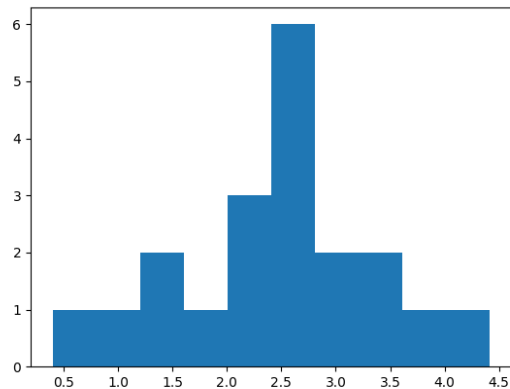
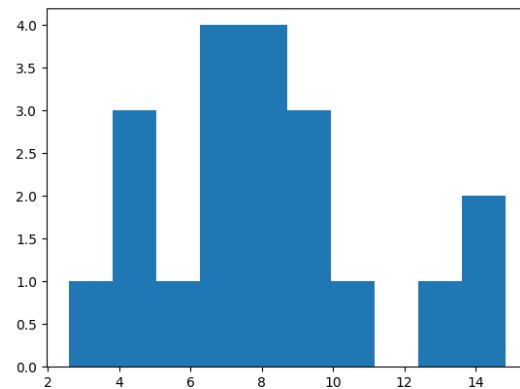


## Bagging: Bootstrap Aggregating



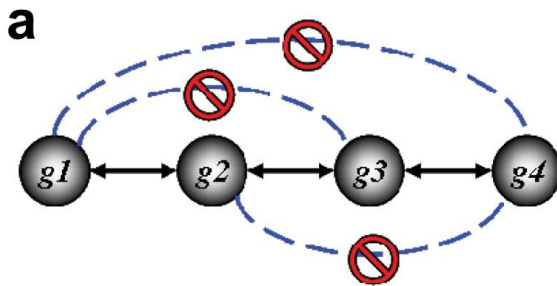
Mean



Variance

## Data Processing Inequality (DPI)

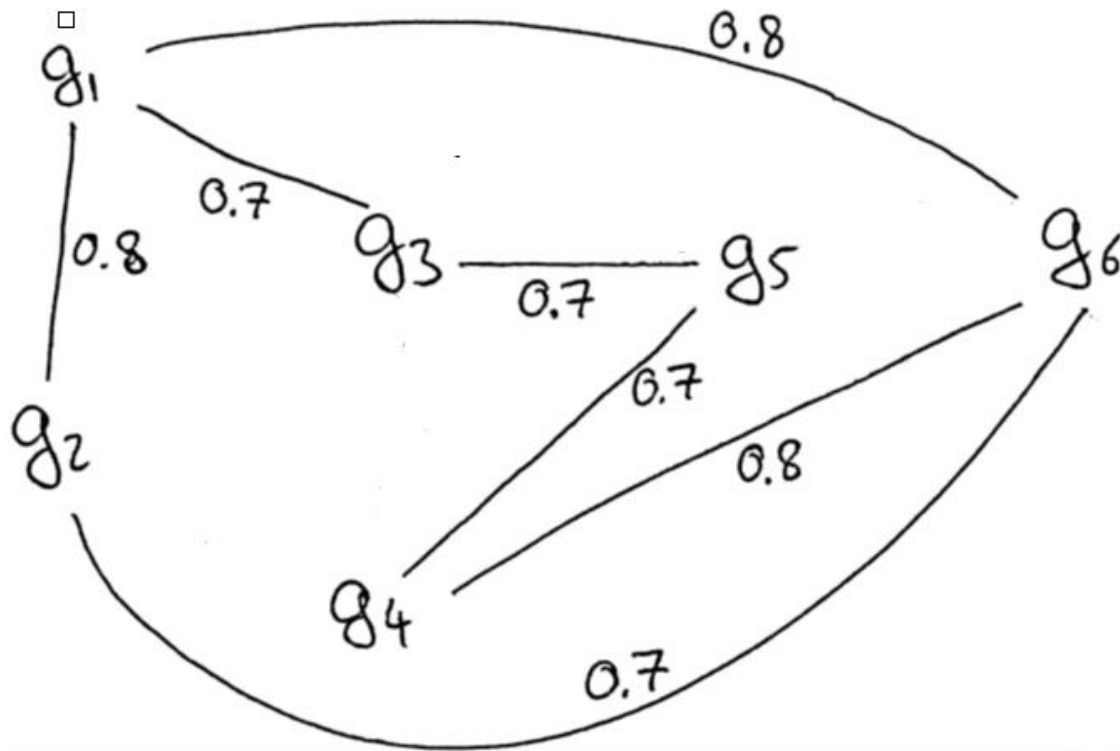
1. DPI:



Examples of the data processing inequality. (a)  $g1$ ,  $g2$ ,  $g3$ , and  $g4$  are connected in a linear chain relationship. Although all six gene pairs will likely have enriched mutual information, the DPI will infer the most likely path of information flow. For example,  $g1 \leftrightarrow g3$  will be eliminated because  $I(g1, g2) > I(g1, g3)$  and  $I(g2, g3) > I(g1, g3)$ .  $g2 \leftrightarrow g4$  will be eliminated because  $I(g2, g3) > I(g2, g4)$  and  $I(g3, g4) > I(g2, g4)$ .  $g1 \leftrightarrow g4$  will be eliminated in two ways: first, because  $I(g1, g2) > I(g1, g4)$  and  $I(g2, g4) > I(g1, g4)$ , and then because  $I(g1, g3) > I(g1, g4)$  and  $I(g3, g4) > I(g1, g4)$ . The issue could be a nonzero DPI threshold is used, if one gene regulate a pathway, the pathway between regulator and gene should not be removed.

