry data can therefore be combined in the same likelihood by formally recognizing this distinction in the model. We demonstrate a model for integrating capture-recapture data with RSF data under a Poisson model of space usage. We present and analyze data from a study of black bears in southwest NY, USA to which we fit a variety of models that highlight the differences between models including only SCR data or models that include both SCR and RSF data. We also provide a simulation study to evaluate the model and for the reader to become more familiar with the models and data. This integration of SCR and RSF models wil allow researchers to model how the landscape and habitat influence the movement and space use of individuals around their home range, using non-invasively collected capture-recapture data that can be augmented with telemetry data.

**Keywords:** Black bears, Habitat selection, Landscape structure, Multiple data sources, Resource selection functions, RSF, Telemetry, Utilization distribution