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Chapter 9

State-space Covariates

Underlying all spatial capture recapture models is a point process model describing the distribution of individual activity centers (\mathbf{s}_i) within the state space (\mathcal{S}). So far we have focused our discussion on the homogeneous binomial point process, $\mathbf{s}_i \sim \text{Uniform}(\mathcal{S})$, $i = 1, 2, \dots, N$, where N is the size of the population. This is a model of “spatial-randomness”¹ because the intensity of the activity centers is constant across the study area and the activity centers are distributed independently of each other.

The spatial-randomness assumption is often viewed as restrictive because ecological processes such as territoriality and habitat selection can result in non-random distributions of organisms. We have argued, however, that this assumption is less restrictive than may be recognized because the homogeneous point process actually allows for infinite possible configurations of activity centers. Furthermore, given enough data, the uniform prior will have very little influence on the estimated locations of activity centers. Nonetheless, the homogeneous point process model does not allow one to model population density using covariates—a central objective of much ecological research. For example, a homogeneous point process model may result in a density surface map indicating that individuals were more abundant in one habitat than another, but it does not do so explicitly. A more direct approach would be to model density using covariates as is done in generalized linear models (GLMs).

In this chapter we will present a method for fitting inhomogeneous binomial point process models using covariates in much the same way as is done with GLMs. The covariates we consider differ from those covered in previous chapters, which were typically attributes of the animal (*e.g.* sex, age) and were used to model movement or encounter rate. In contrast, here we wish to model covariates that are defined for all points in \mathcal{S} , which we will refer to as state-space, or density, covariates. These may include continuous covariates such as elevation, or discrete covariates such as habitat type.

¹The phrase “complete spatial-randomness” is reserved for the homogeneous Poisson point process

? were the first to propose an inhomogeneous point process model for SCR models, and our approach is similar to theirs with the exception that we will use a binomial rather than a Poisson model because the binomial model is easily integrated into our data augmentation scheme and is consistent with the objective of determining how a *fixed* number of activity centers are distributed with respect to covariates.

The method we use to accommodate inhomogeneous binomial point process models within our MCMC algorithm is simple—we replace the uniform prior with a prior describing the distribution of the N activity centers conditional on the covariates. Development of this prior, which does not have a standard form, is a central component of this chapter. First we will begin with a review of homogeneous point process models.

9.1 Homogeneous point process revisited

The homogeneous Poisson point process is *the* model of “complete spatial randomness” and is often used in ecology as a null model to test for departures from randomness. Given its central role in the analysis of point processes, it is helpful to compare it with the binomial model that we use in our SCR models. The primary descriptor of the homogeneous point process model is the “intensity” parameter, μ which describes the expected number of points in an infinitesimally small area. The intensity parameter can also be used to determine the expected number of points in any region of the state-space \mathcal{S} . To denote this, we say that the expected number of points in region $B \in \mathcal{S}$ is $n(B) = A(B)\mu$ where $A(B)$ is the area of region B . In words, the expected number of points in B is simply the area of B multiplied by the intensity parameter. One property of the Poisson model is that if we divide the entire state-space into $k = 1, \dots, K$ disjunct regions, the counts $\mathbf{n}(\mathbf{B})$ are independent and identically distributed, (*i.i.d.*). This is one of the distinctions between the Poisson model and the binomial model, for which the counts $n(B_k)$ are not *i.i.d.* as we will explain shortly. This difference is also related to another distinction between the two models, namely that the binomial model conditions on the number of points to be simulated N ; whereas under the Poisson model N is random. Here is some simple **R** code to illustrate this point.

```
mu <- 4                                # intensity
Np <- rpois(1, mu)                     # Np is random
PPP <- cbind(runif(Np), runif(Np))     # Poisson point process

Nb <- 4                                # Nb is fixed
BPP <- cbind(runif(Nb), runif(Nb))     # Binomial point process
```

Note that in both models, the N points are independent of one another and distributed uniformly throughout \mathcal{S} . Thus, the intensity at any point $x \in \mathcal{S}$ is $\mu = 1/A(\mathcal{S})$ where $A(\mathcal{S})$ denotes the area of the state-space. In the **R** code above, the area of the state-space is 1 unit, and thus the intensity is $\mu = 1/1$.

