

# Data Analytics

## SET10109

Graphs and Time

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Course Content: Natalie Kerracher

# Overview

- What is a graph?
- Some features of graph data
- Different ways to visually represent graphs and trees: considerations, advantages, disadvantages
- Visual approaches for the temporal dimension

# Reading

## Required

- Munzner, T. (2014). *Visualization Analysis and Design*.  
Chapter 9 – Arrange Networks and Trees

## Recommended

- Von Landesberger, T., Kuijper, A., Schreck, T., Kohlhammer, J., van Wijk, J. J., Fekete, J.-D., & Fellner, D. W. (2011). Visual Analysis of Large Graphs: State-of-the-Art and Future Research Challenges. *Computer Graphics Forum*, 30(6), 1719–1749. doi:10.1111/j.1467-8659.2011.01898.x
- Aigner, W., Miksch, S., Muller, W., Schumann, H., & Tominski, C. (2007). Visualizing time-oriented data—A systematic view. *Computers & Graphics*, 31(3), 401-409. doi:10.1016/j.cag.2007.01.030

# What is a graph?

Graph  $G = (V, E)$

- $V$  = a set of vertices (nodes)
- $E$  = a set of edges (links)

Useful terminology:

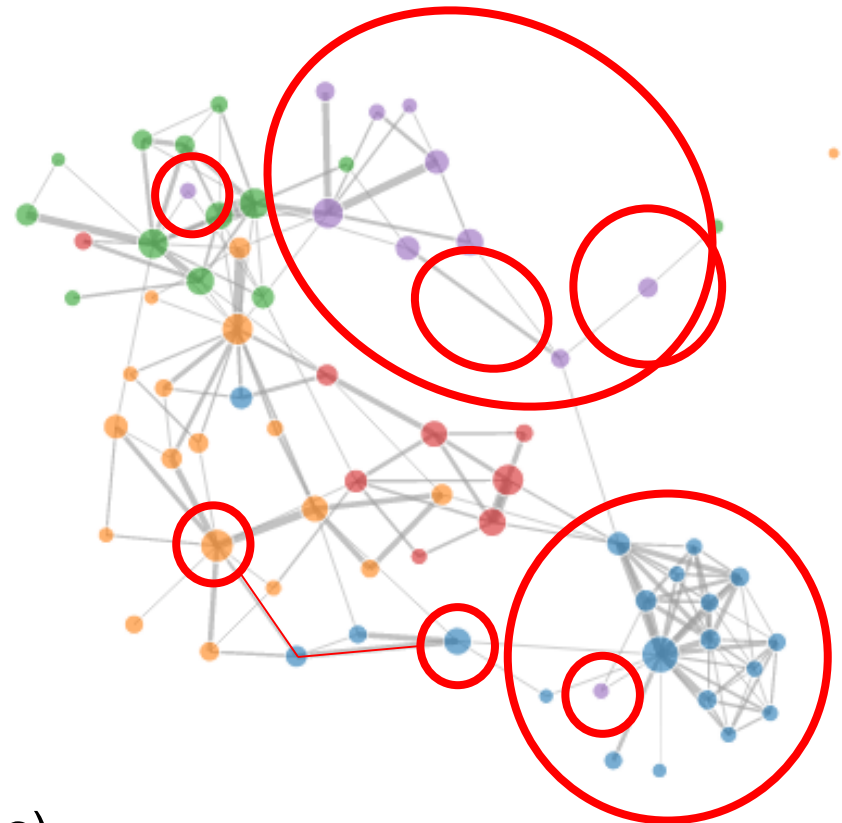
Clusters: based on connectivity

Groups: based on attributes

Paths: between two nodes

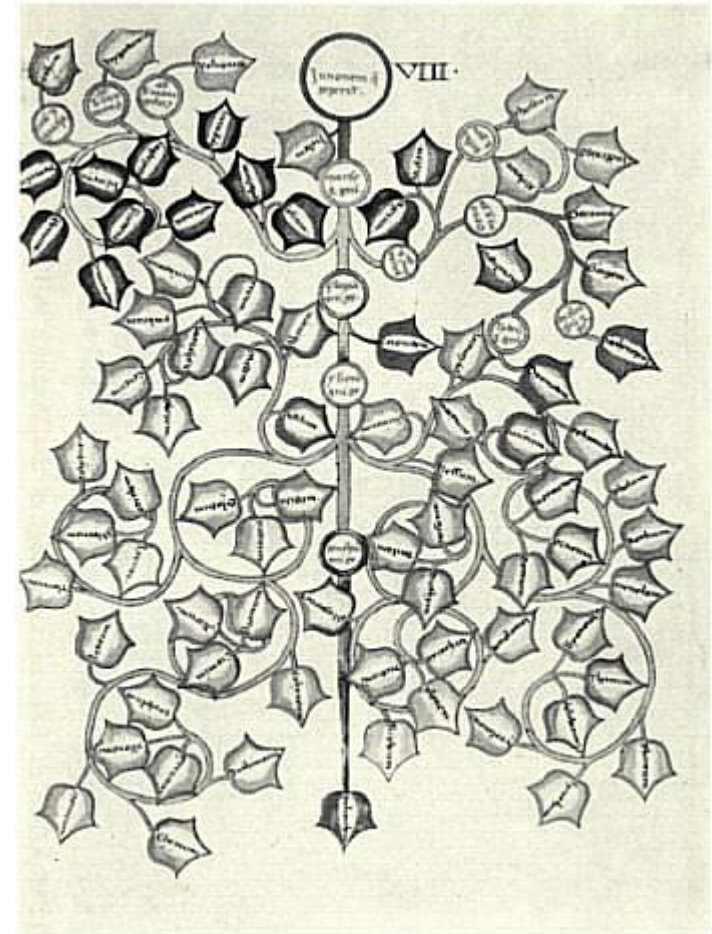
Attributes on nodes

Weightings on edges (weighted graphs)



# Graph Drawing: a Long History

- Graph drawing has been around for a *long* time ('Mill games', ancient Egypt)
- Euler (1707-1783) credited with originating graph theory in 1763
  - Did not make significant use of graph visualisation
- Wasn't until mid 1800s that graph drawings began to appear
  - E.g. illustrations in mathematical papers



Hand drawn family tree from the middle ages.  
(Kruja et al, 2002, Figure 2)



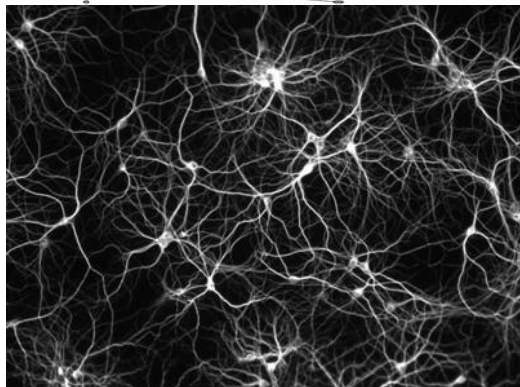
# Sources of graph data

- Social networks
  - Organisational hierarchies
  - Family trees
  - Terrorist networks
  - Social media
- Computer networks
- Transportation networks
- Software systems
- Biological networks
- ...

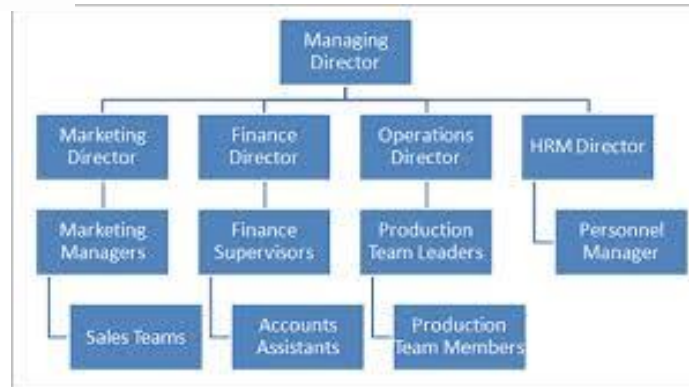


Paul Butler Facebook visualisation (2010)  
Source <http://on.fb.me/hy6dmb>

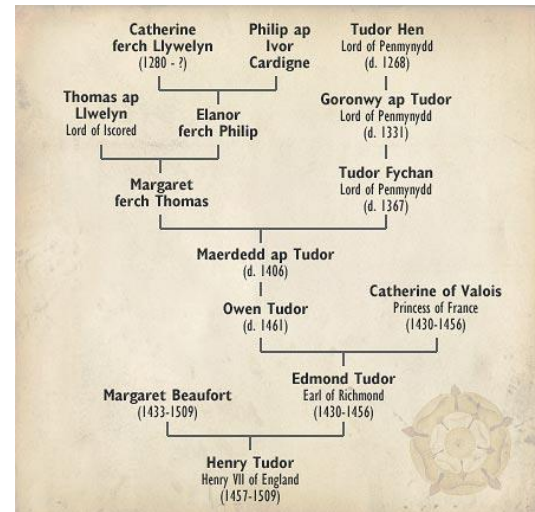
IIS call graph. Source: <http://rixstep.com/1/1/20070206.00.shtml>



Dissociated culture of rat hippocampal neurons  
Paul De Koninck Laboratory - Universite Laval (2005)

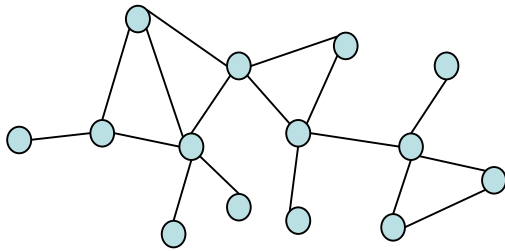


Organisation hierarchy source: [www.tutor2u.net](http://www.tutor2u.net)

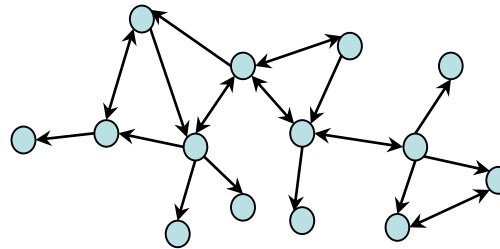


source <http://www.bbc.co.uk/wales/history>

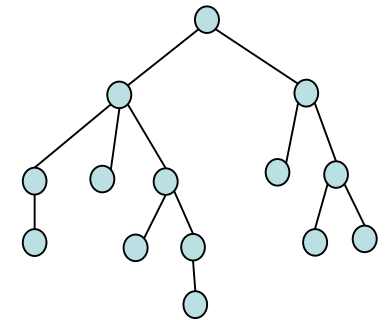
# Graph structure: some considerations



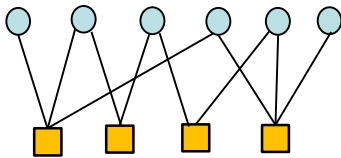
undirected graph



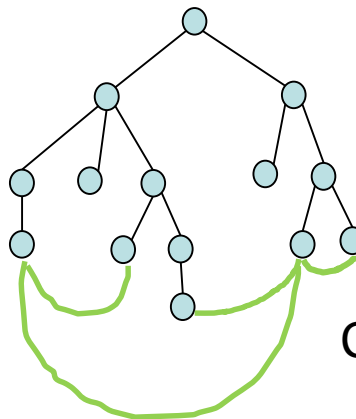
directed graph



Tree  
(hierarchical structure)



bipartite graph



Compound graph

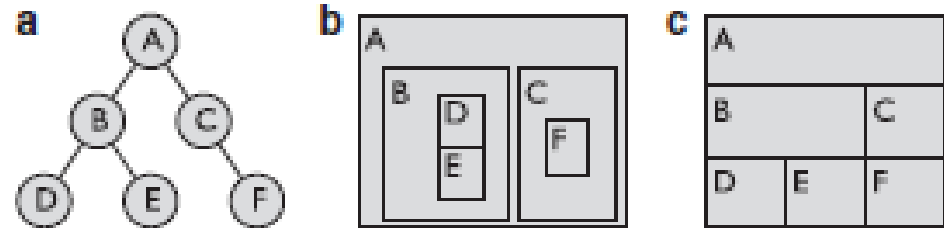
# How can we visually represent graph data?

