

# ASEN 6060

## ADVANCED ASTRODYNAMICS

### Week 2 Discussion

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#### Objectives:

- Apply theoretical knowledge from Weeks 1 and 2 to scenarios in real celestial systems
- Devise foundational maneuvering heuristics
- Identify implementation challenges and useful questions to ask

# Question 1

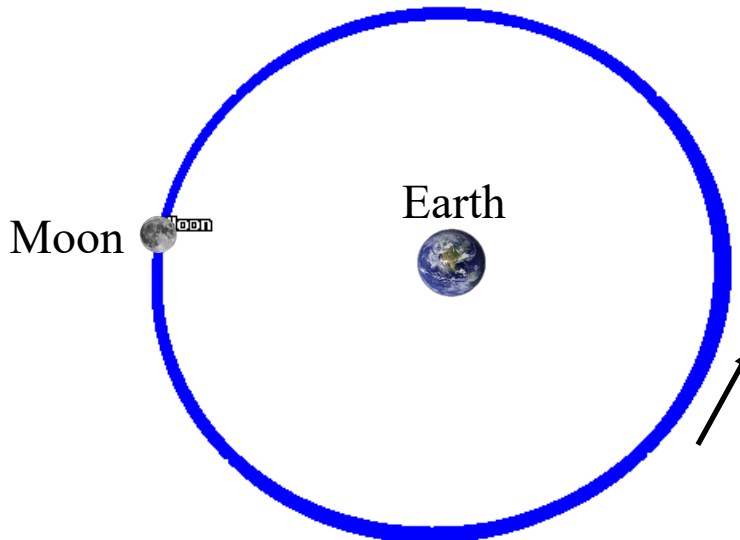
**Question 1:** How would you select appropriate characteristic quantities for nondimensionalization in the Earth-Moon system if we didn't provide an orbital parameters sheet on Canvas?

Approved AGI Educational Alliance Partner

$$m^* = \tilde{M}_1 + \tilde{M}_2$$

$$l^* = \tilde{R}_1 + \tilde{R}_2$$

$$t^* = \left( \frac{(l^*)^3}{\tilde{G}m^*} \right)^{1/2}$$



\* Earth and Moon not to scale!