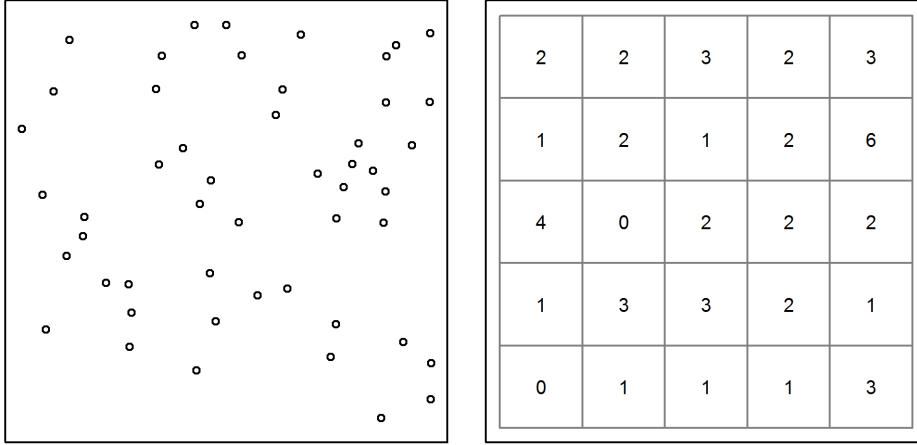


Figure 9.1: Homogeneous binomial point process with $N=50$ points represented in continuous and discrete space.

Although the Poisson model is typically described in terms of μ , the binomial model is not; rather, it is more common to consider a discrete state space, such as a grid with K pixels. Under the binomial model, the number of points in each region is $n(B_k) \sim \text{Bin}(N, p_k)$ where $p_k = A(B)/A(S)$, ie p_k is simply the fraction of the state-space area in B_k . This discrete space representation of the binomial point process is shown in Fig. 9.1. The state-space in this case is the unit square, and thus the probability of a point falling in each of the 25 disjunct regions is $p_k = 1/25$ and thus the expected counts are simply $\mathbb{E}(n(B_k)) = Np_k$. In the figure $N = 50$ and thus we would expect 2 points per pixel, which happens to be the empirical mean of the data in Fig. 9.1. Note also that these counts are not independent realizations from a binomial distribution since $\sum_k n(B_k) = N$. Instead, the model for the entire vector is $\mathbf{n}(\mathbf{B}) \sim \text{Multinomial}(N, \pi = (p_1, p_2, \dots, p_K))$ (?). The dependence among counts has virtually no practical consequence when the number of pixels is large. For example, if we have 100 pixels, the number of counts in one pixels tells you very little about the expected count in another pixel. However, if there are only 2 pixels, then clearly the number of points in one pixel tells you exactly how many will occur in the remaining pixel. To gain familiarity with the multinomial distribution and the discrete representation of space, use the `rmultinom` function in **R** to simulate counts similar to those shown in Fig. 9.1, for example using a command such as:

```

111 n.B_k <- rmultinom(1, size=50, prob=rep(1/25, 25))
112 matrix(n.B_k, 5, 5)

```

The discrete space representation of the binomial point process is of practical importance when fitting SCR models because spatial covariates are almost always represented in a discrete format, often called “rasters” in GIS-speak. In such cases, we often need to change our definition of the prior for an activity center from $s_i \sim \text{Uniform}(\mathcal{S})$ to $s_i \sim \text{Multinomial}(1, \pi)$. In the latter case, the activity center is simply defined as an integer representing pixel “id”. Note also that the multinomial distribution with an index of 1 (*i.e.* `size=1` in `rmultinom`) is referred to as the categorical distribution, which we will frequently use in the BUGS language.

9.2 Inhomogeneous binomial point process

As with the homogeneous model, the inhomogeneous binomial point process model is developed conditional on N . The primary distinction is that the uniform distribution is replaced with another distribution allowing for the intensity parameter to vary spatially. To arrive at this new distribution, define $\mu(x, \beta)$ to be a function of spatially-referenced covariates (β) available at all points of the state space. To be concise we will subsequently drop the vector of coefficients from our notation, and simply use $\mu(x)$. Since an intensity must be strictly positive, it is natural to model $\mu(x)$ using the log-link.

$$\log(\mu(x)) = \sum_{j=1}^J \beta_j v_j(x), \quad x \in \mathcal{S}$$

where β_j is the regression coefficient for covariate $v_j(x)$. To be clear, $v(x)$ is the value of any covariate, such as habitat type or elevation, at location x . This equation should look familiar because it is the standard linear model used in log-linear GLMs. Note, however, that we have no need for an intercept because it would be confounded with N . This should be intuitive since an intercept would represent the expected value of N when $\beta = 0$, but we already have a parameter in the model for expected abundance, namely $\mathbb{E}[N] = \psi M$. Thus an intercept would be redundant, and without it we are still able to achieve our goal of describing the distribution of N activity centers as a function of spatial covariates.

