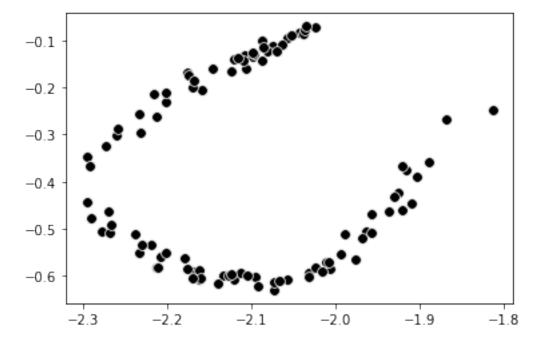
# Assignment3

May 13, 2024

### 1 13.4 Nonlinear Autoencoder Using Neural Networks

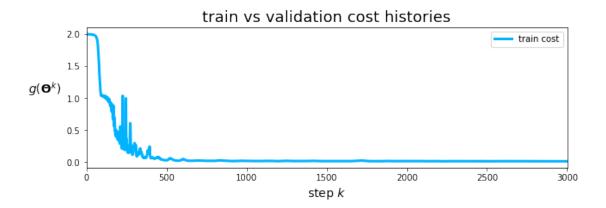


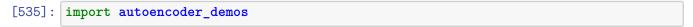
```
[525]: import os
       import sys
       module_path = os.path.abspath(os.path.join('...'))
       if module_path not in sys.path:
           sys.path.append(module_path)
[526]: import history_plotters
       import multilayer_perceptron_batch_normalized
       import multilayer_perceptron
       import normalizers
       import cost_functions
       import un_cost_functions
       import un_optimizers
[527]: import autograd.numpy as np
       class Setup:
           def __init__(self,X,**kwargs):
               # link in data
               self.x = X
               # make containers for all histories
               self.weight_histories = []
               self.train_cost_histories = []
               self.train_accuracy_histories = []
               self.val_cost_histories = []
               self.val_accuracy_histories = []
               self.train_costs = []
               self.train_counts = []
               self.val_costs = []
               self.val_counts = []
           #### define preprocessing steps ####
           def preprocessing_steps(self,**kwargs):
               ### produce / use data normalizer ###
               normalizer_name = 'standard'
               if 'normalizer_name' in kwargs:
                   normalizer_name = kwargs['normalizer_name']
               self.normalizer_name = normalizer_name
               # produce normalizer / inverse normalizer
               s = normalizers.Setup(self.x,normalizer_name)
               self.normalizer = s.normalizer
```

```
self.inverse_normalizer = s.inverse_normalizer
    # normalize input
    self.x = self.normalizer(self.x)
#### split data into training and validation sets ####
def make_train_val_split(self,train_portion):
    # translate desired training portion into exact indecies
    self.train_portion = train_portion
    r = np.random.permutation(self.x.shape[1])
    train_num = int(np.round(train_portion*len(r)))
   self.train_inds = r[:train_num]
   self.val_inds = r[train_num:]
    # define training and testing sets
    self.x_train = self.x[:,self.train_inds]
    self.x_val = self.x[:,self.val_inds]
#### define encoder ####
def choose_encoder(self,**kwargs):
    feature_name = 'multilayer_perceptron'
   if 'name' in kwargs:
        feature_name = kwargs['feature_name']
   transformer = 0
    if feature_name == 'multilayer_perceptron':
        transformer = multilayer_perceptron.Setup(**kwargs)
    elif feature_name == 'multilayer_perceptron_batch_normalized':
        transformer = multilayer_perceptron_batch_normalized.Setup(**kwargs)
    self.feature_transforms = transformer.feature_transforms
    self.initializer_1 = transformer.initializer
# form decoder
def choose_decoder(self,**kwargs):
    feature_name = 'multilayer_perceptron'
    if 'name' in kwargs:
        feature_name = kwargs['feature_name']
    transformer = 0
    if feature_name == 'multilayer_perceptron':
        transformer = multilayer_perceptron.Setup(**kwargs)
    elif feature_name == 'multilayer_perceptron_batch_normalized':
        transformer = multilayer_perceptron_batch_normalized.Setup(**kwargs)
    self.feature_transforms_2 = transformer.feature_transforms
    self.initializer_2 = transformer.initializer
```

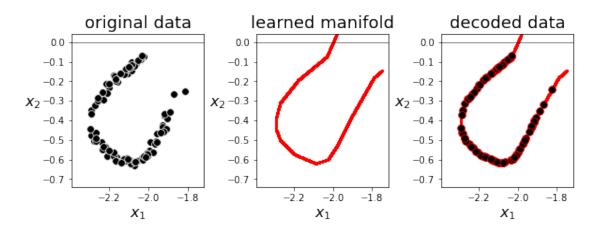
```
def choose cost(self,name,**kwargs):
      # pick cost based on user input
      self.cost_object = un_cost_functions.Setup(name,**kwargs)
      ### with feature transformation constructed, pass on to cost function
→###
      self.cost_object.define_encoder_decoder(self.feature_transforms,self.
→feature_transforms_2)
      self.cost = self.cost_object.cost
      self.cost_name = name
      self.encoder = self.cost object.encoder
      self.decoder = self.cost_object.decoder
   #### run optimization ####
  def fit(self,**kwargs):
      # basic parameters for gradient descent run (default algorithm)
      max_its = 500; alpha_choice = 10**(-1);
      self.w_init_1 = self.initializer_1()
      self.w_init_2 = self.initializer_2()
      self.w_init = [self.w_init_1,self.w_init_2]
      # set parameters by hand
      if 'max_its' in kwargs:
          self.max_its = kwargs['max_its']
      if 'alpha_choice' in kwargs:
          self.alpha choice = kwargs['alpha choice']
      if 'w' in kwargs:
          self.w_init = kwargs['w']
      # batch size for gradient descent?
      self.train_num = np.shape(self.x_train)[1]
      self.val_num = np.shape(self.x_val)[1]
      self.batch_size = np.shape(self.x_train)[1]
      if 'batch_size' in kwargs:
          self.batch_size = min(kwargs['batch_size'],self.batch_size)
      # verbose or not
      verbose = True
      if 'verbose' in kwargs:
          verbose = kwargs['verbose']
       # run gradient descent
      weight_history,train_cost_history,val_cost_history = un_optimizers.
agradient_descent(self.cost,self.w_init,self.x_train,self.x_val,self.
alpha_choice,self.max_its,self.batch_size,verbose=verbose)
```

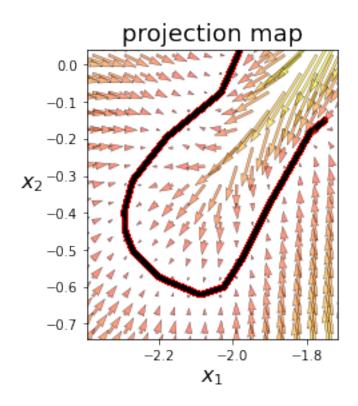
```
# store all new histories
               self.weight_histories.append(weight_history)
               self.train_cost_histories.append(train_cost_history)
               self.val_cost_histories.append(val_cost_history)
           def show_histories(self,**kwargs):
               start = 0
               if 'start' in kwargs:
                   start = kwargs['start']
               if self.train_portion == 1:
                   self.val_cost_histories = [[] for s in range(len(self.
        ⇔val_cost_histories))]
                   self.val_accuracy_histories = [[] for s in range(len(self.
        ⇔val_accuracy_histories))]
               history_plotters.Setup(self.train_cost_histories, self.
        strain_accuracy_histories,self.val_cost_histories,self.
        ⇔val_accuracy_histories,start)
[528]: mylib = Setup(X)
[529]: mylib.preprocessing_steps(normalizer = 'standard')
[530]: # split into training and validation sets
       mylib.make_train_val_split(train_portion = 1)
[531]: # choose features
       mylib.choose_encoder(layer_sizes = [2,10,10,1],scale = 0.2)
       mylib.choose_decoder(layer_sizes = [1,10,10,2],scale = 0.2)
[532]: mylib.choose_cost(name = 'autoencoder')
[533]: mylib.fit(max_its = 3000,alpha_choice = 10**(-1),verbose = False)
[534]: mylib.show_histories()
```





[537]: autoencoder\_demos.show\_encode\_decode(X,mylib,projmap = True,scale = 5)





#### 2 13.8 Batch Normalization

```
[538]: import sklearn sklearn.__version__
```

[538]: '1.0.2'

[539]: conda update scikit-learn

python(69312) MallocStackLogging: can't turn off malloc stack logging because it was not enabled.