Earth Inertial Axes

2 Jan 2020 01:21:00.000

Time Step: 180.00 sec

# *Question 1*

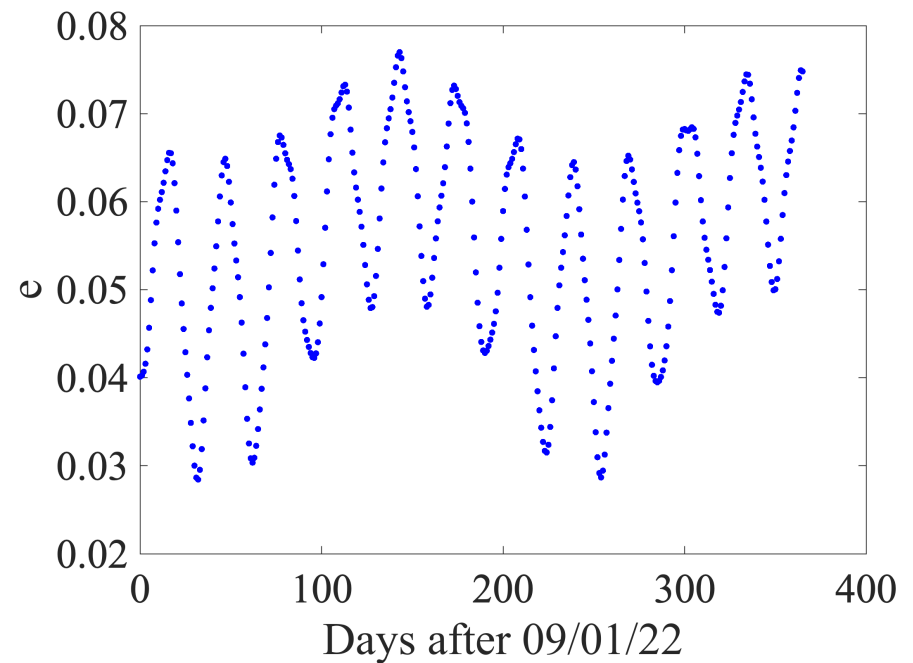
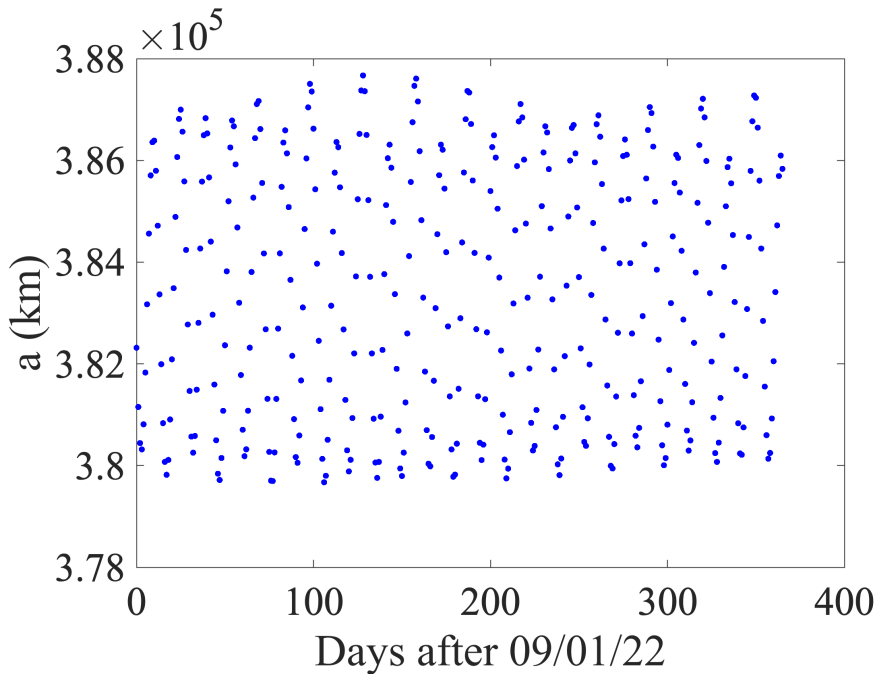
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Group Brainstorming:

# Question 2

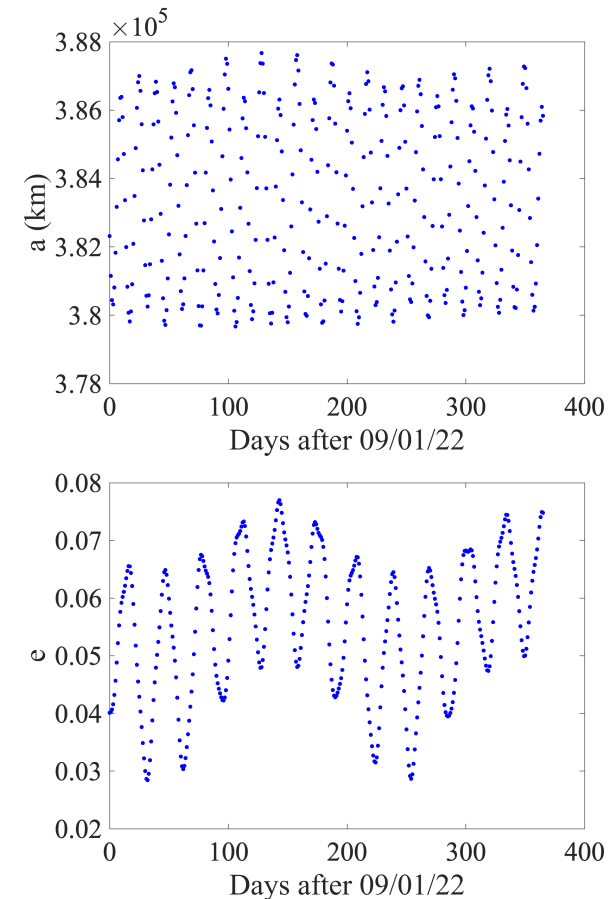
**Question 2:** Is a circular path of the Moon with a single semi-major axis a ‘good’ approximation of the Moon’s actual path?



