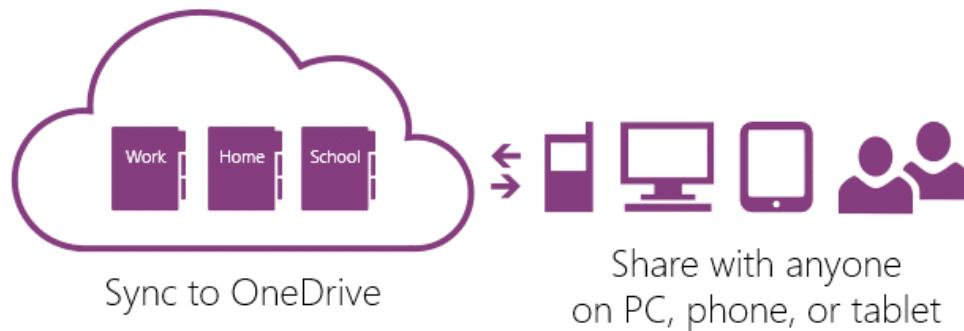


OneNote: one place for all of your notes



[Watch the 2 minute video](#)

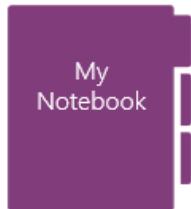
1. Take notes anywhere on the page

Write your name here



2. Get organized

You start with "My Notebook" - everything lives in here

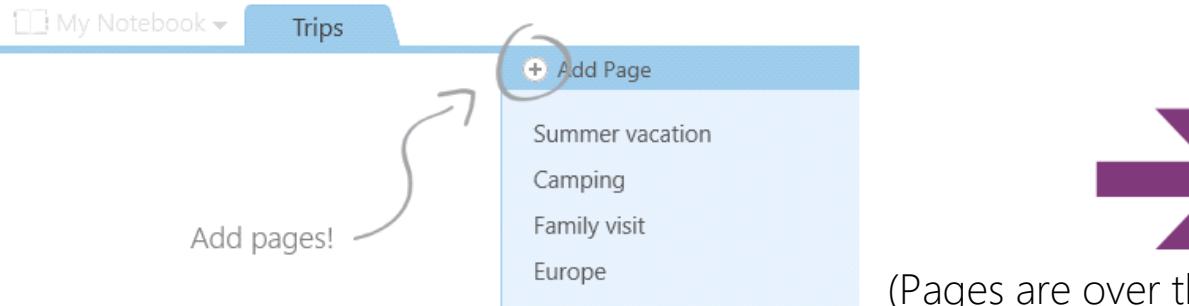


Add **sections** for activities like:

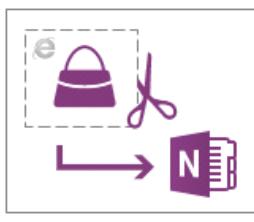


Add **pages** inside of each section:

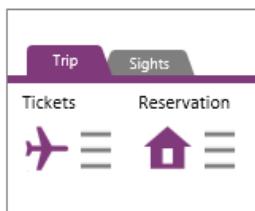




3. For more tips, check out 30 second videos



Clip from
the web



Plan a trip
with others



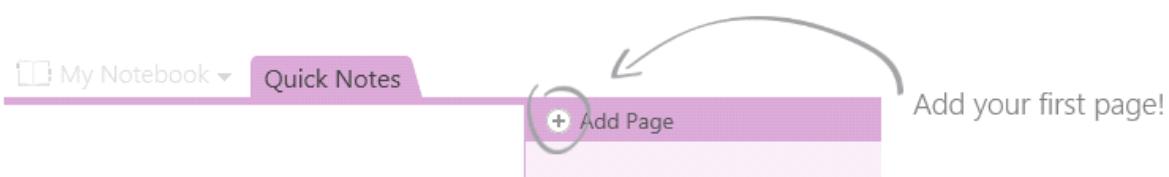
Search notes
instantly



Write notes
on slides

4. Create your first page

You're in the Quick Notes section - use it for random notes



OneNote Basics

The screenshot shows a 'To-do lists' page in OneNote. At the top, there's a purple header bar with the title 'To-do lists'. Below it, there are two sections: 'Shopping list' and 'Priorities'. The 'Shopping list' section contains a bulleted list of items with checkboxes: Milk (checked), Oranges (unchecked), Potatoes (unchecked), Bread (checked), Cereal (unchecked), and Sugar (checked). The 'Priorities' section contains a bulleted list of items with checkboxes: Check messages (unchecked), Call Dave (starred checked), Follow up with Jim (question mark checked), Schedule appt. (checkbox checked), and Call Janet (checkbox unchecked).

Remember everything

- Add Tags to any notes
- Make checklists and to-do lists
- Create your own custom tags



The screenshot shows a travel planning page in OneNote. At the top, there are two tabs: 'Flight details' (purple) and 'Sights to see' (grey). Below the tabs, there are two main sections: 'Transportation' and 'Reservation'. The 'Transportation' section contains a list of items: Arrive at airport at 6am (Ben), Plane departs at 8am, and Plane lands at 2pm. The 'Reservation' section contains a list of items: Hotel is for the 6th – 10th (Tom) and Do we need to extend the reservation by a day?

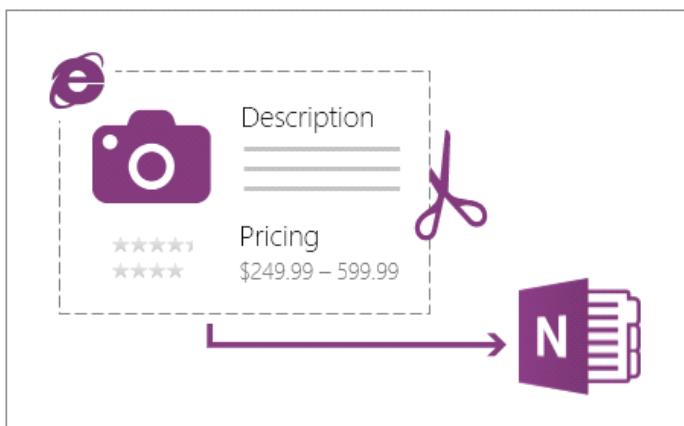
Collaborate with others

- Keep your notebooks on OneDrive
- Share with friends and family
- Anyone can edit in a browser



Keep everything in sync

- People can edit pages at the same time
- Real-Time Sync on the same page
- Everything stored in the cloud
- Accessible from any device



Clip from the web

- ▶ Quickly clip anything on your screen
- ▶ Take screenshots of products online
- ▶ Save important news articles

 in your taskbar

OR

 + S on your keyboard

	Attending?	Overnight?	Vegetarian?
Chris	Yes	Yes	No
Molly	No	No	No
Peter	Yes	No	Yes
Samuel	Yes	Yes	Yes
Stacy	Yes	No	No

Organize with tables

- ▶ Type, then press TAB to create a table
- ▶ Quickly sort and shade tables
- ▶ Convert tables to Excel spreadsheets



Write notes on slides

- ▶ Send PowerPoint or Word docs to OneNote
- ▶ Annotate with a stylus on your tablet
- ▶ Highlight and finger-paint

 in your taskbar

OR

 + N on your keyboard

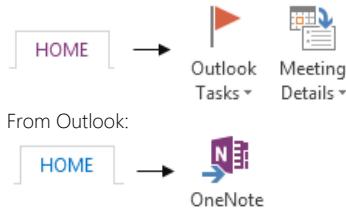
o Status meeting
Conf room 36
John, Felicity

Follow up with John

→

Integrate with Outlook

- Take notes on Outlook or Lync meetings
- Insert meeting details
- Add Outlook tasks from OneNote



x Quarter 1 revenue

	Sales	Revenue	Expenses
Scott	4	5	3
James	2	1	4

Add Excel spreadsheets

- Track finances, budgets, & more
- Preview updates on the page



... Quick Notes

10

Brainstorm without clutter

- Hide everything but the essentials
- Extra space to focus on your notes

in the top corner of the page



Take quick notes

- ▶ Quickly jot down thoughts and ideas
- ▶ They go into your Quick Notes section

 in your taskbar

OR

 + N on your keyboard

(Data Structures & Algorithms)
Advanced

→ Andrew Lee.

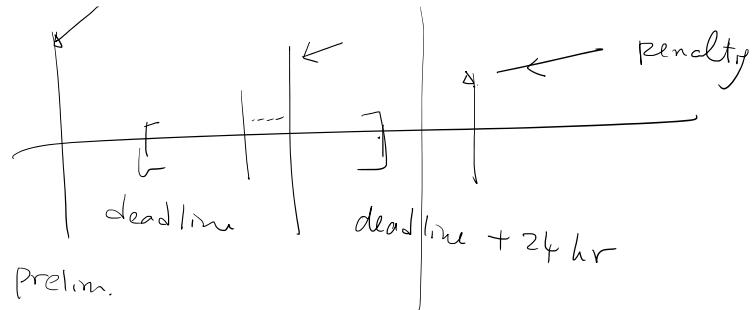
DS + Alg. = Programs

(Wirth)

Organization Meeting

+ Preliminaries

24 hr extension applies



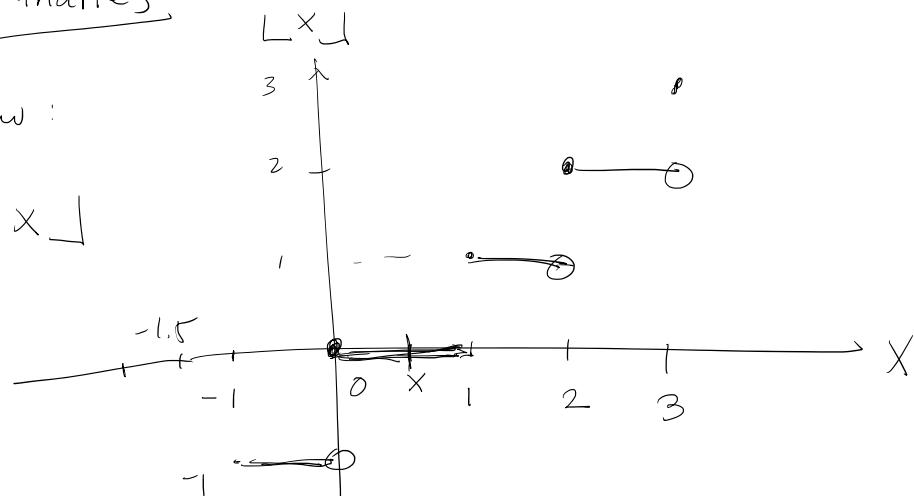
Preliminaries

↗ Appendix of CLRS
Math

Preliminaries

Review :

$\lfloor x \rfloor$



L-1.5]

$$= \begin{cases} -1 \\ -2 \end{cases}$$

Math. Induction

$P(n)$: statement to be proved

✓

base case
n=1

✓

Induction :

$P(n)$ Assumes True

Assumption

Show $P(n+1)$ is true

}

If $P(n)$

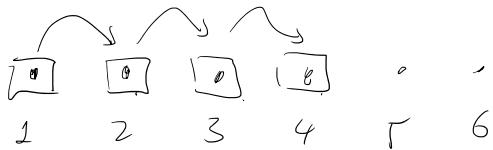
then $P(n+1)$

Then Principle of M. I.

✓

~~shows~~ tells us $P(n)$ is true for

all n .



2016

Sets

$$A = \{1, 2, 3\}$$

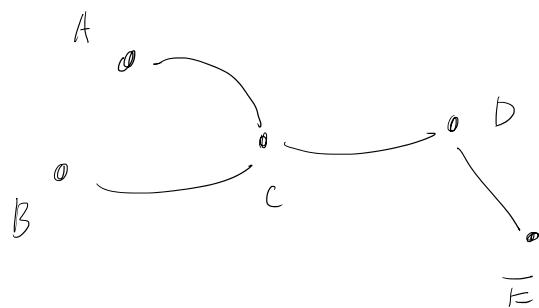
Multisets

$$B = \{\underline{1}, 2, 3, 3, \underline{1}\}$$

$$A \stackrel{?}{=} B \quad (\text{if } A, B \text{ are sets}) \quad \checkmark$$

(if A, B are multisets)

class
example



→ Tree

Vertices

$$= \{A, B, C, D, E\}$$

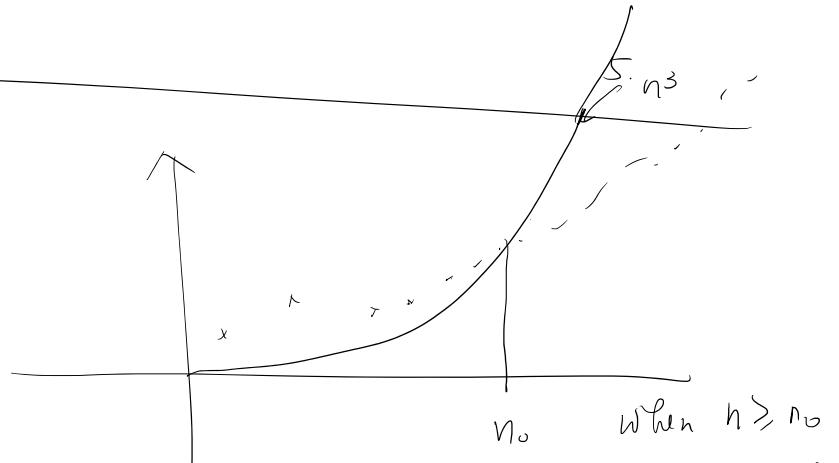
Edges

$$= \{\{A, C\}, \{B, C\}, \{C, D\}, \{D, E\}\}$$

/ remaining
an edge edges

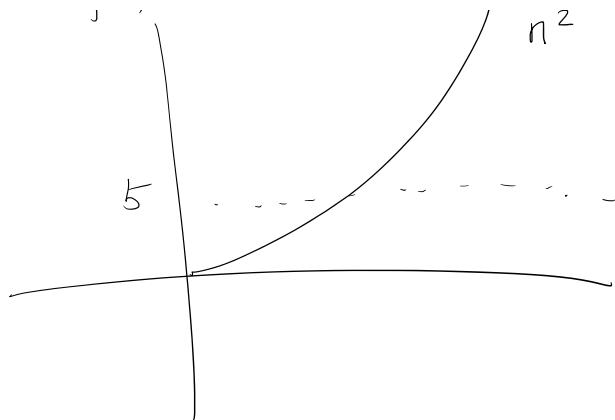
$$f(n) = O(n^3)$$

Upper bound

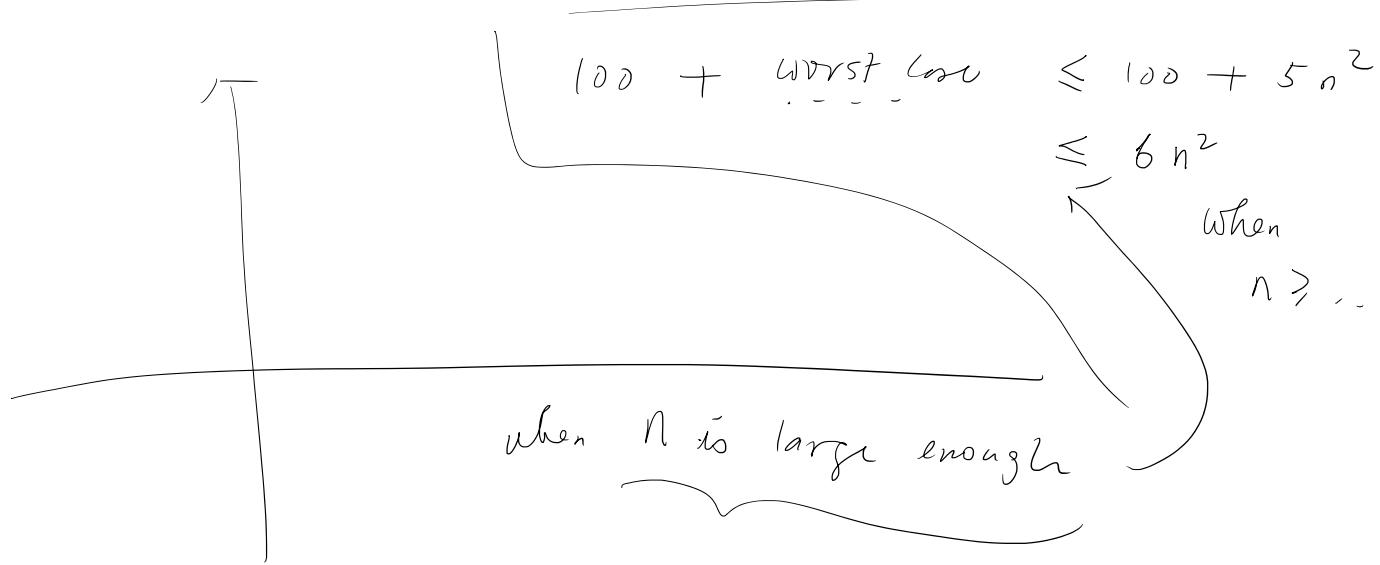


$$f(n)$$

$$n^2$$



$$f(n) = O(n^2)$$



Bubble Sort

worst case : $O(n^2)$

for ($\sim n^{steps}$) {

 for ($\sim n^{steps}$) {

 } constant amount of work

input . 2^n
 k

step . $O(n)$

step $O(\lg_2 k)$

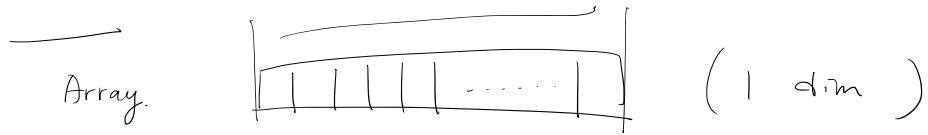
9/7/2016

Wednesday, September 7, 2016 6:43 PM

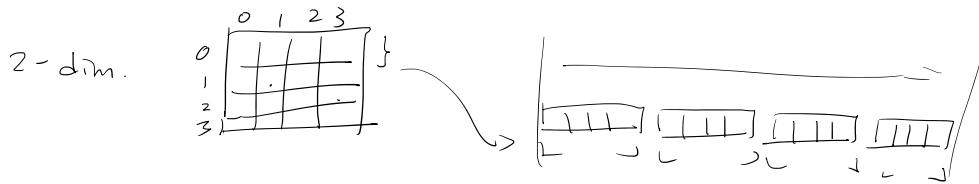
CSE 674

Sequential Allocation

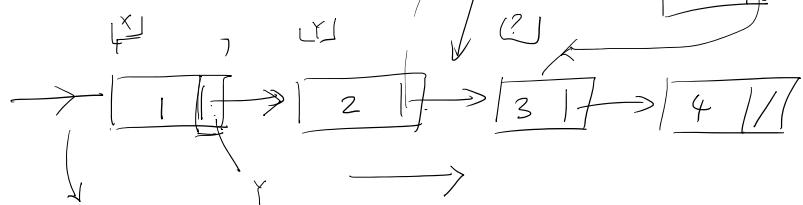
Linked Allocation.



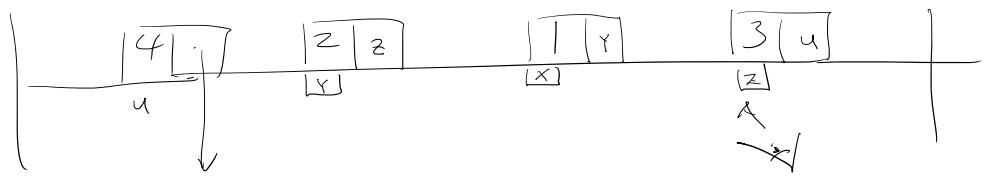
↳ high dimension.



Linked Allocation



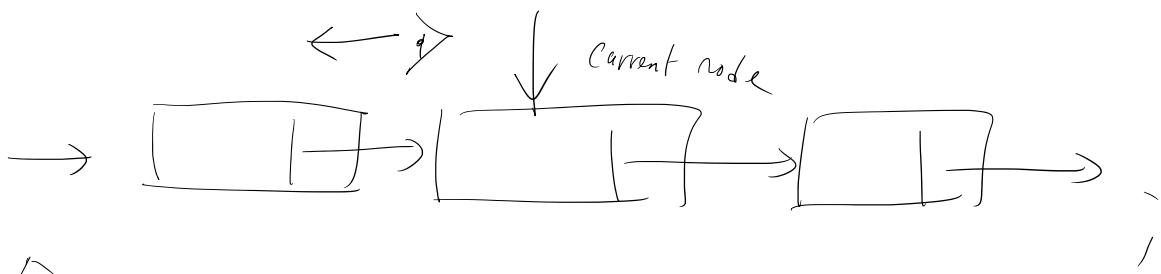
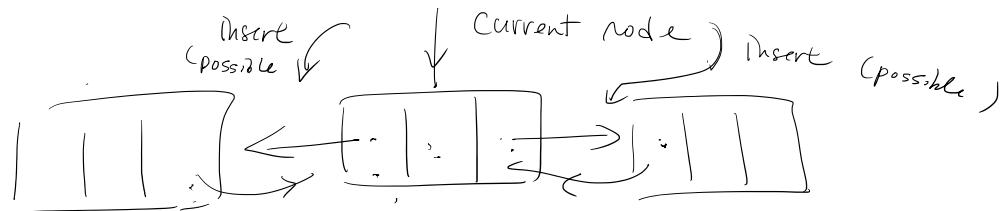
address
location



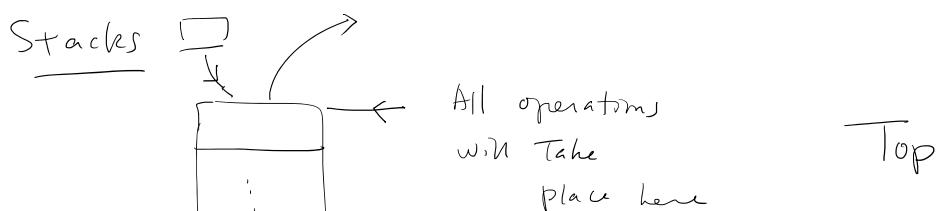
Pointers.cpp (from Phils-ads) 02

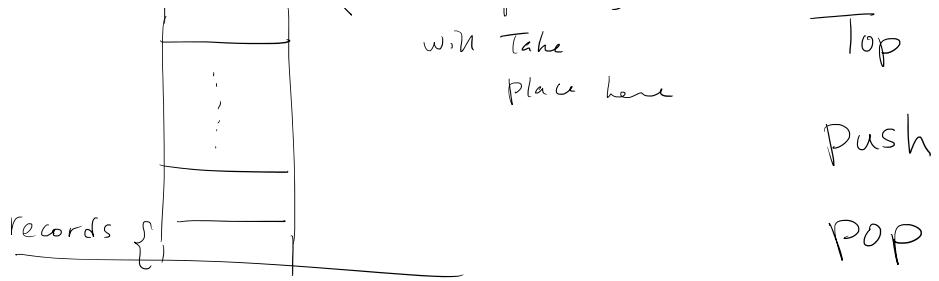


Difference b/w Singly linked list AND Doubly linked list

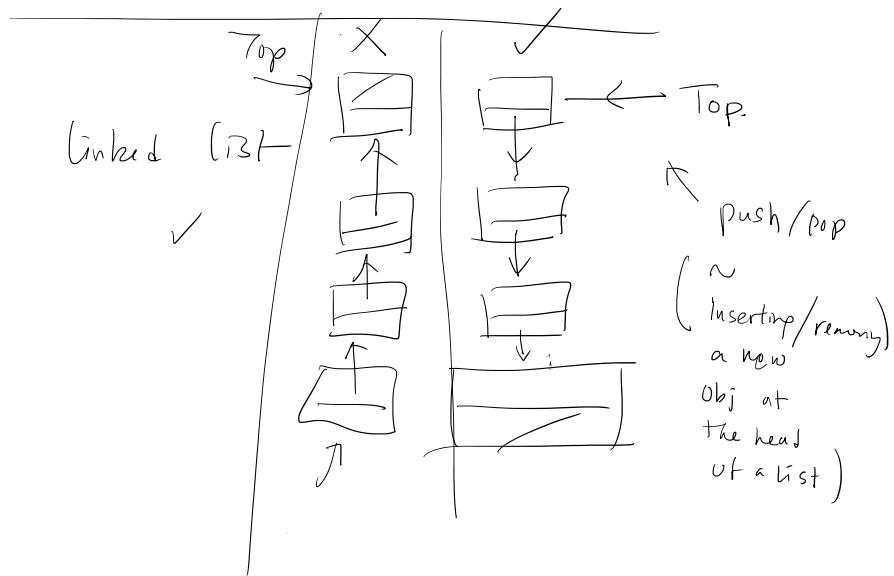


(circular linked list)

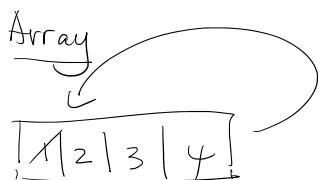
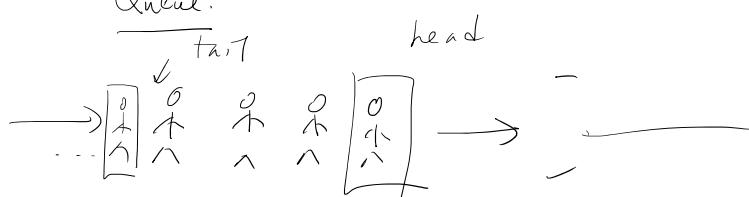




Array ✓



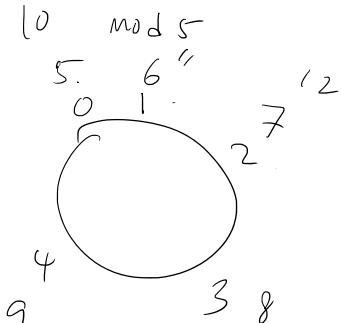
Queue.



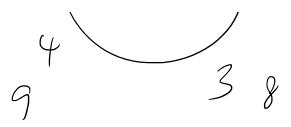
linked list

- enqueue 1
- 2 how to
- 3 Specify
/determine
- deg 1 if a queue
- enqueue 4 is full?

Modulo function



\deg 1 if a queue
empty 4 13 full?
enqueue 5 (empty)



9-12-2016

Monday, September 12, 2016 6:47 PM

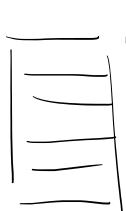
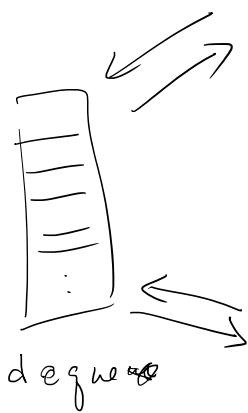
Elementary Data Structures - .

	Stacks	Queues
Sequential Allocation	✓	✓
linked Allocation	✓	

Stacks : LIFO

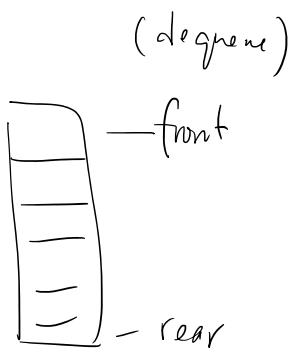
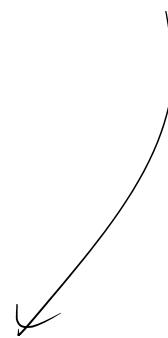
Queues : FIFO

All Brass's example



Top
perform
all operations
at 1 position

Stacks

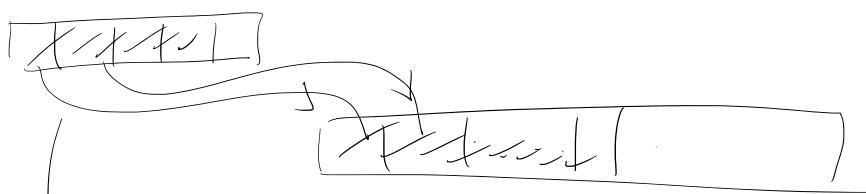


(dequeue)
front
rear
(enqueue)
only

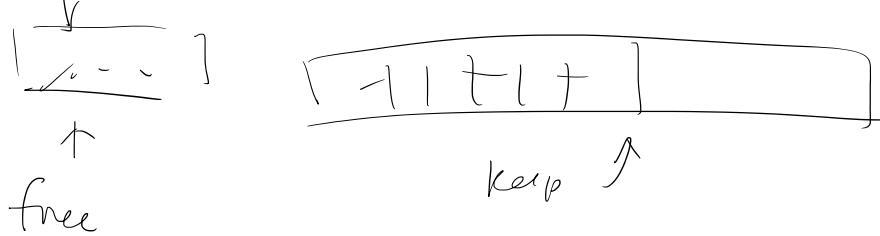
Vectors

approaches the limit, double the size of the array

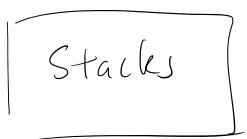
①



②

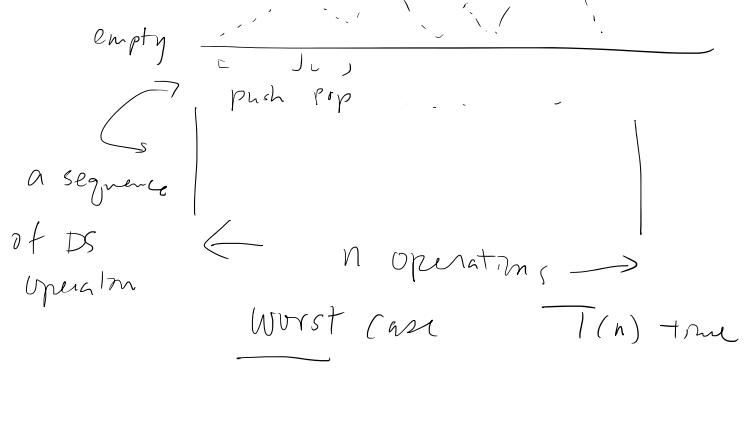


Amortized Analysis



↑ push ↑ pop

Running a program



$$\sum_{n=1}^{\infty} T(n)$$

$$\overline{T(n)} \leq 3n \quad \dots \quad \overline{T(n)} \leq c \cdot n$$

↑
constant

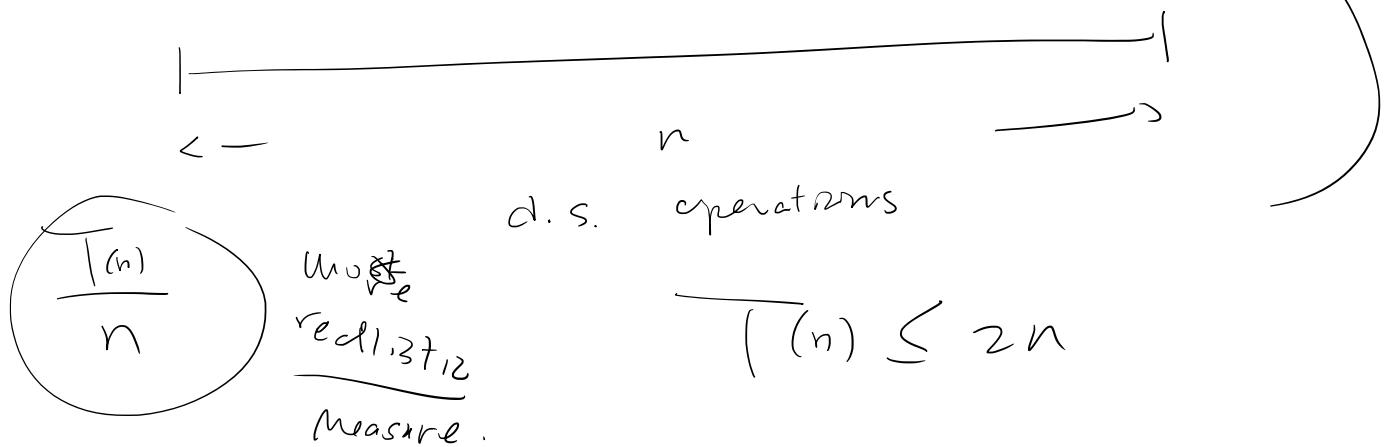
$$\overline{T(n)} \approx c$$

$$\frac{\overline{T(n)}}{n} \approx c_{\infty}$$

$$\frac{\overline{T(n)}}{n} = \Theta(1) \quad \text{constant}$$

Stacks (CLRS Ch. 17.1)

push pop multi pop



9/13/2016 (CIS 477)

Tuesday, September 13, 2016 9:35 AM

$$1+2+\dots+n-1 = \frac{n(n-1)}{2}$$

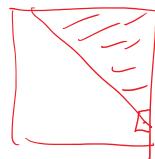
$$\text{Work} \leq \left\lceil \frac{n(n-1)}{2} \right\rceil$$

```

for ( i=1, ..., n ) {
    for ( j=1, ..., n )
        [ do something ]
}

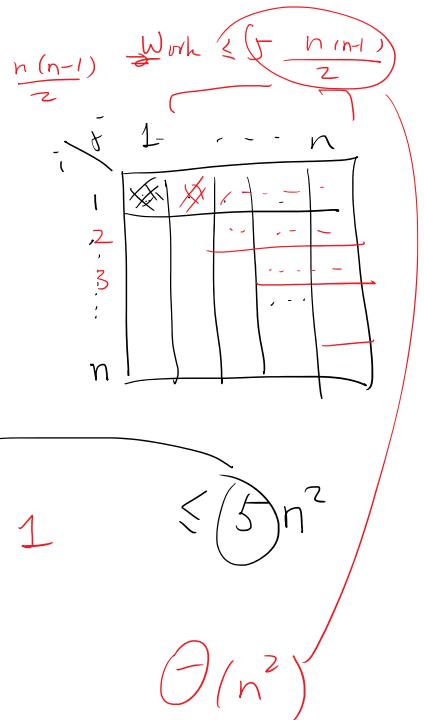
```

→



constant
of steps

$$\leq 5$$



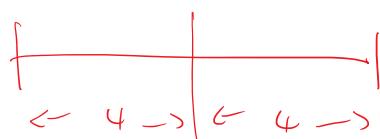
$$\text{for } (i=1 \dots n) \{ \sum_{j=i+1}^n 1 \} \quad \sum_{i=1}^n \left(\sum_{j=i+1}^n 1 \right)$$

HW.

$$\sum \sum \sum \circ$$

Merge Sort : Divide & Conquer. & "Merge"

$$T(8) = T(4) + T(4)$$



$$+ \text{ Merge Step} = 2T(4) + \text{Merge Step}$$

Recurrence tree (in the slide p. 7)

$$T(2000)$$

$$= 3T\left(\frac{2000}{4}\right)$$

$$T(n) = cn^2 + T\left(\frac{n}{4}\right)$$

$$T \sim \Theta(1) \quad n \text{ is small} \quad T\left(\frac{n}{4}\right)$$

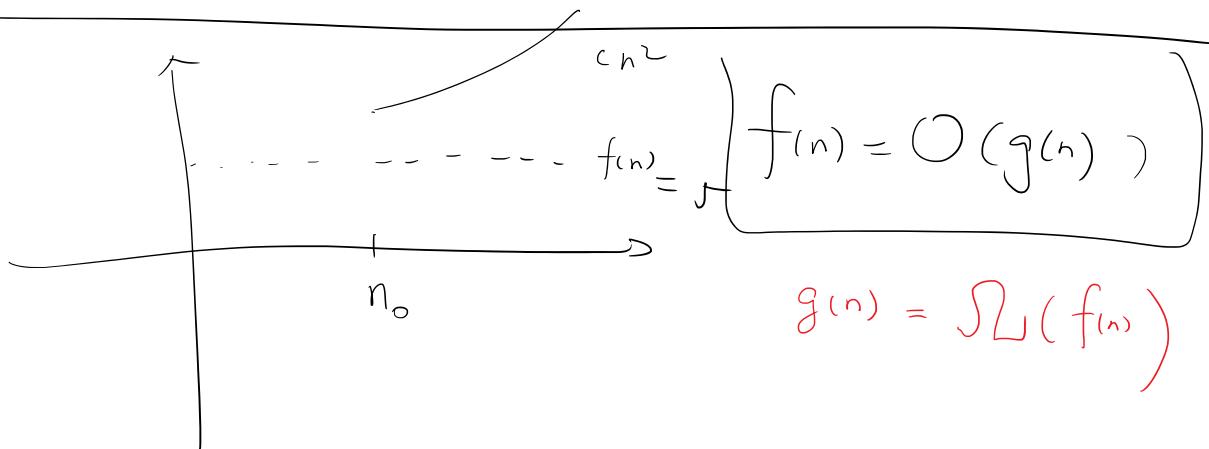
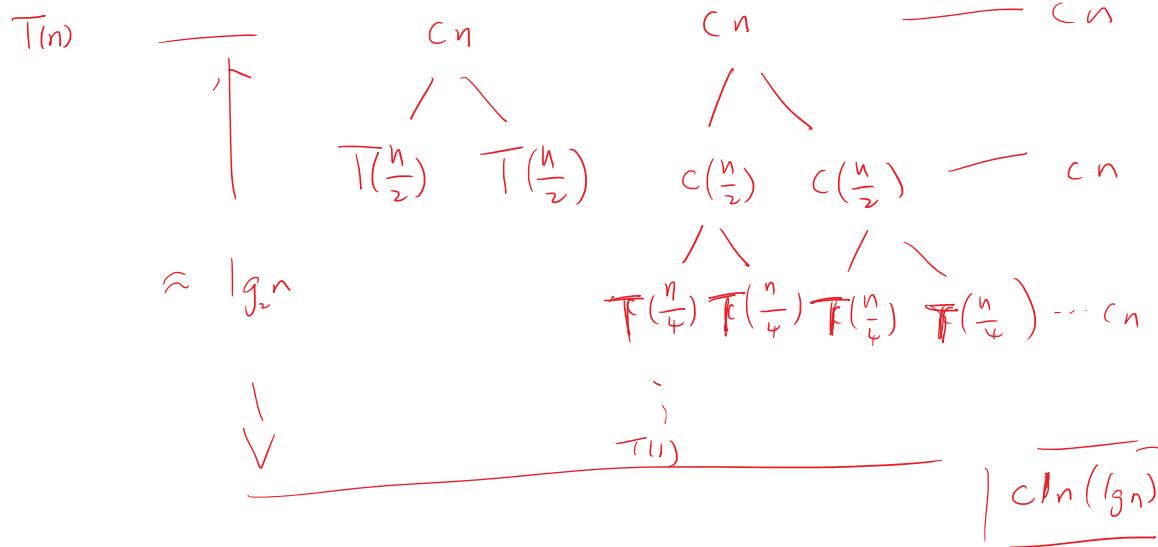
$$= 3 T\left(\frac{2000}{4}\right)$$

$$+ c(2000)^2$$

$$= 3 \left[3 T\left(\frac{2000}{16}\right) + c \left(\frac{2000}{4}\right)^2 \right] + c(2000)^2$$

Recurrence Tree for Merge Sort

$$T(n) = 2 T\left(\frac{n}{2}\right) + \Theta(c n)$$

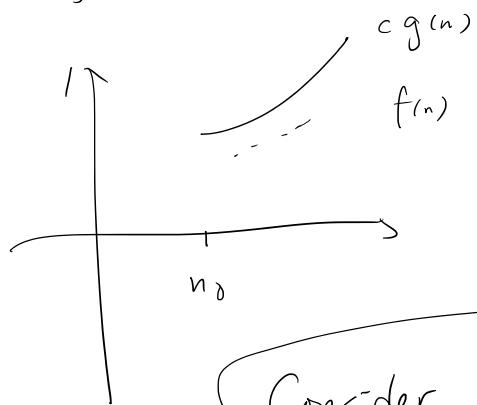


$$\cap \dots \cap (a_{n_0})$$

$$f(n) = \sum g(n)$$

$$f(n) = O(g(n))$$

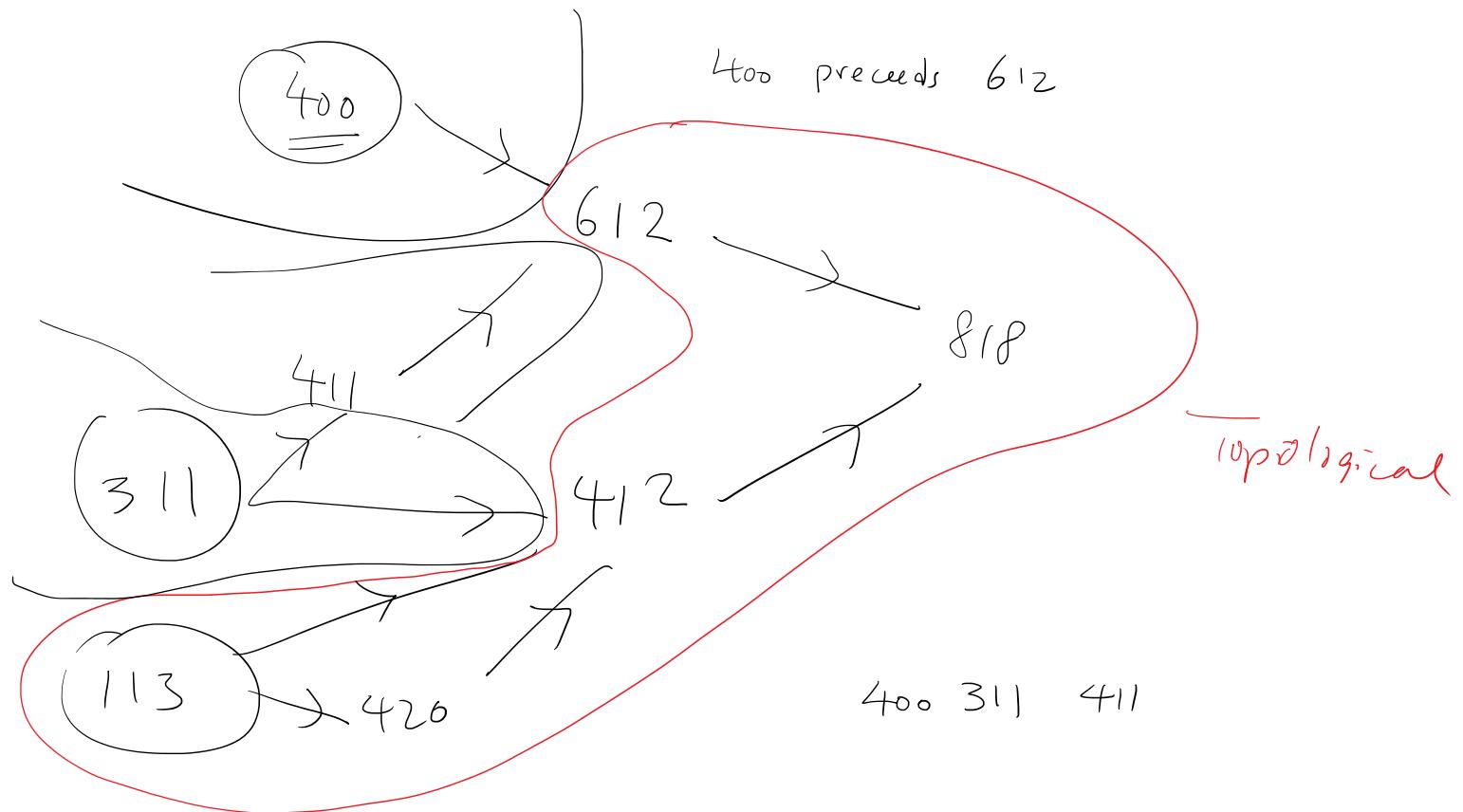
$$f(n) \neq \Omega(g(n))$$



Consider $n \geq \max(n_0, n_1)$

9-14-2016

Wednesday, September 14, 2016 6:43 PM



priority

Queue

FIFO

a b c d e

↑
front

↑
rear

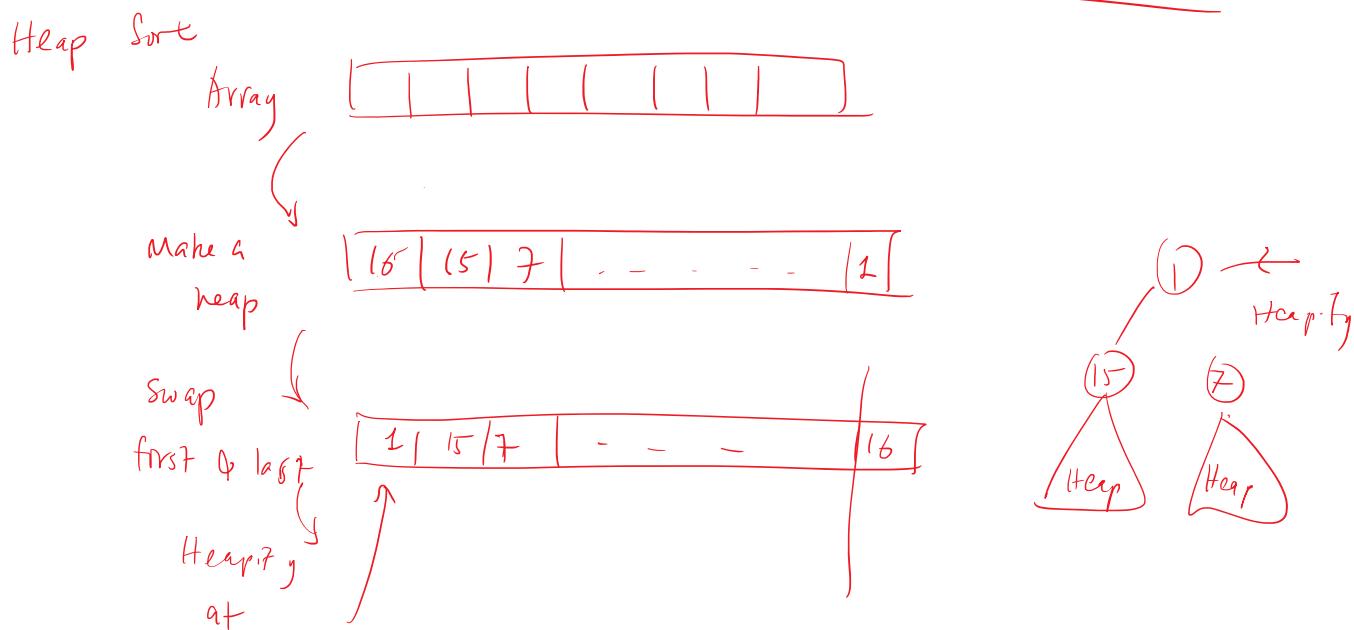
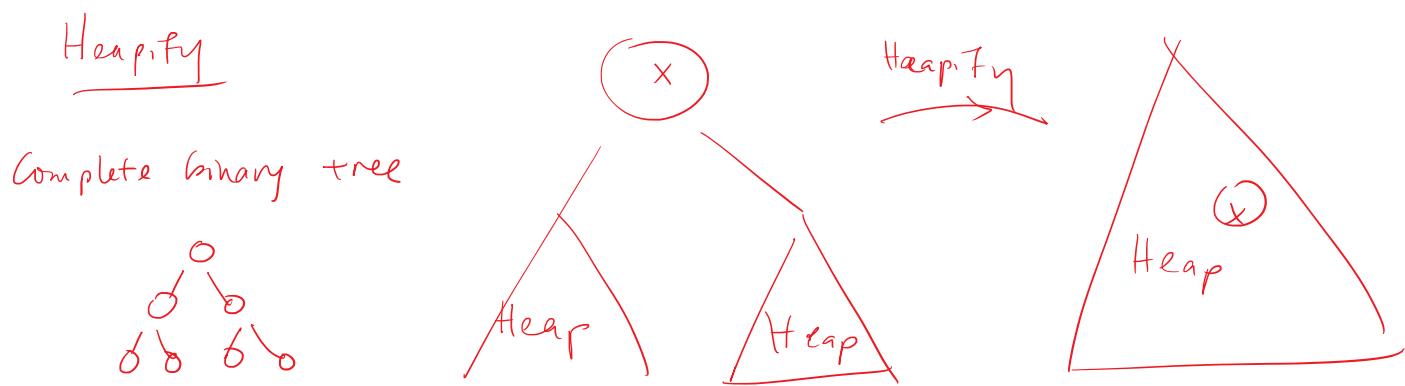
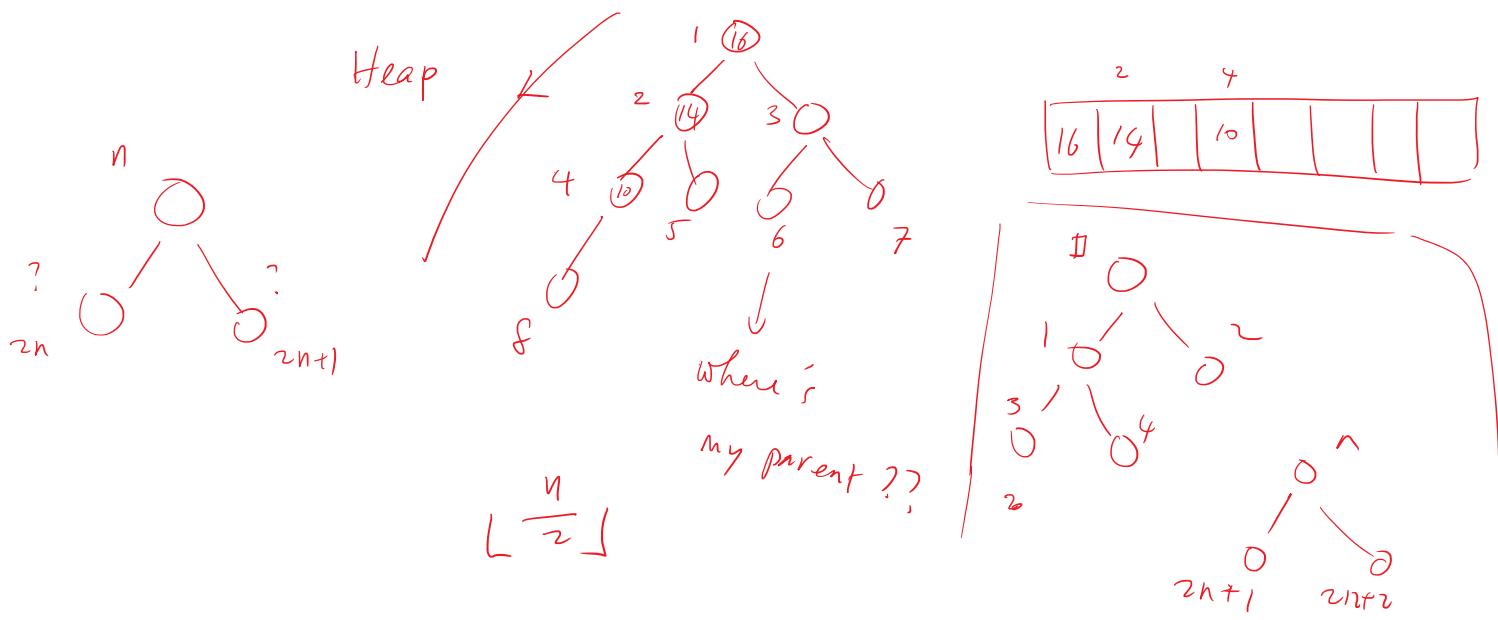
→ [a] < [b] < [c] < [d] < [e]
↓
front

[f]

↑
rear

Priority Queue

May use "Heap" to implement



$\therefore \hookrightarrow$ Complete binary tree of n nodes

$$\text{height} = \sim \lg_2 n ?$$

$$2^h = n$$

*Module: Elementary Data Structures**CSE 674 Advanced Data Structures and Algorithms**Class Activity: A data structure for topological sorting**Question*

Consider the following table, which record a number of college courses and their pre-requisites.

Course	Pre-requisites
612	400, 411
818	412, 612
411	311
412	113, 311, 420
420	113

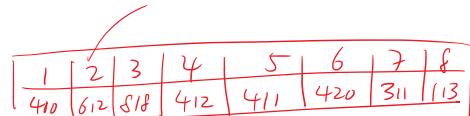


Specify a partial order

Design a data structure and use it to compute an order of taking these courses so that the pre-requisite requirements are all met.