Collecting package metadata (current\_repodata.json): done
Solving environment: |

Updating scikit-learn is constricted by

anaconda -> requires scikit-learn==1.0.2=py39hae1ba45\_1

If you are sure you want an update of your package either try `conda update --all` or install a specific version of the package you want using `conda install <pkg>=<version>`

done

==> WARNING: A newer version of conda exists. <==

current version: 4.13.0 latest version: 24.5.0

```
Please update conda by running
          $ conda update -n base -c defaults conda
      # All requested packages already installed.
      Note: you may need to restart the kernel to use updated packages.
[540]: import super_cost_functions
       import history_plotters
       import multilayer_perceptron_batch_normalized
       import multilayer_perceptron
       import normalizers
       import cost functions
       import super_optimizers
[541]: # get MNIST data from online repository
       from sklearn.datasets import fetch_openml
       x, y = fetch_openml('mnist_784', version=1, return_X_y=True)
       # convert string labels to integers
       y = np.array([int(v) for v in y])[:,np.newaxis]
       print(np.shape(x))
       print(np.shape(y))
      (70000, 784)
      (70000, 1)
[542]: x1 = np.transpose(x)
       y1 = np.transpose(y)
[553]: x_sample, x_test = x[:50000], x[50000:]
       y_sample, y_test=y[:50000],y[50000:]
      splitting to training and validation, randomly selecting the training set.
```

```
[554]: shuffled = np.random.permutation(50000)
       x_sample = x_sample.iloc[shuffled]
       y_sample = y_sample[shuffled]
[555]: print(x_sample.shape)
       print(y_sample.shape)
      (50000, 784)
      (50000, 1)
[556]: class Setup2:
           def __init__(self,x,y,**kwargs):
               # link in data
               self.x = x
               self.y = y
               # make containers for all histories
               self.weight_histories = []
               self.train_cost_histories = []
               self.train_accuracy_histories = []
               self.val_cost_histories = []
               self.val_accuracy_histories = []
               self.train costs = []
               self.train_counts = []
               self.val costs = []
               self.val_counts = []
           #### define preprocessing steps ####
           def preprocessing_steps(self,**kwargs):
               ### produce / use data normalizer ###
               normalizer_name = 'standard'
               if 'normalizer_name' in kwargs:
                   normalizer_name = kwargs['normalizer_name']
               self.normalizer_name = normalizer_name
               # produce normalizer / inverse normalizer
               s = normalizers.Setup(self.x,normalizer_name)
               self.normalizer = s.normalizer
               self.inverse_normalizer = s.inverse_normalizer
               # normalize input
               self.x = self.normalizer(self.x)
           #### split data into training and validation sets ####
           def make_train_val_split(self,train_portion):
               # translate desired training portion into exact indecies
```

```
self.train_portion = train_portion
      r = np.random.permutation(self.x.shape[1])
      train_num = int(np.round(train_portion*len(r)))
      self.train_inds = r[:train_num]
      self.val_inds = r[train_num:]
      # define training and testing sets
      self.x_train = self.x[:,self.train_inds]
      self.x_val = self.x[:,self.val_inds]
      self.y train = self.y[:,self.train inds]
      self.y_val = self.y[:,self.val_inds]
  #### define cost function ####
  def choose_cost(self,name,**kwargs):
      # create training and testing cost functions
      self.cost_object = super_cost_functions.Setup(name,**kwargs)
      # if the cost function is a two-class classifier, build a counter too
      if name == 'softmax' or name == 'perceptron':
          self.count_object = super_cost_functions.
⇔Setup('twoclass_counter',**kwargs)
      if name == 'multiclass_softmax' or name == 'multiclass_perceptron':
          self.count_object = super_cost_functions.

→Setup('multiclass_counter',**kwargs)
      self.cost_name = name
  #### define feature transformation ####
  def choose_features(self,**kwargs):
      ### select from pre-made feature transforms ###
      layer_sizes = [1]
      if 'layer sizes' in kwargs:
          layer_sizes = kwargs['layer_sizes']
      # add input and output layer sizes
      input_size = self.x.shape[0]
      layer_sizes.insert(0, input_size)
      # add output size
      if self.cost_name == 'least_squares' or self.cost_name ==_
layer_sizes.append(self.y.shape[0])
      else:
          num_labels = len(np.unique(self.y))
          if num_labels == 2:
```

```
layer_sizes.append(1)
          else:
               layer_sizes.append(num_labels)
       # multilayer perceptron #
      feature_name = 'multilayer_perceptron'
      if 'name' in kwargs:
          feature_name = kwargs['feature_name']
      if feature_name == 'multilayer_perceptron':
          transformer = multilayer_perceptron.Setup(**kwargs)
          self.feature_transforms = transformer.feature_transforms
           self.multilayer_initializer = transformer.initializer
           self.layer_sizes = transformer.layer_sizes
      if feature_name == 'multilayer_perceptron_batch_normalized':
          transformer = multilayer_perceptron_batch_normalized.Setup(**kwargs)
           self.feature_transforms = transformer.feature_transforms
           self.multilayer_initializer = transformer.initializer
          self.layer_sizes = transformer.layer_sizes
      self.feature_name = feature_name
      ### with feature transformation constructed, pass on to cost function
→###
      self.cost_object.define_feature_transform(self.feature_transforms)
      self.cost = self.cost_object.cost
      self.model = self.cost_object.model
      # if classification performed, inject feature transforms into counter_
→as well
      if self.cost name == 'softmax' or self.cost name == 'perceptron' or___
self.cost_name == 'multiclass_softmax' or self.cost_name ==_

¬'multiclass_perceptron':
          self.count_object.define_feature_transform(self.feature_transforms)
          self.counter = self.count_object.cost
  #### run optimization ####
  def fit(self,**kwargs):
      # basic parameters for gradient descent run (default algorithm)
      max_its = 500; alpha_choice = 10**(-1);
      # set parameters by hand
      if 'max_its' in kwargs:
          self.max_its = kwargs['max_its']
      if 'alpha_choice' in kwargs:
          self.alpha_choice = kwargs['alpha_choice']
```

```
# set initialization
      self.w_init = self.multilayer_initializer()
       # batch size for gradient descent?
      self.train_num = np.size(self.y_train)
      self.val_num = np.size(self.y_val)
      self.batch_size = np.size(self.y_train)
      if 'batch_size' in kwargs:
           self.batch_size = min(kwargs['batch_size'], self.batch_size)
       # verbose or not
      verbose = True
      if 'verbose' in kwargs:
           verbose = kwargs['verbose']
       # optimize
      weight_history = []
      cost_history = []
       # run gradient descent
      weight history, train cost history, val cost history = super optimizers.
ogradient_descent(self.cost,self.w_init,self.x_train,self.y_train,self.

¬x_val,self.y_val,self.alpha_choice,self.max_its,self.
⇒batch size, verbose=verbose)
       # store all new histories
      self.weight_histories.append(weight_history)
      self.train_cost_histories.append(train_cost_history)