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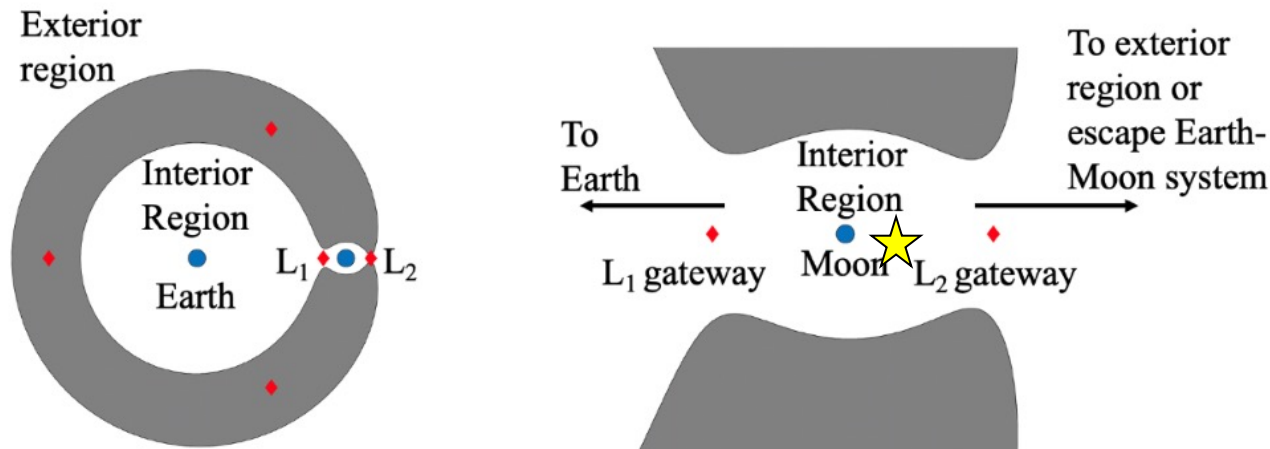
Group Brainstorming:



# Question 3

A spacecraft is located near the Moon and in the Earth-Moon rotating frame with state vector  $[x_0, y_0, 0, \dot{x}_0, \dot{y}_0, 0]^T$

The initial Jacobi constant for this state vector is  $C_0$ , producing ZVCs that resemble the following from lecture:



**Question 3:** Derive an expression for the theoretical minimum magnitude for an impulsive maneuver at ★ for the spacecraft to be guaranteed to never leave the Moon vicinity in the Earth-Moon CR3BP? List all necessary assumptions.

# *Question 3*

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**Question 3:**

**Assumptions:**

# Question 4

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**Question 4:** You have been tasked with designing a maneuver for a planetary defense interceptor mission within the Earth-Moon system. The interceptor spacecraft is currently positioned at  $L_1$  with zero velocity and the goal is for the spacecraft to reach the location of  $L_4$  (with any velocity vector).

A colleague proposes slightly perturbing the state of the spacecraft in manner that does not change the Jacobi constant but would place the spacecraft on a transfer from  $L_1$  to  $L_4$ .

Given your initial understanding of motion in the CR3BP and zero velocity curves, do you think your colleague's plan could work and why?



# *Question 4*

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Group Brainstorming:

# Question 5

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**Question 5:** You and your colleague are each numerically generating a trajectory associated with the same initial state  $[x_0, y_0, 0, \dot{x}_0, \dot{y}_0, 0]^T$  and integration time. You are each using your own code or using off-the-shelf software. Do you expect to recover the exact same state as your colleague after the integration time? Why/why not?

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Group Brainstorming:

# *Question 6*

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**Question 6:** Do you expect the trajectory you have generated to accurately reflect the path of the spacecraft in a high-fidelity model of cislunar space? Why or why not?

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Group Brainstorming:

# *Question 7*

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**Question 7:** What are the implications of your answers to Question 5 and 6 on predicting the future paths of objects in cislunar space (assuming perfect state knowledge)?

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Group Brainstorming:

# *General Takeaways*

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Group Brainstorming: