# **Core Functions**

# **Investment Algorithm Accuracy Simulation**

This notebook simulates the accuracy of different investment algorithms in an uncertain environment. It compares the performance of four different AI models against a benchmark of perfect knowledge. The simulation involves a simple investment task where an agent must decide between investing in a risky asset (a share) or a safe asset (a bond) over multiple trials.

# **Setup and Parameters**

This section sets up the necessary libraries and parameters for the simulation.

- It imports libraries like NumPy, Pandas, Matplotlib and Seaborn.
- It sets a random seed for reproducibility.
- It defines key parameters such as the prior probabilities of a good share (p), the probability of a high payoff for a good share (q), the payoff values for high and low outcomes (high\_payoff, low\_payoff), the bond payoff (bond\_payoff), the number of trials per block (num\_trials), and the number of simulations to run (num\_simulations).

```
# Setup and Parameters
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import itertools
from dataclasses import dataclass
from typing import List, Dict, Tuple, Any, Optional
# Set random seed for reproducibility
np.random.seed(20250410)
## Configuration dataclass for global parameters
@dataclass(frozen=True)
class SimulationConfig:
    p: List[float]
                                 # Prior probabilities of good share
    q: float
                                  # Probability of high payoff for good share
   high_payoff: float  # Y value - high payoff amount
low_payoff: float  # Z value - low payoff amount
bond_payoff: float  # X value - safe bond payoff amount
num_trials: int  # Trials per block
    ai_types: List[str]
                                  # Types of AI to simulate
    beta: float
                                   # Conservatism parameter
```

```
# Create default configuration
DEFAULT_CONFIG = SimulationConfig(
    p=[0.2, 0.5, 0.8],
    q=0.7,
    high_payoff=5,
    low_payoff=1,
    bond_payoff=3,
    num_trials=13,
    num_simulations=10000,
    ai_types=['perfect', 'shortsighted', 'earlycommitment', 'conservative',
    'naiveprior'],
    beta=0.5
)
```

This section defines the core functions for the investment task simulation and analytical solution:

