

Name _____ School _____

INTERMEDIATE DIVISION

Category 1: Right Triangles – includes Trig.

1. (2 pts) On a graph what is the distance between A(-3,-6) and B(3,2)?

1. _____

2. (3 pts) What is the area of an equilateral triangle whose sides measure 10 inches?

2. _____ in²

3. (5 pts) *QUAD* is a quadrilateral with $QU = 12$ inches, $UA = 16$ inches, angle \underline{U} is a right angle, angle QAD is a right angle and angle D is 40° . What is the measure of QD to the nearest tenth of an inch?

3. _____ in

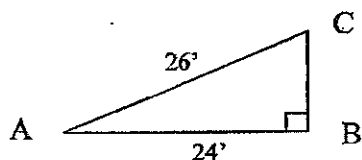
Name _____ School _____

INTERMEDIATE DIVISION

Category 1: Right Triangles – includes Trig.

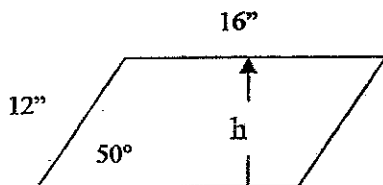
1. (2 pts) In right triangle ABC , find the length of side BC .

1. _____ ft



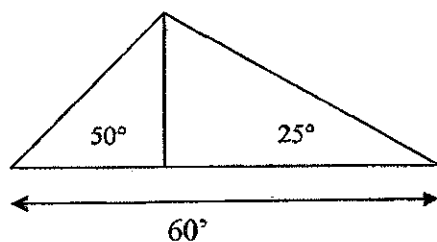
2. (3 pts) Find the height of the parallelogram. Round your answer to 2 decimal places.

2. _____ in



3. (5 pts) Find the height of the vertical pole. Round your answer to 4 decimal places.

3. _____ ft



Name _____

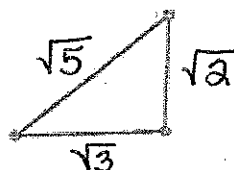
School _____

Intermediate Division

Category 1

Right Triangles and Pythagorean Theorem

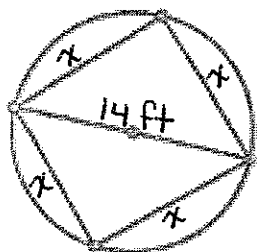
1. (2pts) Given the figure,
is this a right triangle?
Circle your answer and also
support your answer with an
explanation.



ANS YES or NO

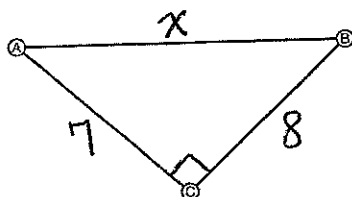
Why? _____

2. (3pts) Find x in this circular figure. Round your answer to the nearest tenths.



ANS _____ ft

3. (5pts) Find the length of x and the angle B in this figure. Answers should be to the nearest tenths.



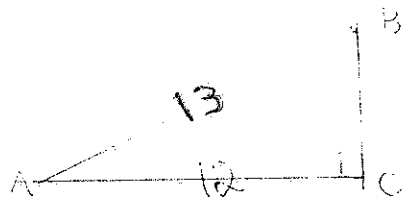
ANS _____

Name _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangles

1. (2 Pts.)

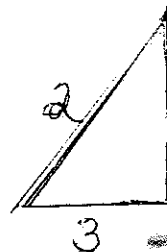
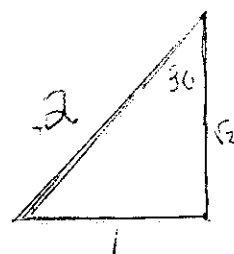
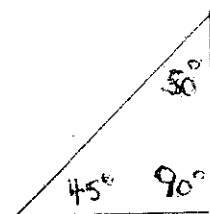
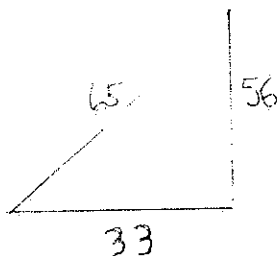
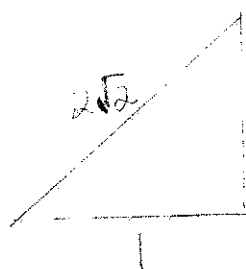


Find the measure of $\angle BAC$. ANS. _____

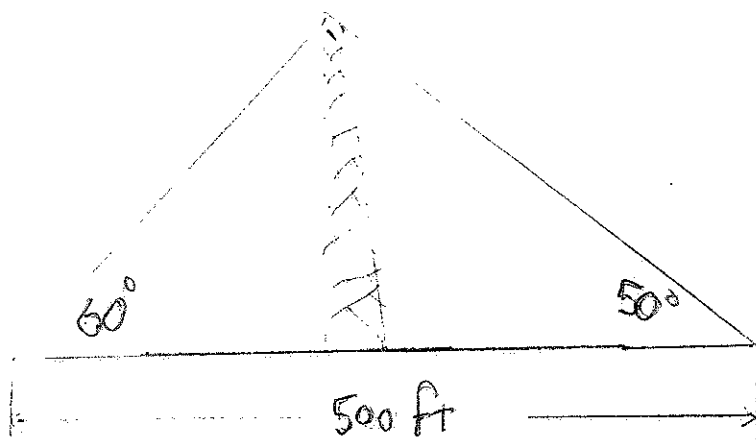
Find the length of \overline{BC} . ANS. _____

GIVE ANSWERS TO NEAREST HUNDREDTHS

2. (3 Pts.) Circle the triangles that are right triangles. (Not drawn to scale.)



3. (5 Pts.) Find the height of this tower, to nearest foot.



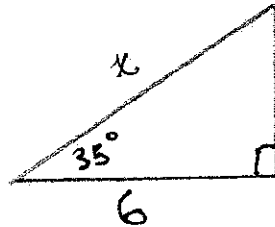
ANS. _____ ft

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

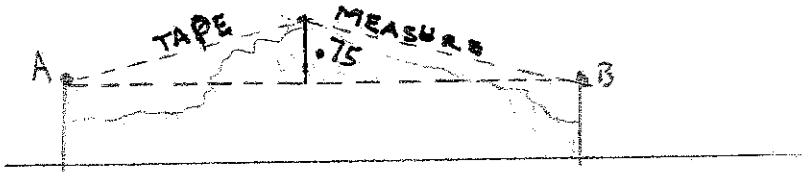
Category 1. Right Triangles

1. (2 Pts.) Solve this triangle for x .



ANS. _____

2. (3 Pts.) Surveying engineers want to measure the distance between two points A and B on rough land. They want to find the actual horizontal distance between A and B. If the earth is 0.75 meters higher midway between the two stakes and if the measuring tape reads 27.0 m, what is the actual distance between A and B?



ANS. _____

3. (5 Pts.) A person travels 8 miles due north, 3 miles due west, 7 miles due north, 11 miles due east. How far is that person from the starting point? Give direction and distance.

ANS. _____

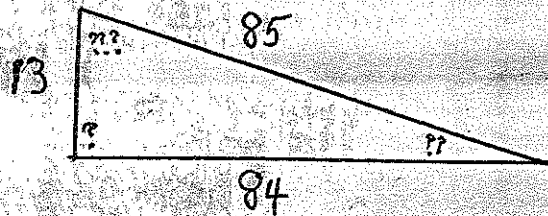
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangles (including Trig and Pythagorean Theorem)

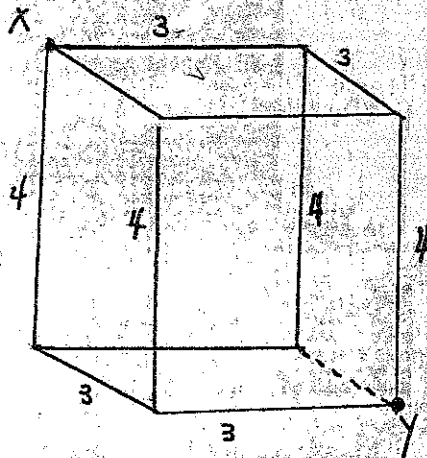
BE SURE TO LABEL ANSWERS. IF NO UNITS ARE GIVEN WRITE UNITS.
(i.e. sq. units, Cubic units)

1. (2 Pts.) Find the area of this triangle.