Now that we have a model of the intensity parameter $\mu(x)$, we need to develop the associated probability density function to use in place of the uniform prior. Remembering that the integral of a pdf must be unity, we can create a pdf by dividing $\mu(x)$ by a normalizing constant, which in this case is the integral of $\mu(x)$ evaluated over the entire state-space. **ANDY, is there a better justification for this?** The probability density function is therefore

$$f(x) = \frac{\mu(x)}{\int_{x \in \mathcal{S}} \mu(x) dx} \quad (9.1)$$

Substituting this distribution for the uniform prior allows us to fit inhomogeneous binomial point process models to spatial capture-recapture data. We can

also use this distribution to obtain the expected number of individuals in any given region. Specifically, the proportion of N expected to occur in any region B when heterogeneity in density is present is $p(B) = \int_B f(x) dx$. These are also the multinomial cell probabilities if the regions are disjoint and compose the entire state-space.

As a practical matter, note that the integral in the denominator of $f(x)$ is evaluated over space, and since we almost always regard space as two-dimensional, this is a two-dimensional integral that can be approximated using the methods discussed in refChXXX. These methods include Monte Carlo integration, Gaussian quadrature, etc... Alternatively, if our state-space covariates are in raster format, *i.e* they are in discrete space, the integral can be replaced with a sum over all pixels, which is much more efficient computationally.

We now have all the tools needed to fit inhomogeneous point process (IPP) models. Before doing so, we note that the IPP for the activity centers results in another IPP for the observation process, $\lambda(x)$. As a reminder, $\lambda(x)$ is the expected number of captures for a trap at point x . As was true for the homogeneous model, this intensity function is a product of the point process intensity and the encounter rate function, $\lambda(x) = \mu(x)g(x)$.

In the next section we walk through a few examples, building up from the simplest case where we actually observe the activity centers as though they were data. In the second example, we fit our new model to simulated data in which density is a function of a single continuous covariate. Example three shows an analysis in discrete space using both **secr** (?) and **JAGS** (?). In the last example, we model the intensity of activity centers for a real dataset collected on jaguars (*Panthera onca*) in Argentina.

9.3 Examples

9.3.1 Simulation and analysis of inhomogeneous point processes

In SCR models, the point process is not directly observed, but in other contexts it is. Examples include the locations of disease outbreaks or the locations of trees in a forest. Fitting inhomogeneous point process models to such data is straight-forward and illustrates the fundamental process that we will later embed in our MCMC algorithm used to fit SCR models.

Suppose we knew the locations of 100 animals' activity centers. To estimate the intensity surface $\mu(x)$ underlying these points, we need to derive the likelihood for our data under this model. Given the pdf $f(x)$ (Eq. 9.1) and assuming that the points are mutually independent of one another, we may write the likelihood as the product of R such terms, where $R = 100$ is the sample size in this case, *i.e* the observed number of activity centers.

$$\mathcal{L}(\beta|\mathbf{x}_i) = \prod_{i=1}^R f(x_i)$$

188 Having defined the likelihood we could choose a prior and obtain the posterior
 189 for β using Bayesian methods, or we can find the maximum likelihood estimates
 190 (MLEs) using standard numerical methods as is demonstrated below.

191 First, let's simulate some data. Simulating data under an inhomogeneous
 192 point process model is often accomplished using indirect methods such as rejection
 193 sampling. Rejection sampling proceeds by simulating data from a standard
 194 distribution and then accepting or rejecting each sample using probabilities
 195 defined by the distribution of interest. For more information, readers should
 196 consult an accessible text such as ?. In our example, we simulate from a uni-
 197 form distribution and then accept or reject using the (scaled) probability density
 198 function $f(x)$. Note that we first define a spatial covariate (elevation) that is a
 199 simple function of the spatial coordinates increasing from the southwest to the
 200 northeast of our state-space.²