Answer

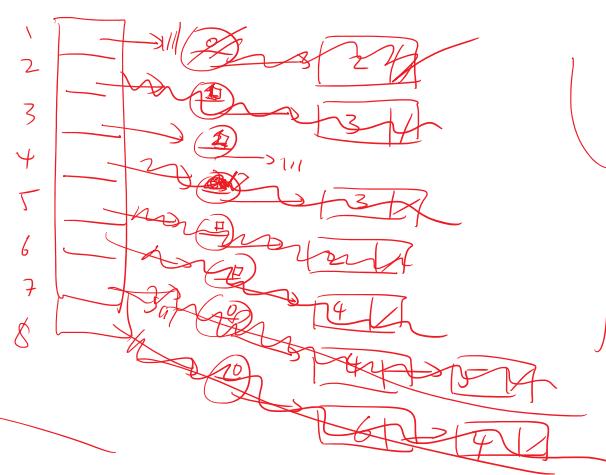
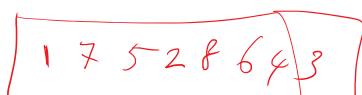
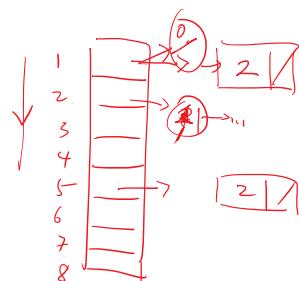
① Simplify.



②

612 requires 400
612 .. 411

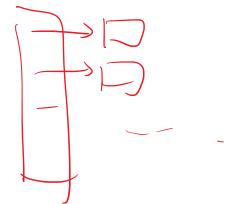
400 → 612
411 →



Answer:

M

succ.-pred relations

 $O(m)$ 

HW 1 :

Q1

$i \setminus j$	1	2	3	4	5
1	2(4)	3(3)	4(2)	5(1)	
2		4(2)	5(1)	6	
3			6	7	
4				8	
5					

for ($i = 1 \dots n$)for ($j = i+1 \dots n$) $n=5$ $i+j-1$

$n=6$

$i \setminus j$	1	2	3	4	5	6
1	2(5)	3(4)	4(3)	5(2)	6(1)	
2		4(3)	5(2)	6(1)		
3			6(1)			
4						
5						
6						

$R_k = \frac{2k(2k-1)}{2}$

$R_1 + \dots + R_k$

$R_k = 1+2+\dots+2k-1$

$R_2 = 1+2+3$

$n = 2k$

$k = \frac{n}{2}$

$\uparrow [1 2 3 4 \dots 2k-1]$

\downarrow

$1 2 3 4 \dots 2k-3$

$1 2 3 4 \dots 2k-5$

\downarrow

$$\text{Ans} = R_1 + \dots + R_K$$

$$\text{Ans} : \sum_{i=1}^k i(2i-1) = \sum_{i=1}^k i - \sum_{i=1}^k i^2$$

$$R_k = \frac{2k(2k-1)}{2}$$

Recurrence

Recurrence

- (1) Substitution Method [- -] ← Solve on
in this class
- [(2) Recursion Tree [Guess]]
- [(3) Master Thm [Apply check]]

Example for Merge Sort

$$f(n) = \Theta(n) \quad a = b = 2$$

Master Thm, which case matches?

? By Master Thm

$$\log_b a = 1. \quad \therefore T(n)$$

$$f(n) = \Theta(n^{\log_b a}) = \Theta(n^1) = \Theta(n)$$

$$f(n) = 1$$

$$a, b = 2.$$

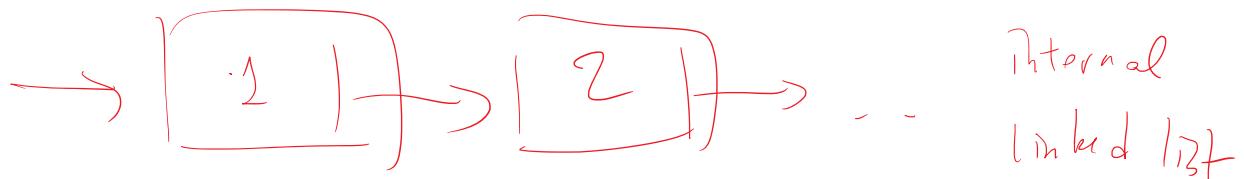
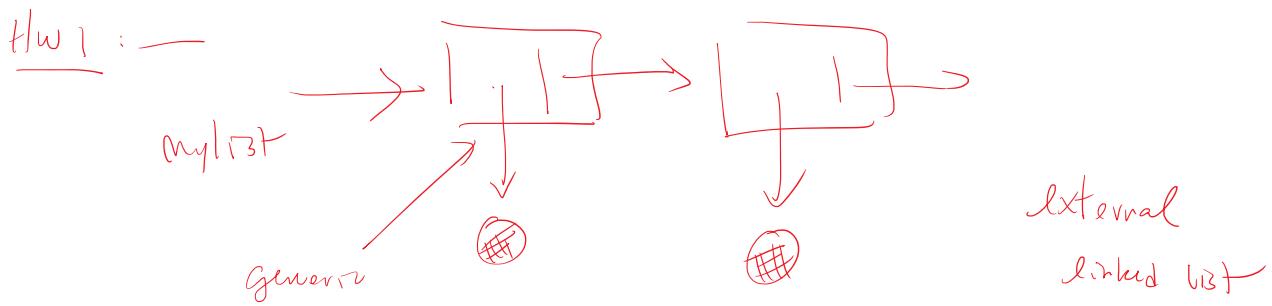
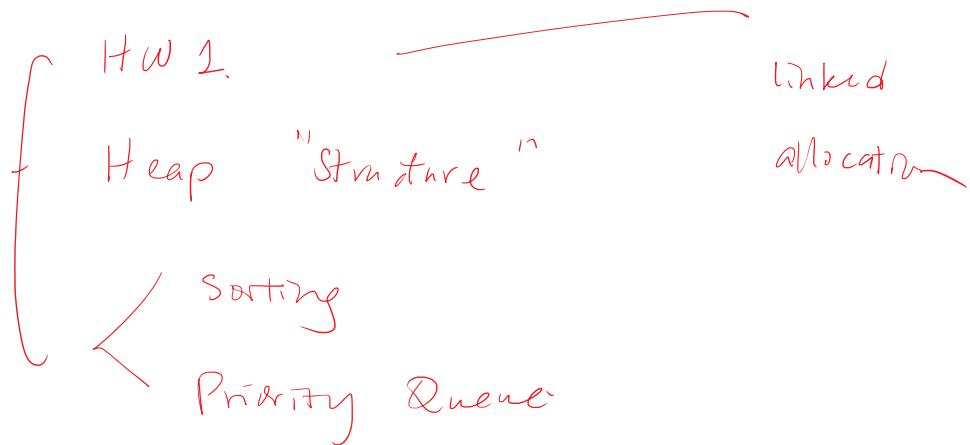
$$T(n) = 2T\left(\frac{n}{2}\right) + 1$$

Case 1

$$T(n) = \Theta(n)$$

Q-19-2016

Monday, September 19, 2016 6:52 PM

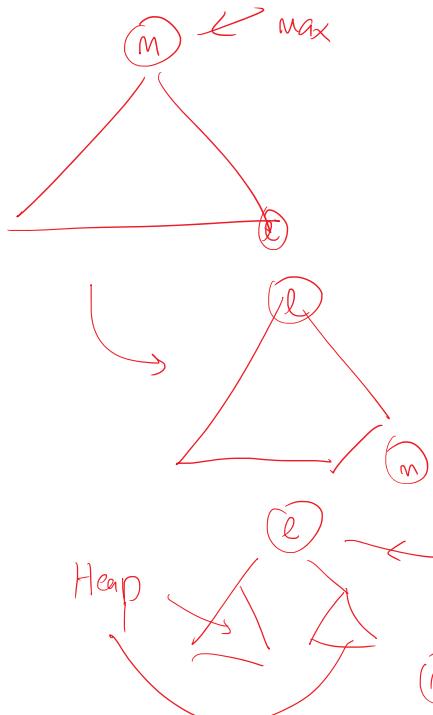


HeapSort ($A[1, \dots, n]$)

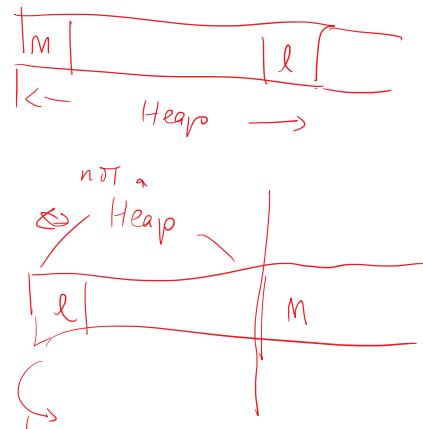
$O(n)$ 1 Build a Heap

- time
(from Analysis)

$\sim n \lg n$



$n > l$



HeapSort

3 $O(n \lg n)$

- time.

A.D.T

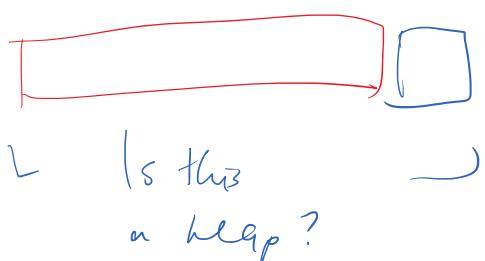
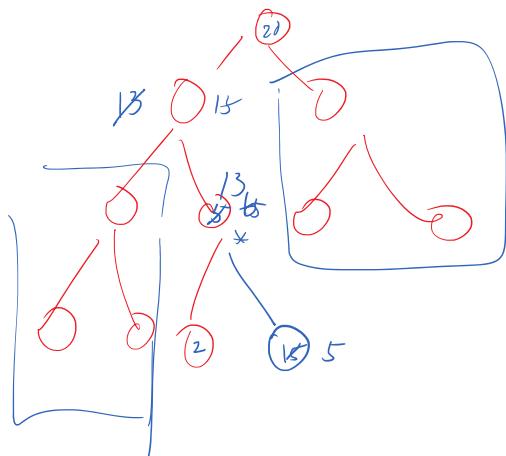
Queue

Engineer
+
dequeue
remove

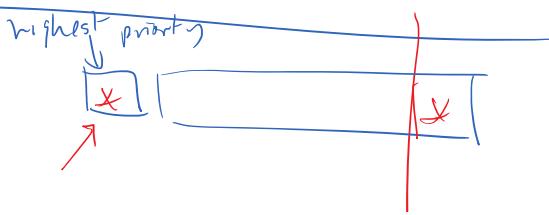
Priority Queue

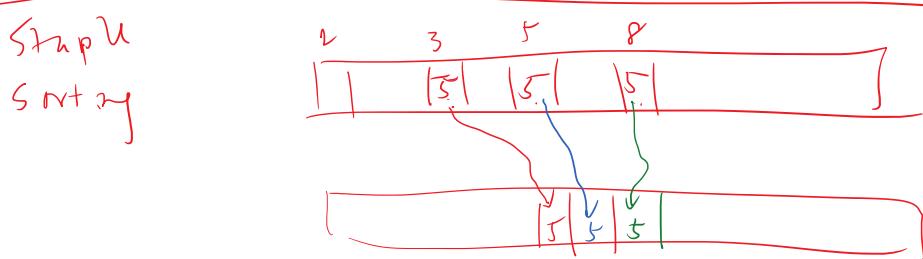
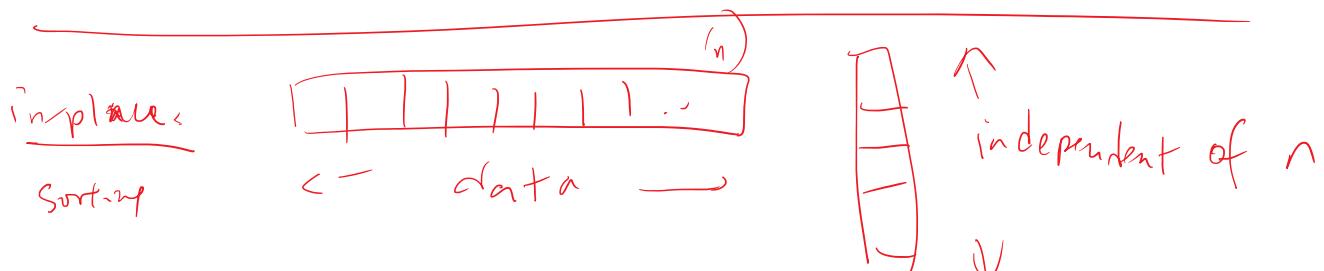
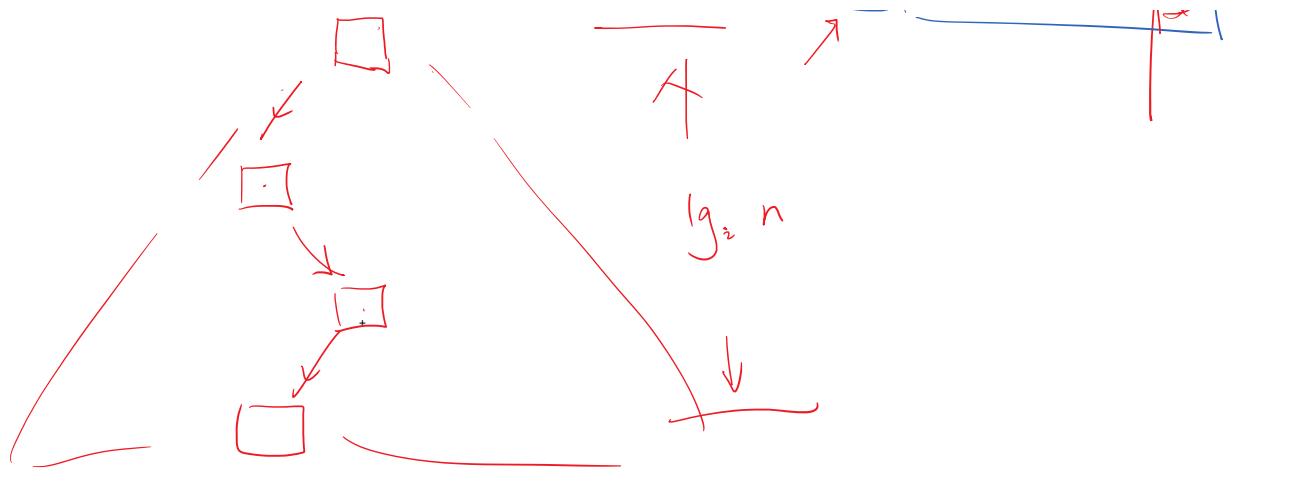