- simulate\_outcomes: Simulates the outcomes (high or low) for a given share type (good or bad) over a specified number of trials. It uses the q probability to determine the likelihood of each outcome.
- calculate\_expected\_return: Calculates the expected return for the risky asset (share) based
  on the posterior probability of it being good. This is used to make informed investment
  decisions.
- get\_correct\_decision: Determines the optimal investment decision (share or bond) given the true share type. This represents perfect knowledge and serves as a benchmark for evaluating the AI models.
- calculate\_posterior: Calculates the posterior probability based on the AI type and available information:
  - For 'perfect': Uses Bayes' rule with all available data, representing the ideal scenario with perfect knowledge and reasoning.
  - For 'shortsighted': Calculates the posterior based only on the most recent outcome, representing an AI with limited memory or focus.
  - For 'earlycommitment': Calculates the posterior based solely on the first outcome, representing an AI that makes an early judgment and sticks to it.
  - For 'conservative': Calculates the posterior using a conservative approach, where it updates insufficiently based on the outcomes.
  - ► For 'naiveprior': Calculates the posterior using all data but assumes a fixed 50/50 prior, representing an AI with an inaccurate understanding of the prior probabilities.
- the get\_ai\_recommendation function, which determines the AI's investment recommendation (share, bond, or indifferent) based on the AI type and the available information.
  - ▶ It takes the AI type, prior probability, outcomes so far, and the current trial number as input.
  - It calculates the posterior probability using the appropriate AI type.
  - It calculates the expected return based on the posterior.
  - ▶ It compares the expected return to the bond payoff and makes a recommendation accordingly.

```
# Investment Task Simulation Functions
def simulate_outcomes(share_type: str, config: SimulationConfig) -> List[str]:
    Simulate high/low outcomes for a given share type
    Parameters:
        share_type: 'good' or 'bad' - the actual quality of the share
       config: Simulation configuration parameters
    Returns:
      Array of 'high' or 'low' outcomes for each trial
    if share type == 'good':
        outcomes = np.random.choice(['high', 'low'], size=config.num_trials,
p=[config.q, 1-config.q])
        return outcomes.tolist() # Convert to list
    else: # share_type == 'bad'
        outcomes = np.random.choice(['high', 'low'], size=config.num_trials,
p=[1-config.q, config.q])
        return outcomes.tolist() # Convert to list
def calculate_expected_return(posterior_good: float, config: SimulationConfig)
-> float:
    11 11 11
   Calculate expected return for the risky asset based on posterior
probability
    Parameters:
        posterior good: probability that the share is good
       config: Simulation configuration parameters
    Returns:
       Expected monetary return of investing in the share
    posterior_bad = 1 - posterior_good
    # Calculate expected return using equation from the experiment design
    return (posterior_good * config.q * config.high_payoff +
            posterior_bad * (1-config.q) * config.high_payoff +
            posterior good * (1-config.q) * config.low payoff +
            posterior_bad * config.q * config.low_payoff)
def get correct decision(true share type: str, config: SimulationConfig) ->
str:
    Determine the correct investment decision given the true share type
    Parameters:
```

```
true_share_type: 'good' or 'bad' - the actual quality of the share
    config: Simulation configuration parameters

Returns:
        'share' or 'bond' or 'indifferent' - the optimal investment choice
"""

# If we know the true share type, posterior probability is either 0 or 1
p_good = 1 if true_share_type == 'good' else 0
expected_return = calculate_expected_return(p_good, config)

if expected_return > config.bond_payoff:
    return 'share'
elif expected_return < config.bond_payoff:
    return 'bond'
else:
    return 'indifferent'</pre>
```

```
# Bayesian Posterior Calculation Function
def calculate_posterior(ai_type: str, p: float, outcomes: List[str],
current trial: int, config: SimulationConfig) -> float:
    Calculate posterior probability based on AI type and available information
    Parameters:
       ai_type: 'perfect', 'shortsighted', 'earlycommitment', 'conservative'
or 'naiveprior'
       p: prior probability of good share
       outcomes: list of all outcomes so far
       current trial: the current trial number (0-indexed)
        config: Simulation configuration parameters
   Returns:
       Updated probability that the share is good
    if not outcomes:
        return p # No evidence yet, return the prior
    # Handle different AI types
    if ai type == 'shortsighted':
       # Short-sighted AI only considers the most recent outcome
        outcomes = [outcomes[-1]]
    elif ai_type == 'earlycommitment':
        # Early commitment AI only uses the first outcome
        outcomes = [outcomes[0]]
    elif ai_type == 'naiveprior':
       # Naïve prior AI uses all data but always assumes a 50/50 prior
        p = 0.5
```

```
# Count high and low outcomes
nH = sum(1 for o in outcomes if o == 'high')
nL = len(outcomes) - nH

# Calculate posterior using Bayes' rule
if ai_type == 'conservative':
    # Conservative AI updates insufficiently
    numerator = p * ((config.q ** nH) * ((1-config.q) ** nL)) **
config.beta
    denominator = numerator + (1-p) * (((1-config.q) ** nH) * (config.q ** nL)) ** config.beta
    else:
        # Standard Bayesian update for other AI types
        numerator = p * (config.q ** nH) * ((1-config.q) ** nL)
        denominator = numerator + (1-p) * ((1-config.q) ** nH) * (config.q ** nL)

return numerator / denominator if denominator != 0 else p
```

```
# AI Decision Function
def get_ai_recommendation(ai_type: str, p: float, outcomes: List[str],
current_trial: int, config: SimulationConfig) -> str:
    Determine AI's recommendation based on AI type and available information
    Parameters:
        ai_type: AI model type
       p: prior probability of good share
       outcomes: list of all outcomes so far
       current trial: the current trial number (0-indexed)
       config: Simulation configuration parameters
    Returns:
        'share', 'bond', or 'indifferent' - the AI's recommendation
    # Calculate posterior probability based on AI type
    posterior_good = calculate_posterior(ai_type, p, outcomes, current_trial,
config)
    # Calculate expected return and make recommendation
    expected_return = calculate_expected_return(posterior_good, config)
    if expected return > config.bond payoff:
        return 'share'
    elif expected_return < config.bond_payoff:</pre>
        return 'bond'
```

```
else:
return 'indifferent'
```

### Metric calculation functions

It calculates exact probabilities for all possible outcome sequences rather than using simulation.