201 The following **R** commands demonstrate the use of rejection sampling to sim-
 202 ulate an inhomogeneous point process for the covariate depicted in Fig. 9.3.1.
 203 The code uses the **cuhre** function in the **R2Cuba** package to integrate the inten-
 204 sity function over space (?).

```
205 # spatial covariate (with mean 0)
206 elev.fn <- function(x) x[1]+x[2]-1
207 # intensity function
208 mu <- function(x, beta) exp(beta*elev.fn(x=x))
209
210 # Simulate PP using rejection sampling
211 set.seed(300225)
212 N <- 100
213 count <- 1
214 s <- matrix(NA, N, 2)
215 beta <- 2 # parameter of interest
216 int.mu <- R2Cuba::cuhre(2, 1, mu, beta=beta)$value
217 elev.min <- elev.fn(c(0,0)) #elev.fn(cbind(0,0))
218 elev.max <- elev.fn(c(1,1)) #elev.fn(cbind(1,1))
219 Q <- max(c(exp(beta*elev.min) / int.mu, #2d(beta),
220           exp(beta*elev.max) / int.mu)) #2d(beta))
221 while(count <= 100) {
222   x.c <- runif(1, 0, 1); y.c <- runif(1, 0, 1)
223   s.cand <- c(x.c,y.c)
224   pr <- exp(beta*elev.fn(s.cand)) / int.mu #2d(beta)
225   if(runif(1) < pr/Q) {
226     s[count,] <- s.cand
227     count <- count+1
228   }
229 }
```

230 The simulated data are shown in Fig 9.3.1. High elevations are represented
 231 by light green and low elevations by dark green. The activity centers of one

²Such functional forms of covariates are rarely available, which is why continuous spatial covariates are more often measured on a discrete grid.

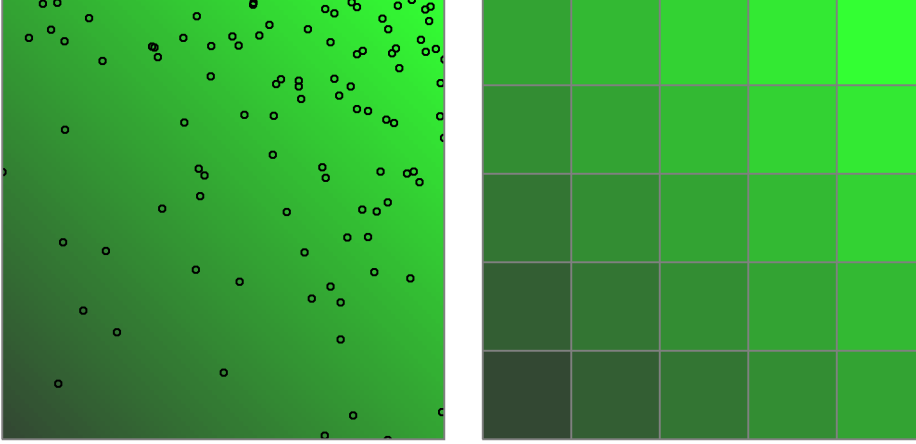


Figure 9.2: An example of a spatial covariate, say elevation, and a realization of a inhomogeneous binomial point process with $N=100$ and $\mu(x) = \exp(\beta \text{Elev})$ where $\beta = 2$.

hundred animals are shown as points, and it is clear that these simulated animals prefer the high elevations. Perhaps they are mountain goats. The underlying model describing this preference is $\log(\mu(x)) = \exp(\beta \times \text{Elevation}(x))$ where $\beta = 2$ is the parameter to be estimated and $\text{Elevation}(x)$ is a function of the coordinates at x , as displayed on the map.

Given these points, we will now estimate β by minimizing the negative-log-likelihood using R's `optim` function.

```

239 # Negative log-likelihood
240 nll <- function(beta) {
241   int.mu <- cuhre(2, 1, mu, beta=beta)$value
242   -sum(beta*elev.fn(s) - log(int.mu))
243 }
244 starting.value <- 0
245 fm <- optim(starting.value, nll, method="Brent",
246            lower=-5, upper=5, hessian=TRUE)
247 c(Est=fm$par, SE=sqrt(1/fm$hessian)) # estimates and SEs

```

Maximizing the likelihood took a small fraction of a second, and we obtained an estimate of $\hat{\beta} = 1.99$. We could plug in this estimate to our linear model at each point in the state-space to obtain the MLE for the intensity surface.