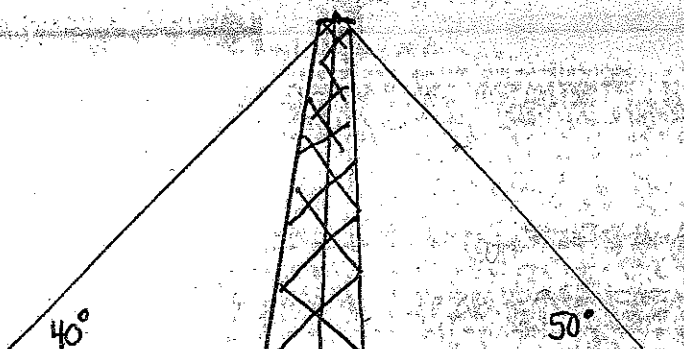
ANS. _____

2. (3 Pts.) Find the length of the diagonal XY in this rectangular solid.



ANS. _____

3. (5 Pts.) Find the height of the tower.



ANS. _____

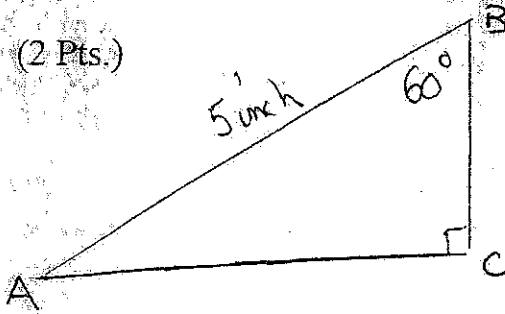
Name _____ No. _____ School _____

INTERMEDIATE DIVISION

Category 1. Right Triangle Trigonometry

ROUND ANSWERS TO 3-PLACE DECIMALS, IF NEEDED.

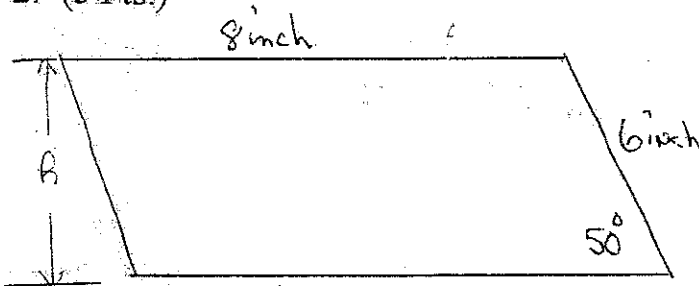
1. (2 Pts.)



Find the length of BC.

ANS. _____ inch

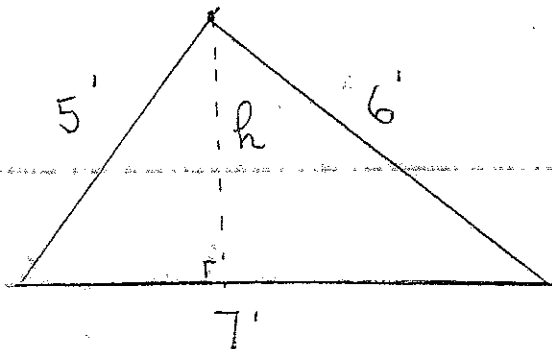
2. (3 Pts.)



Find the height (h) of this parallelogram.

ANS. _____ inch

3. (5 Pts.)



Find h.

ANS. _____

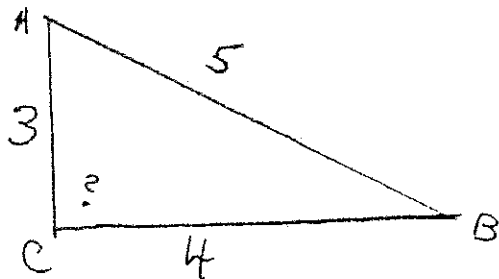
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trigonometry

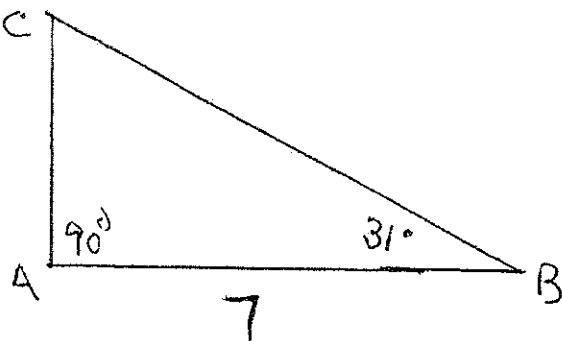
EXPRESS ALL ANSWERS CORRECT TO HUNDREDTHS WHEN NEEDED

1. (2 Pts.) Find the measure of $\angle A$.



ANS. $m\angle A = 53.13^\circ$

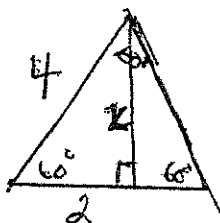
2. (3 Pts.) Find the measure of AC.



$\tan 31^\circ = \frac{x}{7}$

ANS. AC 4.21 units

3. (5 Pts.) Find x in this triangle.



ANS. $x = 2\sqrt{3} \approx 3.46$ units

Name _____ No. _____ School _____

INTER-MEDIATE DIVISION

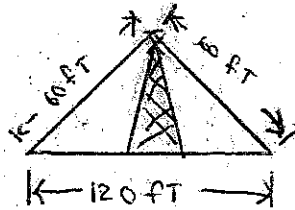
Category 1. Right Triangle Trigonometry

1. (2 Pts.) What are the angles of a 6, 8, 10 triangle? (Give the measure of all three.)

ANS. _____

2. (3 Pts.)

Find the height of this unusual tower.



ANS. _____

3. (5 Pts.) As a train is traveling on a certain track, the engineer observes a column of smoke at a 40° angle to his right. After traveling 10 minutes at 60 mph he observes the same smoke at an angle of 55° behind him and also to his right. How far was the track from the smoke stack?

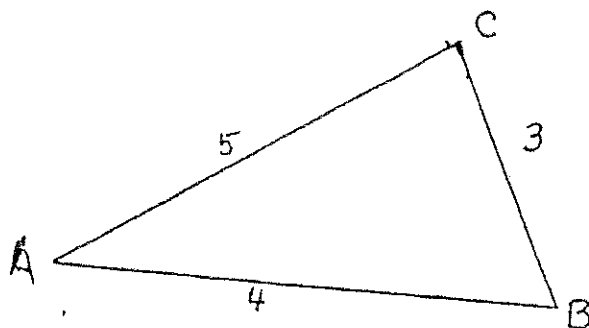
ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

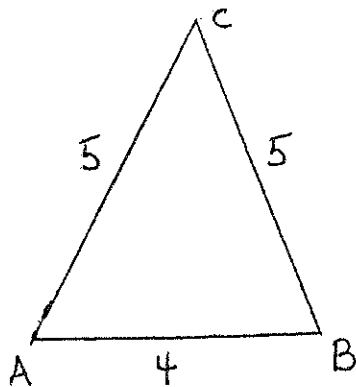
Category 1. Right Triangle Trig

1. (3 Pts.) Find the measure of the angles, (correct to the nearest hundredth of a degree), of this triangle. (Figure not drawn to scale.)



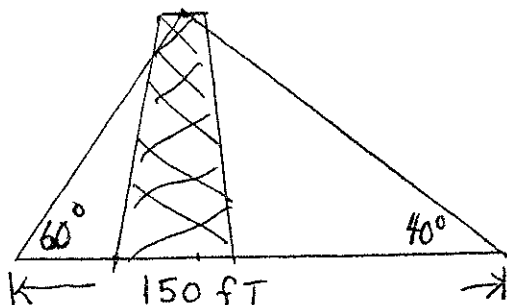
Ans. $m\angle A =$ _____ $^\circ$
 $m\angle B =$ _____ $^\circ$
 $m\angle C =$ _____ $^\circ$

2. (3 Pts.) Find the measure of the angles (correct to the nearest hundredth of a degree), of this triangle. (Figure not drawn to scale.)