- 1. **Ex-Ante correctness**: Evaluates if the AI's recommendation matches the optimal decision based on perfect Bayesian reasoning given available information. It measures statistical optimality regardless of outcome.
- 2. **Ex-Post Type correctness**: Evaluates if the AI's recommendation matches what would have been optimal given perfect knowledge of the share type (good vs bad). This measures alignment with the true underlying asset quality.
- 3. **Ex-Post Payoff correctness**: Evaluates if the AI's recommendation maximized payoff given the actual outcome (high vs low). This measures whether the decision was rewarded by the specific outcome that occurred.

```
################################
# Three correctness measures
################################
def measure ex ante correctness(ai rec: str, true bayes post: float, config:
SimulationConfig) -> float:
    1) Ex-Ante correctness = does the AI's action match the *fully* Bayesian
(perfect) EV?
       - If EV(share) > bond => share is correct
       - If EV(share) < bond => bond is correct
       - If tie => all are correct
    ev share correct = calculate expected return(true bayes post, config)
    if abs(ev_share_correct - config.bond_payoff) < le-15:</pre>
        # Perfect tie => full credit for any rec
    elif ev share correct > config.bond payoff:
        return 1.0 if ai_rec == 'share' else 0.0
        return 1.0 if ai rec == 'bond' else 0.0
def measure_ex_post_share_type(ai_rec: str, share_type: str) -> float:
    2) Old Ex-post measure (share-type):
       - If share is good => share=1, bond=0, indifferent=0.5
       - If share is bad => bond=1, share=0, indifferent=0.5
    if share_type == 'good':
```

```
if ai rec == 'share':
           return 1.0
       elif ai_rec == 'indifferent':
           return 0.5
       else: # bond
           return 0.0
   else: # bad
       if ai rec == 'bond':
            return 1.0
       elif ai rec == 'indifferent':
           return 0.5
       else: # share
           return 0.0
def measure_ex_post_payoff(ai_rec: str, outcome: str) -> float:
   3) Payoff-based ex-post:
      If outcome='high' => share=1, bond=0, indifferent=0.5
      If outcome='low' => bond=1, share=0, indifferent=0.5
   if outcome == 'high':
       if ai_rec == 'share':
            return 1.0
       elif ai_rec == 'bond':
           return 0.0
       else: # indifferent
           return 0.5
   else: # 'low'
       if ai_rec == 'bond':
           return 1.0
       elif ai_rec == 'share':
           return 0.0
       else:
           return 0.5
def calculate_accuracy_metrics(ai_rec: str, true_posterior: float,
true_share_type: str,
                              outcome: str, ev_optimal: str) -> Dict[str,
float]:
   Calculate all three accuracy metrics for an AI recommendation
   Parameters:
       ai_rec: AI recommendation ('share', 'bond', or 'indifferent')
       true_posterior: True Bayesian posterior probability of good share
       true_share_type: Actual share type ('good' or 'bad')
       outcome: Actual outcome ('high' or 'low')
       ev_optimal: Statistically optimal decision ('share', 'bond', or
```

```
'indifferent')
    Returns:
      Dictionary containing all three accuracy metrics
    # 1. Ex-ante accuracy (statistical optimality)
    ex_ante = measure_ex_ante_correctness(ai_rec, true_posterior,
DEFAULT CONFIG)
    # 2. Ex-post type accuracy (share-type correctness)
    ex_post_type = measure_ex_post_share_type(ai_rec, true_share_type)
    # 3. Ex-post payoff accuracy (outcome-based)
    ex_post_payoff = measure_ex_post_payoff(ai_rec, outcome)
    return {
        'ex_ante': ex_ante,
        'ex_post_type': ex_post_type,
        'ex_post_payoff': ex_post_payoff
    }
# Correctness measures excluding when equal EV
def measure_ex_ante_forced_choice(ai_rec: str, true_bayes_post: float, config:
SimulationConfig) -> Tuple[float, bool]:
    Ex-Ante correctness excluding EV ties
    Parameters:
       ai_rec: AI recommendation
       true bayes post: True Bayesian posterior
       config: Simulation configuration
    Returns:
       Tuple of (accuracy, should include)
    ev_share = calculate_expected_return(true_bayes_post, config)
    # Check if it's a tie (EV equal to bond payoff)
    is_tie = abs(ev_share - config.bond_payoff) < le-15</pre>
    # If this is a tie, exclude this case
    if is_tie:
        return 0.0, False
    # Otherwise, standard scoring
    if ev_share > config.bond_payoff:
```

```
accuracy = 1.0 if ai_rec == 'share' else 0.0
else: # ev_share < config.bond_payoff
  accuracy = 1.0 if ai_rec == 'bond' else 0.0
return accuracy, True</pre>
```

