Q no 1

```
1
          % Constants
  2
          P=zeros(1,step+1);
          P(1) = 1;
  3
  4
         Q = 0.1;
 5
          R = 0.1;
          U = 0;
  6
  7
          A = 1;
         B = 1;
  8
 9
         H = 1;
 10
         step = 10;
 11
         x=zeros(1,step+1);
 12
          K=zeros(1,step+1);
          z = [0, 0.5, 0.52, 0.49, 0.53, 0.45, 0.54, 0.48, 0.47, 0.46, 0.53];
 13
 14
 15 🖃
         for k=1:step
             xest = x(k) + B*U;
                                                           % Project state ahead
 16
 17
              Pest = A*P(k)*transpose(A) + Q;
                                                           % Project error covariance ahead
              K(k+1) = Pest*transpose(H)*inv(H*Pest*transpose(H)+R); % Compute Kalman Gain
 18
              x(k+1) = xest + K(k+1)*(z(k+1)-H*xest); % Update the estimate zk
 19
 20
              P(k+1) = (eye(size(K(k+1)*H,1))-K(k+1)*H)*Pest; % Update error covariance
 21
Command Window
```

Question no. 2 2/K = 2/K-1+WK-1 YK - ykx + VK

The The	0	0 - 1000
0-0-001	, R20.1, No=0,	Po
7		

y1 y2 0.9 0.8	1.1 1.0
7/0 0.899	7/2 7/3 7/4 9 0.8497 8.9319 0.9514

Iferation 1:

niz notwo = 0 PL=Po+Q=1000+0-001 = L000.001

K12 P1 (P1+R)-1 = 1000.001 * 1 1000.101
10,000
21 = 20. + Kr (41-24) = 0.9999 - (0.9-0)
$P_{1} = \hat{P}_{1} - \hat{P}_{1} + K_{K} = (1 - 0.9939) = 1000.001$
-0.1

After Herahim 1, 21= 0.8309, Kz= 0.9999

Iteration 2 n= 0.8999 Â2 0-1+0,001 = 0.101 K2 = 0.101 + (0-201)-1 = 0,5025 722 0.8999+0.5025(0-8-0.8999) P2 = (1-0,5025) = 0. LOL = 0.0502