ANS. $m\angle A =$ _____ $^\circ$
 $m\angle B =$ _____ $^\circ$
 $m\angle C =$ _____ $^\circ$

3. (5 Pts.) Find the height of this tower. (Figure not drawn to scale.)



ANS. _____

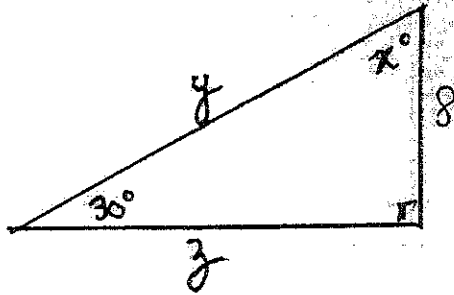
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trig

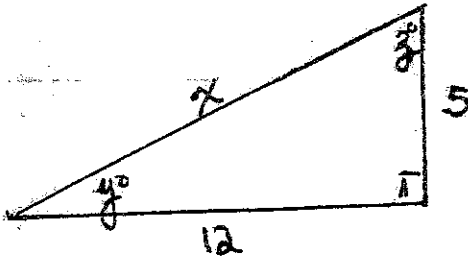
1. (2 Pts.) Solve each of these triangles for x , y , and z . Leave answers in radical form or correct to the nearest thousandth.

a)



$x =$ _____
 $y =$ _____
 $z =$ _____

b)

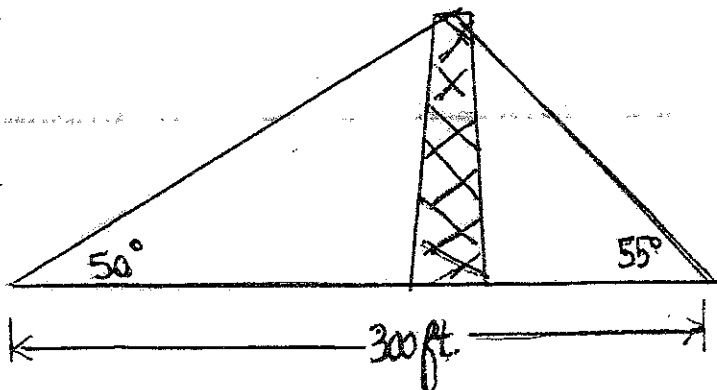


$x =$ _____
 $y =$ _____
 $z =$ _____

2. (3 Pts.) What are the measures of the angles of a 3-4-5 triangle?

ANS. _____

3. (5 Pts.) Find the height of the tower.



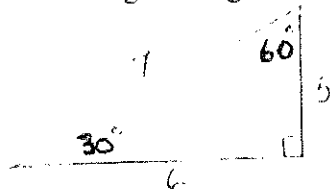
ANS. _____

Name _____ No _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trig

- 1 (2 Pts) Find two things wrong with this figure. (you do not have to show)



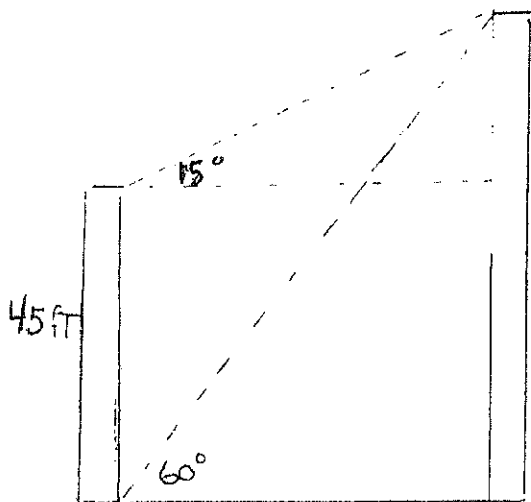
ANS 1) _____

2) _____

- 2 (3 Pts.) From a point 220 feet from the base of the Empire State Building and in the same horizontal plane, the angle of elevation of the top of the building is 80.0° . Find the height of the building.

ANS. _____

- 3 (5 Pts.) Find the height of the taller column.



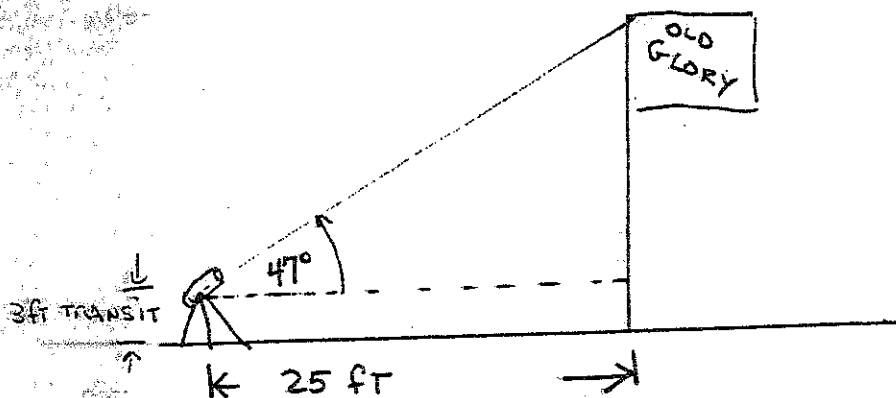
ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

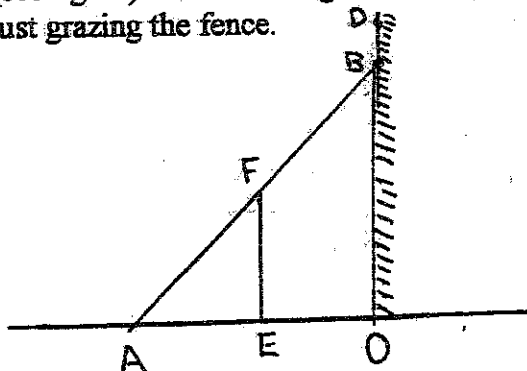
Category 1. Right Triangle Trig

1. (2 Pts.) To the nearest hundredth of a foot, find the height of the flagpole.



ANS. _____

2. (3 Pts.) EF is a fence 5 ft. high at a distance of 3 ft. from the wall OD of a house (see figure). Find the length of a ladder AB inclined at 72° to the horizontal just grazing the fence.



ANS. _____

2. (5 Pts.) The diagonals of a rectangle intersect at an angle of $33^\circ 48'$ and the length of one side is 5 inches. What is the length of a diagonal? (If there are two possible answers, give both).

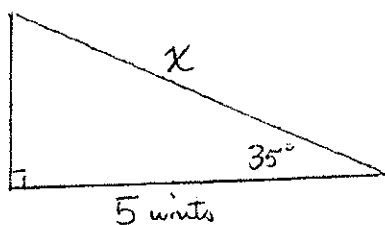
ANS. _____

Name _____ No. _____ School _____

1-H-T-E-R-M-E-D-I-A-T-E D-I-C-I-S-I-O-N

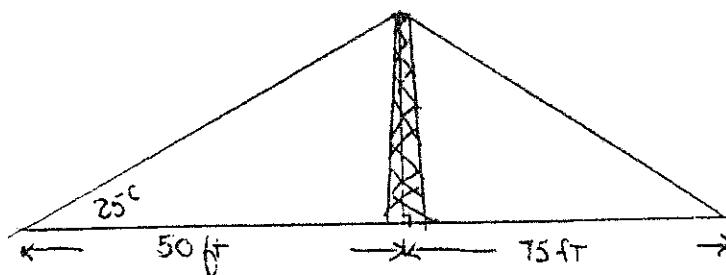
Category 1. Right Triangle Trig

1. (2 Pts.) Solve for x (correct to two decimal places).



