# DIGITAL SYSTEMS AND MICROPROCESSORS (ELE2002M)

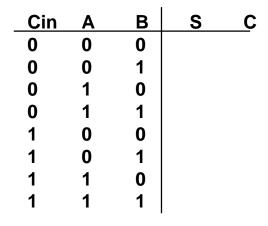
LECTURE -4
COMBINATIONAL LOGIC — ADDERS AND <u>SUBTRACTORS</u>

Instructor:

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#### Full Adder

Develop a truth table and Boolean expressions for the full adder, this circuit also includes a carry in.





## Truth table for full adder

Cin	Α	В	S	Cout
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

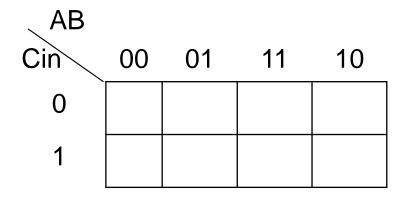
Exercise:

Complete the Karnaugh maps for the Sum and the Carry out columns

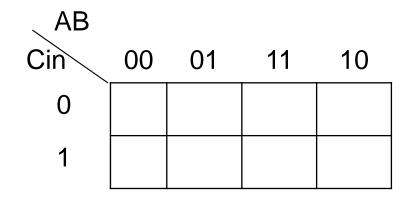
# K-maps for Sum and Carry

**Sum** – 1 when odd number of inputs is 1 = XOR gate

Carry out - simplifies to 3 pairs

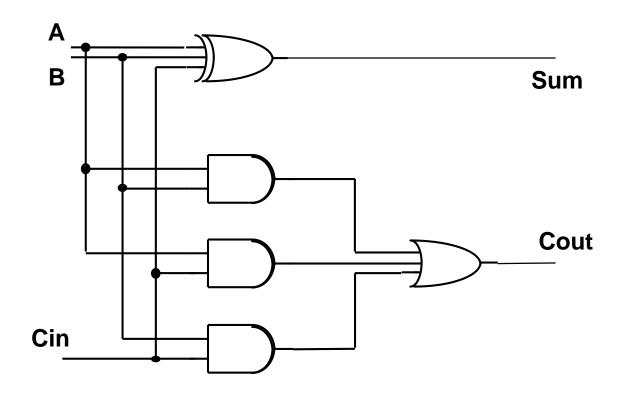


Sum = Cin xor A xor B



$$Cout = A.B + A.Cin + B.Cin$$

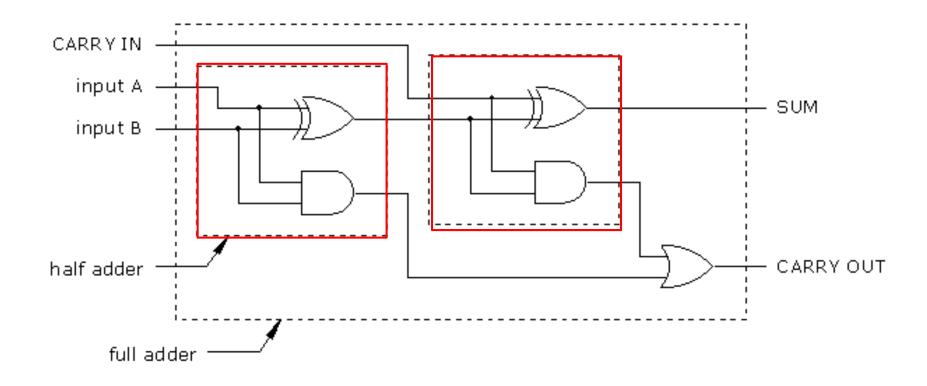
## Full adder circuit



**Sum** = Cin xor A xor B

Cout = A.B + A.Cin + B.Cin

## Full adder circuit with 2 half adders

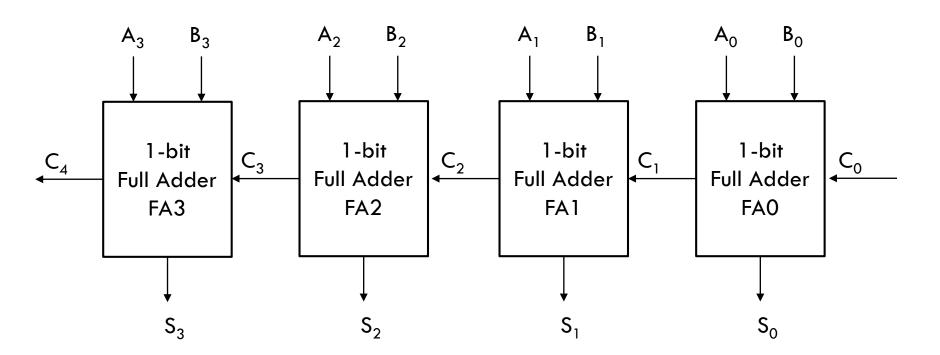


# Binary Adder (Ripple Carry Adder)

- To add two multi-digit binary numbers.
- Consists of several full-adders connected in series.
- The carry-out from previous adder is the carry in to the next full adder.
- The carry out of the final adder (MSB) is the final carry out.
- The carry in of the first adder (LSB) is usually zero.

## 4-bit Addition with Ripple Carry Adder

$$A = A_3 A_2 A_1 A_0$$
$$B = B_3 B_2 B_1 B_0$$



# **Carry Propagation**

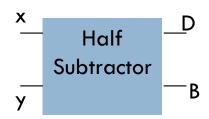
- □ Total propagation time for an addition operation.
- Total propagation time is equal to the propagation delay of a typical gat times the number of gate levels in the circuit.
- Propagation delay for full adders?
- How about generating carry values in advance and use them to calculate the sum?
- An adder that generates carry values in advance (using extra hardware) is known as "Carry Look-ahead Adder"
- Read "Carry Propagation", page 147 in the book.

### Half Subtractor

- A simple 2-input half-subtractor consists of 2 inputs and 2 outputs.
- Two inputs x and y form the minuend and the subtrahend.
- D is the difference output
- □ B is the borrow output

$$D = x'y + xy' \text{ and } B = x'y$$

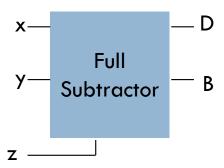
Imlementation?



X	У	D	В
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

#### Full Subtractor

- Full subtractor has 3 inputs and 2 outputs.
- X, y and z are inputs to be subtracted, where z is the borrow from previous stage.
- D and B are the outputs.
- □ D =
- □ B =



X	У	Z	D	В
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

# Binary Subtractor

- □ How did we do Binary subtraction (A-B) earlier?
  - Input A added to 2's complement of B.
- □ How to implement this?
  - Complement each data bit of B by placing an inverter between B and input of full adder.
- □ How to add a '1' to get 2'complement?
  - $\square$  Make  $C_0$  as '1'

## Adder-Subtractor Unit

- A control input 'M' is used to to determine whether the operation is addition or subtraction
- If M is '0' then addition is performed.
- If M is '1' then input B<sub>i</sub> is inverted and C<sub>i</sub> is taken as '1' to perform a subtraction operation.

M	xi	yi	Ci
0	$A_{i}$	$B_{i}$	0
1	$A_{i}$	B <sub>i</sub> '	1

M	A <sub>i</sub>	B <sub>i</sub>	x <sub>i</sub>	y <sub>i</sub>
0	0	0	0	0
0	0	1	0	1
0	1	0	1	0
0	1	1	1	1
1	0	0	0	1
1	0	1	0	0
1	1	0	1	1
1	1	1	1	0