n= 0.8497, kg=0.5025

Iteration 3

m = 0.8497 P2 2 0.0502+0.001 20.0512

Kz= 0-0512 + (0.1512)-1 = 0-3386 23-0.8497+0-3386+LLI-0,84971-0-9345 P3 = (1-0.3386) + 0.0512 = 0.0339

713=0.9345, P3=0.0339, K3=0.3386

Iferation 4

29 - 0-9345

第-0.0339+0.001

20.0349

79= 0.9514, Rg=0.2587

kq = 0.0349 + 0.0349) = = 0.2587

714 = 0.9345+0.2587(1-0.9345) - 0.9514

Pq = (1-0.2587)+0.0349 = 0.0259

```
YK+L = A74+ BUK+WKN N(0,0)
                                                                                                         quen, A. [1], B. [-0.5], C. [1 0]
                                                                                                                                                                                                                                                      UK=1

YUK+L) | YUK+2) X K | 95], PKK= [10 0], 0: [1 0], R=1

97-9 99-4
Solution: - \lambda_{1} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 9 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 9 & 1 \\ 1 & 1 \end{bmatrix} + \begin{bmatrix} -0.5 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 10 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 10 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 12 \\ 1 & 2 \end{bmatrix}
\hat{P}_{1} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 10 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 10 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 11 & 1 \\ 0
                                                                                                                        N_{L} = \hat{N}_{L} + k_{L} (y_{K} - N^{*}\hat{N}_{L}) = \begin{bmatrix} 95.5 \\ 2 \end{bmatrix} + \begin{bmatrix} 0.9231 \\ 0.0769 \end{bmatrix} \begin{pmatrix} 100 - \begin{bmatrix} 1 & 0 \end{bmatrix} & \begin{bmatrix} 95.5 \\ 2 \end{bmatrix} \end{pmatrix} - \begin{bmatrix} 99.6538 \\ 2-3462 \end{bmatrix}
P_{L} = (I - k_{L} + N) + \hat{R}_{L} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 0.9231 \\ 0.0769 \end{bmatrix} + \begin{bmatrix} 12 & 12 \\ 0.0769 \end{bmatrix} + \begin{bmatrix} 0.9231 \\ 0.9231 \end{bmatrix} + \begin{bmatrix} 0.9231 \\ 0.9
                                                                                                                                        7(K)=[99.653] K [0.923L]
                                                                    Stor k+1

\hat{A}_{1} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 99.6538 \\ 2.2462 \end{bmatrix} + \begin{bmatrix} -0.5 \\ 1 \end{bmatrix} \begin{bmatrix} 13 & 2.3462 \end{bmatrix}

\hat{A}_{2} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 0.9231 & 0.0769 \\ 0.0769 & 1.9231 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 4 & 2 \\ 2 & 2.9231 \end{bmatrix}

k_{2} = \begin{bmatrix} 4 & 2 \\ 2 & 2.9231 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 2 & 2.9231 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.4 \end{bmatrix}

                                                                                                                                                                                n_{2} = \begin{bmatrix} 101.5 \\ 3.3462 \end{bmatrix} + \begin{bmatrix} 0.8 \\ 0.4 \end{bmatrix} \begin{pmatrix} 97.9 - [1 0] \begin{bmatrix} 101.5 \\ 3.3462 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} 98.1769 \\ 3.0692 \end{bmatrix}
                                                                                                                                                                             P_{2} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 0.8 \\ 0.4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} 4 & 2 \\ 2 & 2.3231 \end{bmatrix} \cdot \begin{bmatrix} 0.8 & 0.4 \\ 0.4 & 2.1231 \end{bmatrix}
                                                                                                    Step K+2 94.882 K3 - [0.8253]
                                                                                                              Kalman gain = K K+1 K+2

[0.9231] [0.8] [0.8253]

[0.0769] [0.4] [0.4409]
```

```
1
         % Constants
 2
         P = [10 0; 0 1];
 3
         Q = [1 0; 0 1];
 4
         R = 1;
 5
         x = [95;1];
 6
         A = [1 1; 0 1];
 7
         B = [-0.5 1];
 8
         H = [1 0];
 9
         U = 1;
10
         z = [0\ 100\ 97.9\ 94.4];
         step = 3;
11
         KalmanGain=[0;0];
12
13
         for k=1:step
14
             xest = A*x + B*U;
                                           % Project state ahead
15
            Pest = A*P*transpose(A)+ Q;  % Project error covariance ahead
16
17
             K = Pest*transpose(H)*inv(H*Pest*transpose(H)+R); % Compute Kalman Gain
18
             x = xest + K*(z(k+1)-H*xest); % Update the estimate zk
19
             P = (eye(size(P,2))-K*H)*Pest; % Update error covariance
20
21
         end
22
         disp("Kalman Gain:")
```

Command Window

```
0.9231 0.8000 0.8253
0.0769 0.4000 0.4409
```

Kalman gain for k, k+1 and k+2.

Trucker) = = 1 milk) + [0] wk) yck). [2 1] nelk) A. [-0.5 1]. B. [0], C=4=[2 1], P. [10 0], Q. 1. [1 0]. R=5 Say [NIK)]. [0], Vx. [1] (supposed) Iteration 1 2 = [-0.5 1] [0] + [0] [1] [1] [1] [0] $\hat{P}_{\mathbf{x}} = \begin{bmatrix} -0.5 & 1 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} 10 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} -0.5 & 0.5 \\ 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 4.5 & -1.5 \\ -1.5 & 3.5 \end{bmatrix}$ 10 valuer of meanment with varionce (2001 is assumed

K= [4.5 -1.5] [2] [22 17 [4.5 -1.5] [2] + 5) -1 = [0.3659]

