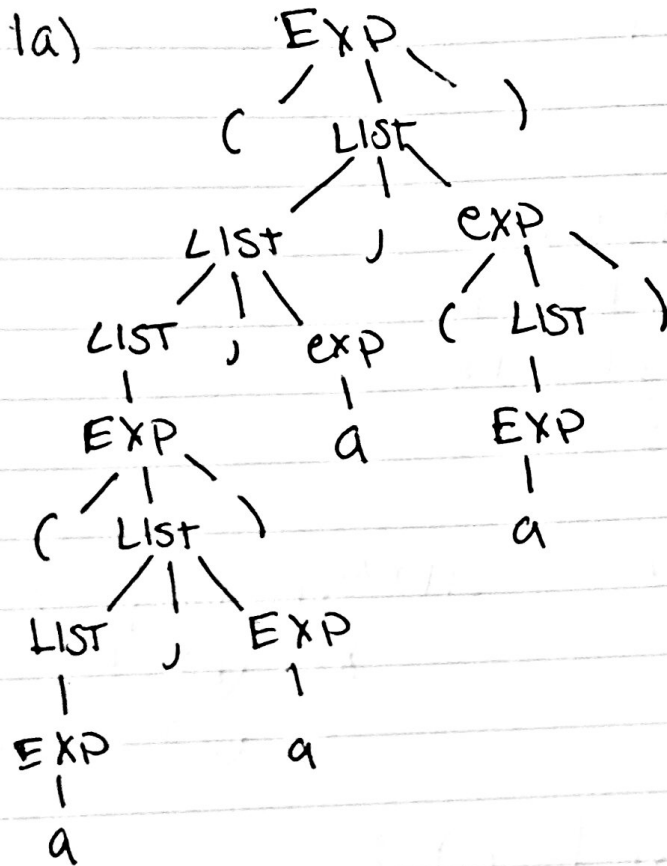
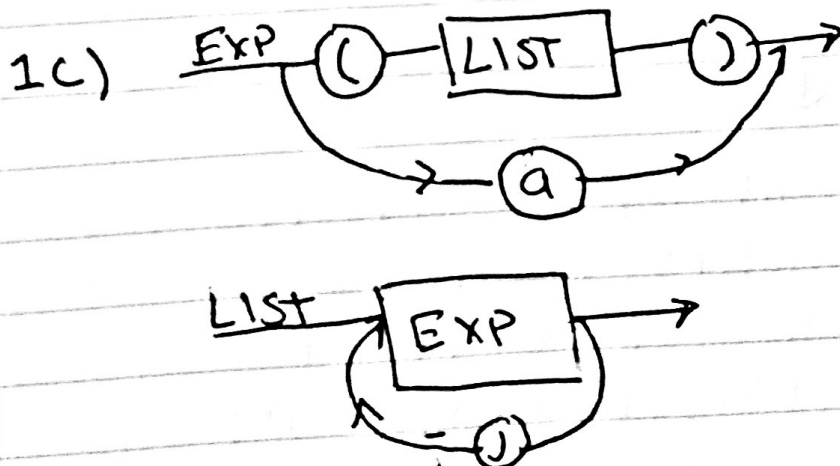


$$\begin{aligned} 1) \text{ EXP} &::= (\text{LIST}) \mid a \\ \text{LIST} &::= \text{LIST}, \text{EXP} \mid \text{EXP} \end{aligned}$$

$$\begin{aligned} \text{1d) FIRST(EXP)} &= \{a, (\} \\ \text{FIRST(LIST)} &= \{)\} \\ \text{FIRST(LIST)} &= \text{FIRST(EXP)} \\ &= \{a, (\} \\ \text{FOLLOW(LIST)} &= \{)\} \end{aligned}$$
$$\begin{aligned} \text{Follow}(\text{Exp}) &= \text{Follow}(\text{List}) \\ &= \{ \}, \{ \} \end{aligned}$$