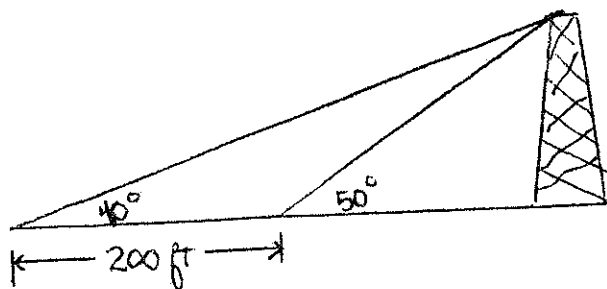
ANS. $x =$ _____

2. (3 Pts.) Find the height of the tower (correct to two decimal places).



ANS. _____

3. (5 Pts.) Find the height of the tower (correct to two decimal places).



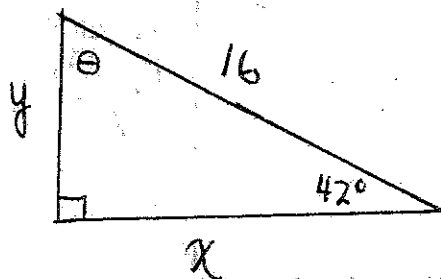
ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trig

1. (2 Pts.) Find x and y and θ for this triangle (correct to the nearest hundredth).



$x =$

$y =$

$\theta =$

ANS. _____

2. (3 Pts.) Solve each for θ where $0^\circ < \theta < 90^\circ$

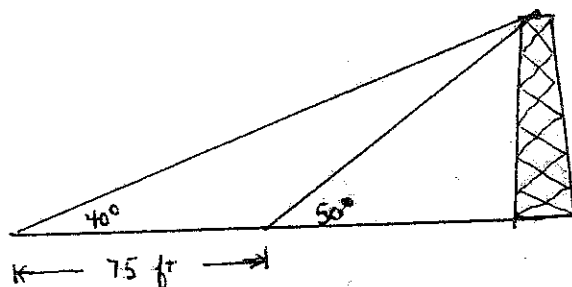
a) $\sin \theta = .1234$ ANS. _____

b) $\theta = \sin^{-1} .4321$ ANS. _____

c) $\theta = \arccos .5$ ANS. _____

d) $\cos \theta = 1.2345$ ANS. _____

3. (5 Pts.) Find the height of the tower to the nearest tenth of a foot.



ANS. _____

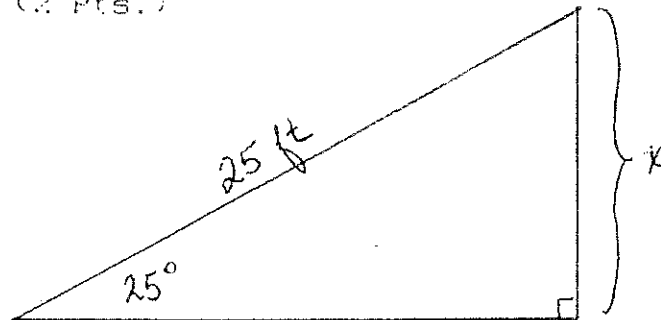
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trigonometry

Calculators may be used in this category.

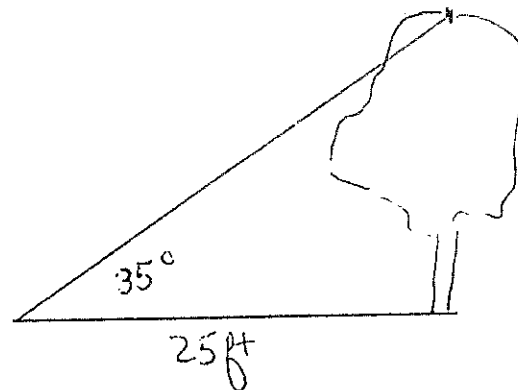
1. (2 Pts.)



What is the length of x ?

ANS. _____

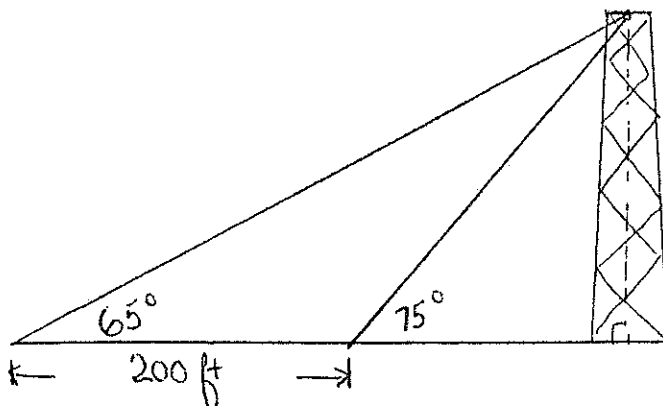
2. (3 Pts.)



What is the height of the tree?

ANS. _____

3. (5 Pts.)



What is the height of the tower?

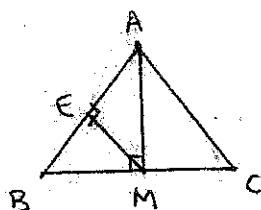
ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trig

1. (2 Pts.)



$$\angle B = \angle C = 40^\circ$$

$$AM \perp BC$$

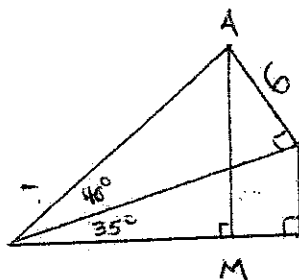
$$ME \perp AB$$

$$AC = 5 \text{ units}$$

Find EM

ANS. _____

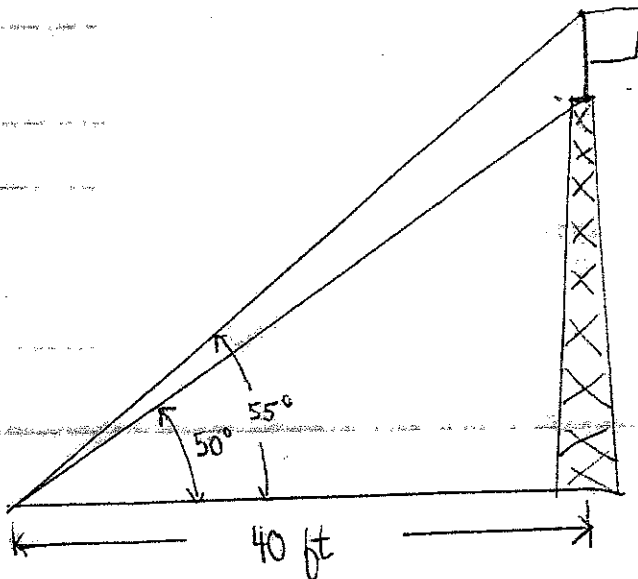
2. (3 Pts.)



Find the length of AM.

ANS. _____

3. (5 Pts.)



Find the height of the flag pole.

ANS. ft

Name _____ No. _____ School _____

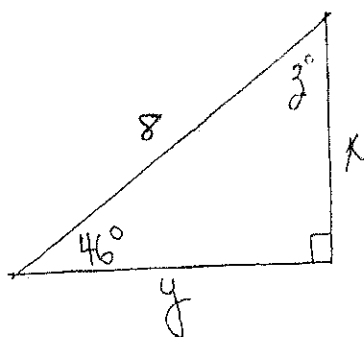
I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trig

Calculators may be used in this category

1. (2 Pts.)

Find answers correct to 2 decimal places.

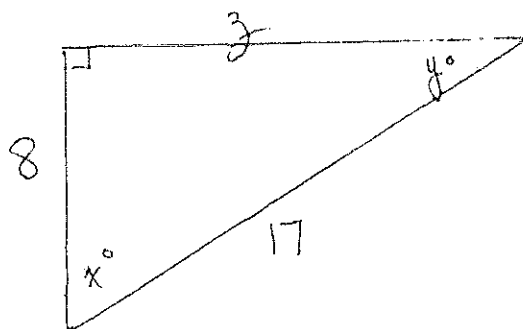


$x =$ _____

$y =$ _____

$z =$ _____

2. (3 Pts.)