-1.5 3.5] [1] (-1.5 3.5] [2] (-1.5 3.5) [1] $26 = \begin{bmatrix} 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 0.3459 \\ 0.0244 \end{bmatrix} \begin{bmatrix} 0.5 - [2 \ 1] \begin{bmatrix} 0 \\ 1 \end{bmatrix} \end{bmatrix} = \begin{bmatrix} -0.1829 \\ 0.9878 \end{bmatrix}$ $P_{L} = \begin{bmatrix} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} - \begin{pmatrix} 0.3659 \\ 0.0244 \end{pmatrix} \begin{pmatrix} 2 & 1 \end{pmatrix} \end{bmatrix} \begin{bmatrix} 4.5 & -1.5 \\ -1.5 & 3.5 \end{bmatrix} = \begin{bmatrix} 1.7561 & -1.6829 \\ -1.6829 & 3.4878 \end{bmatrix}$ $\frac{1}{2} = \begin{bmatrix} -0.5 & 1 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} -0.1829 \\ 0.9878 \end{bmatrix} + \begin{bmatrix} 0 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \cdot \begin{bmatrix} 0.8963 \\ 1.0915 \end{bmatrix} + \begin{bmatrix} 3.2439 & 1.4024 \\ 1.4024 & 1.4390 \end{bmatrix} + \begin{bmatrix} 0 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} 1.35 & 1.6 \\ -1.68 & 34 \end{bmatrix} \begin{bmatrix} -0.5 & 0.5 \\ 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 3.2439 & 1.4024 \\ 1.4024 & 1.4390 \end{bmatrix} + \begin{bmatrix} 0.5 & 0.5 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} -1.68 & 34 \end{bmatrix} \begin{bmatrix} -0.5 & 0.5 \\ 1 & 0 \end{bmatrix} + \begin{bmatrix} 0.2425 & 1.4024 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} -1.68 & 34 \end{bmatrix} \begin{bmatrix} -1.68 & 34 \end{bmatrix} = \begin{bmatrix} 0.8963 & 0.5 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} 0.8963 & 0.5 \\ 0.5 & 0 \end{bmatrix} = \begin{bmatrix} 0.8963 & 0.5 \\ 0.5 & 0 \end{bmatrix} = \begin{bmatrix} 0.8963 & 0.5 \\ 0.5 & 0.5 \end{bmatrix} = \begin{bmatrix} 0.8963 & 0.5 \\ 0.$ $k_2 = \begin{bmatrix} 3.2939 & 1.4024 \\ 1.4029 & 1.4390 \end{bmatrix} \begin{bmatrix} 2 & 1 \end{bmatrix} \begin{bmatrix} 2 & 1 \end{bmatrix} \begin{bmatrix} 3.2435 & 1.4024 \\ 1.4029 & 1.4390 \end{bmatrix} \begin{bmatrix} 2 \end{bmatrix} + 5 \end{bmatrix}^{-1} \begin{bmatrix} 0.3153 \\ 0.1636 \end{bmatrix}$ $\gamma_{2} = \begin{bmatrix} 0.8963 \\ 1.0915 \end{bmatrix} + \begin{bmatrix} 0.3153 \\ 0.1696 \end{bmatrix} \begin{pmatrix} 0.52 - \begin{bmatrix} 2 \\ 1 \end{bmatrix} \begin{bmatrix} 0.8963 \\ 0.0915 \end{bmatrix} \end{pmatrix} \cdot \begin{bmatrix} 0.1509 \\ 0.6905 \end{bmatrix}$ $\beta_{2} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} - \begin{bmatrix} 0.3153 \\ 0.1696 \end{pmatrix} \begin{pmatrix} 2 & 1 \end{bmatrix} \begin{bmatrix} 0.2439 & 1.4024 \\ 1.4024 & 1.4390 \end{bmatrix} \cdot \begin{bmatrix} 0.3561 & 0.0643 \\ 0.0643 & 0.2193 \end{bmatrix}$ $\frac{1}{\sqrt{3}} \left[\begin{array}{c} 0.5 & 1 \\ 0.5 & 0 \end{array} \right] \left[\begin{array}{c} 0.1509 \\ 0.6905 \end{array} \right] + \left[\begin{array}{c} 0 \\ 1 \end{array} \right] \left[\begin{array}{c} 1 \\ 0.9295 \end{array} \right] \\