*From: ARACNE: An Algorithm for the Reconstruction of Gene Regulatory Networks in a Mammalian Cellular Context*

2.



Network inference challenge

1.

**WGCNA:** 1. Construct a gene co-expression network represented mathematically by an adjacency matrix, the element of which indicates co-expression similarity between a pair of genes. 2. Identify modules 3. Relate modules to phenotypes 4. Study inter-module relationships 5. Find key drivers in interesting modules

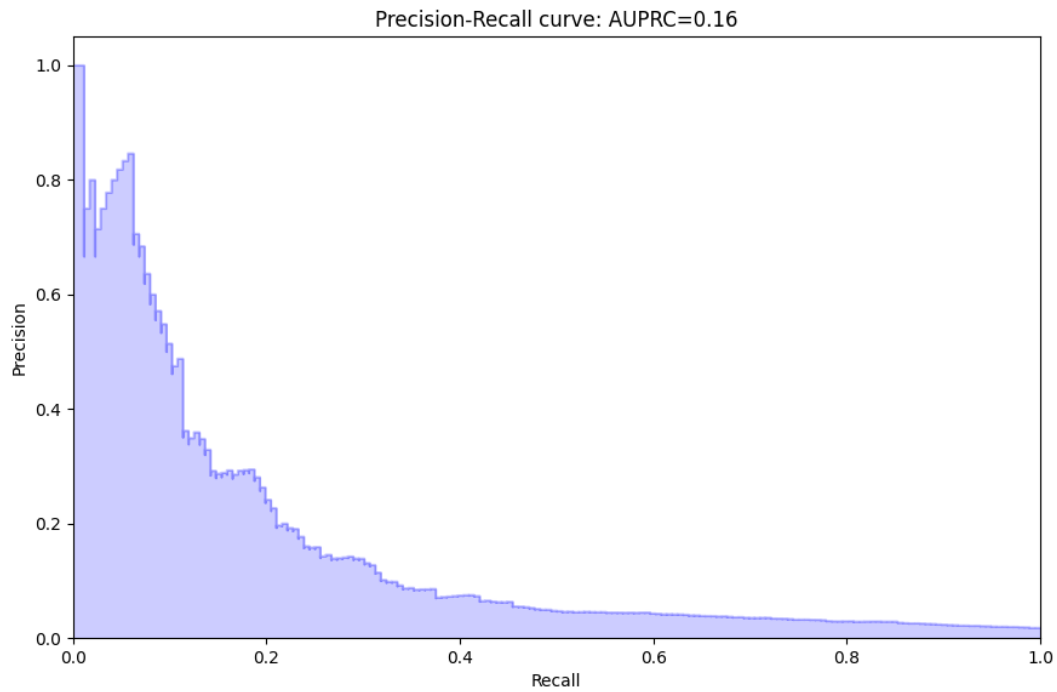
**TIGRESS:** Using a popular feature selection method, least angle regression (LARS) combined with stability selection for GRN inference.

**GENIE3:** The targeted networks are directed graphs with  $p$  nodes, where each node represents a gene, and an edge directed from one gene  $i$  to another gene  $j$  indicates that gene  $i$  (directly) regulates the expression of gene  $j$ . We only consider unsigned edges; when gene  $i$  is connected to gene  $j$ , the former can be either an activator or a repressor of the latter.

**ARACNE:** Identify candidate interactions by estimating pairwise gene expression profile mutual information,  $I(g_i, g_j) \equiv I_{ij}$ , an information-theoretic measure of relatedness that is zero iff  $P(g_i, g_j) = P(g_i)P(g_j)$ . Then filter MIs using an appropriate threshold,  $I_0$ , computed for a specific  $p$ -value,  $p_0$ , in the null-hypothesis of two independent genes. Thus in its second step, ARACNE removes the vast majority of indirect candidate interactions ( $\phi_{ij} = 0$ ) using a well-known information theoretic property, the data processing inequality (DPI).

**CLR:** CLR filtered with negative PCC, least angle regression of time series, TF perturbation data1

2.



### Network inference using single-cell data

As the ground truth for assessing accuracy, we use synthetic networks with predictable trajectories, literature-curated Boolean models and diverse transcriptional regulatory networks. A strategy to simulate single-cell transcriptional data from synthetic and Boolean networks **that avoids pitfalls of previously used methods**. Networks from multiple experimental single-cell RNA-seq datasets collected and use BEELINE frame work to evaluate.