      self.val_cost_histories.append(val_cost_history)
       # if classification produce count history
      if self.cost_name == 'softmax' or self.cost_name == 'perceptron' or_u
⇒self.cost_name == 'multiclass_softmax' or self.cost_name ==_
⇔'multiclass_perceptron':
           train_accuracy_history = [1 - self.counter(v,self.x_train,self.

    y_train)/float(self.y_train.size) for v in weight_history]

           val_accuracy_history = [1 - self.counter(v,self.x_val,self.y_val)/
→float(self.y_val.size) for v in weight_history]
           # store count history
           self.train_accuracy_histories.append(train_accuracy_history)
           self.val_accuracy_histories.append(val_accuracy_history)
  #### plot histories ###
  def show_histories(self,**kwargs):
      start = 0
```

```
if 'start' in kwargs:
                   start = kwargs['start']
               if self.train_portion == 1:
                   self.val_cost_histories = [[] for s in range(len(self.
        →val_cost_histories))]
                   self.val_accuracy_histories = [[] for s in range(len(self.
        →val_accuracy_histories))]
               history_plotters.Setup(self.train_cost_histories,self.

¬train_accuracy_histories,self.val_cost_histories,self.

        ⇔val_accuracy_histories,start)
           #### for batch normalized multilayer architecture only - set normalizers to_{\sqcup}
        ⇔desired settings ####
           def fix normalizers(self,w):
               ### re-set feature transformation ###
               # fix normalization at each layer by passing data and specific weight_{\sqcup}
        \hookrightarrow through network
               self.feature_transforms(self.x,w);
               # re-assign feature transformation based on these settings
               self.testing_feature_transforms = self.transformer.
        →testing_feature_transforms
               ### re-assign cost function (and counter) based on fixed architecture_
        →###
               funcs = cost_functions.Setup(self.cost_name,self.x,self.y,self.
        →testing_feature_transforms)
               self.model = funcs.model
[580]: import super_setup
[581]: mylib2 = super_setup.Setup(x_sample,y_sample)
[582]: mylib2.preprocessing_steps(normalizer = 'standard')
[583]: mylib2.make_train_val_split(train_portion = 1)
        TypeError
                                                   Traceback (most recent call last)
        File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/indexes/base.py:
         →3802, in Index.get_loc(self, key, method, tolerance)
           3801 try:
        -> 3802
                    return self._engine.get_loc(casted_key)
           3803 except KeyError as err:
```

```
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/_libs/index.pyx:138, in
 →pandas._libs.index.IndexEngine.get_loc()
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/_libs/index.pyx:144, in
 →pandas._libs.index.IndexEngine.get_loc()
TypeError: '(slice(None, None, None), array([469, 531, 229, 350, 564, 684, 464,
 442, 261,
             24, 354, 260, 105,
       736, 420, 234, 465, 383, 232, 85,
                                           5, 214, 668, 720, 765, 386,
       268, 633, 431, 300, 425, 599, 181, 576, 435, 473, 215, 253, 318,
       135, 394, 481, 589, 429, 334, 505, 486, 267, 500, 667,
       438, 755, 358,
                       61, 410,
                                95, 285, 196, 462, 767, 397, 445, 518,
                      81, 372,
                                10, 550, 359, 128, 758, 570, 451, 414,
       65, 244, 502,
       769, 661, 374,
                       26, 665, 513, 492, 310, 272, 539, 400, 713, 349,
       588, 346, 264, 321, 145, 620, 311, 391, 526, 453, 644, 102, 233,
       412, 273, 193, 711, 117, 362, 59, 34, 13, 460, 730, 634, 293,
       51, 162, 466, 585, 508, 389, 648, 692,
                                                 9, 344, 316, 148, 369,
                                  2, 454, 175, 441, 696, 754, 507, 338,
       471, 324, 275, 141, 426,
       738, 123, 560, 291, 71, 559, 21, 618, 527, 118, 495, 119, 554,
       160, 549, 304, 132,
                           36, 422, 732, 525, 14, 510, 107, 582, 673,
                 83, 265, 199, 330, 301, 737, 299, 328, 468, 133, 574,
       491, 756, 187, 726, 725, 694, 168, 750, 583, 664, 379, 688, 129,
       274, 224,
                98, 161, 64, 703, 57, 704, 30, 130, 337, 623,
       543, 169, 540, 751, 432,
                                88, 403, 630, 207, 327, 191, 649, 669,
       523, 289, 343, 749, 75, 779, 760, 256, 573, 222, 146, 562, 279,
       547, 496, 635, 555, 131, 485, 287, 714, 74, 53, 602,
                                                               39,
       748, 613, 458, 551, 99, 143, 332, 590, 521, 437, 174, 566, 516,
       357, 155, 104, 619, 638, 467, 100, 56, 452, 381, 257, 434, 771,
                                 4, 203, 712, 16, 97, 345,
       625, 173, 655, 249, 239,
                                48, 326, 561, 163, 308, 387, 248, 614,
       76, 651, 45, 62, 709,
            86, 483, 517, 715, 757, 753, 245, 641, 368, 341, 190, 329,
       242, 276, 360, 653, 192, 681, 31, 290, 231, 385, 415, 729,
       735, 535, 269, 776, 84, 80, 536, 474, 125, 364, 695, 298,
       195, 246, 739, 306, 743, 448, 584, 171, 382, 419, 493,
       79, 281, 674, 774, 575, 235, 206, 722, 546, 416, 142, 501,
       361, 617, 93, 522, 565, 645, 719, 721, 363, 676, 172, 687, 380,
       377, 157, 677, 459, 761, 28, 201, 134, 252, 666, 611, 140, 430,
       529, 149, 710, 303, 266, 553, 27,
                                          69, 775, 378, 558, 724, 418,
            91, 254, 637, 717, 506, 417, 433, 689, 691, 541, 263,
       600, 159, 323, 587, 52, 646, 700, 11, 367, 658, 405, 482, 731,
       671, 164, 208, 194, 702, 701, 106, 288, 479, 777, 250, 137, 772,
            12, 115, 241, 440, 376, 251, 356, 572, 621, 456, 185, 503,
       631, 497, 728, 487, 247, 533, 331, 42, 511,
                                                    72, 686, 563,
            46, 612, 220, 136, 413, 461, 716, 718, 399, 484,
       366, 408, 578, 608, 639, 616, 165, 763, 556, 597, 315, 605,
       138, 342, 150, 577, 654, 68, 449, 305, 370, 601, 183, 524, 225,
       271, 494, 628, 532, 286, 373, 424, 504, 200, 212, 421, 340, 259,
        44, 659, 388, 67, 443, 371, 230, 176, 211, 77, 544, 675, 734,
```

```
351, 209, 446, 38, 764, 384, 592, 314, 406, 660, 699, 683, 744,
       103, 604, 470, 698, 586, 610, 216, 568, 177, 670, 404, 243, 221,
       213, 427, 109, 114, 690, 579, 685, 35, 151, 348, 678, 530, 571,
       255, 110, 121, 205, 154, 626, 428, 284, 295, 37, 705, 552, 217,
       228, 43, 606, 706, 262, 642, 111, 258, 278, 450, 762, 280,
       607, 393, 47, 55, 476, 569, 534, 598, 594, 746, 499, 112, 270,
       650, 96, 439, 490, 657, 409, 320, 768, 49, 636, 29, 179, 455,
       593, 392, 742, 25, 498, 528, 520, 297, 352, 50, 40, 647, 204,
       302, 353, 782, 632, 237, 317, 515, 580, 463, 609, 557, 108, 198,
       693, 663, 113, 294, 355, 41, 662, 640, 629, 759, 127, 186, 733,
       447, 313, 398, 101, 227, 747, 336, 402, 680, 395, 436, 423, 365,
       477, 15, 153, 73, 727, 202, 679, 166, 457, 741, 309, 78, 167,
       488, 70, 509, 156, 218, 603,
                                     7, 122, 94, 682, 92, 740, 778,
       307, 567, 781, 32, 223, 90, 656, 296, 147, 652, 723, 319, 210,
       411, 475, 512, 596, 766, 189, 697,
                                           1, 643, 58, 124, 624, 396,
       277, 519, 752, 375, 144, 347, 770, 548, 17, 152, 672, 322, 292,
