

Review

What is the variable space requirement?

$$\begin{aligned} f(n) &= n * f(n-1) & \text{for } n > 1 \\ f(n) &= 1 & \text{for } n \leq 1 \end{aligned}$$

Given that $n=N$, the **size** of the input parameter= K , and the **size** of return address= M .

Q1: • **Iterative**

```
double iterFact(int n)
{
    int i;
    double answer;
    if ((n == 0) || (n == 1)) return 1.0;
    answer = 1.0;
    for (i = n; i > 1; i--)
        answer *= i;
    return answer;
}
```

Ans: 0

Q2: • **Recursive**

```
double recurFact(int n)
{
    if ((n==0) || (n==1)) return 1.0;
    return n*recurFact(n-1);
}
```

n=2,3,...,N

size += K

n=1

size += K

size += M

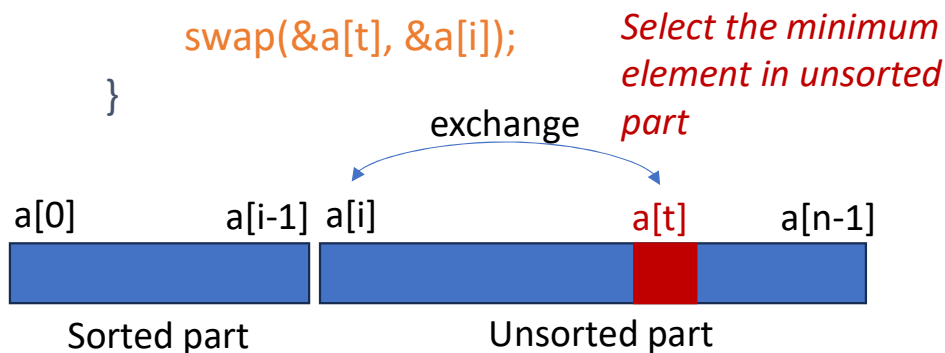
size += M

Total: $N*(K+M)$

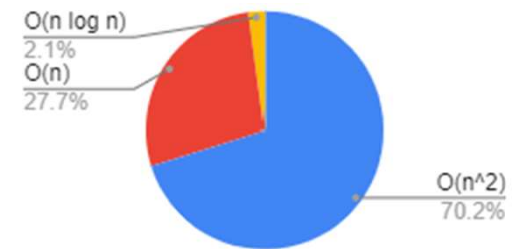
What is the time complexity?

- **Selection sort**

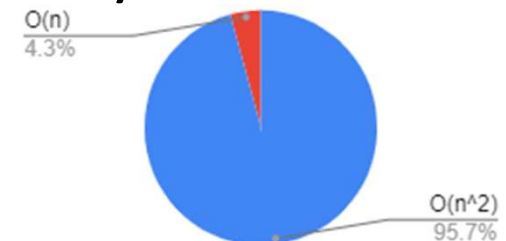
```
for (i = 0; i < n-1; i++)  
{ /*Find the minimum element in a[i:n-1]*/  
  int t = i;  
  for (j = i+1; j < n; j++)  
    if (a[j] < a[t])  
      t = j;  
  /* Swap the minimum element with the a[i]*/  
  if (t != i)  
    swap(&a[t], &a[i]);  
}
```



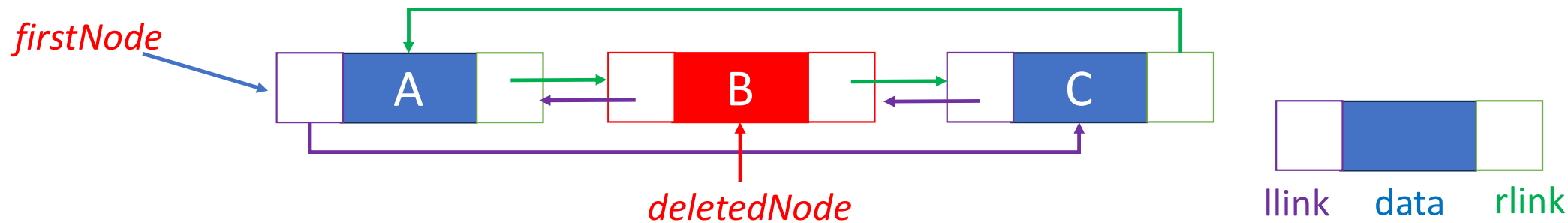
- Q3: Given a list in **increasing** order, what is the time complexity of selection sort?



- Q4: Given a list in **decreasing** order, what is the time complexity of selection sort?



Deleting the node containing “B” (*deletedNode*)



- Q5: Please describe the procedure to remove *deletedNode* from the doubly circular linked list. The node includes three fields: llink, data, and rlink.

```
deletedNode->llink->rlink = deletedNode->rlink;  
deletedNode->rlink->llink = deletedNode->llink;  
free(deletedNode);
```

How do we improve these answers?

把要刪除的左邊元素rlink連到右邊元素，
右邊元素的llink連到左邊元素

Delete link between AB and
between BC.

Link rlink of A to C

Link llink of C to A

前一個的rlink 指向下一個
下一個的llink 指向前一個

```
C->leftlink=B->leftlink;  
A->rightlink=B->rightlink;  
free(B);
```

A=beforeNode

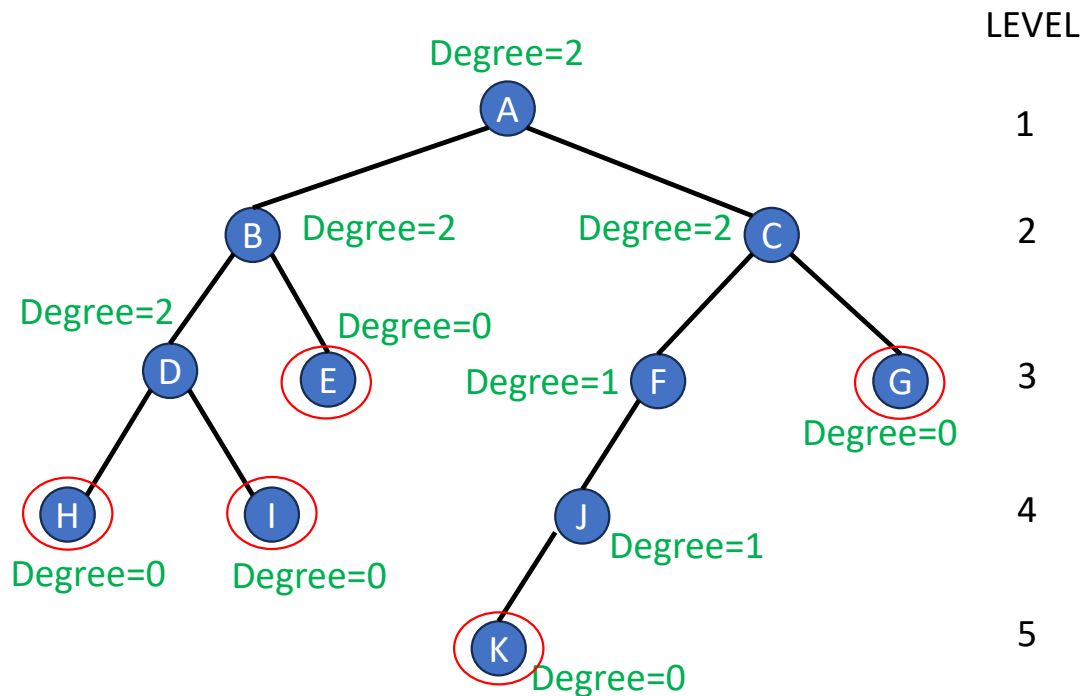
B=deletedNode

```
beforeNode->rlink=deletedNode->rlink
```

```
deletedNode->rlink->llink=beforeNode
```

```
free(deletedNode)
```

Binary tree



LEVEL

1

2

3

4

5

Q6: The degree of the tree 2

Q7: The depth of the tree 5

Q8: List the leaf nodes
H, I, J, E, K, G have degree=0.

Q9: The sibling of node E
D and E have the same parent B.

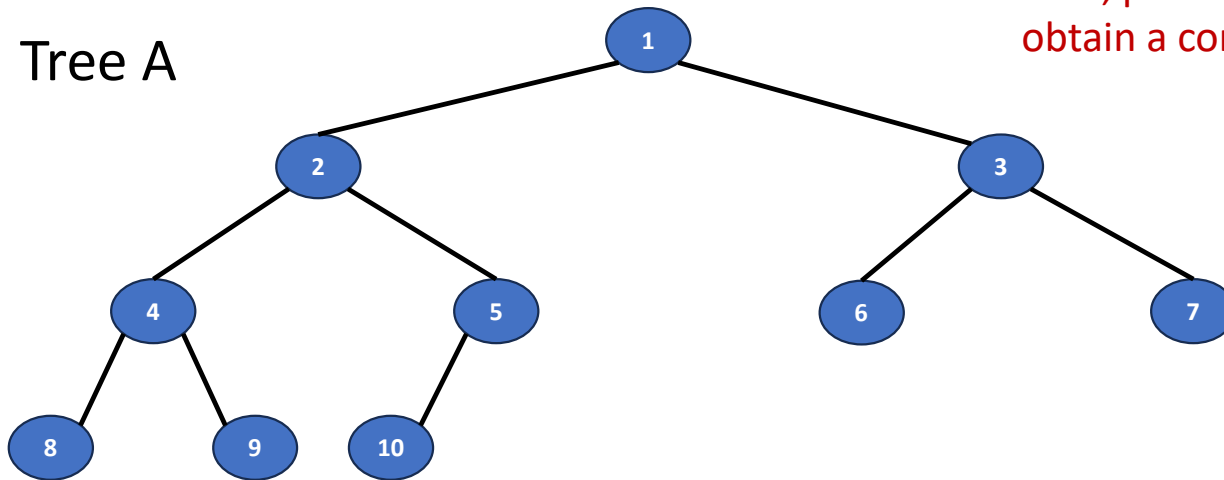
Q10: The children of node C
 Nodes in the next level of C
 and linking to C are F and G.

Q11: The level of node K 5

Q12: Are Tree A and Tree B complete binary trees?

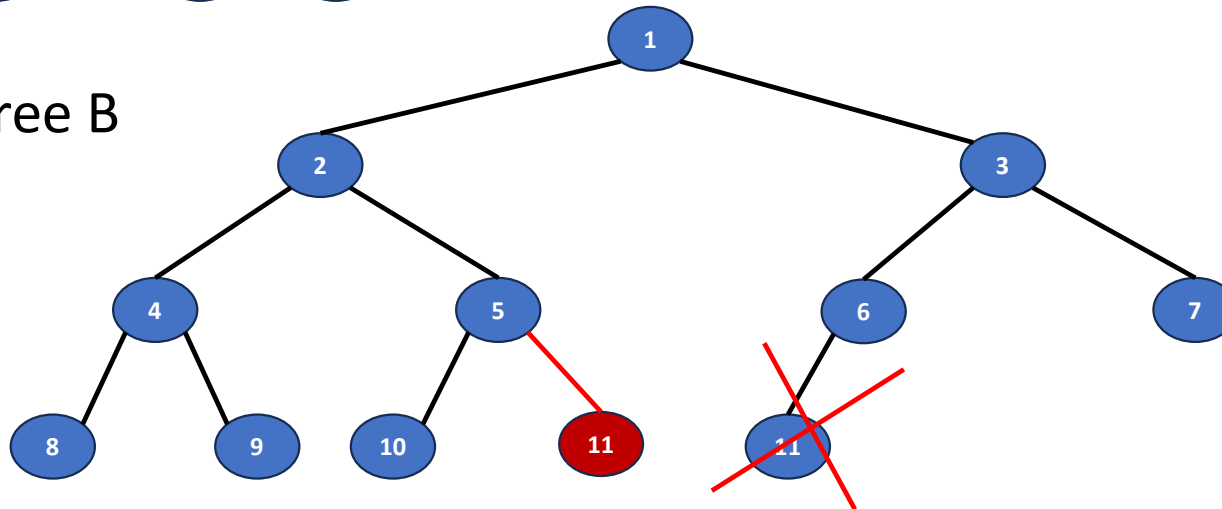
If no, please describe how to modify the tree to obtain a complete binary tree.

- Tree A



YES

- Tree B

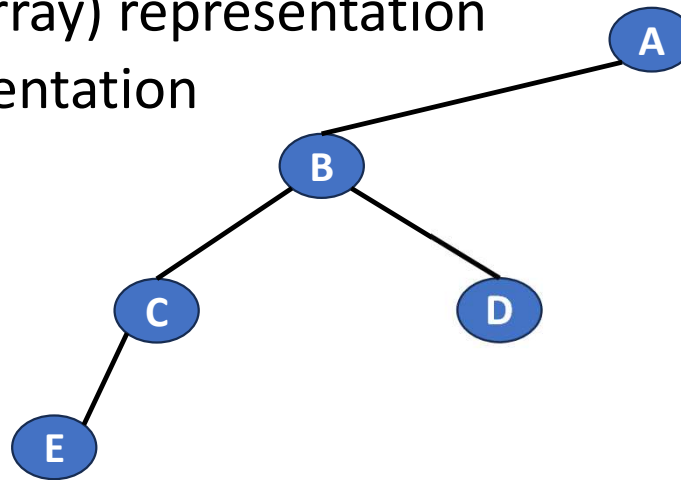


NO

1. Remove 11
2. Move 11 to be child of node 5
3. Insert a right child for node 5

Exercise

- Draw the internal memory representation of the binary tree
 1. Using sequential (array) representation
 2. Using linked representation



tree[]

