

| Main Topic             | Sub-topic                   | Definition   | Where to Use                       | Formulas  | Use Case                       | Example                                       | Main Goal                                  |
|------------------------|-----------------------------|--|------------------------------------|---|--------------------------------|---|--|
| Descriptive Statistics | Central Tendency            | Measures of average  | EDA, reporting                     | Mean = $\Sigma x/n$ , Median, Mode  | Summarize sales data           | Mean revenue = ₹10K                           | Summarize data                             |
|                        | Dispersion                  | Spread of data   | Quality control                    | Range, Variance, SD   | Product dimension variability  | SD of delivery time = 2 hrs                   | Measure consistency                        |
|                        | Skewness                    | Measures the <b>asymmetry</b> of a distribution                            | EDA, distribution check            | Skewness = $3(\text{Mean} - \text{Median})/\text{SD}$ or using 3rd moment | Income distribution skew       | Positive skew (long right tail)               | Identify direction of data imbalance       |
|                        | Kurtosis                    | Measures the <b>tailedness</b> (peakedness) of a distribution              | Risk analysis, QC                  | Excess Kurtosis = $(\mu_4/\sigma^4) - 3$                                  | Financial returns sharp peaks  | High kurtosis (leptokurtic)                   | Detect presence of outliers or heavy tails |
| Inferential Statistics | Estimation                  | Estimate population parameters   | Survey sampling                    | CI = Mean $\pm$ Z*(SD/ $\sqrt{n}$ )                                       | Predict avg. voter turnout     | CI = 60% $\pm$ 3%                             | Generalize from sample                     |
|                        | Hypothesis Testing          | Test population assumptions using sample data                              | A/B testing, drug trials, UX tests | p-value, t-test, z-test, chi-square                                       | Compare control vs test group  | $p < 0.05 \rightarrow$ reject null hypothesis | Make data-driven decisions                 |
|                        | Confidence Interval         | Range of values likely to contain population parameter                     | Estimating unknown parameters      | CI = mean $\pm$ Z * ( $\sigma / \sqrt{n}$ )                               | Estimating average income      | CI = ₹52,000 $\pm$ ₹2,000                     | Express uncertainty in estimates           |
| Hypothesis Testing     | Null Hypothesis (H0)        | Default assumption (no effect or no difference)                            | All tests begin with H0            | –   | Assume both drugs work equally | H0: $\mu_1 = \mu_2$                           | Benchmark to test against                  |
|                        | Alternative Hypothesis (H1) | Contradicts H0, represents a real effect or change                         | When evidence suggests a change    | –   | New drug better than old       | H1: $\mu_1 \neq \mu_2$                        | What we try to prove                       |
|                        | P-value                     | Probability of observing a test statistic as extreme as sample assuming H0 | All statistical tests              | P = P(T > t_obs_H0)   |                                | Compare with $\alpha$ to decide H0            | $p = 0.03 < 0.05 \rightarrow$ Reject H0    |

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| Hypothesis Testing  | Significance Level ( $\alpha$ ) | Threshold below which H0 is rejected  | All statistical tests               | Common $\alpha = 0.05, 0.01$                                       | Control Type I error rate                    | $\alpha = 0.05$ means 5% false positive rate                  | Decide cutoff for significance           |
|                     | One-Tailed Test                 | Tests effect in one direction   | Direction-specific testing          | –  | Is new design better than old?               | H1: $\mu_1 > \mu_2$   | Test for improvement only                |
|                     | Two-Tailed Test                 | Tests effect in both directions   | General comparisons                 | –  | Is there any difference?                     | H1: $\mu_1 \neq \mu_2$  | Check for any change                     |
|                     | Type I Error ( $\alpha$ )       | Rejecting H0 when it's actually true (false positive)                       | Significance level                  | –  | False claim drug works                       | $\alpha = 0.05$   | Control false positives                  |