       444, 708, 184, 745, 595, 197, 489, 622, 60, 542, 236, 188, 407,
       538, 219, 170, 390, 335, 339, 120, 139, 226, 158, 478, 537, 472,
       480, 240, 54, 178, 283, 333, 126, 180, 707, 615, 116, 282, 773,
       545, 581, 780, 312]))' is an invalid key
During handling of the above exception, another exception occurred:
InvalidIndexError
                                          Traceback (most recent call last)
Cell In[583], line 1
---> 1 mylib2.make_train_val_split(train_portion = 1)
File ~/Desktop/GitHub_Files/435-deep-learning/super_setup.py:58, in_
 →make_train_val_split(self, train_portion)
            self.y_train = self.y[:,self.train_inds]
            self.y_val = self.y[:,self.val_inds]
---> 58 #### define cost function ####
     59 def choose_cost(self,name,**kwargs):
            # create training and testing cost functions
     60
     61
            self.cost_object = super_cost_functions.Setup(name,**kwargs)
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/frame.py:3807, in_
 →DataFrame.__getitem__(self, key)
   3805 if self.columns.nlevels > 1:
   3806
            return self._getitem_multilevel(key)
-> 3807 indexer = self.columns.get_loc(key)
   3808 if is_integer(indexer):
   3809
            indexer = [indexer]
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/indexes/base.py:
 →3809, in Index.get_loc(self, key, method, tolerance)
   3804
                raise KeyError(key) from err
   3805
            except TypeError:
```

```
# If we have a listlike key, _check_indexing_error will raise
   3806
   3807
                  InvalidIndexError. Otherwise we fall through and re-raise
   3808
                # the TypeError.
                self._check_indexing_error(key)
-> 3809
   3810
   3812 # GH#42269
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/indexes/base.py:
 →5925, in Index._check_indexing_error(self, key)
   5921 def _check_indexing_error(self, key):
            if not is_scalar(key):
   5922
   5923
                # if key is not a scalar, directly raise an error (the code below
   5924
                # would convert to numpy arrays and raise later any way) -
 →GH29926
-> 5925
               raise InvalidIndexError(key)
InvalidIndexError: (slice(None, None), array([469, 531, 229, 350, 564,
                       24, 354, 260, 105,
 →684, 464, 442, 261,
       736, 420, 234, 465, 383, 232, 85,
                                            5, 214, 668, 720, 765, 386,
       268, 633, 431, 300, 425, 599, 181, 576, 435, 473, 215, 253, 318,
       135, 394, 481, 589, 429, 334, 505, 486, 267, 500, 667,
       438, 755, 358,
                      61, 410, 95, 285, 196, 462, 767, 397, 445, 518,
       65, 244, 502,
                      81, 372, 10, 550, 359, 128, 758, 570, 451, 414,
                      26, 665, 513, 492, 310, 272, 539, 400, 713, 349,
       769, 661, 374,
       588, 346, 264, 321, 145, 620, 311, 391, 526, 453, 644, 102, 233,
       412, 273, 193, 711, 117, 362, 59, 34, 13, 460, 730, 634, 293,
       51, 162, 466, 585, 508, 389, 648, 692,
                                                9, 344, 316, 148, 369,
       471, 324, 275, 141, 426,
                                  2, 454, 175, 441, 696, 754, 507, 338,
       738, 123, 560, 291, 71, 559, 21, 618, 527, 118, 495, 119, 554,
       160, 549, 304, 132, 36, 422, 732, 525, 14, 510, 107, 582, 673,
                 83, 265, 199, 330, 301, 737, 299, 328, 468, 133, 574,
       491, 756, 187, 726, 725, 694, 168, 750, 583, 664, 379, 688, 129,
       274, 224, 98, 161, 64, 703, 57, 704, 30, 130, 337, 623, 19,
       543, 169, 540, 751, 432, 88, 403, 630, 207, 327, 191, 649, 669,
       523, 289, 343, 749, 75, 779, 760, 256, 573, 222, 146, 562, 279,
       547, 496, 635, 555, 131, 485, 287, 714, 74, 53, 602,
       748, 613, 458, 551, 99, 143, 332, 590, 521, 437, 174, 566, 516,
       357, 155, 104, 619, 638, 467, 100, 56, 452, 381, 257, 434, 771,
       625, 173, 655, 249, 239,
                                 4, 203, 712, 16, 97, 345, 33, 182,
       76, 651, 45, 62, 709, 48, 326, 561, 163, 308, 387, 248, 614,
            86, 483, 517, 715, 757, 753, 245, 641, 368, 341, 190, 329,
       242, 276, 360, 653, 192, 681, 31, 290, 231, 385, 415, 729,
       735, 535, 269, 776, 84, 80, 536, 474, 125, 364, 695, 298,
       195, 246, 739, 306, 743, 448, 584, 171, 382, 419, 493,
       79, 281, 674, 774, 575, 235, 206, 722, 546, 416, 142, 501,
       361, 617, 93, 522, 565, 645, 719, 721, 363, 676, 172, 687, 380,
       377, 157, 677, 459, 761, 28, 201, 134, 252, 666, 611, 140, 430,
       529, 149, 710, 303, 266, 553, 27, 69, 775, 378, 558, 724, 418,
```

```
631, 497, 728, 487, 247, 533, 331, 42, 511, 72, 686, 563,
                    46, 612, 220, 136, 413, 461, 716, 718, 399, 484,
              366, 408, 578, 608, 639, 616, 165, 763, 556, 597, 315, 605,
              138, 342, 150, 577, 654, 68, 449, 305, 370, 601, 183, 524, 225,
              271, 494, 628, 532, 286, 373, 424, 504, 200, 212, 421, 340, 259,
               44, 659, 388,
                              67, 443, 371, 230, 176, 211, 77, 544, 675, 734,
                              38, 764, 384, 592, 314, 406, 660, 699, 683, 744,
              351, 209, 446,
              103, 604, 470, 698, 586, 610, 216, 568, 177, 670, 404, 243, 221,
              213, 427, 109, 114, 690, 579, 685, 35, 151, 348, 678, 530, 571,
              255, 110, 121, 205, 154, 626, 428, 284, 295, 37, 705, 552, 217,
                   43, 606, 706, 262, 642, 111, 258, 278, 450, 762, 280,
              607, 393, 47, 55, 476, 569, 534, 598, 594, 746, 499, 112, 270,
                    96, 439, 490, 657, 409, 320, 768,
                                                       49, 636, 29, 179, 455,
              593, 392, 742,
                              25, 498, 528, 520, 297, 352, 50, 40, 647, 204,
              302, 353, 782, 632, 237, 317, 515, 580, 463, 609, 557, 108, 198,
              693, 663, 113, 294, 355, 41, 662, 640, 629, 759, 127, 186, 733,
              447, 313, 398, 101, 227, 747, 336, 402, 680, 395, 436, 423, 365,
              477, 15, 153, 73, 727, 202, 679, 166, 457, 741, 309, 78, 167,
                   70, 509, 156, 218, 603,
                                              7, 122, 94, 682, 92, 740, 778,
                              32, 223,
                                        90, 656, 296, 147, 652, 723, 319, 210,
              307, 567, 781,
              411, 475, 512, 596, 766, 189, 697,
                                                   1, 643, 58, 124, 624, 396,
              277, 519, 752, 375, 144, 347, 770, 548, 17, 152, 672, 322, 292,
              444, 708, 184, 745, 595, 197, 489, 622, 60, 542, 236, 188, 407,
              538, 219, 170, 390, 335, 339, 120, 139, 226, 158, 478, 537, 472,
              480, 240, 54, 178, 283, 333, 126, 180, 707, 615, 116, 282, 773,
              545, 581, 780, 312]))
[584]: # choose cost
       mylib2.choose_cost(name = 'multiclass_softmax')
[585]: # choose dimensions of fully connected multilayer perceptron layers
       layer sizes = [10, 10, 10, 10]
       mylib2.choose_features(feature_name = 'multilayer_perceptron',layer_sizes = __
        →layer_sizes, activation = 'relu', scale = 0.1)
[586]: mylib2.fit(max_its = 10,alpha_choice = 10**(-2),verbose = False,batch_size =__
        ⇒200)
       AttributeError
                                                  Traceback (most recent call last)
       Cell In[586], line 1
       ----> 1<sub>LI</sub>
         mylib2.fit(max_its = 10,alpha_choice = 10**(-2),verbose = False,batch_size =
```

514, 91, 254, 637, 717, 506, 417, 433, 689, 691, 541, 263, 66, 600, 159, 323, 587, 52, 646, 700, 11, 367, 658, 405, 482, 731, 671, 164, 208, 194, 702, 701, 106, 288, 479, 777, 250, 137, 772, 783, 12, 115, 241, 440, 376, 251, 356, 572, 621, 456, 185, 503,

```
File ~/Desktop/GitHub Files/435-deep-learning/super_setup.py:143, in fit(self,_
         →**kwargs)
           140 if 'batch_size' in kwargs:
                   self.batch size = min(kwargs['batch size'],self.batch size)
       --> 143 # verbose or not
           144 verbose = True
           145 if 'verbose' in kwargs:
       AttributeError: 'Setup' object has no attribute 'y_train'
[587]: # component-wise normalized version
      mylib2.choose_features(feature_name =_
        ⇔'multilayer perceptron batch normalized',layer sizes =
        ⇔layer_sizes,activation = 'relu',scale = 0.1)
      mylib2.fit(max_its = 10,alpha_choice = 10**(-1),verbose = False,w_init = mylib.
        ⇔w_init,batch_size = 200)
       AttributeError
                                                 Traceback (most recent call last)
       Cell In[587], line 3
             1 # component-wise normalized version
             2 mylib2.choose_features(feature_name =__
        ultilayer_perceptron_batch_normalized',layer_sizes = layer_sizes,activation
         ---> 3<sub>11</sub>
         omylib2.fit(max_its = 10,alpha_choice = 10**(-1),verbose = False,w_init = mylio.w_init,batch
       File ~/Desktop/GitHub Files/435-deep-learning/super_setup.py:143, in fit(self,
         →**kwargs)
           140 if 'batch_size' in kwargs:
                   self.batch_size = min(kwargs['batch_size'],self.batch_size)
       --> 143 # verbose or not
           144 verbose = True
           145 if 'verbose' in kwargs:
       AttributeError: 'Setup' object has no attribute 'y_train'
 []:  # plot cost function history
      labels = ['regular', 'batch-normalized']
      mylib2.show_multirun_histories(start = 0,labels = labels)
```