0.5 & 0 \end{array} \left[\begin{array}{c} 0.1509 \\ 0.6905 \end{array} \right] + \left[\begin{array}{c} 0 \\ 1 \end{array} \right] \left[\begin{array}{c} 1 \\ 0.9295 \end{array} \right] \\
0.5 & 0 \end{array} \left[\begin{array}{c} 0.7560 \\ 0.9245 \end{array} \right] \left[\begin{array}{c} 0.756 \\ 0.064 \end{array} \right] \left[\begin{array}{c} 0.9760 \\ 0.9245 \end{array} \right] \\
0.5 & 0 \end{array} \left[\begin{array}{c} 0.9245 \\ 0.9245 \end{array} \right] \left[\begin{array}{c} 0.756 \\ 0.064 \end{array} \right] \left[\begin{array}{c} 0.979 \\ 0.978 \end{array} \right] \left[\begin{array}{c} 2 \\ 1 \end{array} \right] + 5 \right)^{-1} \cdot \left[\begin{array}{c} 0.2747 \\ 0.1597 \end{array} \right] \\
0.1972 \quad 0.778 \quad 0.1597 \quad 0.$

```
Q no 4 a)
      % Input Data
      A = [0.5 1; -0.5 0];
      B = [0;1];
      C = [2 1];
      Q = 1;
      R = 5;
      Y = [.50 .52 .49 .53 .45 .54 .48 .47 .46 .53]; % Assumed
      U = 1; % Assumed
      P = [10 0; 0 1]; % Assumed
      X = [0;0];
      KG = [0;0];
      xPredict = [0;0];
      pPredict = [0 0; 0 0];
      updatedStates = [0;0];
      updatedCovariance = [0 0; 0 0];
      for i=1:10
        % Make predictions
        X = A*X + B*U;
        xPredict = [xPredict X];
        P = A*P*transpose(A) + Q;
        pPredict = [pPredict P];
        % Calculate Kalman Gain
        K = P*transpose(C)*(inv(C*P*transpose(C)+R));
        KG = [KG K];
        % Update estimates
        X = X + K^*(Y(i)-C^*X);
        updatedStates = [updatedStates X];
        P=(eye(size(P,2))-K*C)*P;
        updatedCovariance = [updatedCovariance P];
      end
 Kalman Gain
 ans =
     0.3659 0.3153 0.2747 0.2733 0.2726 0.2725 0.2725 0.2725 0.2725 0.2725
     0.0244 0.1696 0.1597 0.1630 0.1627 0.1628 0.1627 0.1627 0.1627 0.1627
```

Q no 4 b)

```
% Input Data A = [0\ 1\ 0;\ .25\ 0\ 1;\ 0\ 0\ 0]; B = [2;0;1]; C = [1\ 0\ 0;\ 1\ -1\ 1]; U = 1; P = [10\ 0\ 0;\ 0\ 1\ 0;\ 0\ 0\ 1];\ \text{\% Assumed} Q = 5; R = [2\ 0;\ 0\ 3]; Y = [.50\ .52\ .49\ .53\ .45\ .54\ .48\ .47\ .46\ .53];\ \text{\% Assumed} X = [0;\ 0;\ 0]; KG = [0\ 0;\ 0\ 0;\ 0\ 0]; xPredict = [0\ 0;\ 0\ 0;\ 0\ 0]; updatedStates = [0\ ;\ 0;\ 0]; updatedCovariance = [0\ 0\ 0;\ 0\ 0\ 0];
```

```
Kalman Gain
ans =
 Columns 1 through 14
 Columns 15 through 20
                       0.6534
  0.6533 0.2162
            0.6534 0.2162
                             0.2162
  0.6555 0.0868 0.6551
0.3264 0.3415 0.3260
                  0.0871
                       0.6553
                             0.0870
                            0.3416
                  0.3416
                       0.3261
```