1b) EBNF

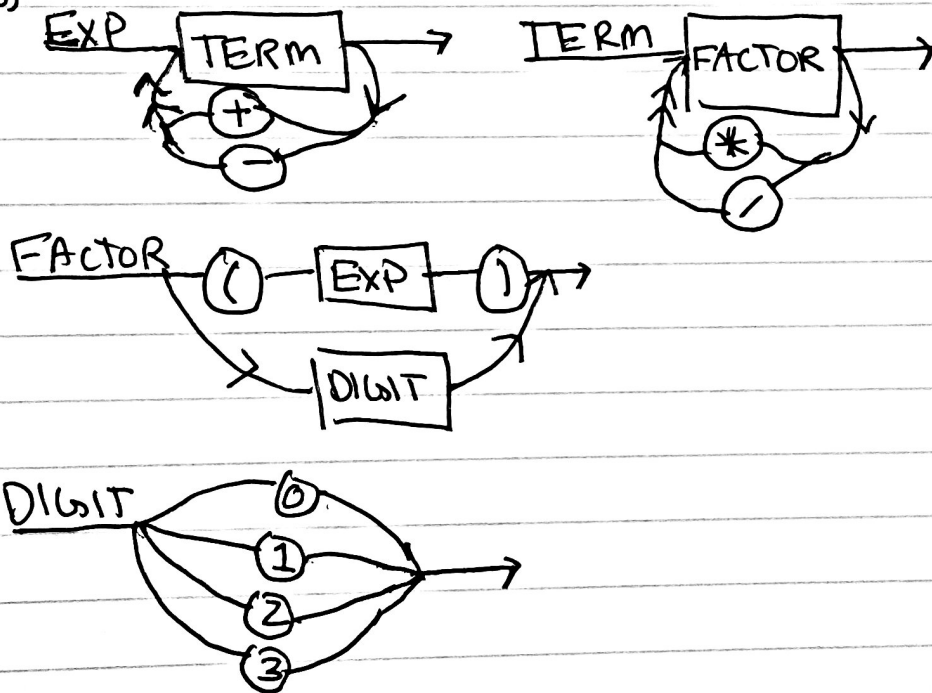
$$\begin{aligned} \text{EXP} &::= (\text{LIST}) \{a\} \\ \text{LIST} &::= \langle \text{EXP} \rangle \{, \text{EXP}\} \end{aligned}$$


2)  $EXP ::= EXP + TERM \mid EXP - TERM \mid TERM$   
 $TERM ::= TERM * FACTOR \mid TERM / FACTOR \mid FACTOR$   
 $FACTOR ::= (EXP) \mid DIGIT$   
 $DIGIT ::= 0 \mid 1 \mid 2 \mid 3$

2a) EBNF

$EXP ::= TERM \{ (+|-) TERM \}$   
 $TERM ::= FACTOR \{ (*|/) FACTOR \}$   
 $FACTOR ::= (EXP) \mid DIGIT$   
 $DIGIT ::= 0 \mid 1 \mid 2 \mid 3$

2b)



2c) First set of any two choices must not have any tokens in common.

ex)  $FACTOR ::= (EXP) \mid DIGIT$

$$FIRST(EXP) \cap FIRST(DIGIT) = \emptyset$$

• When structures are optional

ex)  $S \rightarrow B[A]D$

If A is optional, then

$$FIRST(A) \cap FOLLOW(A) = \emptyset$$

$$2d) \text{ FIRST(DIGIT)} = \{0, 1, 2, 3\}$$

$$\text{FIRST(FACTOR)} = \text{FIRST(EXP)} \cup \text{FIRST(DIGIT)}$$

$$= \{(\{ \cup \{0, 1, 2, 3\}) = \{(0, 1, 2, 3)\}$$

$$\text{FIRST(TERM)} = \text{FIRST(FACTOR)} = \{(0, 1, 2, 3)\}$$

$$\text{FIRST(EXP)} = \text{FIRST(TERM)} = \{(0, 1, 2, 3)\}$$

$$\text{FOLLOW(EXP)} = \{)\}$$

$$\text{FOLLOW(TERM)} = \{+ -\} \cup \text{FOLLOW(EXP)}$$

$$\{+ -\} \cup \{)\} = \{+ - )\}$$

$$\text{FOLLOW(FACTOR)} = \{* /\} \cup \text{FOLLOW(TERM)}$$

$$= \{* / + - )\}$$

$$\text{FOLLOW(DIGIT)} = \text{FOLLOW(FACTOR)} = \{* / + - )\}$$

$$2e) \text{ FIRST(DIGIT)} \cap \text{FOLLOW(DIGIT)} =$$

$$\{0, 1, 2, 3\} \cap \{* / + - )\} = \emptyset$$

<b>Exp()</b> <b>Term()</b> If token == '+' Match('+') Else if token == '-' Match('-') <b>Term()</b> Match(\$)	<b>Digit()</b> If token in [0, 1, 2, 3] Match(token) Else Error
<b>Term()</b> <b>Factor()</b> If token == '*' Match('*') Else if token == '/' Match('/') <b>Factor()</b> Match(\$)	<b>Factor()</b> If token == '(' Match('(') Exp() If token == ')' Match(')') else Digit() Match(\$)
• Valid Input: • 2/3\$ ✓ • (1-2)*3\$ ✓ • Invalid Input: 22-3\$ X 2/\$ X	<b>Match()</b> If token == t advanceTokenPtr else error

- This code implements both left and right associative operators. It uses different levels of non-terminals to express operator precedence.
- User Information:
  - 1) enter string using numbers 0 to 3 and the symbols +, -, \*, /, (, and )
  - 2) The end string variable will be the dollar sign (\$)
  - 3) Program determines whether or not the input string is a valid expression.