### 3 13.9 Early Stopping Cross-Validation

```
[456]: # load in dataset
       csvname = datapath + 'noisy_sin_sample.csv'
       data = np.loadtxt(csvname, delimiter = ',')
       x = data[:-1,:]
       y = data[-1:,:]
       print(np.shape(x))
       print(np.shape(y))
      (20, 2)
      (1, 2)
[457]: import polys
       import cost_functions3
       import optimizers
[472]: class Setup3:
           def __init__(self,x,y,**kwargs):
               # link in data
               self.x = x
               self.y = y
               # make containers for all histories
               self.weight_histories = []
               self.train_cost_histories = []
               self.train_count_histories = []
               self.valid_cost_histories = []
               self.valid_count_histories = []
           #### define feature transformation ####
           def choose_features(self,name,**kwargs):
               ### select from pre-made feature transforms ###
               # multilayer perceptron #
               if name == 'multilayer perceptron':
                   self.transformer = multilayer_perceptron.Setup(**kwargs)
                   self.feature transforms = self.transformer.feature_transforms
                   self.initializer = self.transformer.initializer
                   self.layer_sizes = self.transformer.layer_sizes
               if name == 'multilayer_perceptron_batch_normalized':
                   self.transformer = multilayer_perceptron_batch_normalized.

→Setup(**kwargs)
                   self.feature_transforms = self.transformer.feature_transforms
                   self.initializer = self.transformer.initializer
                   self.layer_sizes = self.transformer.layer_sizes
```

```
# polynomials #
      if name == 'polys':
          self.transformer = polys.Setup(self.x,self.y,**kwargs)
          self.feature_transforms = self.transformer.feature_transforms
          self.initializer = self.transformer.initializer
          self.degs = self.transformer.D
      self.feature name = name
  #### define normalizer ####
  def choose_normalizer(self,name):
      # produce normalizer / inverse normalizer
      s = normalizers.Setup(self.x,name)
      self.normalizer = s.normalizer
      self.inverse_normalizer = s.inverse_normalizer
      # normalize input
      self.x = self.normalizer(self.x)
      self.normalizer_name = name
  #### split data into training and validation sets ####
  def make_train_valid_split(self,train_portion):
      # translate desired training portion into exact indecies
      r = np.random.permutation(self.x.shape[1])
      train num = int(np.round(train portion*len(r)))
      self.train_inds = r[:train_num]
      self.valid inds = r[train num:]
      # define training and validation sets
      self.x_train = self.x[:,self.train_inds]
      self.x_valid = self.x[:,self.valid_inds]
      self.y_train = self.y[:,self.train_inds]
      self.y_valid = self.y[:,self.valid_inds]
  #### define cost function ####
  def choose_cost(self,name,**kwargs):
      # create cost on entire dataset
      funcs = cost_functions3.Setup(name, self.x, self.y, self.
→feature_transforms,**kwargs)
      self.full_cost = funcs.cost
      self.full_model = funcs.model
      # create training and validation cost functions
      funcs = cost_functions3.Setup(name,self.x_train,self.y_train,self.

→feature_transforms,**kwargs)
```

```
self.cost = funcs.cost
       self.model = funcs.model
       funcs = cost_functions3.Setup(name,self.x_valid,self.y_valid,self.

→feature_transforms,**kwargs)

      self.valid cost = funcs.cost
       self.valid model = funcs.model
       # if the cost function is a two-class classifier, build a counter too
       if name == 'softmax' or name == 'perceptron':
           funcs = cost_functions3.Setup('twoclass_counter',self.x_train,self.

    y_train,self.feature_transforms,**kwargs)
           self.counter = funcs.cost
           funcs = cost_functions3.Setup('twoclass_counter',self.x_valid,self.

    y_valid, self.feature_transforms, **kwargs)

           self.valid_counter = funcs.cost
       if name == 'multiclass_softmax' or name == 'multiclass_perceptron':
           funcs = cost_functions3.Setup('multiclass_counter',self.

¬x_train, self.y_train, self.feature_transforms, **kwargs)

           self.counter = funcs.cost
           funcs = cost_functions3.Setup('multiclass_counter', self.

¬x_valid,self.y_valid,self.feature_transforms,**kwargs)

           self.valid_counter = funcs.cost
       self.cost name = name
  #### run optimization ####
  def fit(self,**kwargs):
       # basic parameters for gradient descent run (default algorithm)
      max its = 500; alpha choice = 10**(-1);
       self.w_init = self.initializer()
       optimizer = 'gradient_descent'
       epsilon = 10**(-10)
       # set parameters by hand
       if 'max_its' in kwargs:
           self.max_its = kwargs['max_its']
       if 'alpha_choice' in kwargs:
           self.alpha_choice = kwargs['alpha_choice']
       if 'optimizer' in kwargs:
           optimizer = kwargs['optimizer']
       if 'epsilon' in kwargs:
           epsilon = kwargs['epsilon']
       if 'init' in kwargs:
```

```
print ('here')
           self.w_init = kwargs['init']
       # batch size for gradient descent?
       self.num_pts = np.size(self.y_train)
       self.batch_size = np.size(self.y_train)
       if 'batch size' in kwargs:
           self.batch_size = kwargs['batch_size']
       # optimize
       weight history = []
       # run gradient descent
       if optimizer == 'gradient_descent':
           weight_history = optimizers.gradient_descent(self.cost,self.
→alpha_choice, self.max_its, self.w_init, self.num_pts, self.batch_size)
       if optimizer == 'RMSprop':
           weight_history = optimizers.RMSprop(self.cost,self.
alpha_choice,self.max_its,self.w_init,self.num_pts,self.batch_size)
       # run gradient descent
       if optimizer == 'newtons_method':
           epsilon = 10**(-10)
           if 'epsilon' in kwargs:
               epsilon = kwargs['epsilon']
           weight history = optimizers.newtons method(self.cost,epsilon,self.
max_its,self.w_init,self.num_pts,self.batch_size)
       # compute training history
      train_cost_history = [self.cost(v,np.arange(np.size(self.y_train))) for_

y in weight_history]

       # store all new histories
       self.weight histories.append(weight history)
       self.train_cost_histories.append(train_cost_history)
       # compute validation history
       if len(self.valid_inds) > 0:
           valid_cost_history = [self.valid_cost(v,np.arange(np.size(self.
→y_valid))) for v in weight_history]
           self.valid_cost_histories.append(valid_cost_history)
       # if classification produce count history
```

```
if self.cost_name == 'softmax' or self.cost_name == 'perceptron' or_
        Self.cost_name == 'multiclass_softmax' or self.cost_name ==_

¬'multiclass_perceptron':
                   train count history = [self.counter(v) for v in weight history]
                   self.train_count_histories.append(train_count_history)
                   if len(self.valid inds) > 0:
                       valid_count_history = [self.valid_counter(v) for v in_
        →weight_history]
                       self.valid_count_histories.append(valid_count_history)
           #### plot histories ###
           def show_histories(self,**kwargs):
               start = 0
               if 'start' in kwargs:
                   start = kwargs['start']
               history_plotters.Setup(self.train_cost_histories, self.
        →train_count_histories,self.valid_cost_histories,self.
        ⇔valid_count_histories,start)
           #### for batch normalized multilayer architecture only - set normalizers to_{\sqcup}
        ⇔desired settings ####
           def fix normalizers(self,w):
               ### re-set feature transformation ###
               # fix normalization at each layer by passing data and specific weight_{\sqcup}
        \hookrightarrow through network
               self.feature_transforms(self.x,w);
               # re-assign feature transformation based on these settings
               self.validation_feature_transforms = self.transformer.
        ⇔validation_feature_transforms
               ### re-assign cost function (and counter) based on fixed architecture
        ⇒###
               funcs = cost_functions.Setup(self.cost_name,self.x,self.y,self.
        →validation feature transforms)
               self.model = funcs.model
[473]: mylib3 = Setup3(x,y)
[474]: layer_sizes = [1,10,10,10,1]
[475]: | mylib3.choose_features(name = 'multilayer_perceptron',layer_sizes = ___
        ⇔layer sizes,activation = 'tanh')
[476]: mylib3.choose_normalizer(name = 'standard')
```

```
[477]: mylib3.make_train_valid_split(train_portion = 0.66)
[478]: mylib3.choose_cost(name = 'least_squares')
[136]: mylib3.fit(max_its = 10000,alpha_choice = 10**(-1))
       ValueError
                                                  Traceback (most recent call last)
       Cell In[136], line 1
       ----> 1 mylib.fit(max_its = 10000,alpha_choice = 10**(-1))
       Cell In[120], line 130, in Setup3.fit(self, **kwargs)
            128 # run gradient descent
           129 if optimizer == 'gradient_descent':
                   weight history =
        --> 130
         optimizers.gradient_descent(self.cost,self.alpha_choice,self.max_its,self.w_i lit,self.num_r
           132 if optimizer == 'RMSprop':
                    weight_history = optimizers.RMSprop(self.cost,self.alpha_choice,sel...)

→max_its,self.w_init,self.num_pts,self.batch_size)
       File ~/Desktop/GitHub_Files/435-deep-learning/optimizers.py:38, in_
         agradient descent(g, alpha, max its, w, num pts, batch size, **kwargs)
             35 batch_inds = np.arange(b*batch_size, min((b+1)*batch_size, num_pts))
             37 # plug in value into func and derivative
        ---> 38 cost_eval,grad_eval = grad(w,batch_inds)
             39 grad_eval.shape = np.shape(w)
            41 # normalize?
       File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/wrap_util.py:20, in_u
         sunary to nary.<locals>.nary operator.<locals>.nary f(*args, **kwargs)
             18 else:
                    x = tuple(args[i] for i in argnum)
       ---> 20 return unary_operator(unary_f, x, *nary_op_args, **nary_op_kwargs)
       File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/differential_operator.
         →py:138, in value_and_grad(fun, x)
           134 @unary_to_nary
           135 def value_and_grad(fun, x):
                    """Returns a function that returns both value and gradient. Suitabl
            136

¬for use

                    in scipy.optimize"""
           137
        --> 138
                    vjp, ans = _make_vjp(fun, x)
                    if not vspace(ans).size == 1:
            139
                        raise TypeError("value_and_grad only applies to real_
            140
         ⇔scalar-output "
                                        "functions. Try jacobian, elementwise_grad or "
            141
                                        "holomorphic_grad.")
           142
```

```
File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/core.py:10, in_
 ⇔make_vjp(fun, x)
      8 def make_vjp(fun, x):
            start node = VJPNode.new root()
            end_value, end_node =
                                   trace(start_node, fun, x)
---> 10
            if end node is None:
                def vjp(g): return vspace(x).zeros()
File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/tracer.py:10, in_u
 ⇔trace(start_node, fun, x)
      8 with trace_stack.new_trace() as t:
            start_box = new_box(x, t, start_node)
            end_box = fun(start_box)
---> 10
            if isbox(end_box) and end_box._trace == start_box._trace:
     11
     12
                return end_box._value, end_box._node
File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/wrap_util.py:15, in_
 unary_to_nary.<locals>.nary_operator.<locals>.nary_f.<locals>.unary_f(x)
     13 else:
            subargs = subvals(args, zip(argnum, x))
     14
---> 15 return fun(*subargs, **kwargs)
File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/misc/flatten.py:32, i:

→flatten_func.<locals>.<lambda>(_x, *args)
     30 def flatten_func(func, example):
           _ex, unflatten = flatten(example)
            _func = lambda _x, *args: flatten(func(unflatten(_x), *args))[0]
---> 32
            return _func, unflatten, _ex
File ~/Desktop/GitHub Files/435-deep-learning/cost functions3.py:80, in Setup.
 →least_squares(self, w, iter)
     77 y_p = self.y[:,iter]
     79 # compute cost
---> 80 cost = np.sum((self.model(x p,w) - y p)**2)
     81 return cost/float(np.size(x_p))
File ~/Desktop/GitHub_Files/435-deep-learning/cost_functions3.py:54, in Setup.
 →model(self, x, w)
     52 f = 0
     53 if len(self.sig.parameters) == 2:
           f = self.feature_transforms(x,w[0])
---> 54
     55 else:
            f = self.feature_transforms(x)
File ~/Desktop/GitHub Files/435-deep-learning/multilayer perceptron.py:100, in_
 →Setup.standard_feature_transforms(self, a, w)
     96 def standard_feature_transforms(self,a, w):
```

```
# loop through each layer matrix
            for W in w:
     98
                # compute inner product with current layer weights
     99
--> 100
                a = W[0] + \frac{np.dot(a.T, W[1:])}{}
                # output of layer activation
    102
    103
                a = self.activation(a).T
File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/tracer.py:44, in_u
 ⇔primitive.<locals>.f_wrapped(*args, **kwargs)
     42 parents = tuple(box._node for _
                                           , box in boxed_args)
     43 argnums = tuple(argnum
                                for argnum, _ in boxed_args)
---> 44 ans = f_wrapped(*argvals, **kwargs)
     45 node = node_constructor(ans, f_wrapped, argvals, kwargs, argnums, __
 →parents)
     46 return new_box(ans, trace, node)
File ~/opt/anaconda3/lib/python3.9/site-packages/autograd/tracer.py:48, in⊔
 sprimitive.<locals>.f_wrapped(*args, **kwargs)
            return new_box(ans, trace, node)
     47 else:
            return f_raw(*args, **kwargs)
---> 48
File <__array_function__ internals>:200, in dot(*args, **kwargs)
ValueError: shapes (1,20) and (1,10) not aligned: 20 (dim 1) != 1 (dim 0)
```