Problem: show connections, and thus relationships, clearly

Common relational layouts:

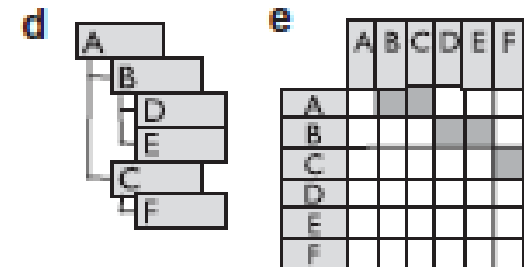
- Network (Graph) Data

- Node-link diagrams
- Matrix



- Tree / Hierarchy Data

- Node-link diagrams
- Adjacency layouts
- Space-filling (treemaps, icicle plots)



Graham & Kennedy (2010), Figure 3

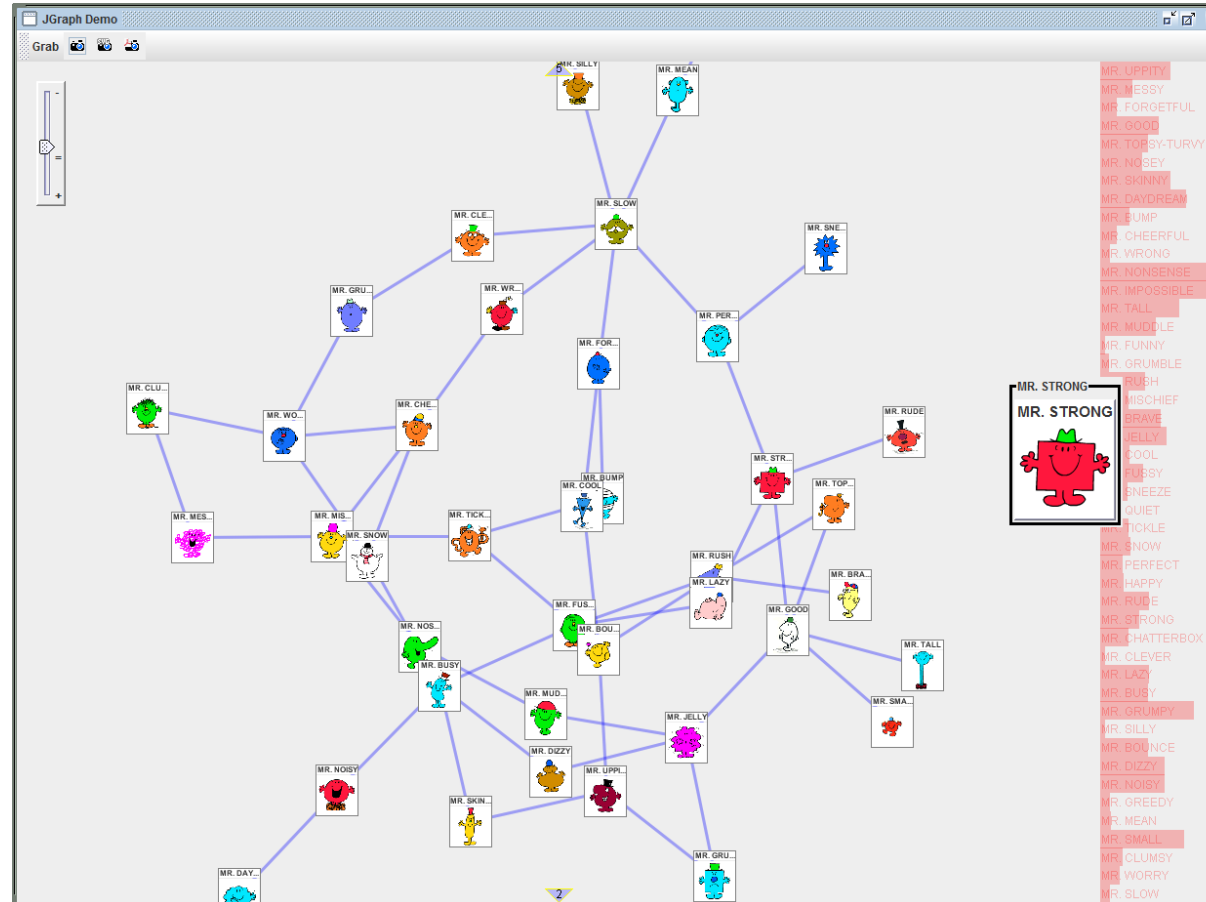
- Useful resource: Manuel Lima's website

<http://www.visualcomplexity.com/vc/>



# Network – Node-Link

- The most common form of showing a network is with a node-link diagram
- Nodes represent entities, edges represent the relationships between them
- Readily understood by viewers

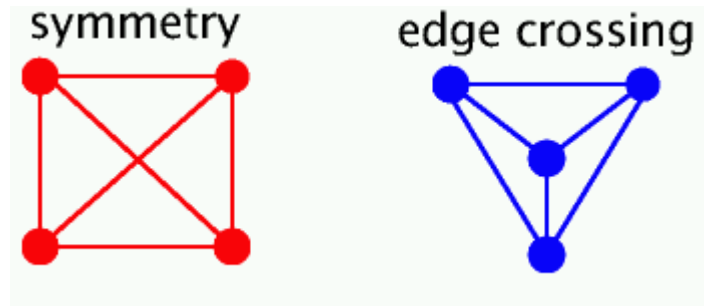
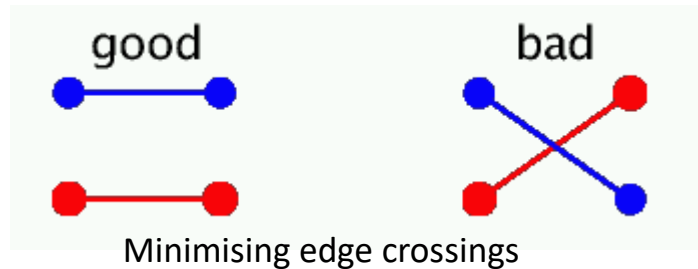
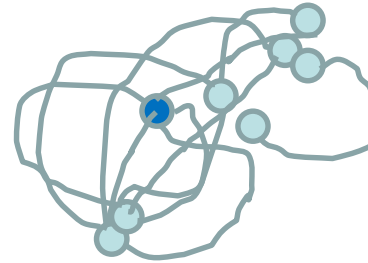


# Graph Drawing Issues

Key Challenge: graph layout

Optimise readability

Graph aesthetics:



Mutually incompatible criteria

From Munzner (2006)

Difficulties:

- Some criteria mutually incompatible

- Computation time and complexity (most criteria individually NP-hard)



# Summary of aesthetic considerations

## Node Metrics

Cluster similar nodes

Distribute nodes evenly

Keep nodes apart from edges

Maximize node orthogonality

Nodes should not overlap  
(except for nested nodes)

## Edge Metrics

Minimize edge crossings

Keep edge lengths uniform

Minimize edge length (total and  
maximum)

Minimize edge bends

Keep edge bends uniform (an-  
gle/position)

Maximize edge orthogonality

Maximize minimum edge an-  
gles

## Overall Layout Metrics

Maximize consistent flow di-  
rection

Keep correct aspect ratio

Minimize area

Maximize convex faces

Maximize global symmetry

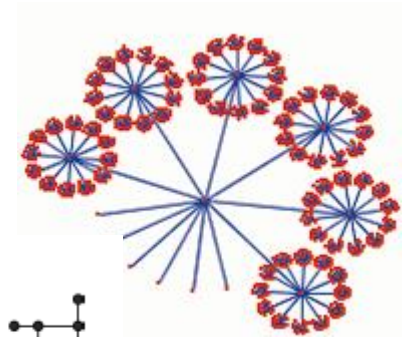
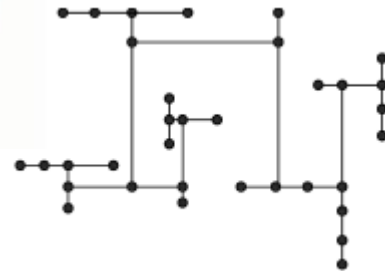
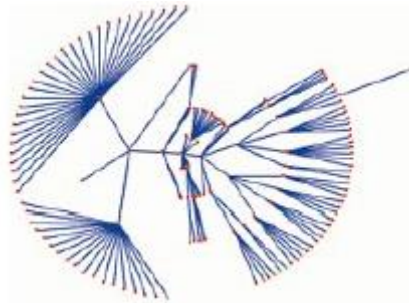
Maximize local symmetry

# Layout algorithms

A key challenge for graph drawing is the computation of the layout of nodes and edges

Categories of layout algorithms (classified according to type of node placement (von Landesberger et al. (2011)):

- Force directed
- Constraint-based
- Multiscale approaches
- Layered layouts
- Non-standard layouts



Images: Herman et al (2000)

Force directed algorithms are common: each node is pulled together into a final layout by its edges (see e.g. <http://bl.ocks.org/mbostock/4062045>)

See von Landesberger et al (2011) or Herman et al (2000) as a starting point if you're interested in layout algorithms...



**Exercise: draw the following graph, trying to follow the principles of a “good layout”**

9 nodes labelled 1-9

12 edges:

1-2    2-5    6-8

1-3    3-6    6-9

1-4    4-7    7-9

2-1    5-8    8-5

**Exercise: draw the following graph, trying to follow the principles of a “good layout”**

9 nodes labelled 1-9

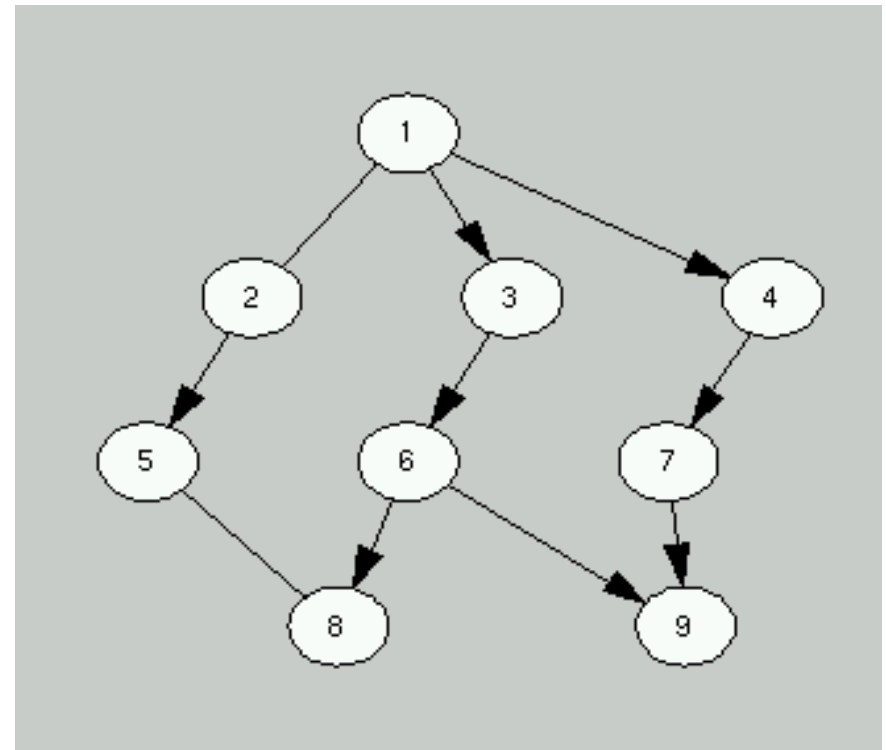
12 edges:

1-2    2-5    6-8

1-3    3-6    6-9

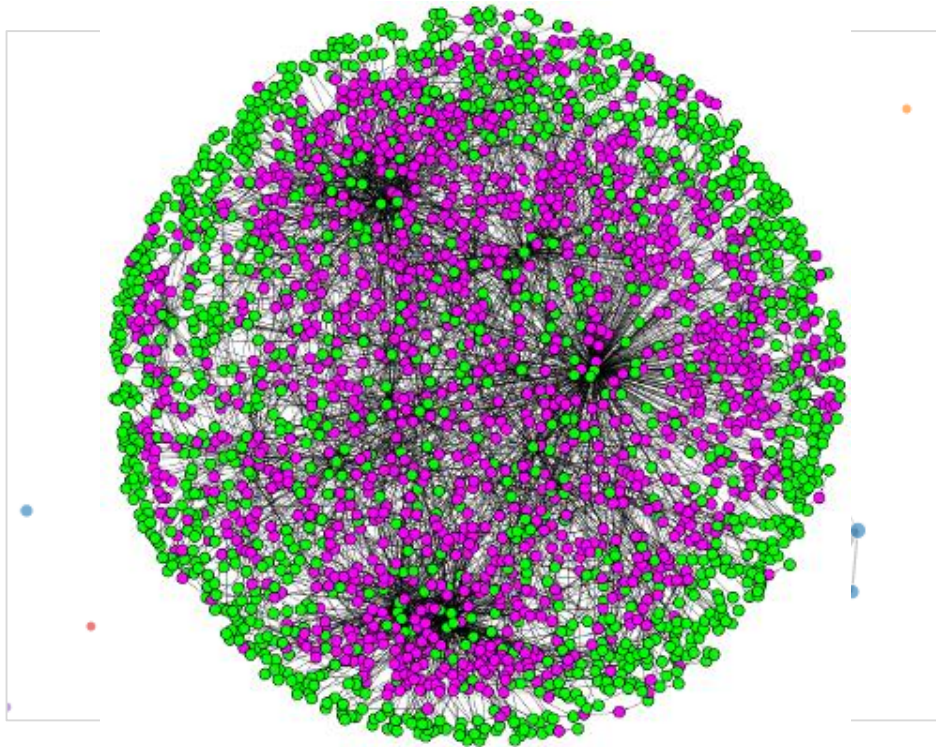
1-4    4-7    7-9

2-1    5-8    8-5





# Graph Drawing Issues: Scale



Node-link diagram  
“Hairball”

<http://eagereyes.org/techniques/graphs-hairball>

Problems of scale:

Computation

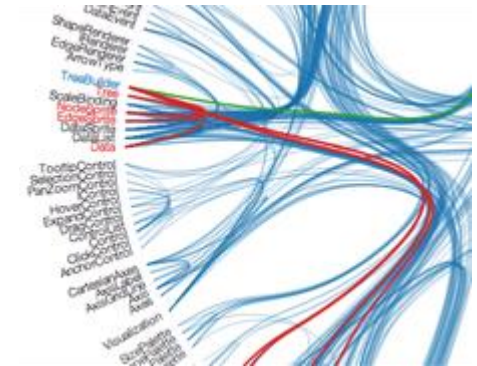
- Computationally expensive
- Time to render

Readability:

- Leads to occlusion
- Makes interaction difficult
- Run out of screen space to draw nodes

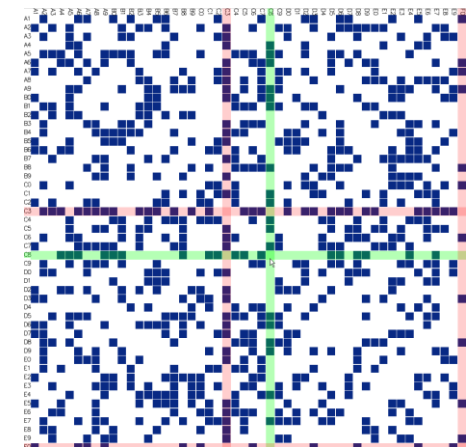
# Overcoming issues of scale

- Parallel processing on the GPU (for faster computation)
- Larger screen
- Reduction techniques
  - Edge bundling
  - Node bundling (clustering)
- Interaction techniques
- Use an alternative representation e.g. matrix



Edge bundling + interaction

<http://mbostock.github.io/d3/talk/20111116/bundle.html>

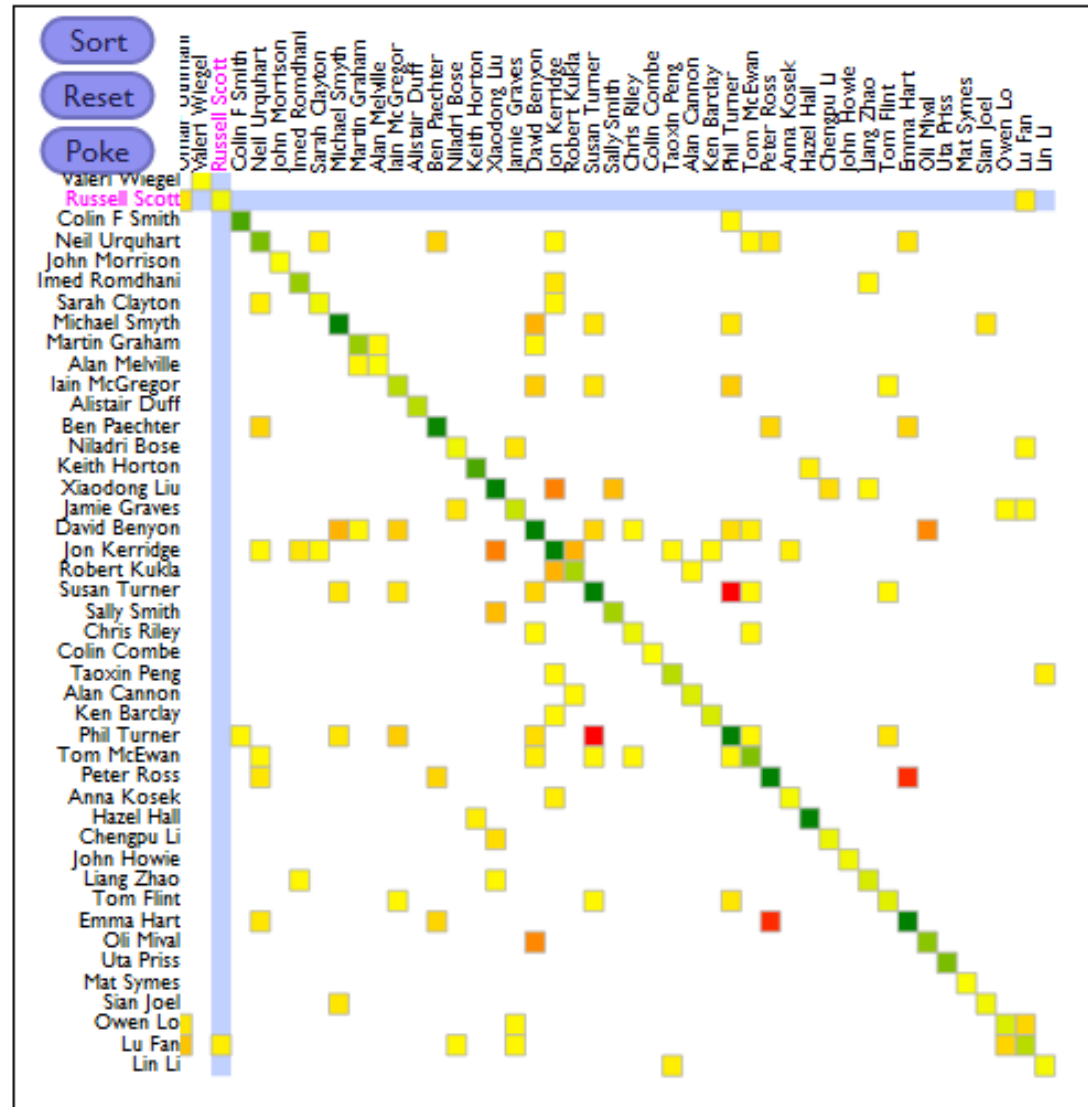


Matrix (Ghoniem et al. 2005)

# Network – Matrix



- Entities (nodes) arranged on x/y axes
- Connections shown as marks between rows and columns



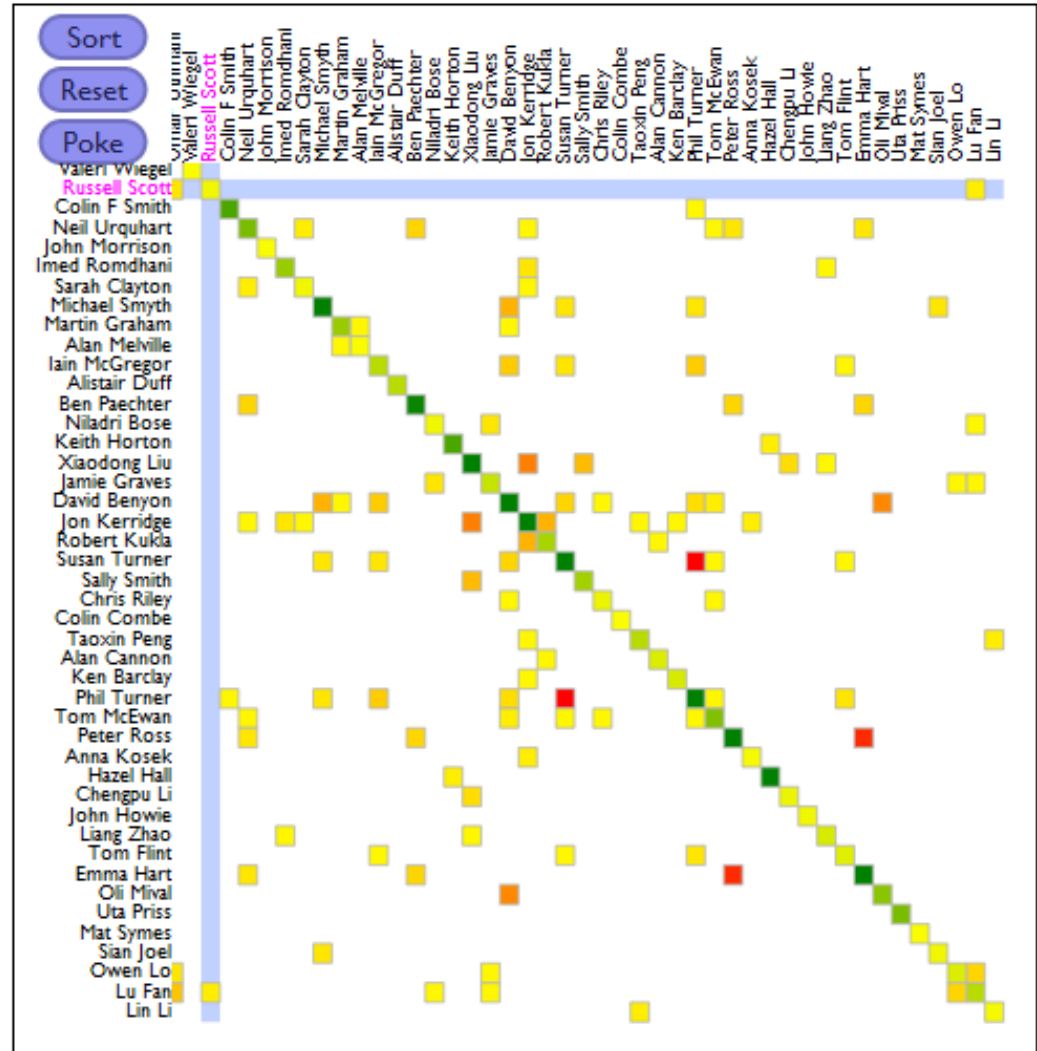
# Network – Matrix

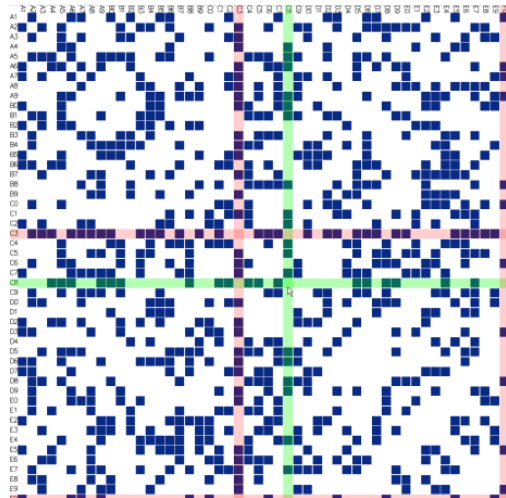
## Advantages:

- Scale well
- No clutter, easy to calculate layout
- Outperform node-links on most tasks, where graph > 20 nodes (Ghoniem et al., 2005)

## Disadvantages:

- Not intuitive
- Hard to follow paths
- Often sparse (space issues)
- Require ordering to show clusters



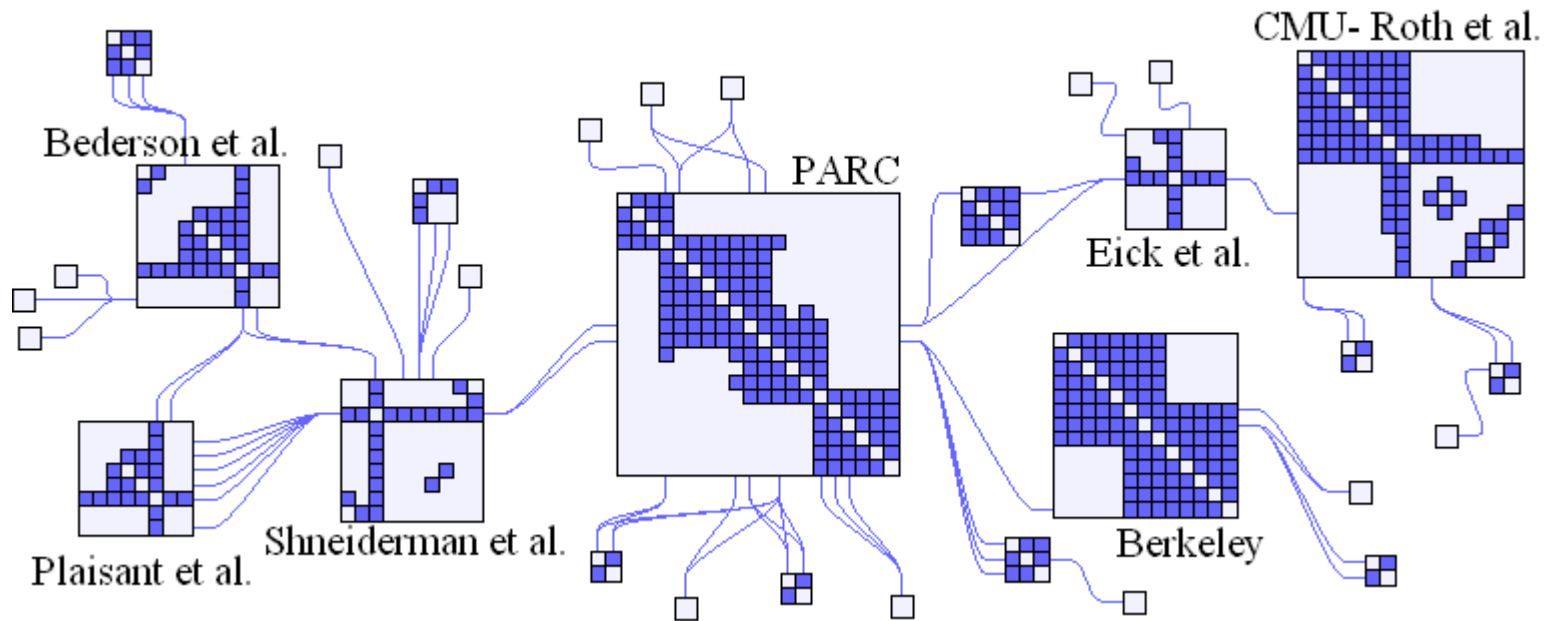


- + Intuitive
- + Good for path-finding tasks
- + Good for showing structure in sparse graphs
- Do not scale well (readability, computation)

- + Ability to scale as no edges, so no path-crossing
- + Outperform node links on most tasks
- Less intuitive
- Less good for sparse graphs
- Not good for path finding tasks

Require ordering to show clusters

# Node-link/Matrix Hybrid



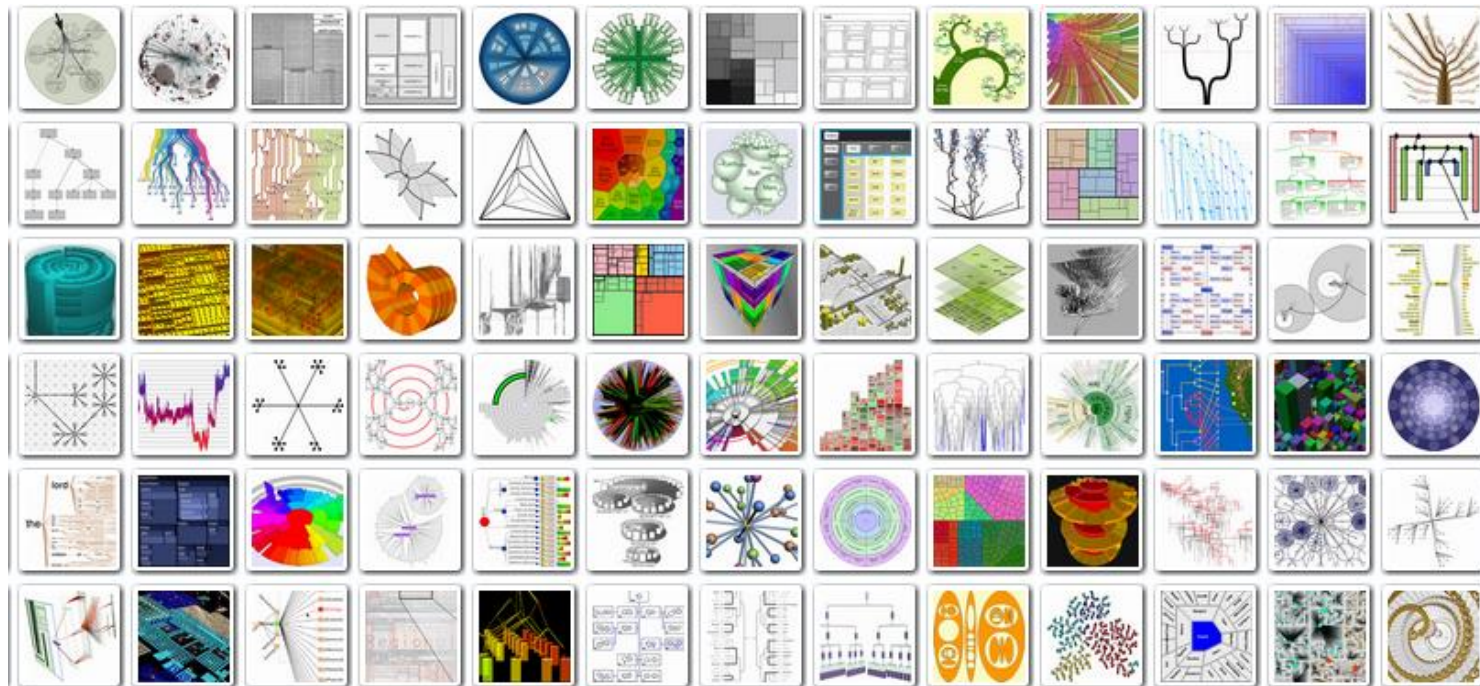
NodeTrix: Matrix/node-link hybrid (small world networks)  
(Henry, Fekete, & McGuffin, 2007)



# **VISUAL REPRESENTATIONS OF HIERARCHICAL DATA (TREES)**

# Tree visualisation

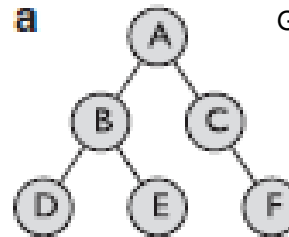
- Excellent resource: [www.treevis.net](http://www.treevis.net)
- Can search based on ‘three design axes’:
  - Dimensionality (2D, 3D, or hybrid)
  - Edge representation (explicit, implicit, or hybrid)
  - Node alignment (radial, axis-parallel, or free)



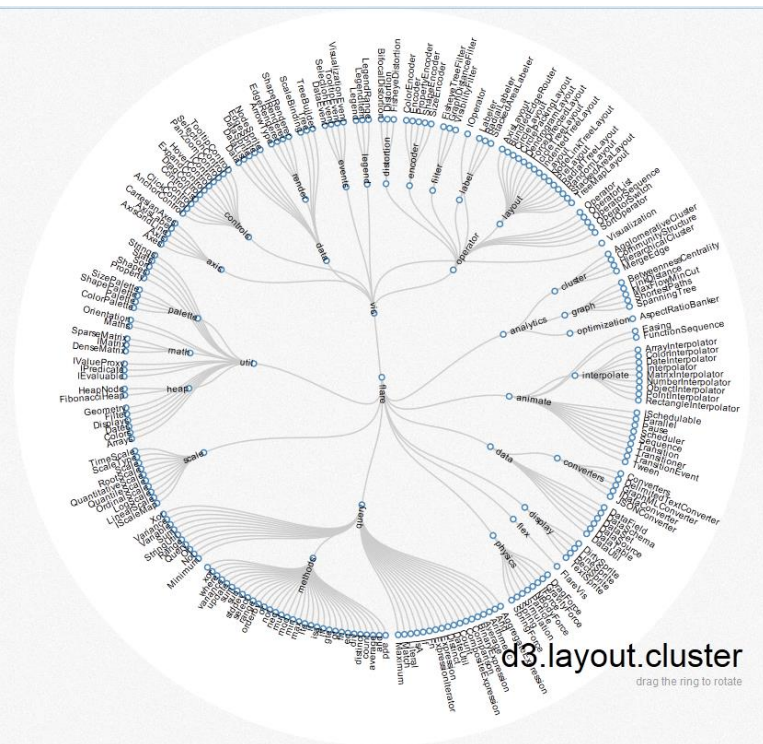
# Tree – Node-Link

- Understandable but not very space efficient

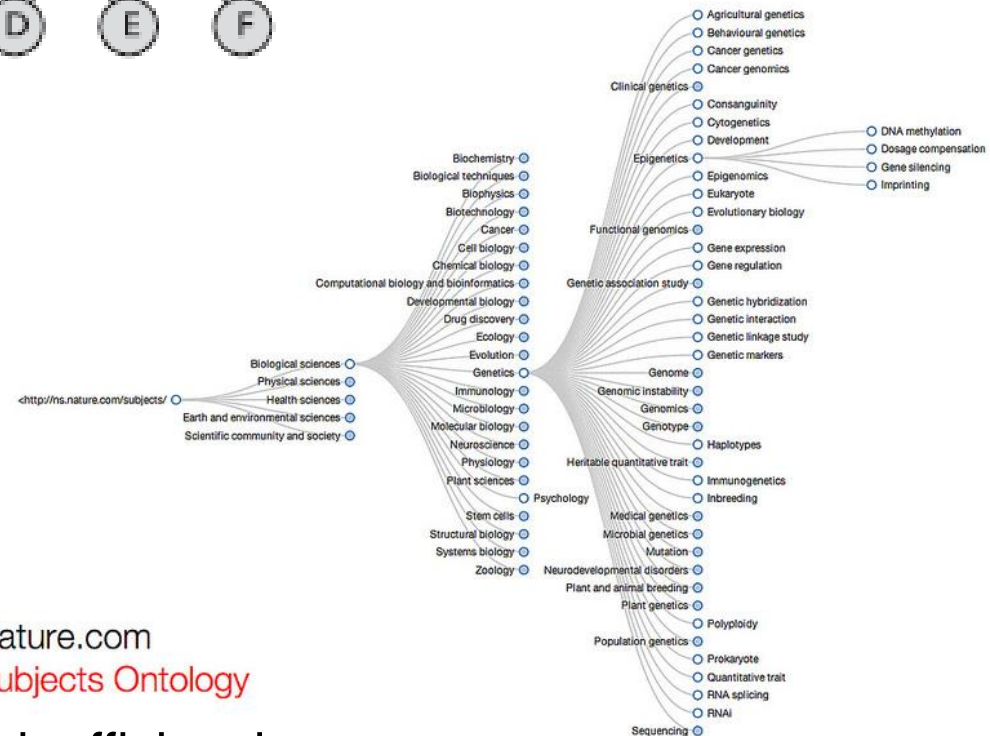
a



Graham & Kennedy (2010)



Nature.com  
Subjects Ontology



- Interaction to help overcome space inefficiencies e.g.

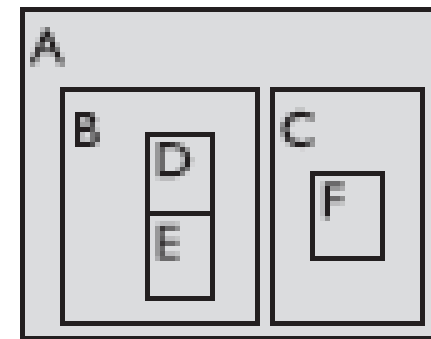
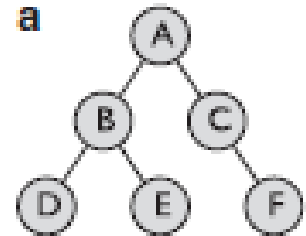
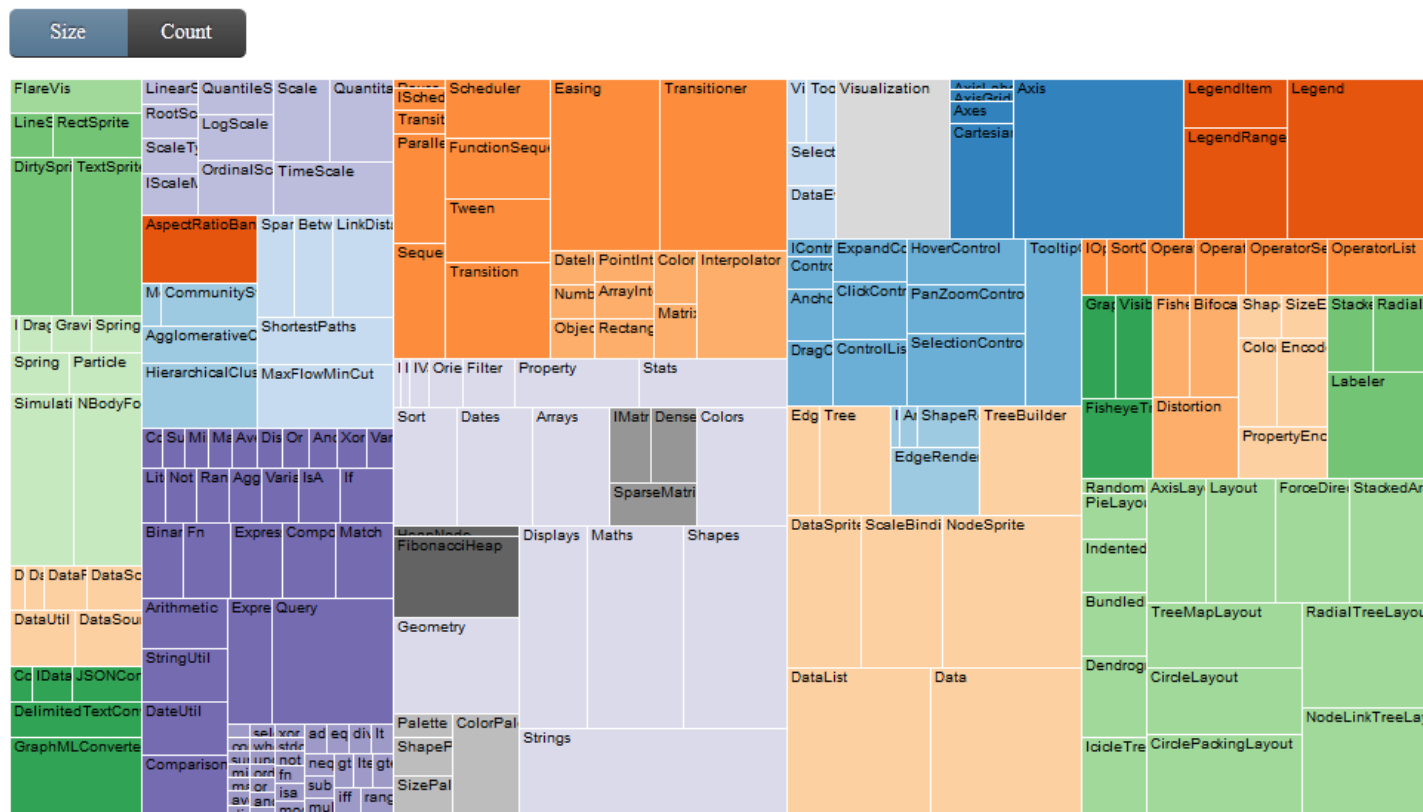
<http://bl.ocks.org/mbostock/4339083>

# TreeMap

- Enclosure encodes hierarchy
- Space-efficient but structure harder to interpret

d3.js

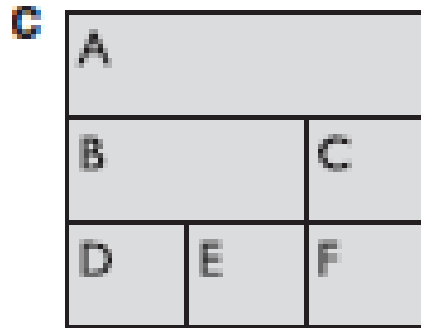
Treemap



Graham & Kennedy (2010)

# Tree – Adjacency layouts

- Halfway house between node-link and a treemap



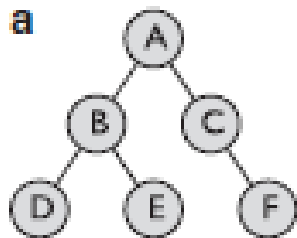
Graham & Kennedy (2010)



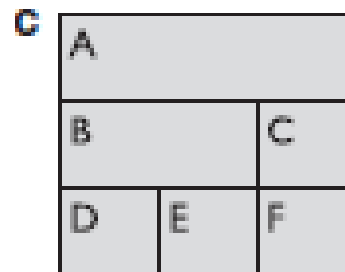
D3.js partition layout

# Tree layouts: summary

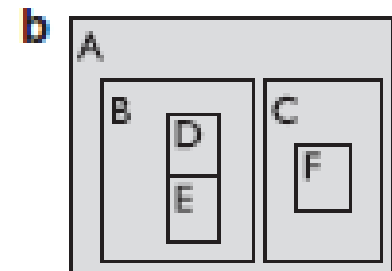
Node-link



Adjacency



Tree map



Graham & Kennedy (2010)



- More space
- More intuitive
- Structure easier to interpret

- Less space
- Less intuitive
- Structure harder to interpret
- Emphasises leaf nodes
- Cannot encode edge attributes



# Graph vis tools

Easy to use graph visualisation tools:

- NodeXL (<http://nodexl.codeplex.com/>)
- Gephi (<https://gephi.org/>)



# TIME

# Visualising temporal data

- Useful resources: [www.timeviz.net](http://www.timeviz.net) (survey) and HCIL's summary of temporal visualisation projects  
<http://www.cs.umd.edu/hcil/temporalviz/>

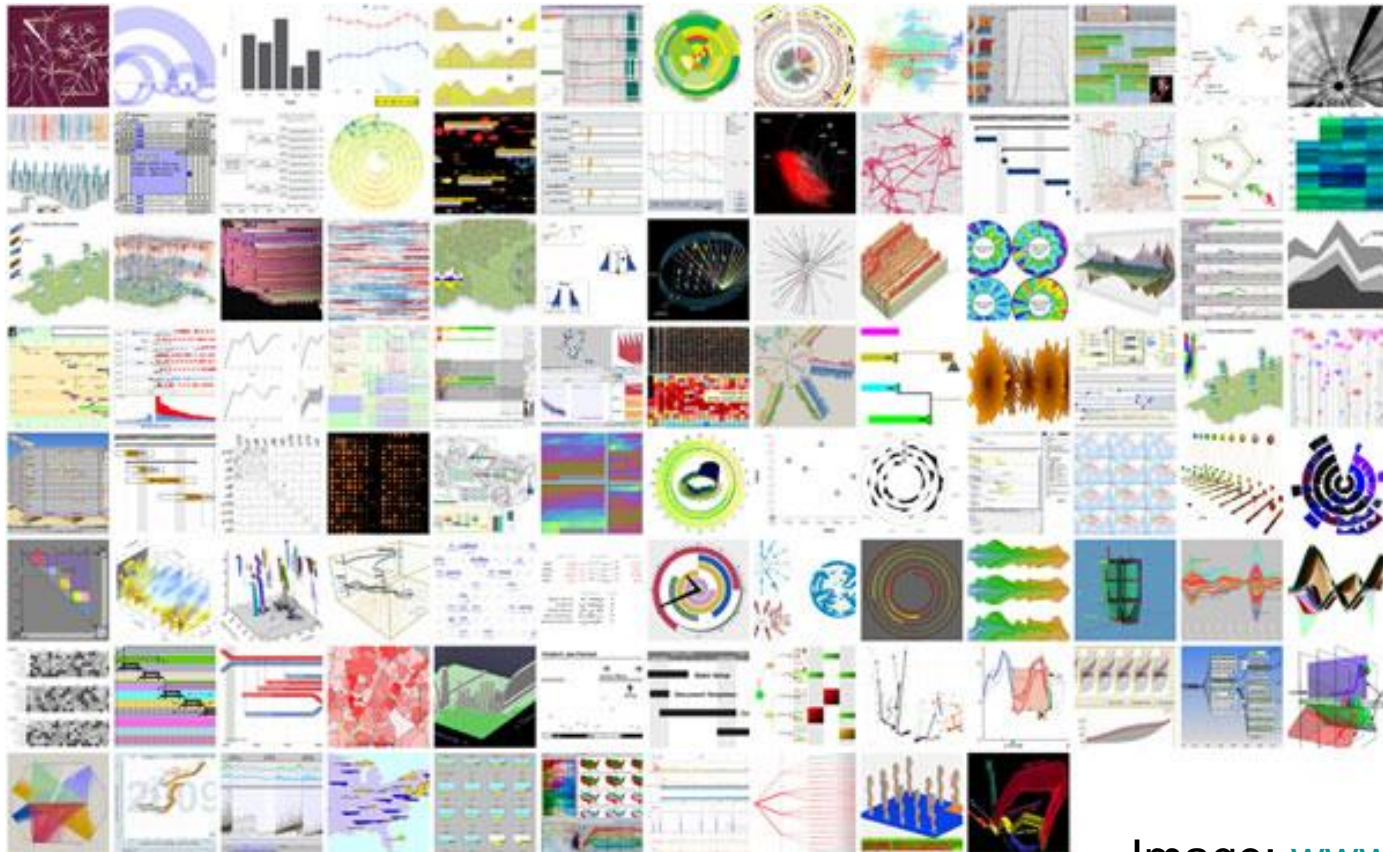
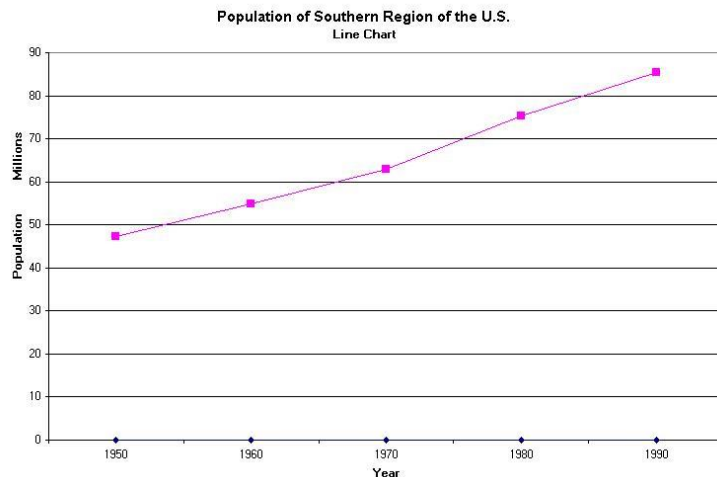


Image: [www.timeviz.net](http://www.timeviz.net)

# Visualising temporal data

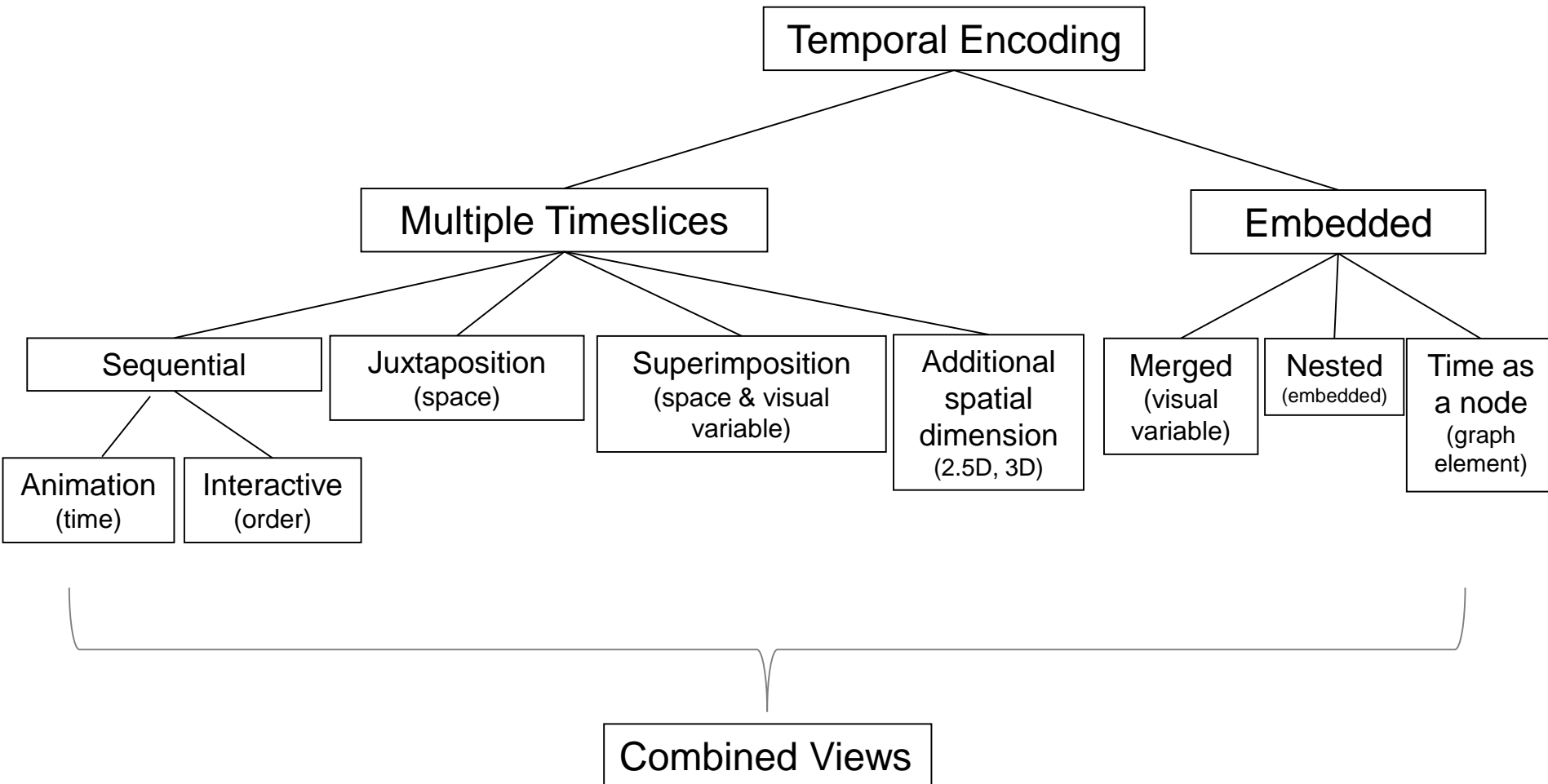
- Time is special – we can't just treat it like any other dimension
- (unlike spatial data) it has no inherent mapping in space
- For tabular data over time, we can use e.g. line charts



Line chart image [ciese.org](https://ciese.org)

- Problem: relational, spatial, and multidimensional data over time
  - we use up two dimensions laying out the graph or showing the map

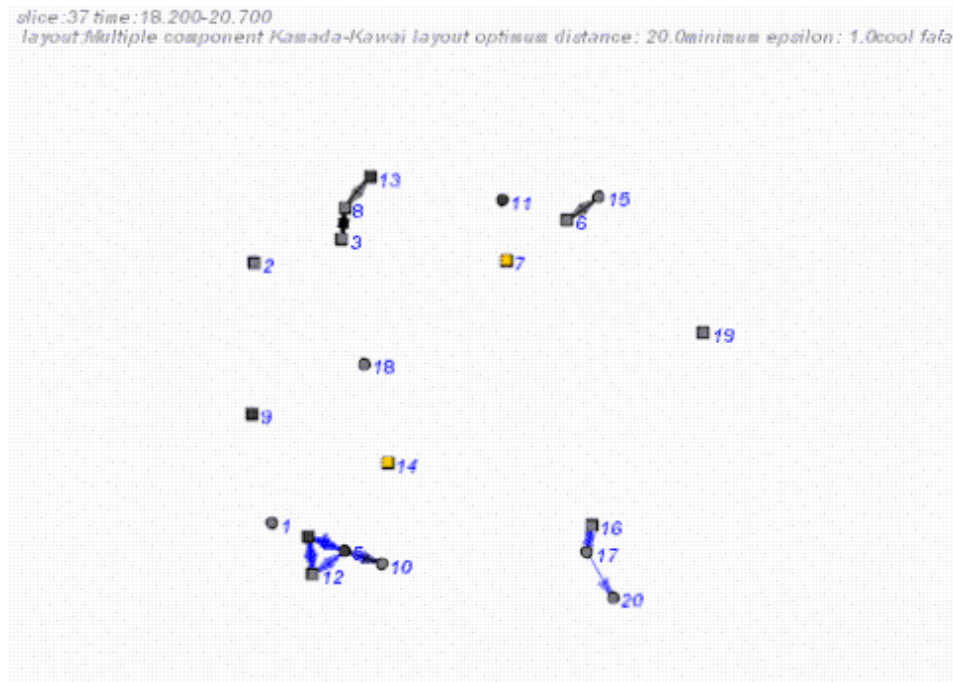
# Encoding the temporal dimension: approaches



# **TIMESLICE APPROACHES**



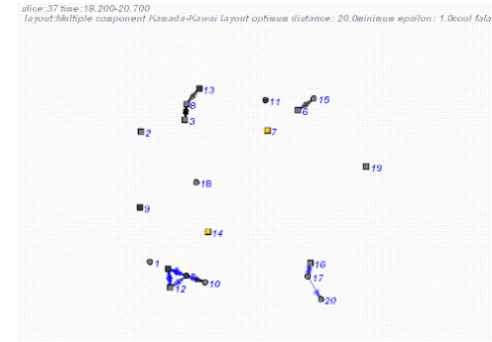
# Sequential: Mapping time to time (animation)



Bender-deMoll & McFarland's (2006) animation of a classroom attention network, using SoNIA.

Available at [http://www.cmu.edu/joss/content/articles/volume7/deMollMcFarland/images/cls33\\_10\\_16\\_96.gif](http://www.cmu.edu/joss/content/articles/volume7/deMollMcFarland/images/cls33_10_16_96.gif)

# Sequential: Mapping time to time (animation)



## Advantages:

- An extra encoding channel
- People enjoy animation (even when it's not helping them)
- Reduces clutter – full screen space available
- More accurate for certain tasks (graph studies)

## Disadvantages:

- Tasks take longer – need to view the whole sequence
- Cognitive overhead - comparison of timeslices need to be performed in memory
- Lack of interaction makes it difficult for the user to explore the data

# Animation as an encoding channel

- Showing images sequentially to convey change over time

## Animation

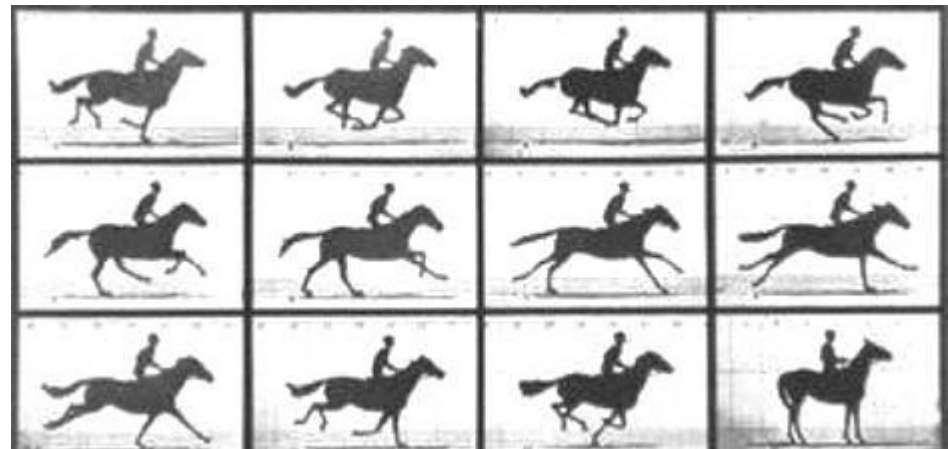
- Good:
  - Transitions (Heer & Robertson, 2007)
  - Simple comparison of adjacent items (Fekete, 2002)
  - (Narrated) storytelling (Robertson, Fernandez, Fisher, Lee, & Stasko, 2008)  
e.g. Gapminder
- Not so good:
  - In analysis e.g. making comparisons, exploring data (less accurate, slower)
  - When conveying complex systems (Tversky, Morrison, & Betrancourt, 2002)

# Animation: hard to perceive accurately

- Perception of motion may not be accurate (Tversky et al. 2002)



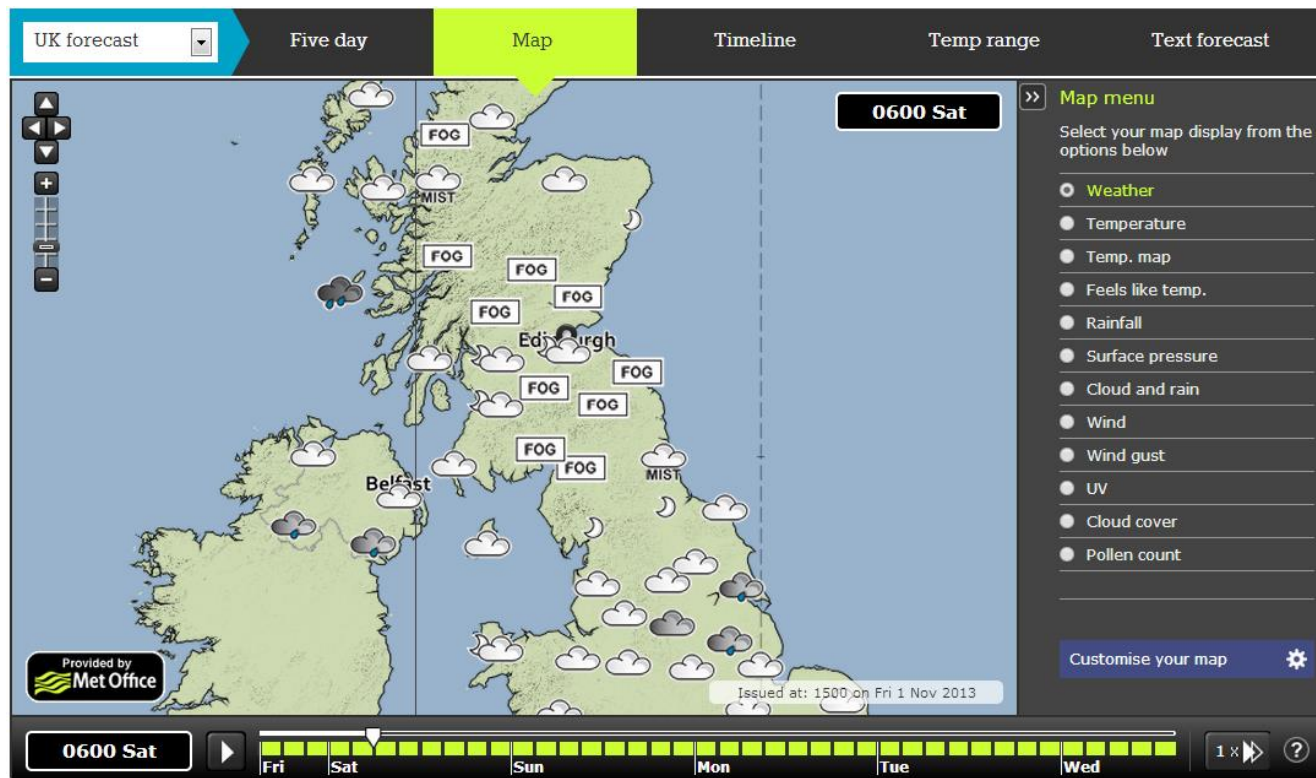
Stubbs (1724 - 1806)



Muybridge, 1878

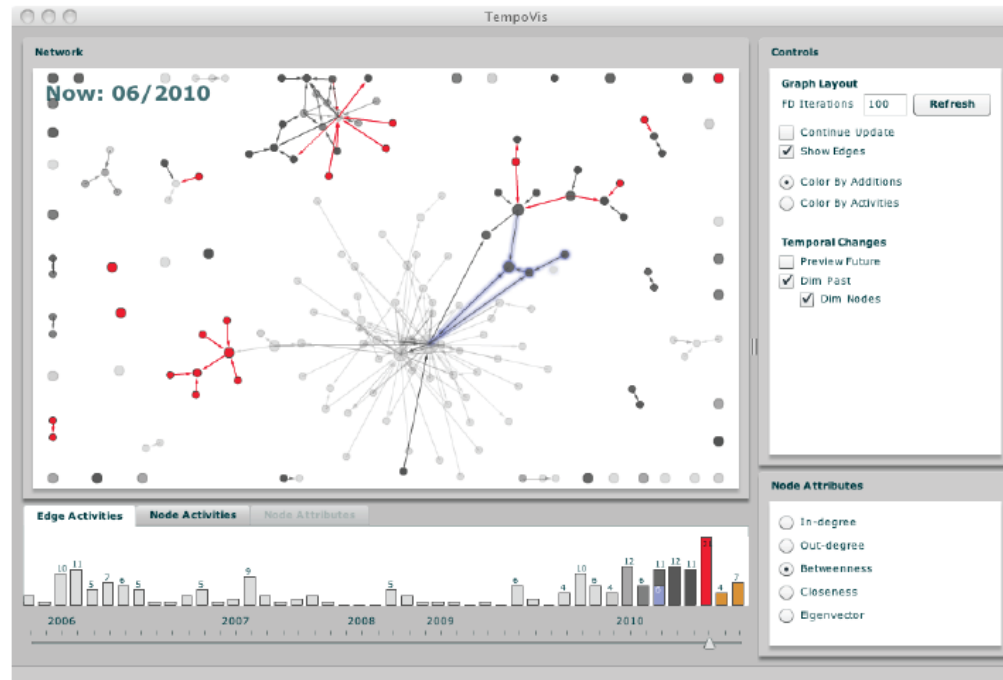
# Animation: cognitive burden

Test: which representation is easier animation or timeline?



<http://www.metoffice.gov.uk/public/weather/forecast/map>

# Sequential: Interactive approach (slideshow)



Ahn et al.'s (2010) TempoVis prototype interface –use of timeslider interaction to navigate through different timepoints

# Mapping time to space 1: Juxtaposition (small multiples)





# Sequential vs Juxtaposed views

- Showing images sequentially to convey change over time

- Advantages:

- Extra encoding channel
    - More screen space -> clutter reduction (Ellis & Dix, 2007)
    - More “fun”/“exciting” than static approaches (Robertson et al., 2008)
    - Can spot local changes between timeslices

- Disadvantage:

- Cognitive overhead – comparison performed in memory
    - Tasks take longer (Robertson et al., 2008; Archambault et al., 2011)
    - Less accurate; confusing (Robertson et al., 2008)

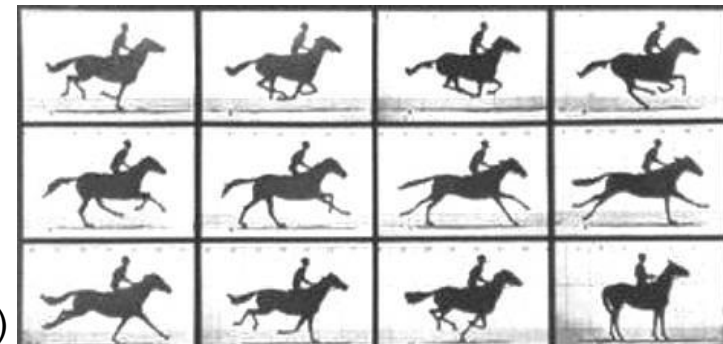
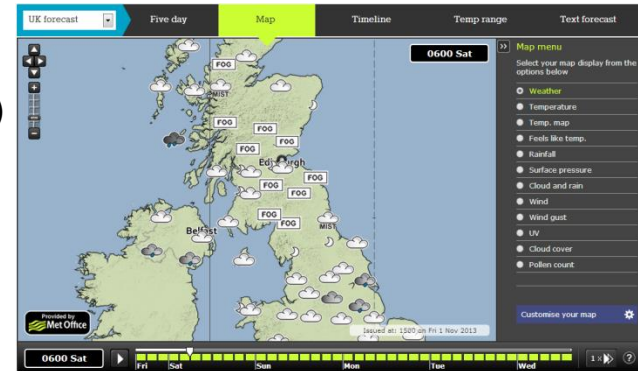
- Animation

- Good:

- Transitions (Heer & Robertson, 2007)
    - Simple comparison of adjacent items (Fekete, 2002)
    - Storytelling (Robertson et al., 2008)

- Not so good:

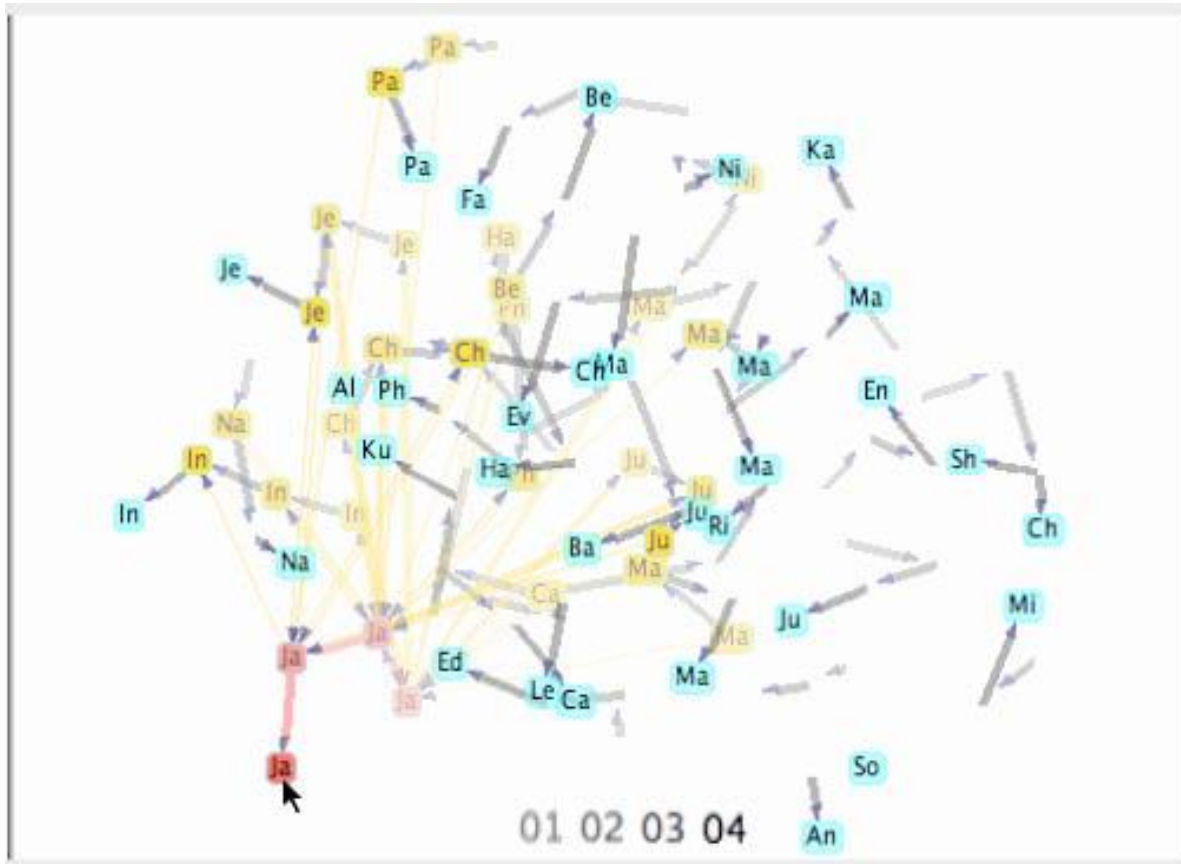
- In analysis, when conveying complex systems (Tversky, Morrison, & Betrancourt, 2002)



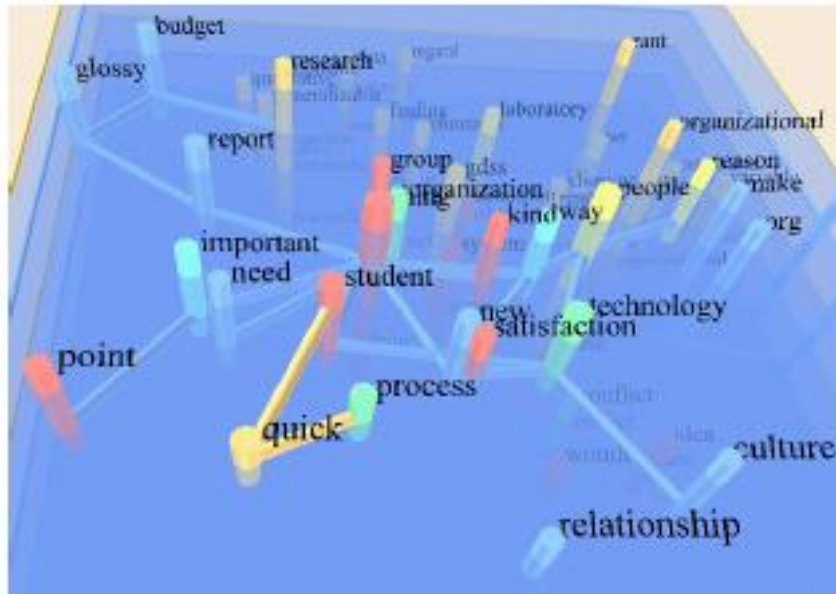
## Mapping time to space & visual variable : Superimposition

- Four timeslices overlaid (each node appears multiple times)
- Opacity used to distinguish time (most recent = opaque, older = more transparent)
- Red is highlight on mouse-over (shows single node).

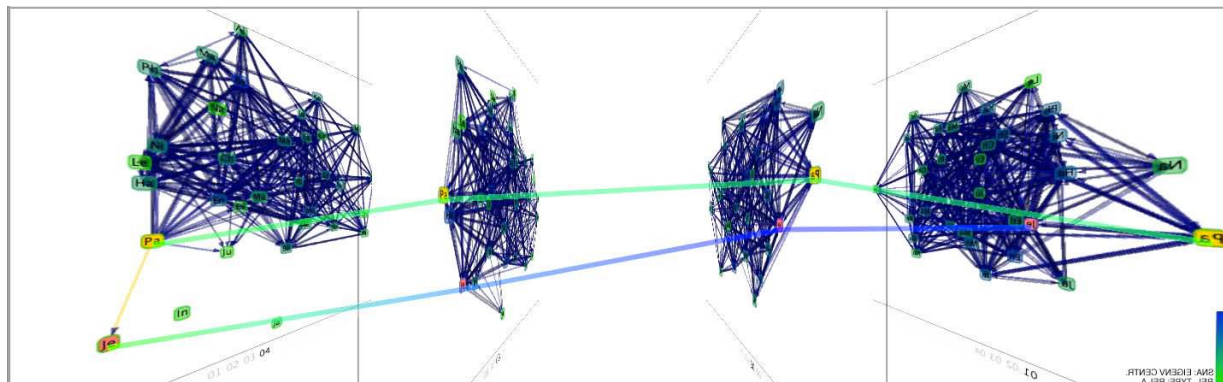
*Federico et al (2011), fig 3.*



## Mapping time to an additional spatial dimension (2.5D, 3D)



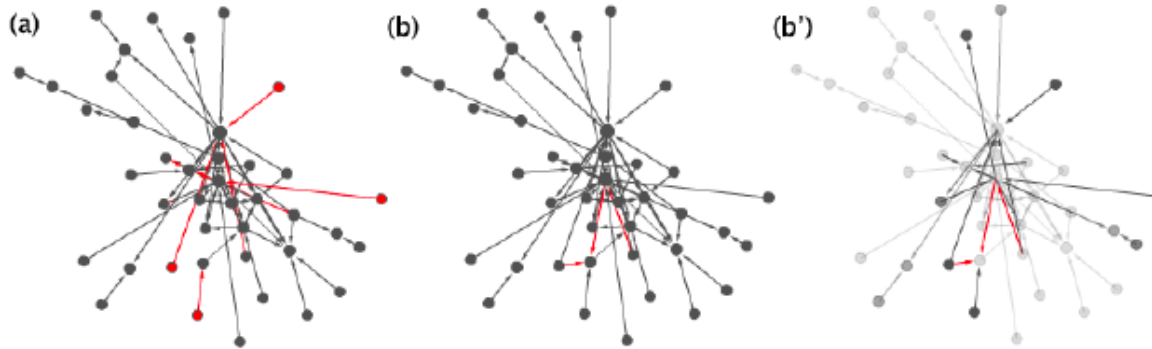
3D: Brandes and Corman (2003)



2.5D: Federico et al. (2011)

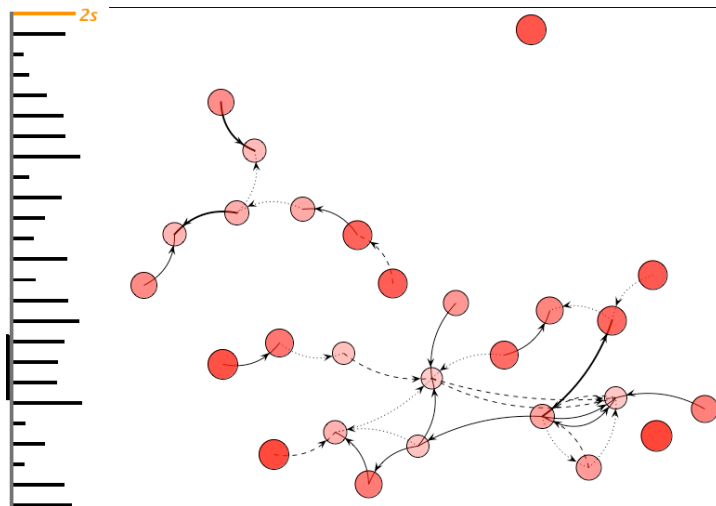
# EMBEDDED APPROACHES

# Mapping time to a visual variable: merged



In (b'), older activities  
painted in lower intensities to  
show their age

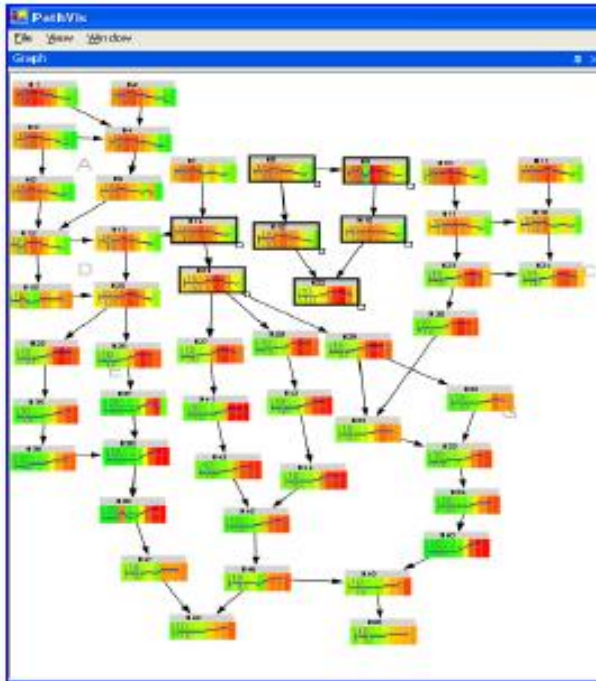
*from Ahn, Taieb-maimon and  
Sopan (2010), fig 3, p6*



Line length encodes the amount of time which has  
passed between changes

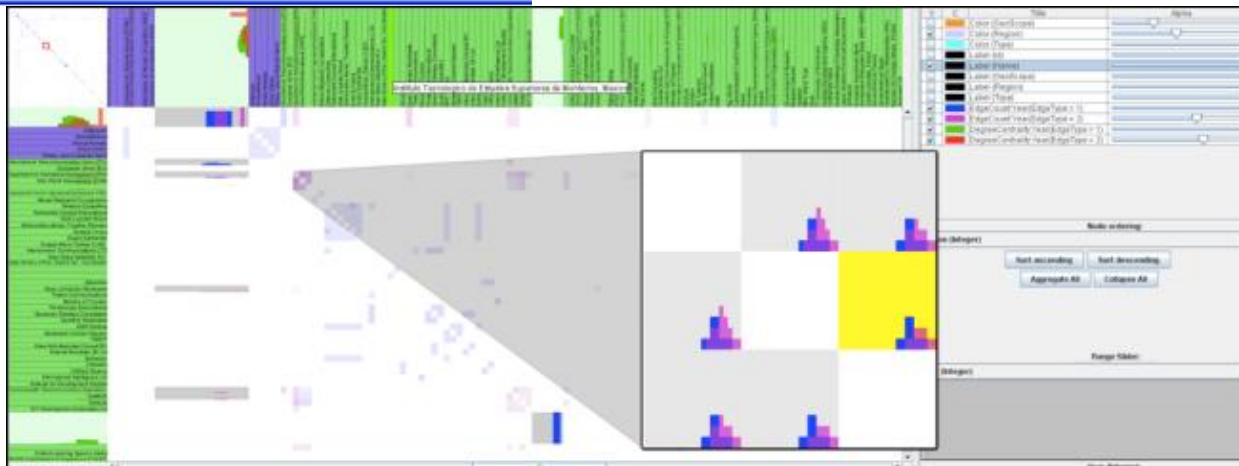
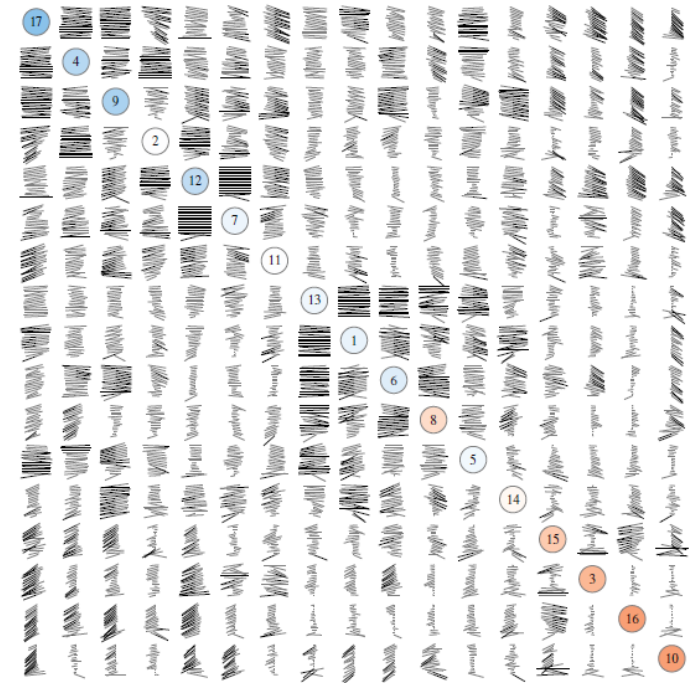
*Shannon, Quigley, & Nixon (2010).*

# Nested time



heat maps  
embedded in  
node link graph  
vertices (Saraiya  
et al., 2005);

histograms  
embedded in  
matrix (Yi et al.,  
2010)

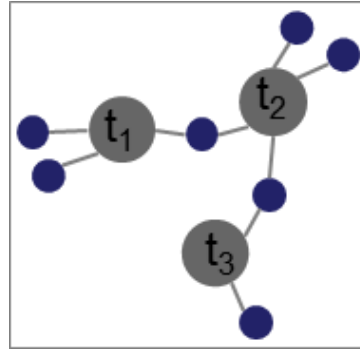


Gestaltmatrix  
(gestalt lines  
embedded in a  
matrix) (Brandes  
& Nick, 2011)

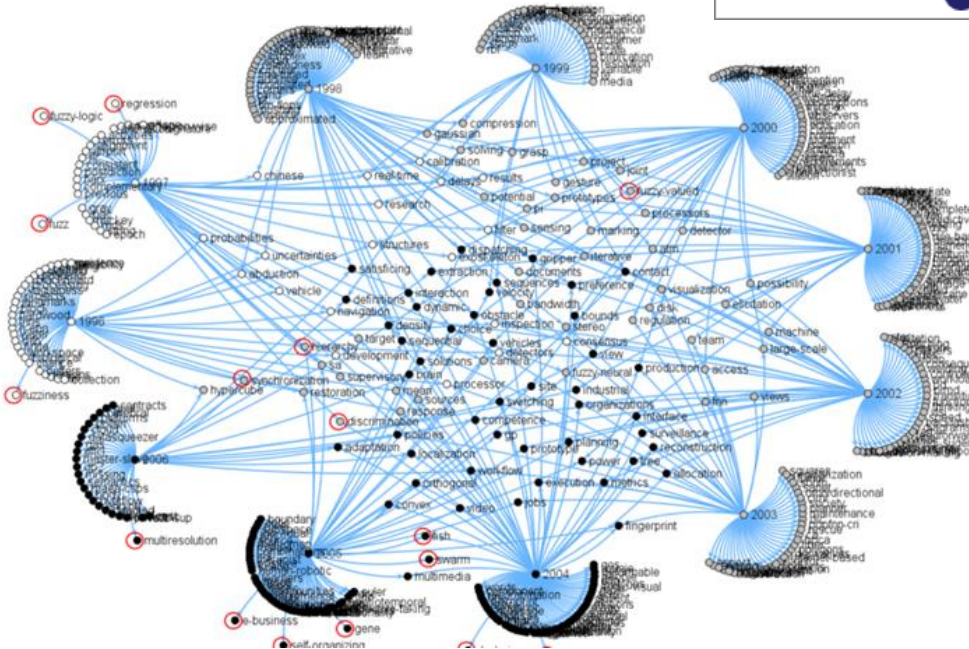




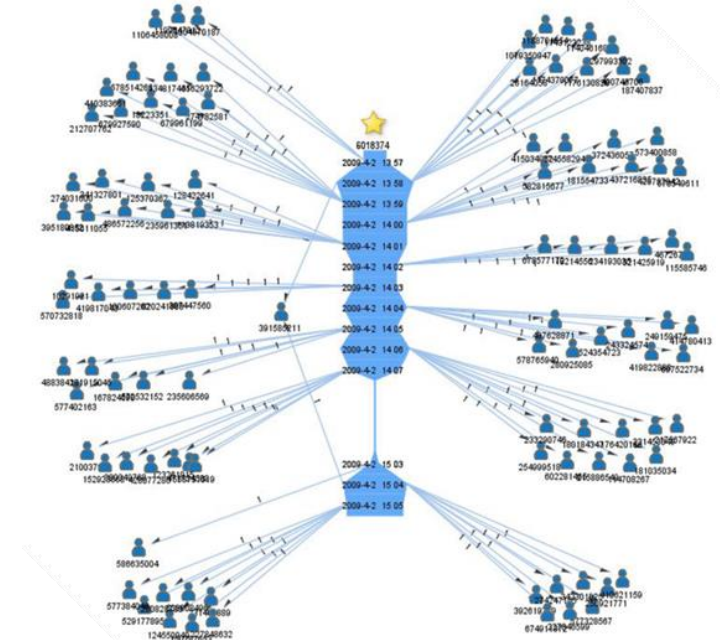
# Embedded: Time as a node



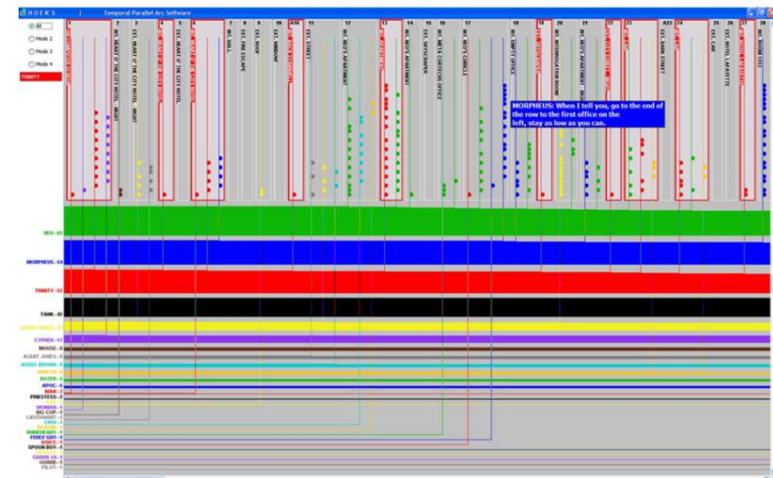
Edinburgh Napier  
UNIVERSITY



Thiel, Dill, Kötter, & Berthold (2007, Figure 3)



1.5D (Shi, Wang, & Wen, 2011, Figure 1)



TIPAD - Parallel Arc Diagrams (Hoek, 2011, Figure 14)

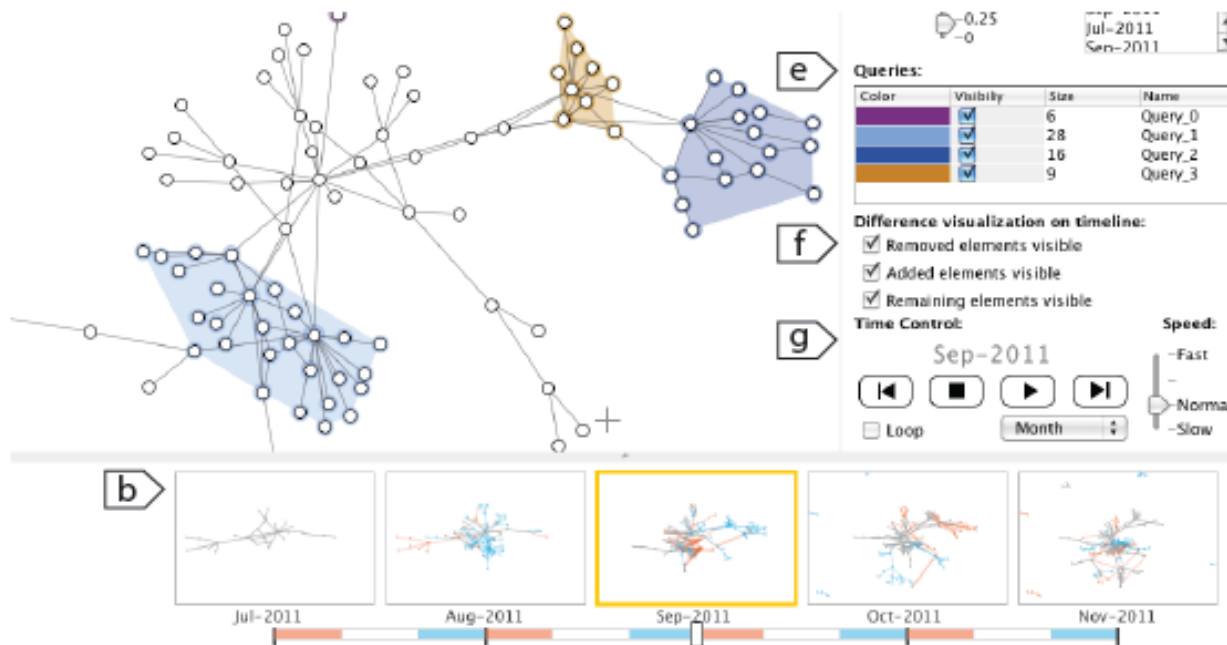


# COMBINING TECHNIQUES

# Combining Techniques

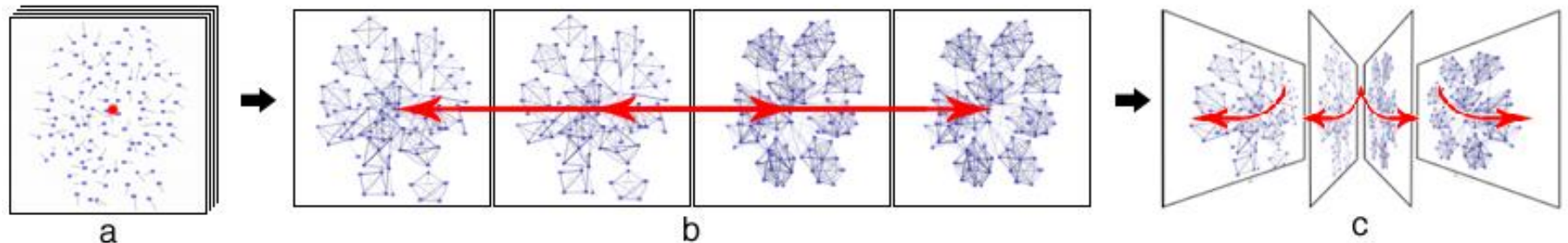
- Multiple views maximise insight and balance strengths and weaknesses of individual techniques
  - > combine different temporal and/or graph structural encodings
- Examples from literature:
  - Show different techniques in same screen space (MCV)
  - Allow user to select and switch between views
  - Allow users to select different views 'in situ'

# Combined approaches: multiple view in same screen space



Animation and small multiples – GraphDiaries  
(Bach, 2012)

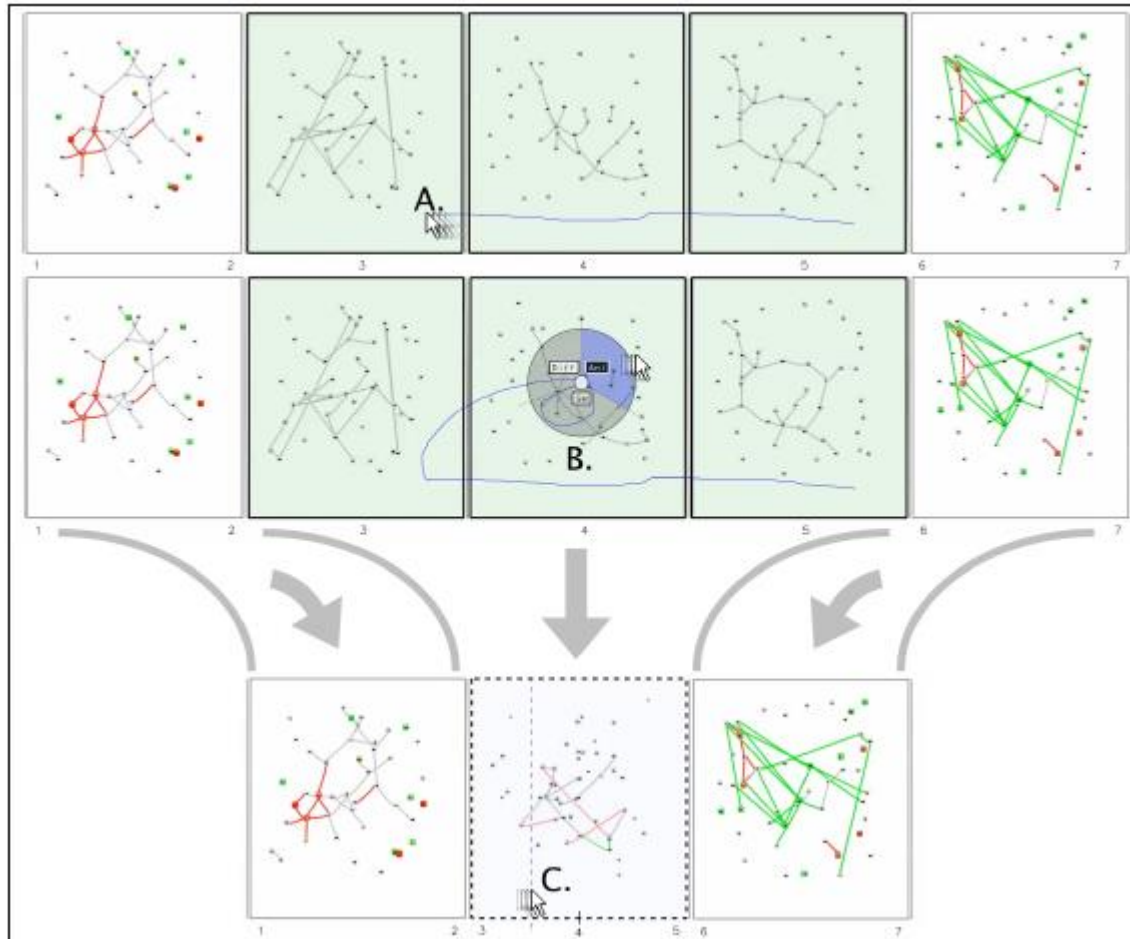
# Combined approaches: user selects and switches between views



(a) superimposition, (b) juxtaposition, (c) 2.5D (Federico et al. 2011)

Interaction/transitioning technique designed to help orientate users when switching between views

# Combined approaches: user selects views ‘in situ’



DiffAni (Rufiange and McGuffin, 2013, Fig. 5: “Interactively converting three small multiple tiles into a single animation tile”)

System offers juxtaposed, sequential and difference map (merged) views.

# SUMMARY

# Take away

What you should take away from this lecture...

- What a graph is
- The different techniques for representing graph data
- The advantages and disadvantages of each
- The approaches available for representing temporal data and the advantages and disadvantages of each

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