|                     | Type II Error ( $\beta$ )       | Not rejecting H0 when it's false (false negative)                           | Power analysis                      | –  | Miss a real drug effect                      | $\beta = 0.2$   | Control false negatives                  |
|                     | T-Test                          | Compares means between groups (when population SD is unknown, small sample) | Compare two means                   | $t = (\bar{X}_1 - \bar{X}_2) / \sqrt{[(s_1^2/n_1) + (s_2^2/n_2)]}$ | Drug A vs Drug B effect                      | Test if new drug has better mean recovery time                | Compare means of small samples           |
|                     | F-Test                          | Compares <b>variances</b> of two populations                                | Variance testing before ANOVA       | $F = s_1^2 / s_2^2$ (s = sample variance)                          | Test if two processes have equal variability | $F = \text{Var}(\text{Group A}) / \text{Var}(\text{Group B})$ | Assess equality of variances             |
|                     | Chi-Square Test                 | Tests <b>association</b> between categorical variables or goodness of fit   | Categorical data, independence, fit | $\chi^2 = \sum [(O - E)^2 / E]$                                    | Gender vs Preference, Dice fairness          | $\chi^2 = 10.2, df = 4, p < 0.05$                             | Test independence or distribution shape  |
|                     | ANOVA (One-Way)                 | Compare means across 3 or more groups                                       | Group mean comparison               | $F = \text{MS}_{\text{between}} / \text{MS}_{\text{within}}$       | Compare A/B/C variants                       | $F = 3.6, p < 0.05 \rightarrow$ Significant difference        | Generalize t-test to >2 groups           |
| Sampling Techniques | Z-Test                          | Compare sample mean to population mean (large n or known $\sigma$ )         | Mean testing with known SD          | $z = (\bar{X} - \mu) / (\sigma / \sqrt{n})$                        | Population testing with known SD             | $z = 2.5, p < 0.05 \rightarrow$ Significant result            | Test population mean with known variance |
|                     | Simple Random                   | Equal chance for every item   | Surveys                             | -  | General voter polling                        | Lottery method  | Reduce bias                              |

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|                     | Stratified                   | Divide by subgroups                        | Population analysis       | -  | Income-based study      | Divide by salary ranges                      | Better representation         |
|                     | Cluster                      | Random groups or clusters                  | Geographical sampling     | -  | City-wise polling       | Random schools in districts                  | Cost-efficient sampling       |
|                     | Systematic                   | Every kth item                             | Manufacturing, production | -  | Quality control         | Pick every 10th item                         | Simple implementation         |
| Probability         | Classical                    | Based on theory                            | Games, experiments        | $P(A) = \text{Favorable/Total outcomes}$ | Dice games              | $P(6) = 1/6$                                 | Quantify theoretical outcomes |
|                     | Empirical                    | Based on past data                         | Forecasting               | $P = \text{freq}(A)/n$                   | Weather prediction      | $P(\text{Rain}) = 0.6$                       | Use observed data             |
|                     | Subjective                   | Based on belief                            | Expert systems            | -  | Stock forecast          | $P(\text{Growth}) = 0.8$ (belief)            | Model expert opinion          |
|                     | Conditional                  | Probability of A given B                   | Risk analysis             | $P(A/B) = P(A \cap B)/P(B)$              |                         | Defects by supplier                          | $P(\text{Defect})$            |
|                     | Bayes' Theorem               | Update beliefs with evidence               | Medical diagnosis         | $P(A/B) = [P(B/A) \cdot P(A)]/P(B)$      |                         |  | Test accuracy                 |
| Descriptive Summary | 5-Number Summary             | Statistical spread                         | Boxplots, visualization   | -  | Understand distribution | [Min, Q1, Median, Q3, Max]                   | Summarize distribution shape  |
| Combinatorics       | Permutations                 | Arrangements where order matters           | Ranking, passwords        | $nPr = n! / (n-r)!$                      | Arrange 3 of 5 books    | $P(5,3) = 60$                                | Count ordered outcomes        |
|                     | Combinations                 | Selections where order doesn't matter      | Group selection, lottery  | $nCr = n! / (r!(n-r)!)$                  | Choose 3 players from 5 | $C(5,3) = 10$                                | Count unordered outcomes      |
| Distributions       | Normal Distribution          | Bell-shaped, symmetric curve               | Heights, exam scores      | PDF formula                              | Model scores            | Mean=Median=Mode                             | Model natural variation       |
|                     | Binomial Distribution        | Success/failure in fixed trials            | Surveys, quality checks   | $P(X=k) = C(n,k)p^k(1-p)^{(n-k)}$        | Yes/No answers          | $P(3 \text{ heads in } 5 \text{ flips})$     | Model binary outcomes         |
|                     | Poisson Distribution         | Count of rare events in interval           | Traffic, calls            | $P(X=k) = \lambda^k e^{-\lambda} / k!$   | Calls per min           | $\lambda = 3 \rightarrow P(2 \text{ calls})$ | Model rare events             |
|                     | Standard Normal Distribution | Normal distribution with $\mu=0, \sigma=1$ | Z-score analysis          | $Z = (x-\mu)/\sigma$                     | Standardize marks       | $Z = 1.5$                                    | Compare across datasets       |

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|                   | Log-Normal Distribution | Distribution of $\log(x)$ is normal             | Income, biology, stocks | $\log(X) \sim N(\mu, \sigma^2)$                                       | Stock returns, income    | log-normal distribution                     | Model skewed positive data  |
|                   | Bernoulli Distribution  | Only two outcomes: success/failure              | Binary outcome modeling | $P(X=1)=p$ ,<br>$P(X=0)=1-p$  | Coin toss, trial success | $P(\text{success})=0.5$                     | Model single binary event   |
| Relationships     | Correlation             | Measures strength and direction of relationship | EDA, feature selection  | $r = \text{Cov}(X,Y)/(\sigma_X \cdot \sigma_Y)$                       | Study time vs marks      | $r = 0.85 \rightarrow$ strong +ve           | Identify linear link        |
|                   | Covariance              | Measures direction of joint movement            | Portfolio analysis      | $\text{Cov}(X,Y) = \sum (x-\bar{X})(y-\bar{Y})/(n-1)$                 | Stocks A & B             | $\text{Cov} > 0 \rightarrow$ both rise      | Track co-movement           |
| Data Scaling      | Normalization           | Scale data to 0–1 range                         | ML, image data          | $(x-\text{min})/(\text{max}-\text{min})$                              | Pixel scaling            | [0,1] range                                 | Uniform scale               |
|                   | Standardization         | Scale data to mean=0, SD=1                      | ML models, z-scores     | $(x-\text{mean})/\text{SD}$   | PCA, Z-score use         | $Z = 1.2$                                   | Handle different units      |
|                   | Mean Normalization      | Centers values around 0 using mean              | ML preprocessing        | $(x-\text{mean})/(\text{max}-\text{min})$                             | Salary data scaling      | Normalized range: -1 to 1                   | Center around mean          |
|                   | Robust Scaling          | Uses median and IQR to scale                    | Skewed/outlier data     | $(x-\text{median})/\text{IQR}$  | Income distribution      | Less impacted by outliers                   | Handle outliers robustly    |
|                   | Log Transformation      | Reduces skew, compresses data range             | Right-skewed data       | $\log(x)$ or $\log(x+1)$  | Sales data               | $\log(1000) = 3$                            | Normalize positive skew     |
|                   | Decimal Scaling         | Scales down by powers of 10                     | Financial data          | $x / 10^j$ (j makes $ x  < 1$ )                                       | x                        | $< 1$ )                                     | ₹100000 becomes 1           |
| Outlier Detection | Z-Score Method          | Measures distance from mean in SDs              | Cleaning data           | $Z = (x-\text{mean})/\text{SD}$                                       | Remove extreme points    | $Z = 4 \rightarrow$ outlier                 | Detect distant values       |
|                   | IQR Method              | Uses quartiles to detect extremes               | Boxplots, visuals       | Outlier: $< Q1-1.5 \times \text{IQR}$ or $> Q3+1.5 \times \text{IQR}$ | Identify anomalies       | $\text{Value} > Q3 + 1.5 \times \text{IQR}$ | Remove statistical extremes |