[138]:

## 4 13.10 Hand Written Digit Recognition Using Neural Networks

```
[183]: from sklearn.model_selection import train_test_split

[279]: # get MNIST data from online repository
    from sklearn.datasets import fetch_openml
    x, y = fetch_openml('mnist_784', version=1, return_X_y=True)

[280]: # convert string labels to integers
    y = np.array([int(v) for v in y])[:,np.newaxis]

    print(np.shape(x))
    print(np.shape(y))

    (70000, 784)
    (70000, 1)
```

```
[285]: x1 = x.T
       y1 = y.T
[286]: | # standard normalization function - with nan checker / filler in-er
       def standard_normalizer(x1):
           # compute the mean and standard deviation of the input
           x_means = np.nanmean(x1,axis = 1)[:,np.newaxis]
           x_stds = np.nanstd(x1,axis = 1)[:,np.newaxis]
           # create standard normalizer function
           normalizer = lambda data: (data - x_means)/x_stds # create inverse standard_
        \rightarrownormalizer
           inverse normalizer = lambda data: data*x stds + x means # return normalizer
           return normalizer, inverse normalizer
       normalizer,inverse_normalizer = standard_normalizer(x1.T)
       x1 = normalizer(x1.T).T
[331]: x_{\text{sample}}, x_{\text{test}} = x[:50000], x[50000:]
       y_sample, y_test=y[:50000],y[50000:]
[332]: shuffled = np.random.permutation(50000)
       x_sample = x_sample.iloc[shuffled]
       y_sample = y_sample[shuffled]
[333]: mylib4 = Setup3(x_sample,y_sample)
[334]: layer_sizes = [784,100,100,10]
[335]: | mylib4.choose_features(name = 'multilayer_perceptron', layer_sizes = __
        ⇔layer_sizes,activation = 'maxout',scale=0.1)
[336]: mylib4.choose_normalizer(name = 'standard')
[337]: # split into training and testing sets
       mylib4.make_train_valid_split(train_portion = 5/6)
        TypeError
                                                   Traceback (most recent call last)
        File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/indexes/base.py:
         →3802, in Index.get_loc(self, key, method, tolerance)
           3801 try:
                    return self._engine.get_loc(casted_key)
        -> 3802
           3803 except KeyError as err:
```

```
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/_libs/index.pyx:138, in
 →pandas._libs.index.IndexEngine.get_loc()
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/_libs/index.pyx:144, in
 →pandas._libs.index.IndexEngine.get_loc()
TypeError: '(slice(None, None, None), array([ 99, 223, 442, 376, 273, 643, 676,
 9702, 758, 204, 503,
                       19, 760,
       186, 306,
                 53, 599, 363, 148, 578, 713, 28, 261, 51, 238, 270,
                        4, 123, 766, 49, 726, 263, 604, 337, 269, 408,
         8, 312,
       111, 315, 600, 492, 521, 745, 241, 354, 341, 386, 747, 725, 342,
                                64, 519, 455, 209, 479, 449, 407, 562,
                  18,
                      86, 58,
       162, 170, 303, 765, 435, 338, 775, 268, 502, 310, 25, 611, 200,
       551, 552, 563, 731, 727,
                                69, 180, 323, 271, 360, 374, 299, 582,
       151, 752, 179, 137, 232,
                                65, 222, 633, 15, 567, 61, 608,
       368, 672, 473,
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                                 80, 644, 149, 730, 501, 739, 593, 350,
                        6, 175, 668,
                                       1, 772, 509, 249, 565, 622, 348,
       524, 656,
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                             7, 712, 532, 220, 441, 693, 741, 471, 781,
       305, 185, 451, 462, 413, 23, 227, 681, 707, 780, 541, 155, 483,
       757, 344, 389, 367, 579, 729, 477, 545, 601, 456, 419, 591, 352,
       660, 345, 433, 634, 507, 301, 395, 35, 630, 645, 674, 288, 230,
                             3, 158, 587, 429, 121, 401, 190, 602, 351,
       432, 557,
                 24, 658,
       210, 242, 778, 92, 671, 276, 112, 317, 556, 423, 682, 612, 213,
       536, 214, 128, 623, 629, 328, 628, 52, 168, 688, 539, 188, 197,
       160, 259, 358, 690, 83, 239, 625, 718, 504, 133, 475, 490, 603,
       382, 670, 192, 246, 616, 464, 516, 706, 349, 701, 531, 698, 357,
                 81, 549, 280, 617, 217,
                                          73, 147, 231, 176, 225, 443,
                 85, 618, 664, 764, 32,
                                           29, 145, 560, 181, 476, 282,
       257,
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                                96, 542, 398, 759, 109, 219,
            16, 383, 588, 695,
                                                               27, 169,
       446, 346, 125, 403, 347, 33, 590,
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       453, 773, 639, 171, 44, 189, 334, 636, 245, 653, 420,
                                                               82, 640,
       375, 102, 777, 13, 550, 466, 183, 251, 364, 172, 748, 585,
       416, 140, 292, 697, 428, 275, 184, 229, 381, 330, 500, 196, 233,
       592, 610, 152, 447, 744, 584, 746, 320, 256, 683, 353, 498, 207,
       546, 448, 146, 515, 400, 325, 47, 626, 10, 234, 377, 212, 321,
       710, 355, 465, 526, 525, 583, 289, 517, 696, 411, 182, 421, 414,
       201, 285, 167, 38, 685, 326, 356, 136, 37, 405, 283, 689, 756,
       637, 115, 117, 324, 371, 218, 114, 751, 426, 46, 547, 692,
       412, 119, 762, 512, 569, 393, 753, 108, 537, 332, 56, 215, 409,
       763, 161, 106, 216, 104, 553, 62, 571, 253, 694, 776, 596, 373,
       632, 107, 704, 703, 445, 638, 522, 771, 613, 540, 679,
       736, 627, 424, 150, 474, 173, 783, 723, 506, 318, 675, 478, 406,
       372, 410, 165,
                      94, 495, 469, 298, 397, 237, 459, 686, 425, 122,
       770, 394, 178, 388, 174, 605, 430, 308,
                                                 2, 194, 530, 529, 359,
       365, 597, 316, 313, 266, 740, 304, 663, 508, 513, 262, 472, 450,
       258, 576, 684, 36, 291, 418, 458, 641, 143, 272, 124, 101, 295,
```

```
715, 568, 208, 652, 646, 520, 768, 720, 333, 699, 260, 485, 457,
       221, 614, 387, 755, 651, 714, 279, 392, 236, 415, 286, 586, 577,
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       366, 749, 267, 45, 322, 631, 518, 293, 274, 264, 100, 226, 41,
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       493, 203, 735, 132, 199, 470, 129, 339, 467, 589, 17, 620, 497,
       91, 284, 336, 116, 118, 126, 452, 558, 166, 454, 206, 95, 319,
       535, 74, 654, 574, 659, 327, 737, 278, 544, 724, 39, 561, 297,
       135, 157, 708, 732, 191, 647, 72, 79, 677, 156, 378, 527, 774,
       650, 559, 307, 78, 87, 281, 329, 489, 141, 139, 294, 595, 97,
       510, 673, 484]))' is an invalid key
During handling of the above exception, another exception occurred:
InvalidIndexError
                                          Traceback (most recent call last)
Cell In[337], line 2
      1 # split into training and testing sets
---> 2 mylib4.make_train_valid_split(train_portion = 5/6)
Cell In[330], line 59, in Setup3.make train valid split(self, train portion)
     56 self.valid_inds = r[train_num:]
     58 # define training and validation sets
---> 59 self.x_train = self.x[:,self.train_inds]
     60 self.x_valid = self.x[:,self.valid_inds]
     62 self.y_train = self.y[:,self.train_inds]
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/frame.py:3807, in_
 →DataFrame. getitem (self, key)
   3805 if self.columns.nlevels > 1:
            return self._getitem_multilevel(key)
-> 3807 indexer = self.columns.get_loc(key)
   3808 if is_integer(indexer):
   3809
            indexer = [indexer]
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/indexes/base.py:
 →3809, in Index.get_loc(self, key, method, tolerance)
                raise KeyError(key) from err
   3804
   3805
            except TypeError:
                # If we have a listlike key, _check_indexing_error will raise
   3806
                # InvalidIndexError. Otherwise we fall through and re-raise
   3807
   3808
                # the TypeError.
-> 3809
                self._check_indexing_error(key)
   3810
                raise
   3812 # GH#42269
File ~/opt/anaconda3/lib/python3.9/site-packages/pandas/core/indexes/base.py:
 →5925, in Index._check_indexing_error(self, key)
   5921 def _check_indexing_error(self, key):
```

```
5922
            if not is_scalar(key):
   5923
                # if key is not a scalar, directly raise an error (the code bel w
   5924
                # would convert to numpy arrays and raise later any way) -
 →GH29926
-> 5925
                raise InvalidIndexError(key)
InvalidIndexError: (slice(None, None, None), array([ 99, 223, 442, 376, 273,...
 →643, 676, 702, 758, 204, 503, 19, 760,
       186, 306,
                 53, 599, 363, 148, 578, 713, 28, 261, 51, 238, 270,
         8, 312,
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                        4, 123, 766,
                                     49, 726, 263, 604, 337, 269, 408,
       111, 315, 600, 492, 521, 745, 241, 354, 341, 386, 747, 725, 342,
       98, 384,
                 18,
                     86, 58,
                                64, 519, 455, 209, 479, 449, 407, 562,
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       551, 552, 563, 731, 727,
                                69, 180, 323, 271, 360, 374, 299, 582,
       151, 752, 179, 137, 232,
                                65, 222, 633, 15, 567, 61, 608,
                                80, 644, 149, 730, 501, 739, 593, 350,
       368, 672, 473,
                      93, 436,
       524, 656,
                        6, 175, 668,
                                       1, 772, 509, 249, 565, 622, 348,
                 76,
       667, 700, 635, 648, 534, 533, 580, 67, 680, 621, 570, 88, 743,
       486, 296, 738, 734,
                            7, 712, 532, 220, 441, 693, 741, 471, 781,
       305, 185, 451, 462, 413,
                                23, 227, 681, 707, 780, 541, 155, 483,
       757, 344, 389, 367, 579, 729, 477, 545, 601, 456, 419, 591, 352,
       660, 345, 433, 634, 507, 301, 395, 35, 630, 645, 674, 288, 230,
       432, 557, 24, 658,
                             3, 158, 587, 429, 121, 401, 190, 602, 351,
                      92, 671, 276, 112, 317, 556, 423, 682, 612, 213,
       210, 242, 778,
       536, 214, 128, 623, 629, 328, 628, 52, 168, 688, 539, 188, 197,
       160, 259, 358, 690, 83, 239, 625, 718, 504, 133, 475, 490, 603,
       382, 670, 192, 246, 616, 464, 516, 706, 349, 701, 531, 698, 357,
                 81, 549, 280, 617, 217, 73, 147, 231, 176, 225, 443,
                 85, 618, 664, 764, 32,
                                          29, 145, 560, 181, 476, 282,
       257,
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                                                               27, 169,
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                                33, 590,
                                          54, 71, 138, 548,
                                                                5, 669,
       453, 773, 639, 171, 44, 189, 334, 636, 245, 653, 420,
                                                               82, 640,
       375, 102, 777, 13, 550, 466, 183, 251, 364, 172, 748, 585, 22,
       416, 140, 292, 697, 428, 275, 184, 229, 381, 330, 500, 196, 233,
       592, 610, 152, 447, 744, 584, 746, 320, 256, 683, 353, 498, 207,
       546, 448, 146, 515, 400, 325, 47, 626, 10, 234, 377, 212, 321,
       710, 355, 465, 526, 525, 583, 289, 517, 696, 411, 182, 421, 414,
       201, 285, 167,
                      38, 685, 326, 356, 136, 37, 405, 283, 689, 756,
       637, 115, 117, 324, 371, 218, 114, 751, 426, 46, 547, 692,
       412, 119, 762, 512, 569, 393, 753, 108, 537, 332, 56, 215, 409,
       763, 161, 106, 216, 104, 553, 62, 571, 253, 694, 776, 596, 373,
       632, 107, 704, 703, 445, 638, 522, 771, 613, 540, 679, 77, 422,
       736, 627, 424, 150, 474, 173, 783, 723, 506, 318, 675, 478, 406,
       372, 410, 165, 94, 495, 469, 298, 397, 237, 459, 686, 425, 122,
       770, 394, 178, 388, 174, 605, 430, 308,
                                                 2, 194, 530, 529, 359,
       365, 597, 316, 313, 266, 740, 304, 663, 508, 513, 262, 472, 450,
       258, 576, 684,
                      36, 291, 418, 458, 641, 143, 272, 124, 101, 295,
       715, 568, 208, 652, 646, 520, 768, 720, 333, 699, 260, 485, 457,
```

