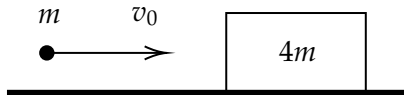


Problem 15

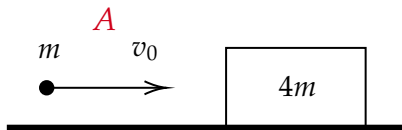
A bullet of mass m and velocity v_0 is fired toward a block of mass $4m$. The block is initially at rest on a frictionless horizontal surface. The bullet penetrates the block and emerges with a velocity of $\frac{v_0}{3}$



- a) Determine the final speed of the block.
- b) Determine the loss in kinetic energy of the bullet.
- c) Determine the gain in the kinetic energy of the block.

Problem 15

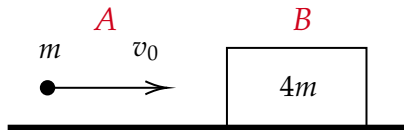
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Problem 15

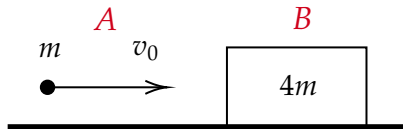
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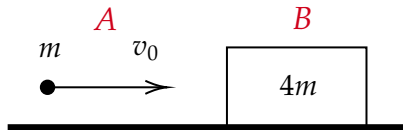
Problem 15

- a) Determine the final speed of the block.



Problem 15

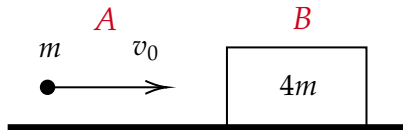
- a) Determine the final speed of the block.



$$m_A v_A + m_B v_B = m_A v'_A + m_B v'_B$$

Problem 15

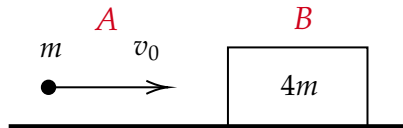
- a) Determine the final speed of the block.



$$m_A v_A + \cancel{m_B v_B} = m_A v'_A + m_B v'_B$$

Problem 15

- a) Determine the final speed of the block.

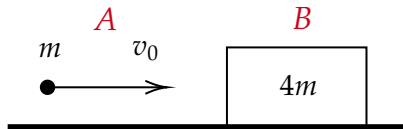


$$m_A v_A + m_B v_B = m_A v'_A + m_B v'_B$$

$$m v_0 = m \left(\frac{v_0}{3} \right) + (4m) v'_B$$

Problem 15

- a) Determine the final speed of the block.



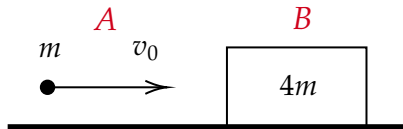
$$m_A v_A + m_B v_B = m_A v'_A + m_B v'_B$$

$$m v_0 = m \left(\frac{v_0}{3} \right) + (4m) v'_B$$

$$\cancel{m} v_0 - \frac{6}{3} > \cancel{m} v_0 = 4m v'_B$$

Problem 15

- a) Determine the final speed of the block.



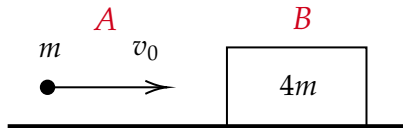
$$m_A v_A + m_B v_B = m_A v'_A + m_B v'_B$$

$$m v_0 = m \left(\frac{v_0}{3} \right) + (4m) v'_B$$

$$m v_0 - \frac{m v_0}{3} = 4m v'_B$$

Problem 15

- a) Determine the final speed of the block.



$$m_A v_A + m_B v_B = m_A v'_A + m_B v'_B$$

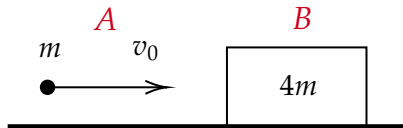
$$m v_0 = m \left(\frac{v_0}{3} \right) + (4m) v'_B$$

$$m v_0 - \frac{6}{3} m v_0 = 4m v'_B$$

$$v'_B = \frac{1}{4} \left(v_0 - \frac{v_0}{3} \right)$$

Problem 15

- a) Determine the final speed of the block.



$$m_A v_A + m_B v_B = m_A v'_A + m_B v'_B$$

$$m v_0 = m \left(\frac{v_0}{3} \right) + (4m) v'_B$$

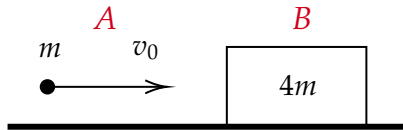
$$m v_0 - \frac{6}{3} m v_0 = 4m v'_B$$

$$v'_B = \frac{1}{4} \left(v_0 - \frac{v_0}{3} \right)$$

$$\boxed{v'_B = \frac{v_0}{6}}$$

Problem 15

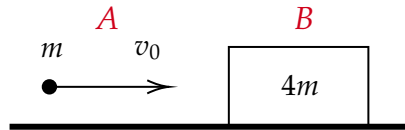
b) Determine the loss in kinetic energy of the bullet.



Problem 15

b) Determine the loss in kinetic energy of the bullet.

$$K = \frac{1}{2}mv^2$$

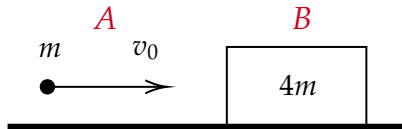


Problem 15

b) Determine the loss in kinetic energy of the bullet.

$$K = \frac{1}{2}mv^2$$

$$K_A = \frac{1}{2}mv_0^2$$



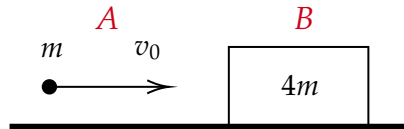
Problem 15

b) Determine the loss in kinetic energy of the bullet.

$$K = \frac{1}{2}mv^2$$

$$K_A = \frac{1}{2}mv_0^2$$

$$K'_A = \frac{1}{2}mv_A'^2$$



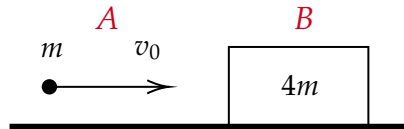
Problem 15

b) Determine the loss in kinetic energy of the bullet.

$$K = \frac{1}{2}mv^2$$

$$K_A = \frac{1}{2}mv_0^2$$

$$\begin{aligned} K'_A &= \frac{1}{2}mv'_A{}^2 \\ &= \frac{1}{2}m\left(\frac{v_0}{3}\right)^2 \end{aligned}$$



Problem 15

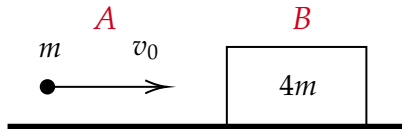
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$$K'_A = \frac{mv_0^2}{18}$$



Problem 15

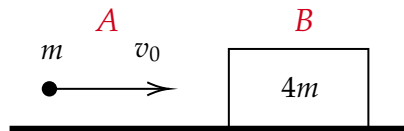
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$$K'_A = \frac{mv_0^2}{18}$$



$$\Delta K_A = K'_A - K_A$$

Problem 15

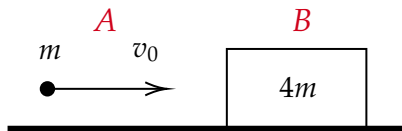
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$$\begin{aligned} K'_A &= \frac{1}{2}mv'_A{}^2 \\ &= \frac{1}{2}m\left(\frac{v_0}{3}\right)^2 \end{aligned}$$

$$K'_A = \frac{mv_0^2}{18}$$



$$\begin{aligned} \Delta K_A &= K'_A - K_A \\ &= \frac{1}{18}mv_0^2 - \frac{1}{2}mv_0^2 \end{aligned}$$

Problem 15

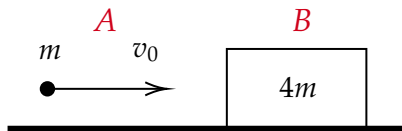
b) Determine the loss in kinetic energy of the bullet.

$$K = \frac{1}{2}mv^2$$

$$K_A = \frac{1}{2}mv_0^2$$

$$\begin{aligned} K'_A &= \frac{1}{2}mv'_A{}^2 \\ &= \frac{1}{2}m\left(\frac{v_0}{3}\right)^2 \end{aligned}$$

$$K'_A = \frac{mv_0^2}{18}$$

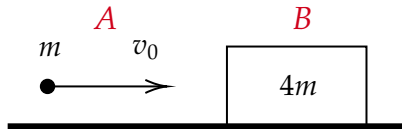


$$\begin{aligned} \Delta K_A &= K'_A - K_A \\ &= \frac{1}{18}mv_0^2 - \frac{1}{2}mv_0^2 \end{aligned}$$

$$\Delta K_A = -\frac{4}{9}mv_0^2$$

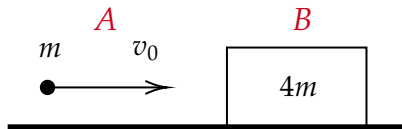
Problem 15

- c) Determine the gain in the kinetic energy of the block.



Problem 15

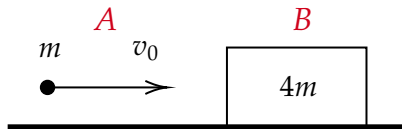
- c) Determine the gain in the kinetic energy of the block.



$$K_B = 0$$

Problem 15

- c) Determine the gain in the kinetic energy of the block.

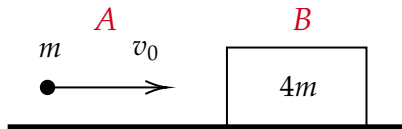


$$K_B = 0$$

$$K'_B = \frac{1}{2} m_B v_B^2$$

Problem 15

- c) Determine the gain in the kinetic energy of the block.

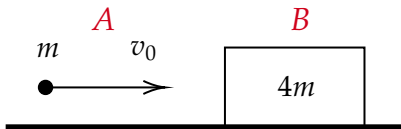


$$K_B = 0$$

$$\begin{aligned} K'_B &= \frac{1}{2} m_B v_B^2 \\ &= \frac{1}{2} (4m) \left(\frac{v_0}{3} \right)^2 = \frac{1}{18} m v_0^2 \end{aligned}$$

Problem 15

- c) Determine the gain in the kinetic energy of the block.



$$K_B = 0$$

$$\begin{aligned} K'_B &= \frac{1}{2} m_B v_B^2 \\ &= \frac{1}{2} (4m) \left(\frac{v_0}{3} \right)^2 = \frac{1}{18} m v_0^2 \end{aligned}$$

$$\Delta K_B = K'_B - K_B = \frac{1}{18} m v_0^2$$