This example demonstrates that if we had the data we wish we had, *i.e.* if we knew the coordinates of the activity centers, we could easily estimate the parameters governing the underlying point process. Unfortunately, in SCR models, the activity centers cannot be directly observed, but spatial re-captures,

that is captures of individuals at multiple locations in space, provide us with the information needed to estimate these latent parameters.

9.3.2 Fitting inhomogeneous point process SCR models

Continuous space

One of the nice things about hierarchical models is that they allow us to break a problem up into a series of simple conditional relationships. Thus, we can simply add the methods described above into our existing MCMC algorithm to simulate the posteriors of β conditional on the simulated values of \mathbf{s}_i . To demonstrate, we will continue with the previous example. Specifically, we will overlay a grid of traps upon the map shown in Fig. 9.3.1. We will then simulate capture histories conditional upon the activity centers shown on the map. Then, we will attempt to estimate the activity center locations as though we did not know where they were, as is the case in real applications.

Here is some **R** code to simulate the encounter histories under a Poisson observation model, which would be appropriate if animals could be detected multiple times at a trap during a single occassion.

```
# Create trap locations
xsp <- seq(-0.8, 0.8, by=0.2)
len <- length(xsp)
X <- cbind(rep(xsp, each=len), rep(xsp, times=len))

# Simulate capture histories, and augment the data
ntraps <- nrow(X)
T <- 5
y <- array(NA, c(N, ntraps, T))

nz <- 50 # augmentation
M <- nz+nrow(y)
yz <- array(0, c(M, ntraps, T))

sigma <- 0.1 # half-normal scale parameter
lam0 <- 0.5 # basal encounter rate
lam <- matrix(NA, N, ntraps)

set.seed(5588)
for(i in 1:N) {
  for(j in 1:ntraps) {
    distSq <- (s[i,1]-X[j,1])^2 + (s[i,2] - X[j,2])^2
    lam[i,j] <- exp(-distSq/(2*sigma^2)) * lam0
    y[i,j,] <- rpois(T, lam[i,j])
  }
}
yz[1:nrow(y),,] <- y # Fill
```

Now that we have a simulated capture-recapture dataset y , and we have augmented it to create the new data object yz , we are ready to begin sampling

from the posteriors. A commented Gibbs sampler written in **R** is available in the accompanying **R** package **scrbook** (see `?scrIPP`). There are two small parts of the **R** code that distinguish it from previous code we have shown to fit homogeneous point processes. First, we need to update the parameter β conditional on all other parameters in the model. The code to do so is:

```

305 D1 <- cuhre(2, 1, mu, lower=c(xlims[1], ylims[1]),
306             upper=c(xlims[2], ylims[2]), beta=beta1)$value
307 beta1.cand <- rnorm(1, beta1, tune[3])
308 D1.cand <- cuhre(2, 1, mu, lower=c(xlims[1], ylims[1]),
309             upper=c(xlims[2], ylims[2]), beta=beta1.cand)$value
310 ll.beta1 <- sum( beta1*elev.fn.v(S) - log(D1) )
311 ll.beta1.cand <- sum( beta1.cand*elev.fn.v(S) - log(D1.cand) )
312 if(runif(1) < exp(ll.beta1.cand - ll.beta1) ) {
313     beta1<-beta1.cand
314 }
```

Next, we need to put the new prior on the activity centers:

```

316 #ln(prior), denominator is constant
317 prior.S <- beta1*cov(S[i,1], S[i,2]) # - log(D1)
318 prior.S.cand <- beta1*(Scand[1] + Scand[2]) # - log(D1)
319 if(runif(1)< exp((ll.S.cand+prior.S.cand) - (ll.S+prior.S))) {
320     S[i,] <- Scand
321     lam <- lam.cand
322     D[i,] <- dtmp
323 }
```

We can apply this modified sampler to our data using the code shown in the help file for **scrIPP**. We obtain posterior distributions summarized in Table 9.2. Mixing is good, and as usual, life is very nice when we are working with simulated data.

Fitting continuous space IPP models is somewhat difficult in **BUGS** because our prior $f(x)$ is not one of the available distributions that come with the software³ **secr** allows users to fit continuous space using polynomials of the x- and y- coordinates, but not for truly continuous covariates. However, these are not really important limitations because discrete space versions are straightforward, and virtually all spatial covariates are defined as such.

³It is possible, if somewhat cumbersome, to add new distributions in **BUGS**.