Insert



degree from a PQ





9-20/ CIS 477

Tuesday, September 20, 2016 9:24 AM

2016

January

S	M	T	W	Th	F	S
			1	2		
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30
31						

February

S	M	T	W	Th	F	S
		1	2	3	4	5
7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29					

March

S	M	T	W	Th	F	S
		1	2	3	4	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30	31		

April

S	M	T	W	Th	F	S
			1	2		
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30

May

S	M	T	W	Th	F	S
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				

June

S	M	T	W	Th	F	S
		1	2	3	4	
5	6	7	8	9	10	11
12	13	14	15	16	17	18
19	20	21	22	23	24	25
26	27	28	29	30		

July

S	M	T	W	Th	F	S
			1	2		
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30
31						

August

S	M	T	W	Th	F	S
		1	2	3	4	5
7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29	30				

September

S	M	T	W	Th	F	S
		1	2	3		
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	

October

S	M	T	W	Th	F	S
			1			
2	3	4	5	6	7	8
9	10	11	12	13	14	15
16	17	18	19	20	21	22
23	24	25	26	27	28	29
30						

November

S	M	T	W	Th	F	S
		1	2	3	4	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30			

December

S	M	T	W	Th	F	S
		1	2	3		
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

Tentative
dates

EXAM 3 : Dec 1 , Dec 8 & 6

EXAM 2 : Nov 3

EXAM 1 : Oct 6 , Oct 11

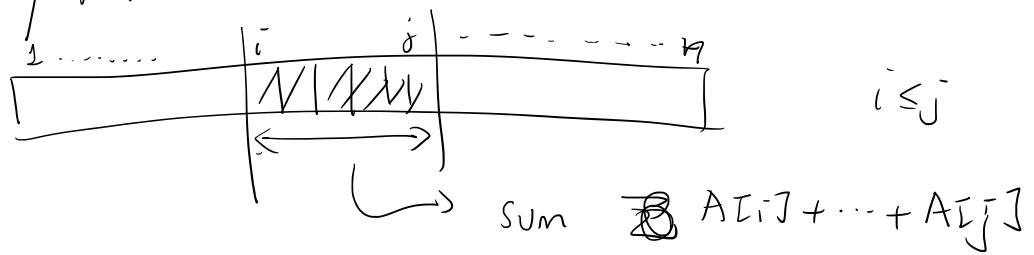
Today Topic: —

Divide & Conquer Paradigm.

Recall: "Recurrence" + "Master Thm"

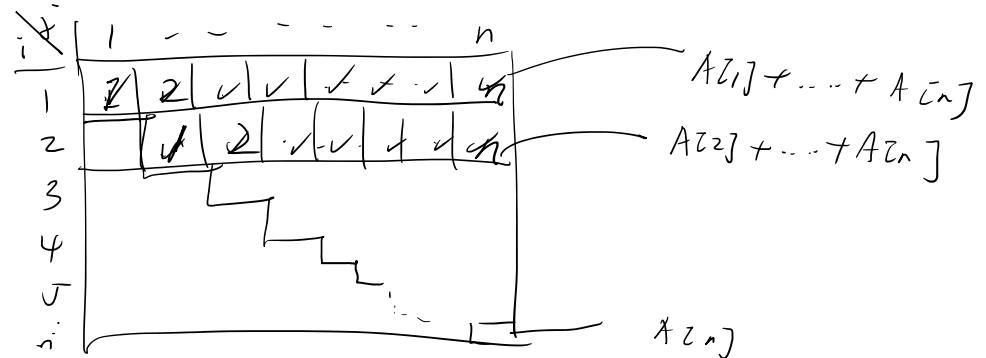
Analysis of Alg using

Max. Subarray Problem



Brute Force

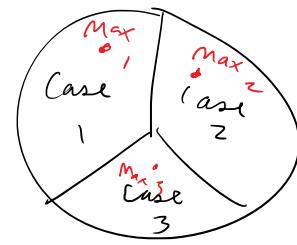
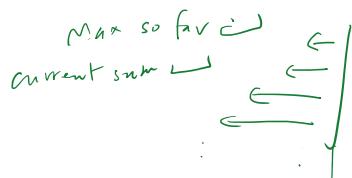
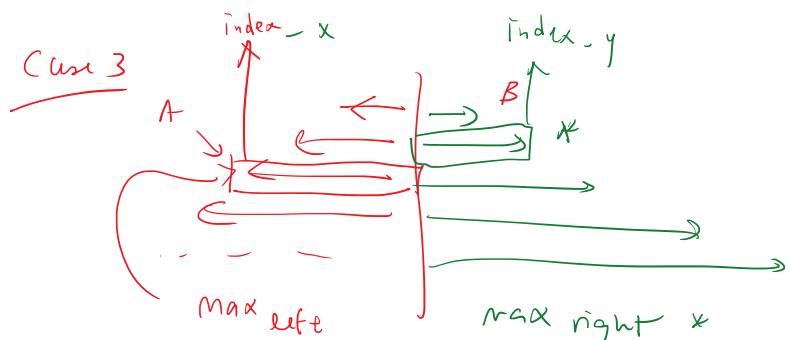
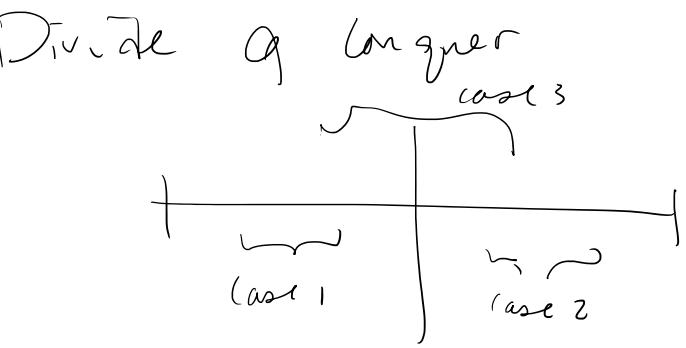
$$\sum_{j=1}^n i(j+1)$$



Divide & Conquer
case 3

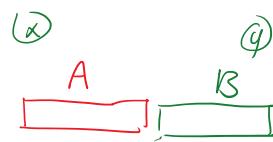


Divide & conquer



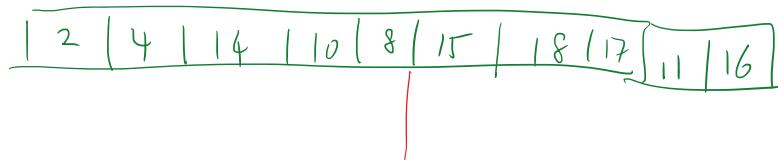
Max = Maximum of

Max 1, Max 2
max 3



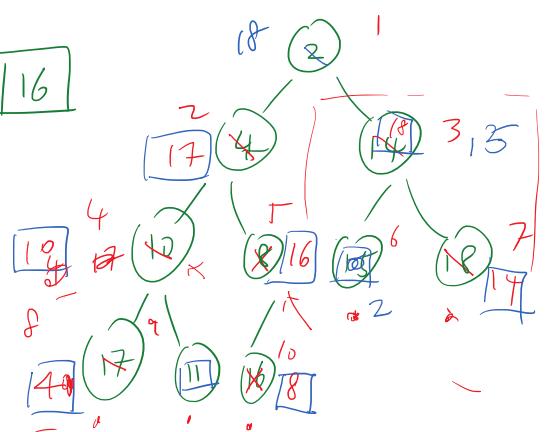
$[2, 4, 14, 10, 8, 15, 18, 17, 11, 16]$

$8, 15, 18, 17,$
 $11, 16]$

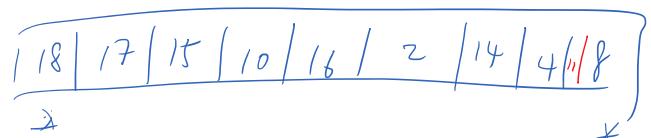


Max Heap?

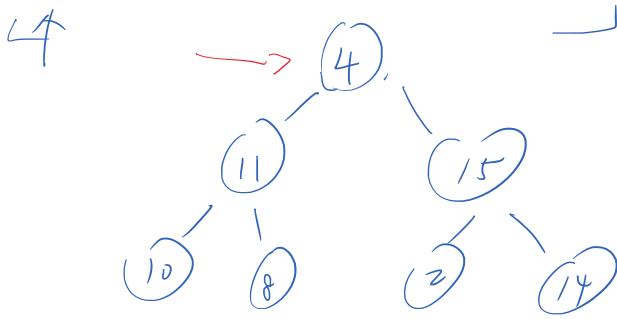
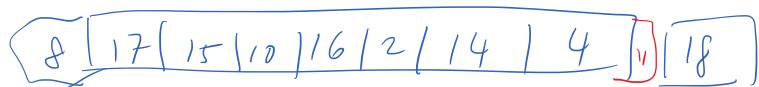
Step 1: Build Heap



$$\left\lfloor \frac{n}{2} \right\rfloor$$

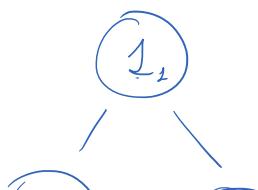
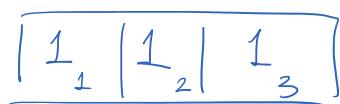


