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Assignment 3

AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

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Abstract—This document contains the solution for Assignment 9 (papoulis question-4.13)

QUESTION 4.13: A fair coin is tossed three times and the random variable x equals the total number of heads. Find and sketch $F_x(x)$ and $f_x(x)$. **Solution**: let x be a random variable which maps to 1 when coin denotes head and 0 when it denotes tail. probability of getting r heads is $\Pr(X = k) = \sum_{i=1}^{k} f(x_i) e^{-ix}$

TABLE I EVENTS AND DESCRIPTION

$$\binom{n}{k} \times p^k \times (1-p)^k$$
 so

$$\Pr(X = 0) = {3 \choose 0} \times \frac{1}{2}^0 \times (1 - \frac{1}{2})^3 = \frac{1}{8}$$
 (1)

$$\Pr\left(X=1\right) = \binom{3}{1} \times \frac{1}{2}^{1} \times \left(1 - \frac{1}{2}\right)^{2} = \frac{3}{8} \qquad (2)$$

$$\Pr(X=2) = {3 \choose 2} \times \frac{1}{2}^2 \times (1 - \frac{1}{2})^1 = \frac{3}{8}$$
 (3)

$$\Pr(X=3) = {3 \choose 3} \times \frac{1}{2} \times (1 - \frac{1}{2})^0 = \frac{1}{8}$$
 (4)

the $F_x(x)$ i.e PMF is given by :

$$\begin{cases} 0, & k < 0 \\ \frac{1}{8}, & k = 0 \text{ or } 3 \\ \frac{3}{8}, & k = 1 \text{ or } 2 \end{cases}$$
 (5)

the $f_x(x)$ CDF is given by :

$$\begin{cases}
0, & k < 0 \\
\frac{1}{8}, & k = 1 \\
\frac{1}{2}, & k = 2 \\
\frac{7}{8}, & k = 3 \\
1, & k > 3
\end{cases}$$
(6)

