

Assignment 3

JARUPULA SAI KUMAR (CS21BTECH11023)

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Outline

1 Question

2 Solution

QUESTION 4.13 : A fair coin is tossed three times and the random variable x equals the total number of heads. Find and sketch $F_x(x)$ and $f_x(x)$. **Solution :** let x be a random variable which maps to 1 when coin denotes head and 0 when it denotes tail.

Table 1: Events and Description

probability of getting r heads is $\Pr(X = k) = \binom{n}{k} \times p^k \times (1 - p)^{n-k}$ so

$$\Pr(X = 0) = \binom{3}{0} \times \frac{1}{2}^0 \times \left(1 - \frac{1}{2}\right)^3 = \frac{1}{8} \quad (1)$$

$$\Pr(X = 1) = \binom{3}{1} \times \frac{1}{2}^1 \times \left(1 - \frac{1}{2}\right)^2 = \frac{3}{8} \quad (2)$$

$$\Pr(X = 2) = \binom{3}{2} \times \frac{1}{2}^2 \times \left(1 - \frac{1}{2}\right)^1 = \frac{3}{8} \quad (3)$$

$$\Pr(X = 3) = \binom{3}{3} \times \frac{1}{2}^3 \times \left(1 - \frac{1}{2}\right)^0 = \frac{1}{8} \quad (4)$$

the $F_x(x)$ i.e PMF is given by :

$$\begin{cases} 0, & k < 0 \\ \frac{1}{8}, & k = 0 \text{ or } 3 \\ \frac{3}{8}, & k = 1 \text{ or } 2 \end{cases} \quad (5)$$

the $f_x(x)$ CDF is given by :

$$\begin{cases} 0, & k < 0 \\ \frac{1}{8}, & k = 1 \\ \frac{1}{2}, & k = 2 \\ \frac{7}{8}, & k = 3 \\ 1, & k > 3 \end{cases} \quad (6)$$