Step 2

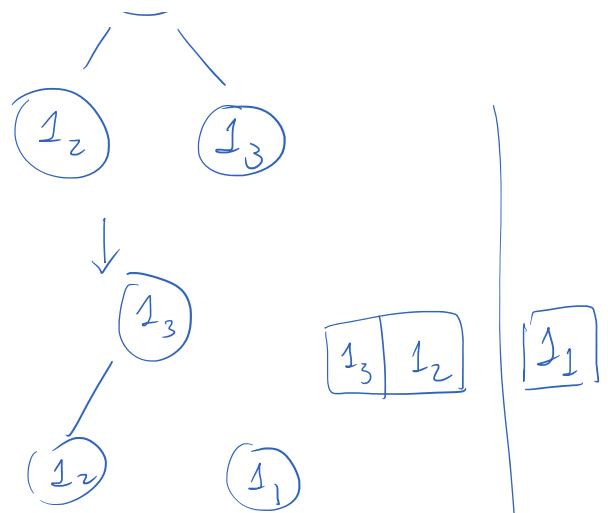


18

Heap Sort \Rightarrow not stable

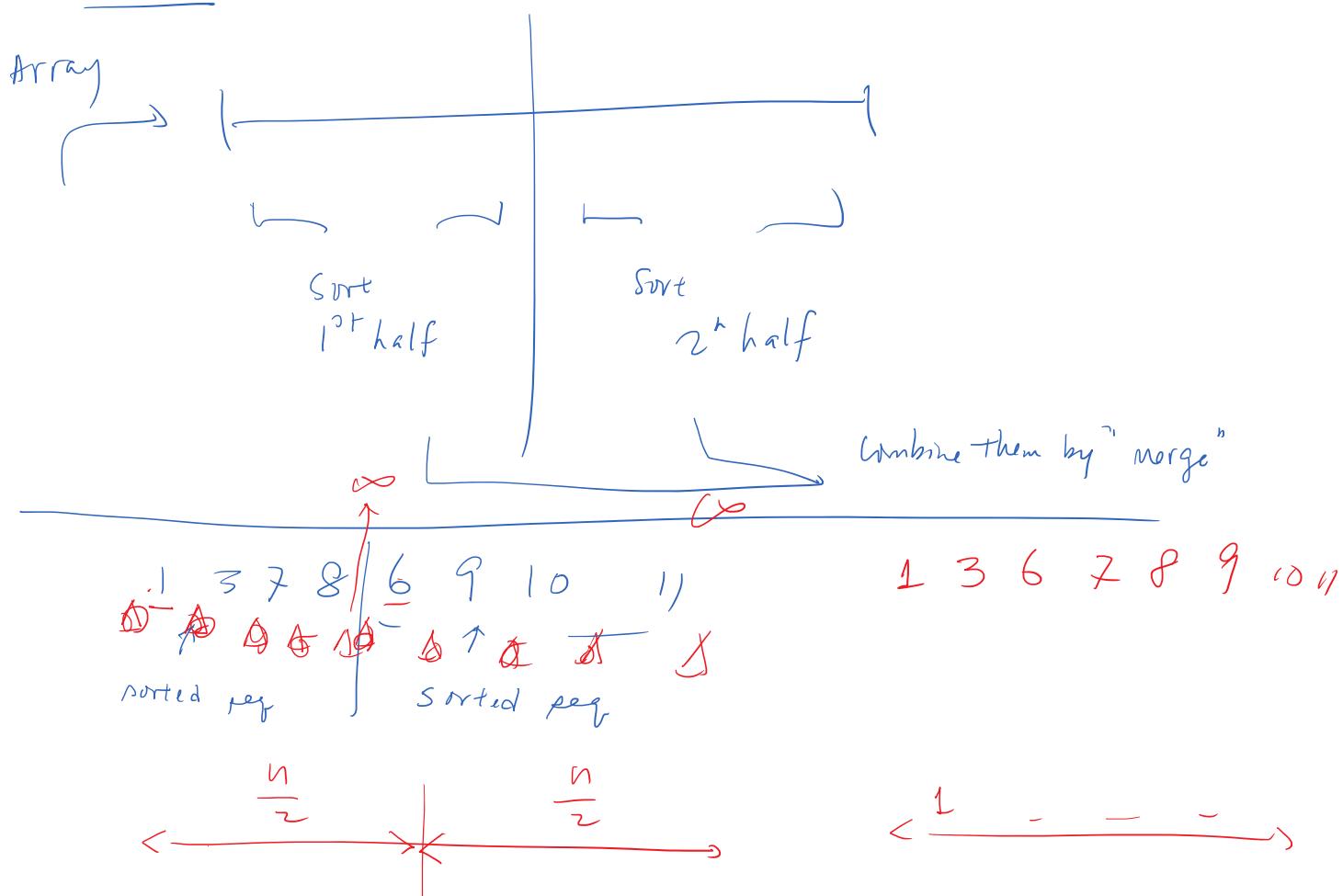


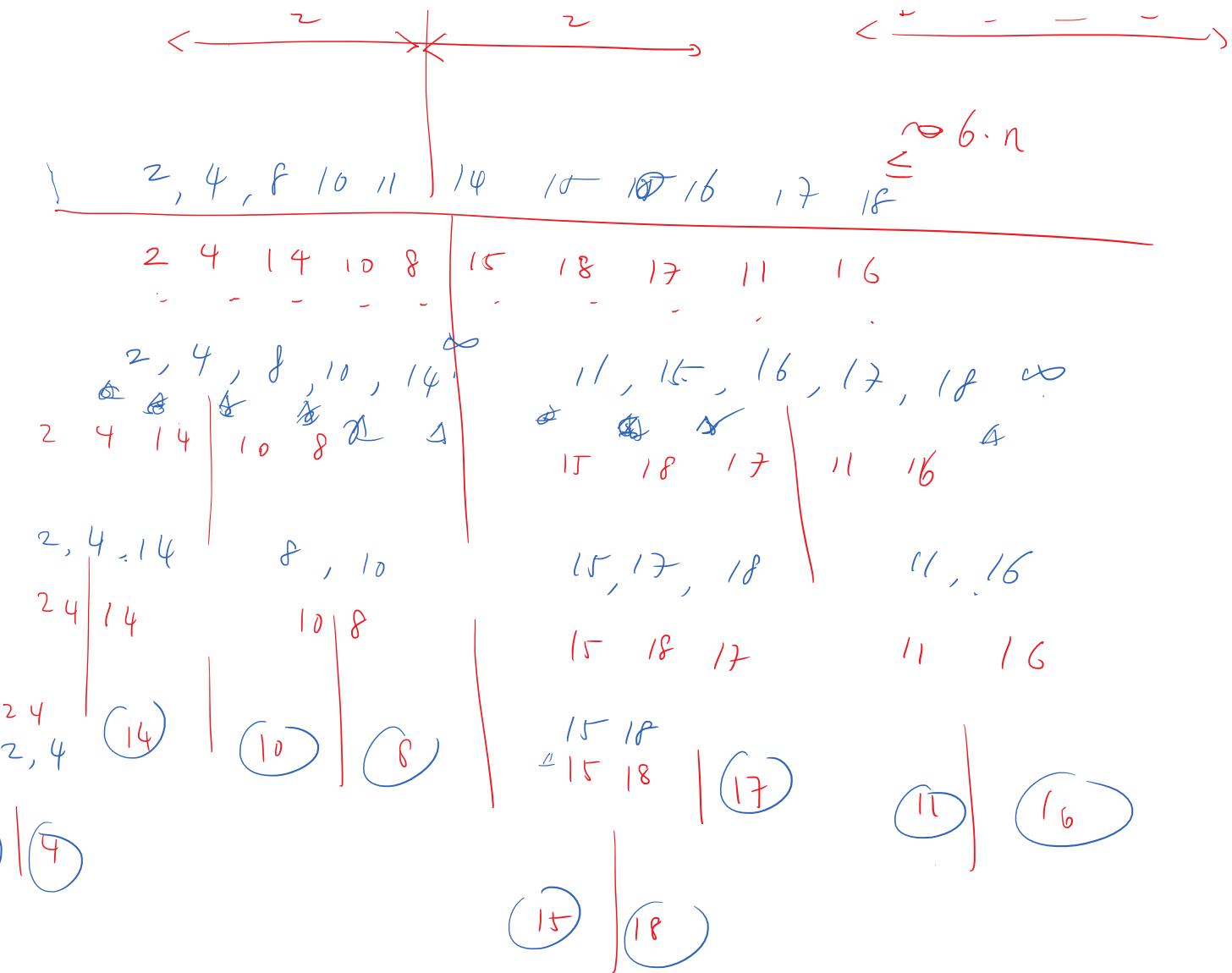
1 2 3 2 1 3



Merge Sort

(divide & conquer)





for divide & conquer alg:—

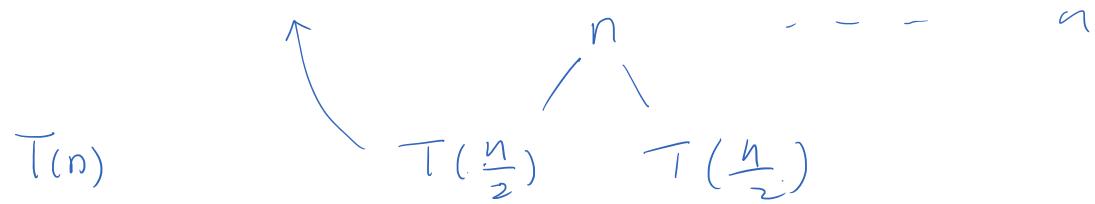


Apply the method
to a subproblem
of then

$$T\left(\frac{n}{b}\right) + \dots + T\left(\frac{n}{b}\right) + T\left(\frac{n}{b}\right)$$

↙ a subproblems ↘

$$\overline{T}(n) = \begin{cases} 1 & n \leq 1 \\ 2 \overline{T}\left(\frac{n}{2}\right) + n & n > 1 \end{cases}$$



1. Hand in HW 2 (Now) to Sid
2. "Job Fair"
3. "Orange Success"
4. "Divide & Conquer"

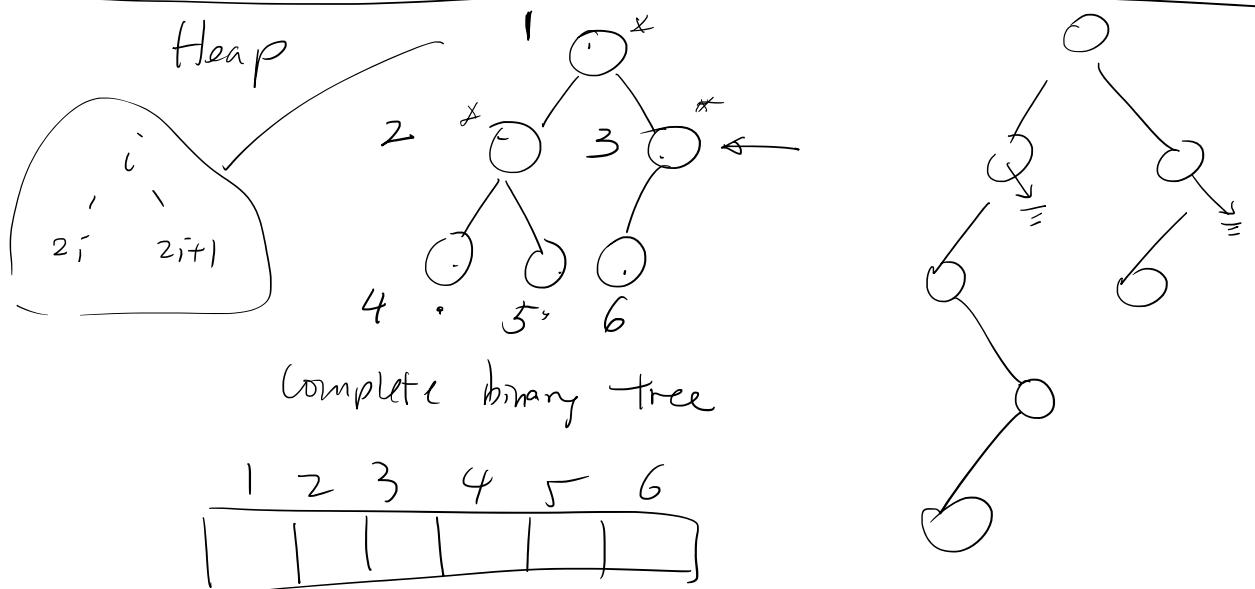
Example: Quicksort

$$\begin{aligned}
 \overline{T}(n) &= \overline{T}(n-1) + \Theta(n) \\
 \overline{T}(n) &= \Theta \overline{T}(n-1) + c_n \\
 &= \overline{T}(n-2) + c'(n-1) + c(n) \\
 &= \overline{T}(n-3) + c''(n-2) + \\
 &\quad c'(n-1) + \\
 &\quad c_n \\
 \therefore \overline{T}(n) &= \dots = \Theta(n^2) \\
 &\text{(worst case)}
 \end{aligned}$$

Quicksort worst case: $\Theta(n^2)$

\hookrightarrow Average case: $\Theta(n \lg n)$ requires new techniques

Heap — Θ^*

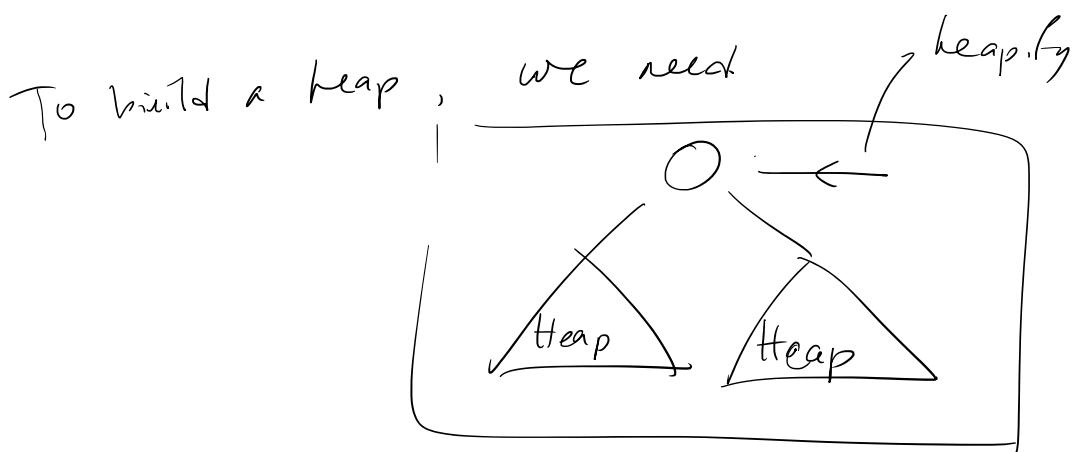


Heap

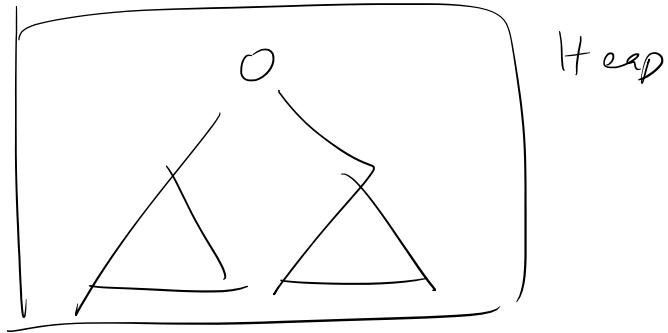


satisfy the max heap property
for any non-left node

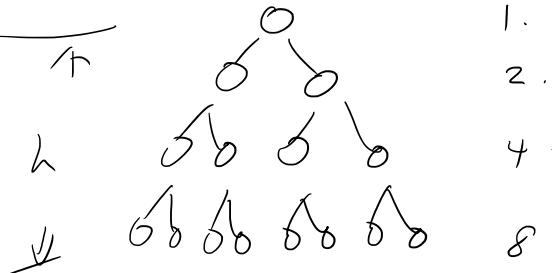
$$n \geq r$$

$$n \geq k$$


After applying heapify.



About
Comp level
binary tree



- 1.
2. a complete binary tree
3. of height h
4. has at most

$$1 + r + r^2 + \dots + r^h \\ = \underline{r^{h+1} - 1}$$

$$1 + 2 + 2^2 + 2^3 + \dots + 2^h \\ \approx 2^{h+1} - 1$$

$$2^h \approx n \text{ nodes}$$

$$h \approx \lg_2 n$$

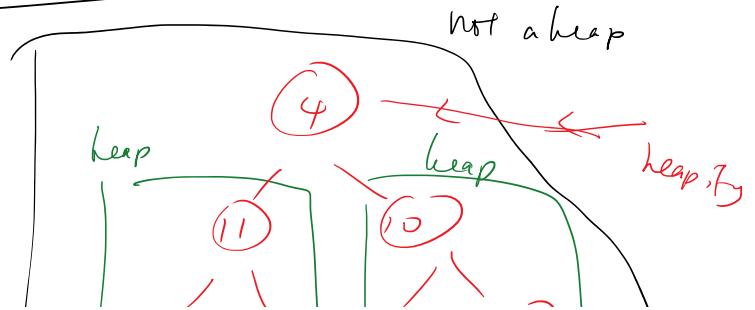
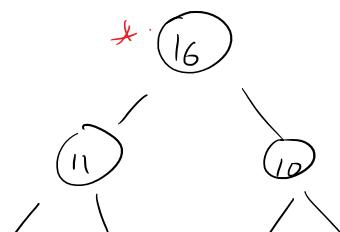
Heapsort

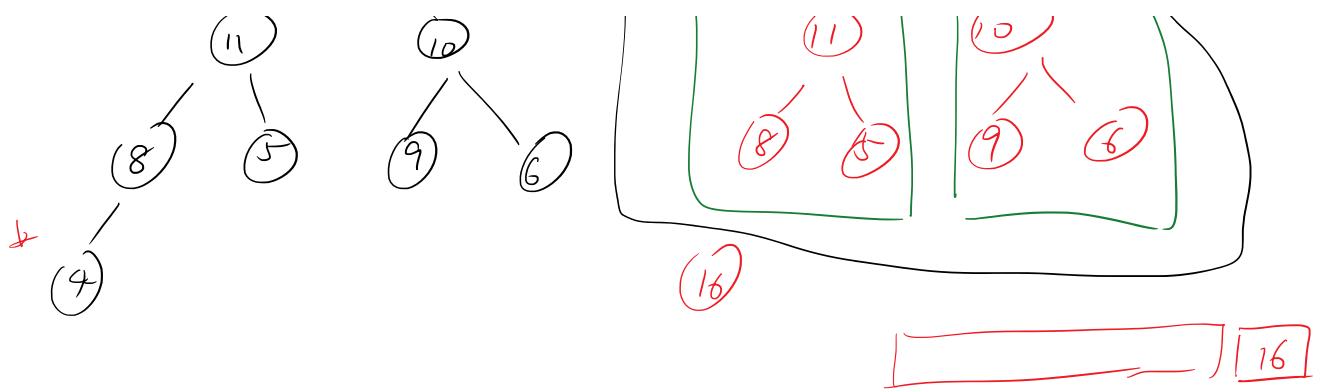
1. Build a heap.

2. "Keep heapify" at the first element

!

$r \in P$





9-26 - 2016

Monday, September 26, 2016 6:47 PM

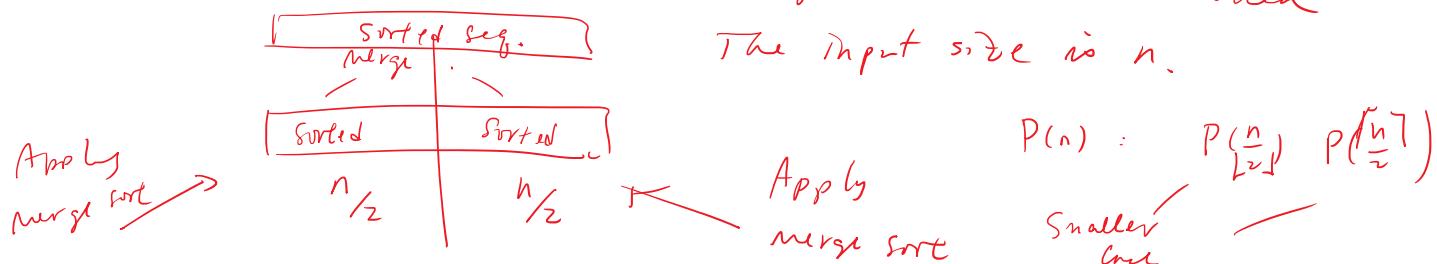
Midterm:

** divide & conquer paradigm :— **

Analysis Time Complexity ↗ Recursion tree to guess
Master Thm to verify.

Correctness { use strong induction
 as a guideline

Merge Sort ~ $P(n)$: Merge sort is correct when



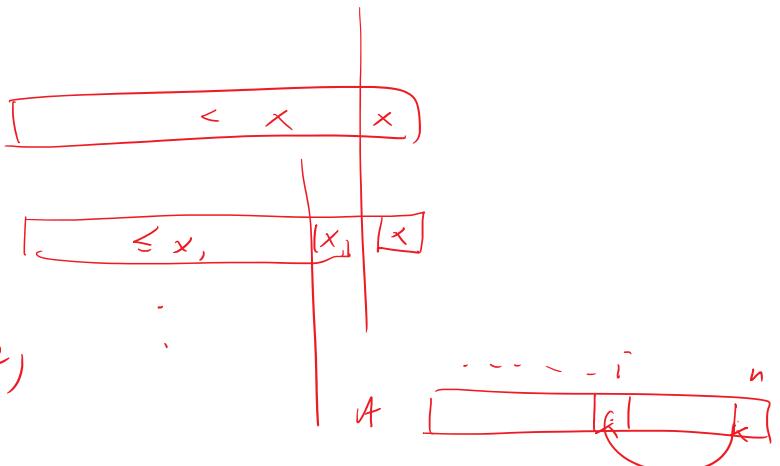
Quicksort :—

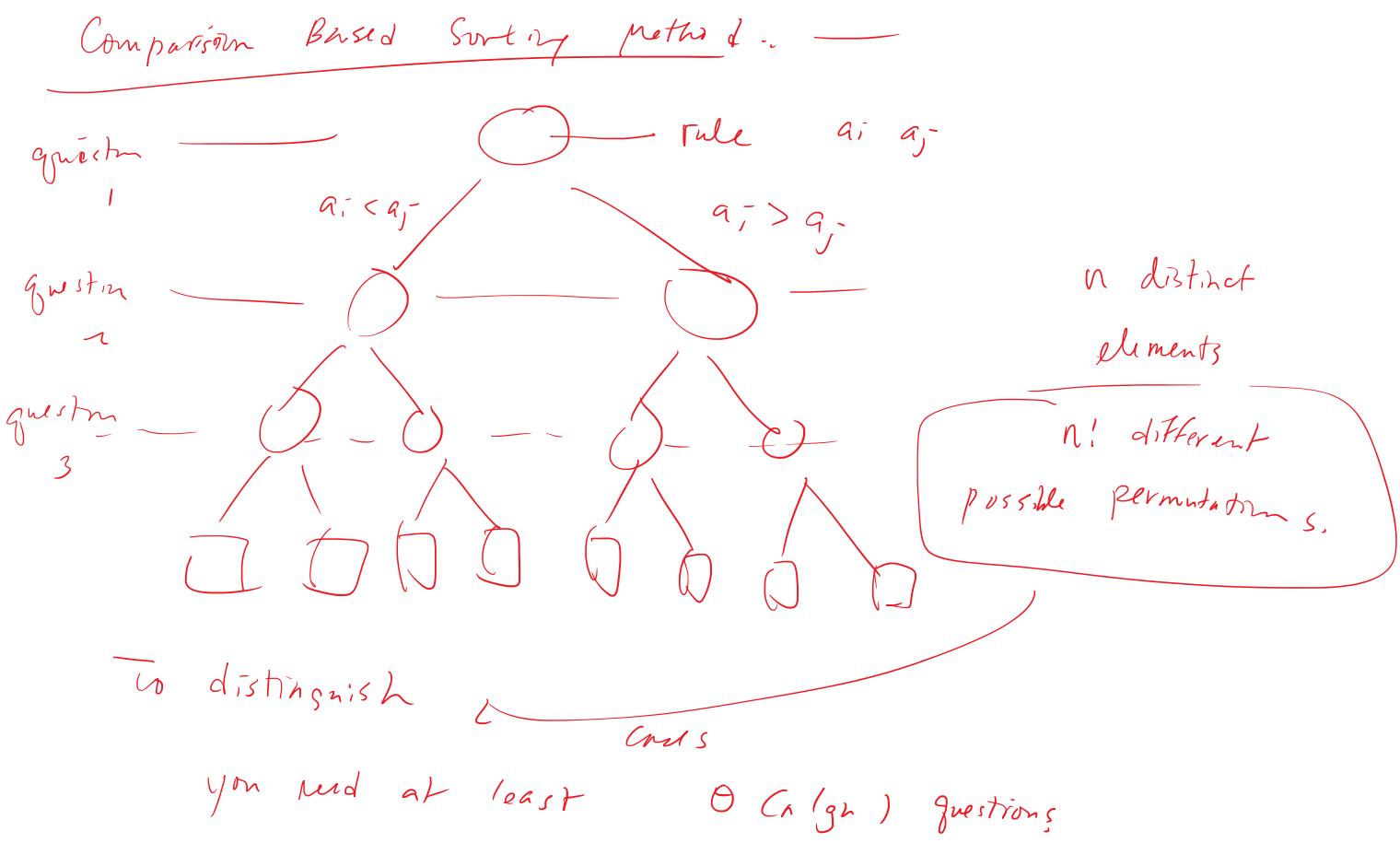
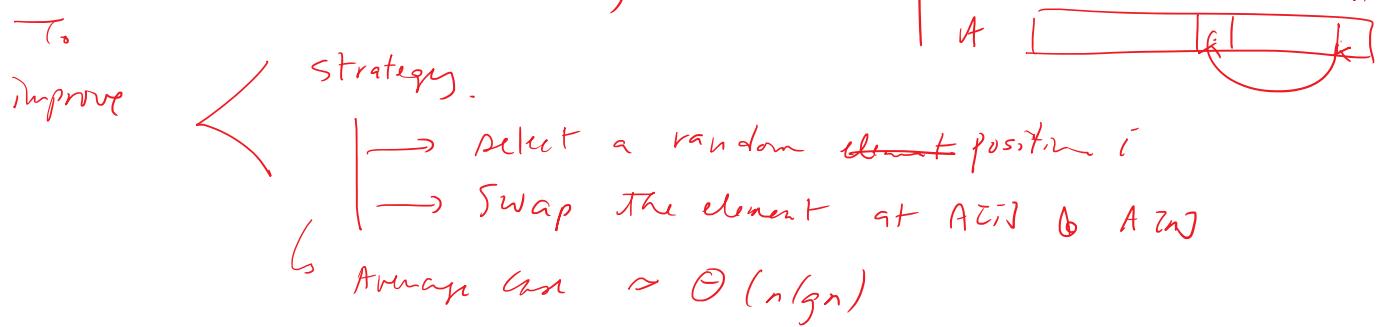
Worst Case

$$T(n) = T(n-1) + \Theta(n)$$

$$\hookrightarrow T(n) = \Theta(n^2)$$

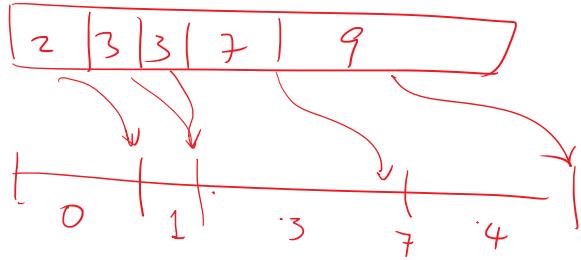
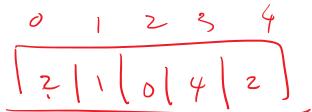
T_n ... / strategy





Counting Sort Stable

not comparison based



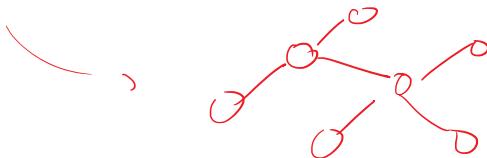
Pseudo code (given $n+k$ slide)

Analysis $\Theta(n) + \Theta(k)$

$\Theta(n+k)$

Leonardo numbers \rightarrow Smooth sort (next time)

Trees \rightarrow (Heapsort)

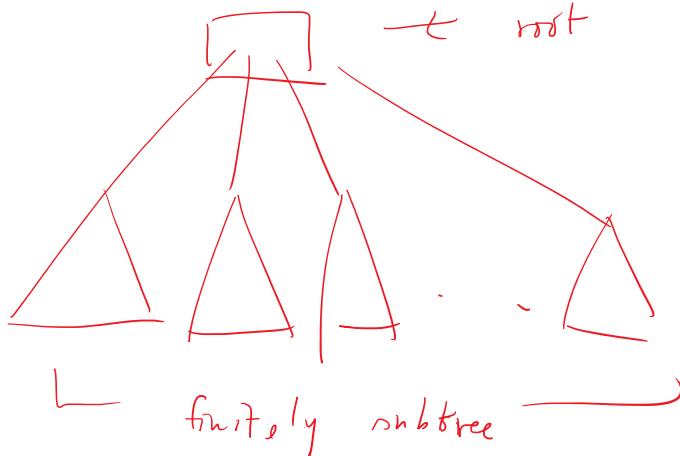


Tree Trees

n vertices
 $n-1$ edges

connected (Graph)

Rooted Tree



Base case 0 root a tree

General case