$x =$ _____

$y =$ _____

$z =$ _____

3. (5 Pts.) $\sec \theta = 1.8926$
 $\theta =$?

ANS. _____

Name _____

No. _____

School _____

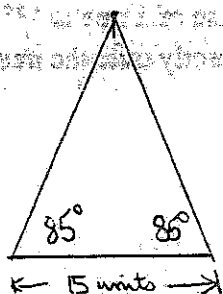
I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 1. Right Triangle Trig
(Calculators may be used in this category.)

1. (2 Pts.) The Golden Rectangle named by ancient Greeks says that a rectangle with sides $\sqrt{5} + 1$ by 2 is the most pleasing to the eye. To further discuss this topic, what is the angle between the diagonal and the longer side?

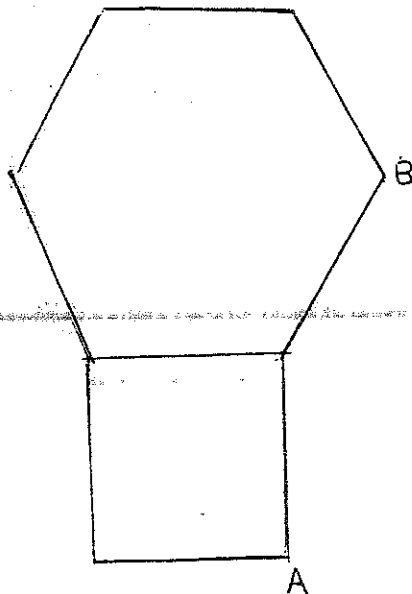
ANS. _____

2. (3 Pts.) Find the area of this triangle.



ANS. _____

3. (5 Pts.) Given a regular hexagon and a square as shown below, find the length of AB when the square has a side of 4 units.



ANS. _____

Category 1
Right Triangle Trig

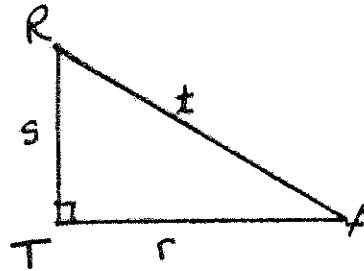
Name: _____

2 points Use the definitions of the three trigonometric ratios to complete each statement.

$\sin A = \underline{\hspace{2cm}}$

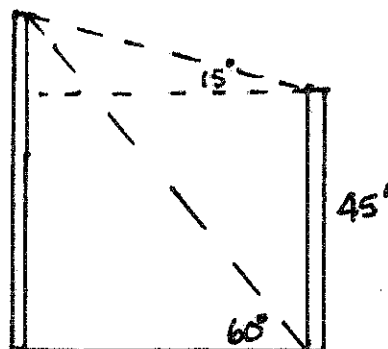
$\cos A = \underline{\hspace{2cm}}$

$\tan A = \underline{\hspace{2cm}}$



3 points An airplane is flying 10,500 feet above the level ground.
The angle of depression from the plane to the base of a tree is $13^\circ 50'$.
How far horizontally must the plane fly to be directly over the tree?

5 points Find the height of the taller column.



Name: _____

Trigonometry

2 points

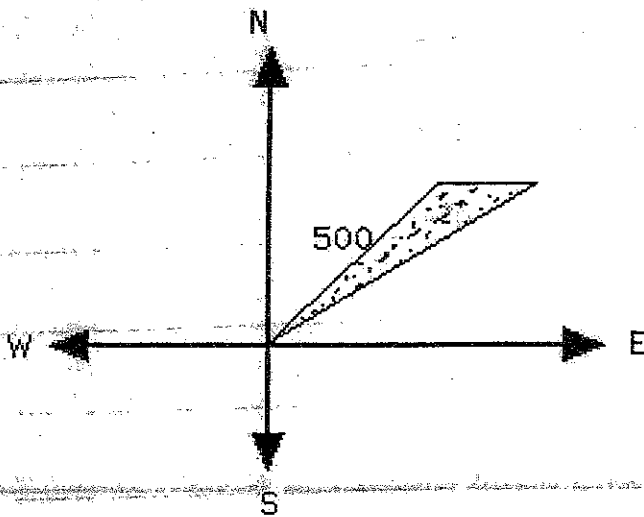
- a. Angles A and B are two acute angles of a right triangle. What is the measure of angle A if the sine of A equals the sine of B? _____
- b. What is the measure of angle A if the tangent of A is 1? _____
- c. As an angle measure gets closer and closer to 0° , the values of the sine ratio gets closer and closer to what value? _____
- d. As an angle measure gets closer and closer to 0° , the values of the cosine ratio gets closer and closer to what value? _____

3 points

Billy's pet bat *Batty* is flying at the end of a 50-foot leash. Using an angle measuring device, Billy spots *Batty* at an angle of 55° up from the horizontal. To the nearest hundredth, how high is *Batty* flying if the leash is taut and anchored to the ground? _____

5 points

A farmer wishes to fence and plant a triangular plot of ground. One side of the plot makes a 45° angle with an east-west line, and is 500 feet long. A second side runs parallel to the east-west line, and the third side makes a 30° angle with the east-west line. Find the perimeter of the plot to the nearest tenth of a foot. _____



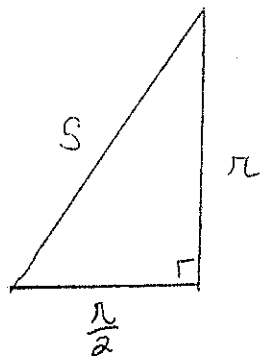
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

CALCULATORS MAY NOT BE USED IN THIS CATEGORY

1 (2 Pts.)



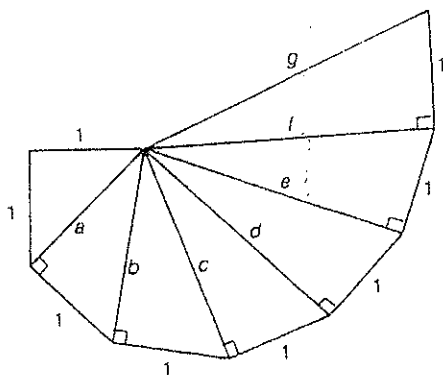
State s in terms of r only.
Simplify form only

ANS. _____

2. (3 Pts.) Use the Pythagorean Theorem to find the distance between the points $(2,1)$ and $(6,3)$.

ANS. _____

3. (5 Pts.)



Find the length of:

$a =$ _____

$b =$ _____

$c =$ _____

$d =$ _____

$e =$ _____

$f =$ _____

$g =$ _____

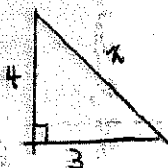
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

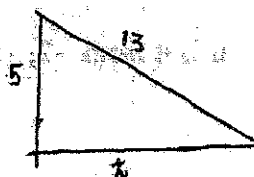
Category 2. Pythagorean Theorem

CALCULATORS MAY NOT BE USED IN THIS CATEGORY

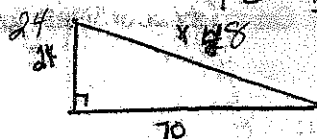
1. (2 Pts.) Find x in each of these triangles.



a) $x = 5$



b) $x = 12$



c) $x =$ _____

2. (3 Pts.) Given the triangle



show that $\sin^2 \theta + \cos^2 \theta = 1$

$$\sin \theta = \frac{a}{c}$$

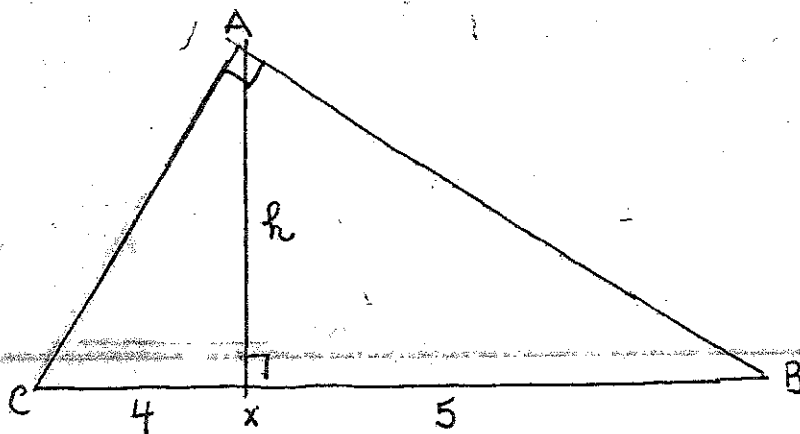
$$\cos \theta = \frac{b}{c}$$

$$\left(\frac{a}{c}\right)^2 + \left(\frac{b}{c}\right)^2 =$$

and $a^2 + b^2 = c^2$

$$\frac{a^2 + b^2}{c^2} = \frac{c^2}{c^2} = 1$$

3. (5 Pts.) Given $\triangle ABC$ with $m\angle A = 90^\circ$, $Cx = 4$, $Bx = 5$, find Ax .



ANS. $\sqrt{20} = 2\sqrt{5}$

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

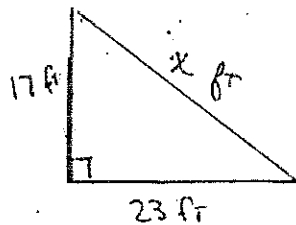
Category 2. Pythagorean Theorem

CALCULATORS ARE NOT ALLOWED IN THIS CATEGORY

1. (2 Pts.) On an xy coordinate graph, how far is it from $(-2, -4)$ to $(2, -1)$?

ANS. _____

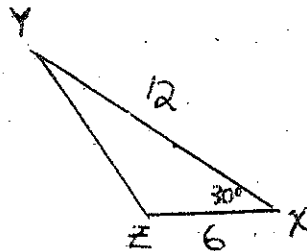
2. (3 Pts.)



Find correct to the nearest whole number, the length of the hypotenuse, of this right triangle.

ANS. _____

3. (5 Pts.) Find correct to the nearest tenth, the length of YZ.



ANS. _____

Name _____ No. _____ School _____

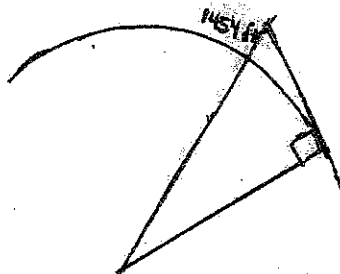
I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

1. (2 Pts.) TRUE - FALSE

- _____ a) The Pythagorean Theorem says a triangle with a 90° angle is a right angle.
- _____ b) The Pythagorean Theorem says $A^2 + B^2 = C^2$.
- _____ c) The Pythagorean Theorem says that a triangle with sides 33, 56, 65 is a right triangle.
- _____ d) The Pythagorean Theorem says the side opposite the 30° angle in a 30° - 60° - 90° right triangle is $1/2$ the hypotenuse.

2. (3 Pts.) How far can you see? The Sears Tower in Chicago is 1454 ft. above ground level. It has an observation tower at the highest level. How far can a person see (with the aid of a telescope) from this tower? Use the radius of the earth as 3960 miles and that 5280 feet = 1 mile.



ANS. _____

3. (5 Pts.) Find the length of the sides of the triangle having vertices at $A(2,-1)$, $B(-2,-4)$, $C(5,3)$.

ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

1. (2 Pts.) The Pythagorean Theorem states that if $A^2 + B^2 = C^2$ then $\angle C$ is a right angle and conversely. What does the "conversely" mean? Explain.

2. (3 Pts.) In $\triangle ABC$, $m\angle B = 90^\circ$, $AB = 8$ in., $AC = 17$ in., D is a point on \overline{BC} such that $BD = 5$ in. Find the area of $\triangle ADC$.

ANS. _____

3. (5 Pts.) \overline{BA} , \overline{CD} are drawn perpendicular to \overline{BC} on opposite sides of \overline{BC} ; $AB = 4$ in.; $BC = 5$ in.; $CD = 6$ in.; CB is produced to a point P such that $PD = 2PA$. Find the length of PB .

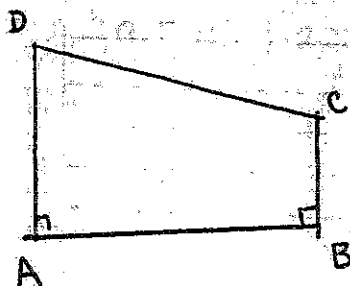
ANS. _____

Name _____ No. _____ School _____

INTERMEDIATE DIVISION

Category 2. Pythagorean Theorem

1. (2 Pts.) In the figure, $AD = 10$ in., $AB = 8$ in., $BC = 4$ in. Find CD .



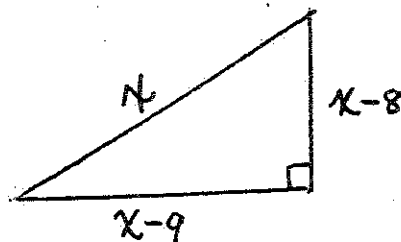
ANS. _____

2. (3 Pts.) PQRS is a quadrilateral in which $\angle PQR$ and $\angle PRS$ are right triangles. If $PQ = 12$ ft., $QR = 9$ ft., $RS = 8$ ft., find the length of PS and the area of PQRS. (Be sure to label answers).

ANS. $PS =$ _____

Area PQRS = _____

3. (5 Pts.) Find the lengths of the sides of this triangle.



ANS. _____

Name _____ No _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

1 (2 Pts) Complete the following chart. (This is part of your answer.)

m	n	$m^2 - n^2$	$2mn$	$m^2 + n^2$
3	1	8	6	10
4	1	15	8	17
3	2	5	12	13
4	3	7	24	25

Are the numbers that you have generated Pythagorean triples?

ANS. YES OR NO
(Circle correct answer.)

2 (3 Pts.) Given

m	n	$m^2 - n^2$	$2mn$	$m^2 + n^2$
25	2	621	100	629
34	7	1107	476	1205

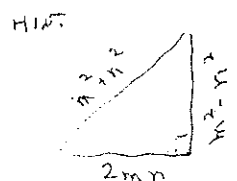
Are 100; 621; 629 Pythagorean triples?

ANS. YES OR NO
(Circle correct answer.)

Are 476; 1107; 1205 Pythagorean triples?

ANS. YES OR NO
(Circle correct answer.)

3. (5 Pts.) Show that $m^2 - n^2$, $2mn$, $m^2 + n^2$ generate Pythagorean triples.



Name _____

No. _____

School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

1. (2 Pts.) Find the missing number in the following sets of Primitive Pythagorean Triples.

(Express answer in simplest radical form or to two decimal places.)

A. 119, 120, _____

B. 120, _____, 241

C. _____, 3599, 3601

2. (3 Pts.) ABCD is a quadrilateral in which $\angle B = \angle D = 90^\circ$

If AB = 6 in., BC = 8 in., CD = 5 in., what

is the length of AD? (Give answer in simplest radical form or correct to hundredths.)

ANS. AD = _____

3. (5 Pts.) Two roads AOB, COD run east and north: a man

"P" passes thru O at 2 pm walking east at 3

mph; a man "Q" passes thru O at 2:30 pm

walking north at 4 mph. When are "P" and "Q"

3 miles apart?

(Express answer correct to the nearest minute)

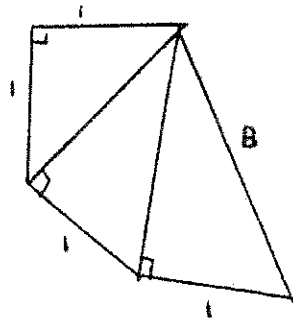
ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

1. (2 Pts.) From the figure, determine B.

