Sequence models

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This document contains my personal notes on sequence models.

1. Embeddings

Embeddings are tensors. You interact with that tensor by indexing into it. It is often used to store encodings of collections of words. For example:

```
>>> nn.Embedding(vocab_sz, n_hidden)
```

creates a set of vocab_sz tensors, each of size n_hidden.

A common thing to do is to something like:

```
>>> embedding = nn.Embedding(10, 3)
>>> input = torch.LongTensor([[1,2,4,5],[4,3,2,9]])
>>> embedding(input)

tensor([[[-0.0251, -1.6902,  0.7172],
         [-0.6431,  0.0748,  0.6969],
         [ 1.4970,  1.3448, -0.9685],
         [-0.3677, -2.7265, -0.1685]],

        [[ 1.4970,  1.3448, -0.9685],
         [ 0.4362, -0.4004,  0.9400],
         [-0.6431,  0.0748,  0.6969],
         [ 0.9124, -2.3616,  1.1151]]])
```

so you can see that the input is [sentence1, sentence2], where sentence 1 consists of words [1,2,4,5]. As an output, we get the corresponding 3-vectors for each word. So the output is:

```
[[[embedding_word_1,    # length 3 vector
   embedding_word_2,
   embedding_word_4,
   embedding_word_5],

  [embedding_word_4,
   embedding_word_3,
   embedding_word_2,
   embedding_word_9]
]]
```

2. Linear layer

Applies a linear transformation to the incoming data: $y = xA^T + b$

```
>>> m = nn.Linear(20, 30)
>>> input = torch.randn(128, 20)
>>> output = m(input)
>>> print(output.size())
torch.Size([128, 30])
```

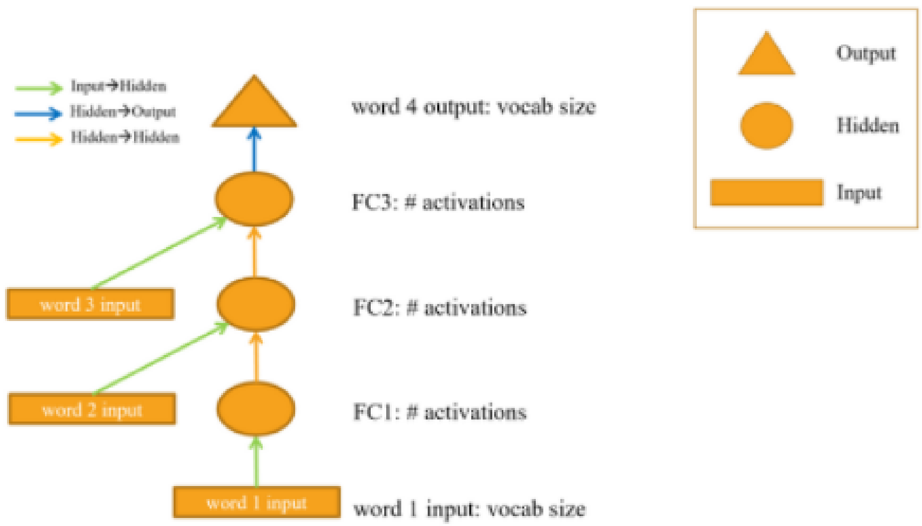

Figure 1. Graphical representation of RNN

3. Recurrent neural network

Torch, by default, applies a multi-layer Elman RNN. This is defined as applying the following function to each element of the input sequence

$$h_t = \sigma_h(W_h x_t + U_h h_{t-1} + b_h) \tag{3.1}$$
$$y_t = \sigma_y(W_y h_t + b_y) \tag{3.2}$$

where x_t is an input vector, h_t is a hidden layer vector, y_t is an output vector, W, U, b are parameter matrices and vector, σ_h, σ_y are activation functions. Note that we don't actually retain the hidden state between lines – we throw it away after every complete training example (a line). We will typically initialize the hidden state to be $h_{t=0} = 0$. Within a particular training instance, on a particular line, we may have different maximum values of $t = T$.

For example, in word classification, where we construct a character-level RNN, in each training loop we will

1. Get an input and target tensor
2. Create a zeroed initial hidden state
3. Read each letter in and:
   - Keep hidden state for next letter
   - Feed the previous hidden state h_{t-1} in with the current input x_t
4. Compare output at the end of the RNN loop to the target
5. Back-propagate

Then return the output and loss.

Bahdanau *et al.* (2014)

References

Bahdanau, D., K. Cho, and Y. Bengio, 2014 Neural machine translation by jointly learning to align and translate. arXiv preprint arXiv:1409.0473 .