

# Multivalued dependency

- ◆ Let  $R$  be a relation schema and let  $X$  and  $Y$  be subsets of the attributes of  $R$ . The multivalued dependency  $X \twoheadrightarrow Y$  is said to hold over  $R$  if, in every legal instance  $r$  of  $R$ , each  $X$  value is associated with a set of  $Y$  values and this set is independent of the values in the other attributes.

OR

For a dependency  $A \twoheadrightarrow B$ , if for a single value of  $A$ , multiple values of  $B$  exist, then the relation will be a multi-valued dependency.

# Multivalued Dependencies

Course	Teacher	Book
Physics101	Green	Electronics
Physics101	Green	Optics
Physics101	Brown	Mechanics
Maths301	Brown	Geometry
Maths301	Green	Vectors
Maths301	Green	Algebra

- Course  $\twoheadrightarrow$  Book
- Course  $\twoheadrightarrow$  Teacher

## Fourth Normal Form (4NF)

- 4NF is a direct generalisation of BCNF.
- A relation will be in 4NF if it is in Boyce Codd normal form and has no multi-valued dependency.
- Let  $R$  be a relation schema,  $X$  and  $Y$  be non empty subsets of the attributes of  $R$ , and  $F'$  be a set of dependencies that includes both FDs and MVDs.
- $R$  is said to be in fourth normal form (4NF), if, for every MVD  $X \twoheadrightarrow Y$  that holds over  $R$ , one of the following statements is true:
  - $Y \subseteq X$  or  $XY = R$  or
  - $X$  is a superkey.

# Fifth normal form (5NF)

- ◆ A relation is in 5NF if it is in 4NF and not contains any join dependency and joining should be lossless.
- ◆ 5NF is satisfied when all the tables are broken into as many tables as possible in order to avoid redundancy.
- ◆ 5NF is also known as Project-join normal form (PJ/NF).

# Join Dependency

- ◆ Join decomposition is a further generalization of Multivalued dependencies.
- ◆ If the join of  $R_1$  and  $R_2$  over  $C$  is equal to relation  $R$ , then we can say that a join dependency (JD) exists. Where  $R_1$  and  $R_2$  are the decompositions  $R_1(A, B, C)$  and  $R_2(C, D)$  of a given relations  $R(A, B, C, D)$ .
- ◆ Alternatively,  $R_1$  and  $R_2$  are a lossless decomposition of  $R$ .