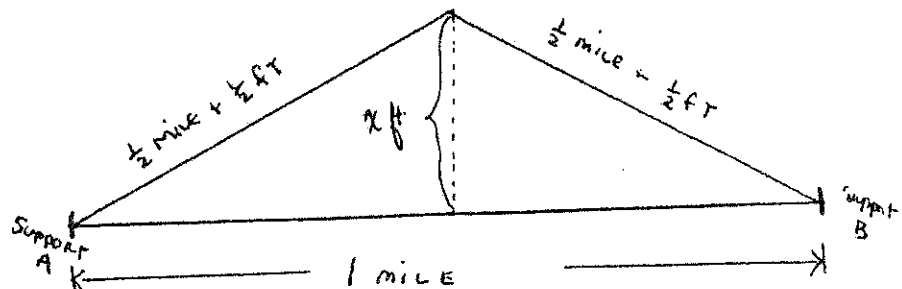


ANS. _____

2. (3 Pts.) Compute the area of a right triangle in which the lengths of the hypotenuse and one leg are 2045 and 693 (a numerologists' delight).

ANS. _____

3. (5 Pts.) A railroad track 1 mile long expands on a very hot day. The track is firmly anchored at both ends and so the track bends in the middle as shown. The track expands 1 foot for the mile length. 1 mile = 5280 ft.



Find how high the track would rise.
(i.e. Find the distance x.

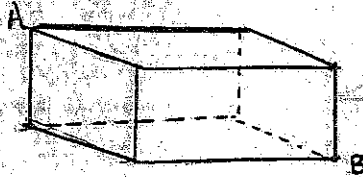
ANS. _____

Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

1. (2 Pts.)



Given a rectangular solid with sides 3, 4, and 5 inches, find the length of a diagonal of the solid (i. e. \overline{AB}), correct to the nearest whole number.

ANS. _____

2. (3 Pts.) A pyramid of height 7.5 inches stands on a square base of side 4 inches; all the slant edges are equal. Find their lengths to the nearest 0.1 of an inch.

ANS. _____

3. (5 Pts.) Given the sides of a triangle as $m^2 - n^2$, $2mn$, and $m^2 + n^2$. Use this information to find 5 sets of Primitive Pythagorean Triples. (i.e. 3 whole numbers that are sides of a right triangle and are not multiples of any other triples.) Of course, one of your 5 sets of Primitive Pythagorean Triples should be 5, 12, 13.

ANS. _____

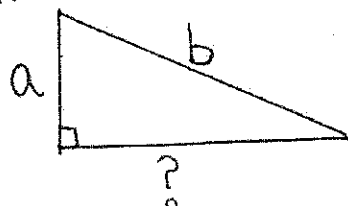
Name _____ No. _____ School _____

I-N-T-E-R-M-E-D-I-A-T-E D-I-V-I-S-I-O-N

Category 2. Pythagorean Theorem

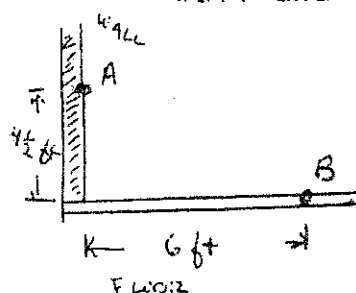
1. (2 Pts.) GIVEN:

Find ? in terms of a and b.



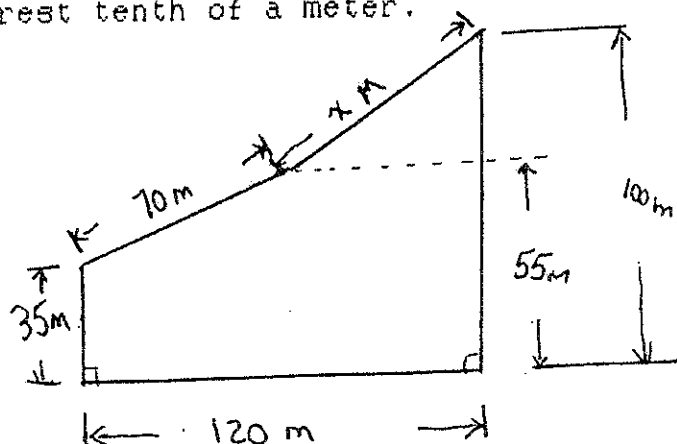
ANS. _____

2. (3 Pts.) In remodeling a house, a carpenter checks the squareness of a wall and a floor. A $4\frac{1}{2}$ foot length is marked off on the wall, (point A), as shown in the figure and a 6 foot length is marked off on the floor, (point B). The measurement from point A to point B is $7' 9"$. Are the wall and the floor square? (SHOW YOUR CALCULATIONS.)



CIRCLE YES OR NO
NOW EXPLAIN

3. (5 Pts.) Determine the distance x correct to the nearest tenth of a meter.



Name _____

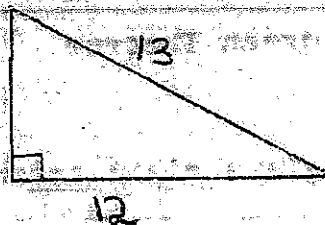
No.

School

INTERMEDIATE DIVISION

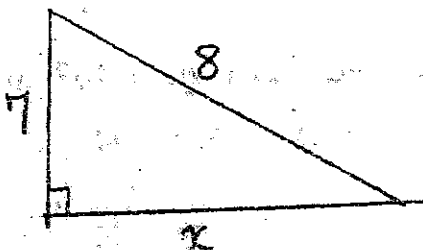
Category 3: Pythagorean Theorem

1. (2 Pts.) Find the area of this triangle.



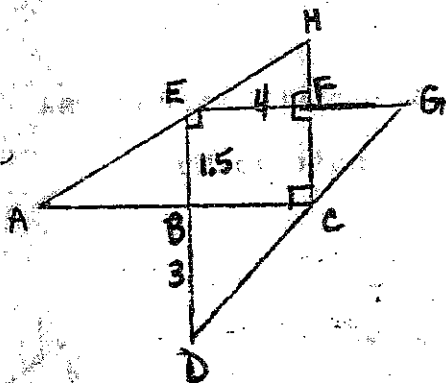
ANS.

2. (3 Pts.) Find the length of x .



ANS.

3. (5 Pts.) Find AH.



Given

DE LEG

$$\overline{HF} \perp \overline{EG}$$

HC L AC

$$EF = 4$$

$BD = 3$

$$DE = 4.5$$

$$m\angle A = m\angle G$$

FILED AM

ANS.

Name _____ No. _____ School _____

INTERMEDIATE DIVISION

Category 3. Pythagorean Theorem

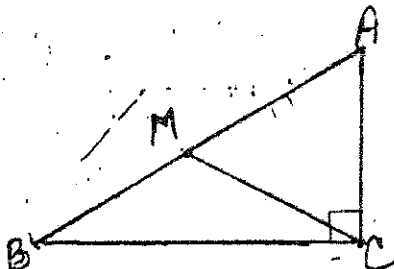
1. (2 Pts.) Is the following triangle a right triangle?

Why or why not? Explain your answer.



ANS. _____

2. (3 Pts.) Given right triangle ABC with $\angle C = 90^\circ$ and M is the midpoint of AB. $AC = 20$, $BC = 21$. Find MC.

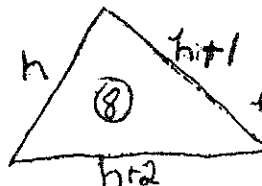
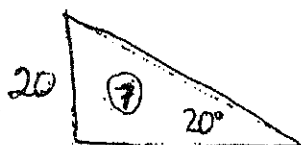
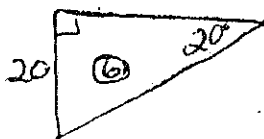
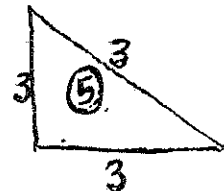
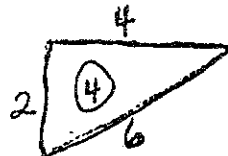
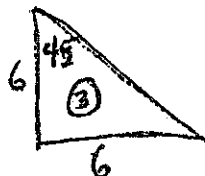
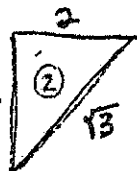
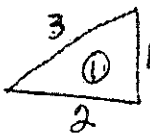


ANS. _____

3. (5 Pts.) Tell which of the following are right triangles.

Sides and angles are drawn to confuse you. Don't go by the

figure, go by the numbers.



for any $h \geq 3$

ANS. _____

Name _____

No. _____

School _____

INTERMEDIATE DIVISION

Category 3. Pythagorean Theorem

1. (2 Pts.)



ABCD is a quadrilateral.

$AB = BC = 10$

$CD = 5$

$\angle ABC = 90^\circ$

$\angle BCD = 90^\circ$

Find AD.

ANS _____

2. (3 pts.) Tell which are not Pythagorean Triangles.

a) 3, 4, 5

b) 5, 12, 13

c) 8, 15, 17

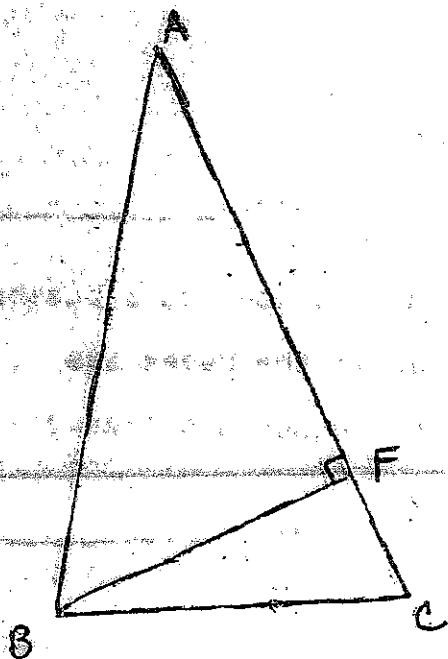
d) 10, 15, 20

e) 20, 21, 29

f) 33, 56, 65

ANS _____

3. (5 pts.)



$AB = AC = 20$

$BC = 10$

BF is an altitude.

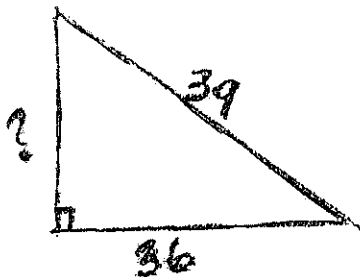
Find FC.

ANS FC = _____

INTERMEDIATE DIVISION

Category 3. Pythagorean Theorem

1. (2 Pts.) Find the missing side of this triangle.



ANS. _____

2. (3 Pts.) AD is an altitude of $\triangle ABC$. If $m\angle C = 45^\circ$ then

a) $AB^2 = BD^2 + DC^2$

b) $AB^2 = BC^2 + AC^2$

c) $AB^2 = BD^2 + AD^2$

d) $AC^2 = AD^2 + DC^2$

e) $AC^2 = AB^2 + BC^2$

Tell which of the above are correct.

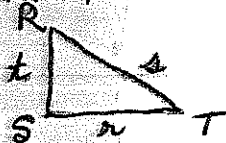
ANS. _____

3. (5 Pts.) Calculate the straight-line distance on a baseball diamond from first base to third base if the bases are 90 ft. apart. (Round your answer to the nearest foot.)

ANS. _____

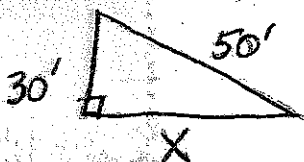
CAT 3 - PYTHAGOREAN THM

- ① GIVEN THE TRIANGLE RST WITH $m\angle S = 90^\circ$, STATE THE PYTHAGOREAN THEOREM IN TERMS OF THE SIDES



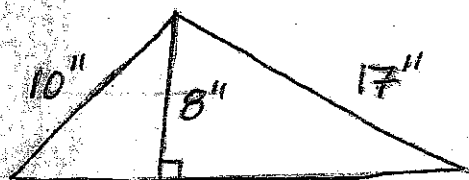
ans. _____

- ② FIND x IN THIS TRIANGLE



ans. _____

- ③ FIND THE AREA OF THIS TRIANGLE



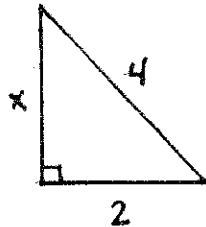
ans. _____

- ④ A helicopter ascends vertically to an altitude of 1000 ft, flies North for 2000 ft, turns and flies due East for 3000 ft. How far is the helicopter from its launching site? (Give answer correct to the nearest 100 ft.)

Category 2
Pythagorean Theorem

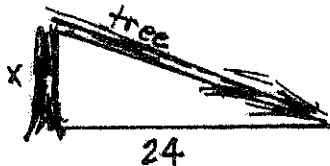
Name: _____

2 points Find the exact length of x .



3 points A man travels 7 km due north, 3 km, due east, 8 km due north,
2 km due east and 1 km due south. How far is he from his starting point?

5 points A giant California redwood tree 36 meters tall cracked in a violent earthquake and fell as if hinged. The tip of the once beautiful tree hit the ground 24 meters from the base. Researchers want to investigate the crack. How many meters up from the base of the tree do the researchers have to climb?

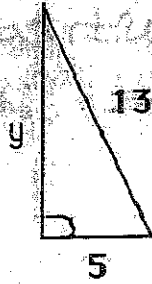
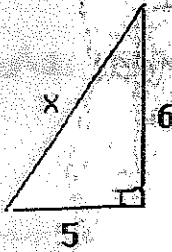


Name: _____

Pythagorean Theorem

2 points

Find the missing side length of each triangle. Give the exact length.



$x = \underline{\hspace{2cm}}$

$y = \underline{\hspace{2cm}}$

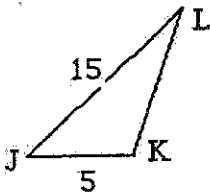
3 points

What is the longest stick that can be placed inside a rectangular box with inside dimensions of 24 inches, 30 inches, and 18 inches?

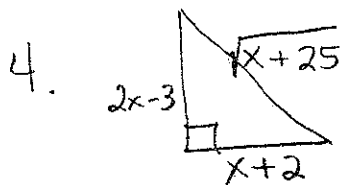
5 points

In $\triangle JKL$, the length of the altitude from L is $5\sqrt{5}$.

Find the length of \overline{KL} (to the nearest tenth).



1. Find the length of a side of a square if a diagonal is
 - a) $6\sqrt{2}$ in.
 - b) 9 in.
 - c) a in.
2. Find the length of an altitude of an equilateral \triangle whose side measures 5 ft.
3. The area of a rhombus is 49 cm^2 and ^{the} length of one diagonal is twice that of the other. Find the length of the shorter diagonal and a side length of the rhombus.



Solve for x

Right Triangle Trig. study guide

Know the following:

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{1}{\cos \theta}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

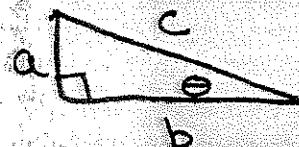
$$\cot \theta = \frac{1}{\tan \theta}$$

$$\sin \theta = \frac{1}{\csc \theta}$$

$$\cos \theta = \frac{1}{\sec \theta}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta}$$

$$\tan \theta = \frac{1}{\cot \theta}$$



SoHcAHToA

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$

Remember, these are reciprocals:

{sin, csc} {cos, sec} {tan, cot}

i.e. $\sin \theta * \csc \theta = 1$

You will probably need these:

$$\cos \theta = \sin(90^\circ - \theta) \text{ i.e. } \cos 32^\circ = \sin 58^\circ$$

$$\sin \theta = \cos(90^\circ - \theta) \text{ i.e. } \sin 43^\circ = \cos 47^\circ$$

Pythagorean Theorem

For any right triangle with legs
a, b and hypotenuse c,

$$a^2 + b^2 = c^2$$

Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$\cot^2 \theta + 1 = \csc^2 \theta$$

$$0 \leq \sin \theta \leq 1$$

$$0 \leq \cos \theta \leq 1$$

$$-\infty \leq \tan \theta \leq +\infty$$