Table 9.1: Posterior summaries from inhomogeneous point proces model

	Mean	SD	2.5%	50%	97.5%
$\sigma = 0.10$	0.1026	0.0048	0.0935	0.1025	0.1123
$\lambda_0 = 0.50$	0.4419	0.0493	0.3496	0.4400	0.5390
$\psi = 0.66$	0.6826	0.0554	0.5762	0.6820	0.7923
$\beta = 2.00$	2.1601	0.3390	1.5193	2.1583	2.8043
$N = 100$	102.7696	6.2689	92.0000	102.0000	117.0000

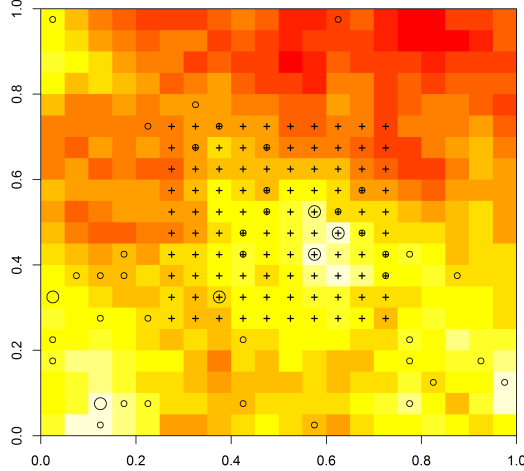


Figure 9.3: Simulated activity centers in discrete space. The spatial covariate, elevation, is highest in the higher areas. Density of activity centers (circles) increases with elevation. Trap locations are shown as crosses.

334 Discrete space

335 To fit discrete space models, we follow the same steps as outlined in Chapter
 336 XXX—we define s_i as pixel ID, and we use the categorical distribution as a
 337 prior. A good example of this is in `+citeKery capricaille`. Here we present
 338 an analysis of the simulated data shown in the right panel of Fig. 9.3.1. The
 339 spatial covariate, let's call it elevation again, was simulated from a kriging type
 340 of model as shown on the help page `ch9simData` in `scrbook`. The points are
 341 the number of activity centers in each pixel, generated from a single realization
 342 of the IPP $\mu(x) = 2elev$.

343 The **BUGS** code to fit an IPP model to these data is shown in the following
 344 panel.

```

345 model{
346   sigma ~ dunif(0, 1)
347   lam0 ~ dunif(0, 5)
348   beta ~ dnorm(0,0.1)
349   psi ~ dbeta(1,1)
350
351   for(j in 1:nPix) {
352     theta[j] <- exp(beta*elevation[j])
353     probs[j] <- theta[j]/sum(theta[])
354   }
355
```

```

356 for(i in 1:M) {
357   w[i] ~ dbern(psi)
358   s[i] ~ dcat(probs[])
359   x0g[i] <- Sgrid[s[i],1]
360   y0g[i] <- Sgrid[s[i],2]
361   for(j in 1:ntraps) {
362     dist[i,j] <- sqrt(pow(x0g[i]-grid[j,1],2) + pow(y0g[i]-grid[j,2],2))
363     lambda[i,j] <- lam0*exp(-dist[i,j]*dist[i,j]/(2*sigma*sigma)) * w[i]
364     y[i,j] ~ dpois(lambda[i,j])
365   }
366 }
367
368 N <- sum(w[])
369 Density <- N/1 # unit square
370 }

```

371 This model can also be fit in **secr**, which refers to the pixel locations as
372 a “mask”. **R** code to fit the models using **secr** and **JAGS** is available in
373 **scrbook**, see `help(ch9secrYjags)`. Results of the comparison are shown in
374 Table ?? and are very similar as expected.

375 Density surface maps can be created for fun, and of course to inform man-
376 agement decisions. [describe how to do this]

377 9.3.3 The jaguar data

378 Estimating density of large felines has been a priority for many conservation
379 organizations, but no robust methodologies existed before the advent of SCR.
380 Distance sampling is not feasible for such rare and cryptic species, and tradi-
381 tional capture-recapture methods yield estimates that are highly sensitive to the
382 subjective choice of the effective survey area. In this example, we demonstrate
383 how readily density can be estimated for a globally imperilled species using
384 SCR. Furthermore, we show how inhomogeneous point process models can be
385 used to test important hypotheses regarding the factors affecting density.

386 [describe study]

Table 9.2: Comparison of **secr** and **JAGS** results

Software	Par	Est.	SD	lower	upper
secr	N	49.2803	5.7535	41.0087	64.3879
	β	2.1772	0.5628	1.0741	3.2804
	λ_0	0.9203	0.0764	0.7824	1.0825
	σ	0.0990	0.0038	0.0918	0.1068
JAGS	N	48.2072	5.4053	39.0000	60.0000
	β	2.1026	0.5323	1.0889	3.1506
	λ_0	0.9328	0.0766	0.7898	1.0921
	σ	0.1004	0.0041	0.0929	0.1089

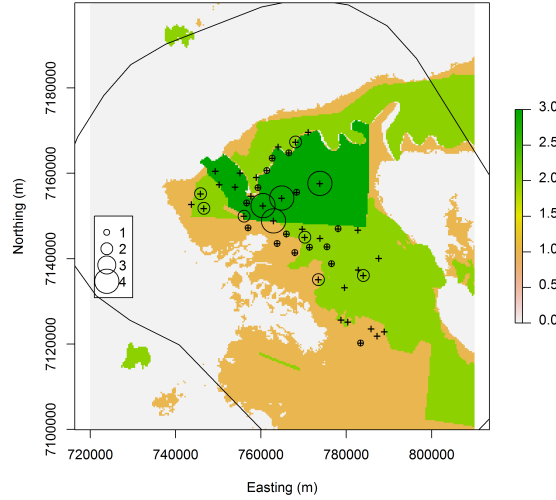


Figure 9.4: Jaguar detections

387 A few aspects of this design are noteworthy. First, the dimensions and
 388 configuration of the trap array differed among the regions of the trap array.
 389 This fact alone could explain variation in the number of animals exposed to
 390 sampling, which would have no biological meaning. Furthermore, the area of
 391 inference is an irregular polygon that was not sampled uniformly. Only by
 392 estimating density can we hope to extrapolate our estimates from the sampled
 393 region to get what we are after. In this case, this is readily accomplished since
 394 the entire state-space can be classified as one of the 3 levels of protection from
 395 poaching. Of course, it general it is always preferable to sample more uniformly
 396 throughout the area of interest in case some unmeasured covariate biases the
 397 extrapolation.

398 To assess the influence of poaching on jaguar density, we considered 2 metrics
 399 of poaching pressure, one political and one continuous measure of accessibility
 400 (Fig xxx).

401 9.4 Summary

402 When state-space covariates are available, we can model density by replacing
 403 the uniform prior on the activity centers with a prior based on a normalized log-
 404 linear function of covariates. This yields a model of the inhomogeneous point
 405 process describing the location of activity centers, which can be used to test
 406 hypotheses about covariates affecting density. In rare cases, these covariates
 407 are truly continuous in the sense that they are defined as a function of space.

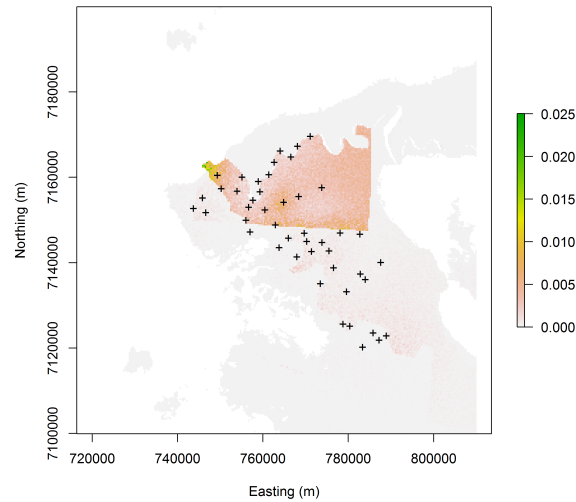


Figure 9.5: Estimated density surface for the jaguar dataset

More often, covariates are represented on rasters, which simplifies the analysis. Fitting these models can be accomplished using **BUGS**, **secr**, or the custom **R** code presented in this chapter and found in the package **scrbook**.

All the examples in this section included a single state-space covariate, but this was for simplicity only. Including multiple covariates poses no additional challenges. Likewise, additional model structure such sex-specific encounter rate parameters or behavioral responses can be accomodated.

9.5 Other ideas

Should have some discussion on some ideas for building flexible models. Might be cool to use the Ickstadt/Wolpert as a model for the inhomogeneous point process. Dont have to do it, just mention it. Also some kind of a spline model or similar.

420 Chapter 10

421 Inhomogeneous Point 422 Process

423 Chapter 11

424 Open models

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