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221, 614, 387, 755, 651, 714, 279, 392, 236, 415, 286, 586, 577,
               113, 90, 255, 678, 717, 572, 566, 491, 615, 440, 362, 244, 437,
               366, 749, 267, 45, 322, 631, 518, 293, 274, 264, 100, 226, 41,
               48, 103, 370, 254, 110, 211, 66, 380, 224, 131, 494, 277, 127,
               493, 203, 735, 132, 199, 470, 129, 339, 467, 589, 17, 620, 497,
               91, 284, 336, 116, 118, 126, 452, 558, 166, 454, 206, 95, 319,
               535, 74, 654, 574, 659, 327, 737, 278, 544, 724, 39, 561, 297,
               135, 157, 708, 732, 191, 647, 72, 79, 677, 156, 378, 527, 774,
               650, 559, 307, 78, 87, 281, 329, 489, 141, 139, 294, 595, 97,
               510, 673, 484]))
[338]: # choose cost
       mylib4.choose_cost(name = 'multiclass_softmax')
                                                  Traceback (most recent call last)
       TypeError
       Cell In[338], line 2
              1 # choose cost
       ----> 2 mylib4.choose_cost(name = 'multiclass_softmax')
       Cell In[330], line 68, in Setup3.choose_cost(self, name, **kwargs)
             66 def choose_cost(self,name,**kwargs):
                    # create cost on entire dataset
        ---> 68
                   funcs =

→cost_functions.Setup(name, self.x, self.y, self.feature_transforms, **kwargs)
                    self.full_cost = funcs.cost
                    self.full_model = funcs.model
            70
       TypeError: __init__() takes 2 positional arguments but 5 were given
[340]: # fit an optimization
       mylib4.fit(optimizer = 'gradient_descent', max_its = 100, alpha_choice = u
        $\(\delta\)\),b atch_size = 500,verbose = True,version = 'standard')
         Cell In[340], line 2
           mylib4.fit(optimizer = 'gradient_descent', max_its = 100, alpha_choice = u
         ⇔10**(-1),b atch_size = 500, verbose = True, version = 'standard')
       SyntaxError: positional argument follows keyword argument
```

[]: