

Assignment 8

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Papoulis chap 4 Ex 4.7

TABLE OF CONTENTS

- 1 Question
- 2 Solution
- 3 Graph
- 4 Codes

Problem

Q) The set of nonnegative real numbers $\{P_i\}$ satisfy $P\{x = X_i\} = P_i$ for all i . and $\sum_{i=1}^{\infty} P_i = 1$. Determine $F(x)$.

Solution

For $x_i \leq x < x_i + 1$, We have

$$\{x\{\xi\} \leq x\} = \bigcup_{x_k \leq x} \{x\{\xi\} = x\} = \bigcup_{k=1}^i \{x\{\xi\} = x\}$$

$$\text{and hence } F(x) = P\{x\{\xi\} \leq x\} = \sum_{k=1}^i p_k \quad x_i \leq x < x_i + 1$$

Here $F(x)$ is a staircase function with an infinite number of steps and the i^{th} step size equals $P_i = 1, 2, 3, 4, \dots, \infty$

see the figure (1)

Staircase function Graph

The $F(x)$ graph is:

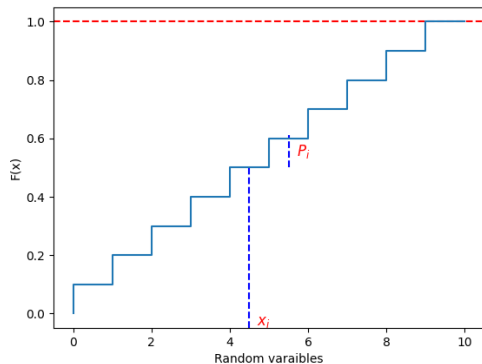


Figure: Staircase function

CODES

Python

Download python code from - Python

Beamer

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