### Simulation analysis

This section defines functions for running the simulations and aggregating the results:

- run\_simulation: Runs a single simulation of the investment task for a given prior probability (p). It simulates outcomes, calculates the correct decision, tracks the AI recommendations, and calculates accuracy metrics.
- run\_all\_simulations: Runs simulations for all prior probabilities (p) and aggregates the results across multiple simulations.

```
# Simulation Runner Functions
def run_simulation(p: float, sim_id: int, config: SimulationConfig) ->
Tuple[Dict[str, Dict[str, float]], List[Dict]]:
   Run a single simulation of the investment task
   Parameters:
       p: Prior probability of good share
       sim id: Simulation ID
       config: Simulation configuration parameters
   Returns:
       Tuple containing:
        - Dictionary of AI performance metrics
        - List of detailed trial data
   # Determine if the share is good or bad based on prior probability
   share_type = 'good' if np.random.random() 
   # Simulate outcomes for all trials
   outcomes = simulate_outcomes(share_type, config)
   # Get the correct decision based on the true share type
   correct_decision = get_correct_decision(share_type, config)
   # Track recommendations and metrics for each AI type
   ai metrics = {ai type: {
        'ex_ante': 0,
        'ex post type': 0,
        'ex_post_payoff': 0,
        'forced correct': 0,
```

```
'forced type correct': 0, # New metric for ex-post type in forced
choice
        'forced payoff correct': 0, # New metric for ex-post payoff in forced
choice
        'forced total': 0
    } for ai_type in config.ai_types}
    detailed data = []
    # Simulate AI recommendations at each trial
    for trial in range(1, config.num_trials + 1):
        # Get outcomes observed so far (excluding current trial)
        observed outcomes = outcomes[:trial-1]
        current outcome = outcomes[trial-1]
       # Get true Bayesian posterior for EV measure
        true_posterior = calculate_posterior('perfect', p, observed_outcomes,
trial-1, config)
       # Calculate expected return based on true posterior
        expected return = calculate expected return(true posterior, config)
       # Determine optimal decision based on expected return
       if expected_return > config.bond_payoff:
            ev optimal decision = 'share'
        elif expected_return < config.bond_payoff:</pre>
            ev_optimal_decision = 'bond'
        else:
            ev_optimal_decision = 'indifferent'
       # For each AI type, get recommendation and measure correctness
        for ai type in config.ai types:
            ai_rec = get_ai_recommendation(ai_type, p, observed_outcomes,
trial-1, config)
            # Ex-Ante correctness (match with statistical optimality)
            ex_ante_correct = measure_ex_ante_correctness(ai_rec,
true_posterior, config)
            # Ex-Post Type correctness (match with true share type)
            ex_post_type_correct = measure_ex_post_share_type(ai_rec,
share_type)
            # Ex-Post Payoff correctness (match with actual outcome)
            ex_post_payoff_correct = measure_ex_post_payoff(ai_rec,
current_outcome)
            # Forced choice Ex-Ante correctness (excluding ties)
```

```
forced correct, should include =
measure_ex_ante_forced_choice(ai_rec, true_posterior, config)
            # Add to metrics
            ai_metrics[ai_type]['ex_ante'] += ex_ante_correct
            ai_metrics[ai_type]['ex_post_type'] += ex_post_type_correct
            ai_metrics[ai_type]['ex_post_payoff'] += ex_post_payoff_correct
            # Only include in forced choice metric if it's not a tie
            if should include:
                ai_metrics[ai_type]['forced_correct'] += forced_correct
                ai_metrics[ai_type]['forced_type_correct'] +=
ex_post_type_correct # Add ex-post type for forced choice
                ai_metrics[ai_type]['forced_payoff_correct'] +=
ex_post_payoff_correct # Add ex-post payoff for forced choice
                ai metrics[ai type]['forced total'] += 1
            # Record detailed data for this trial
            detailed data.append({
                'sim_id': sim_id,
                'prior': p,
                'trial': trial,
                'ai_type': ai_type,
                'true_share_type': share_type,
                'outcome': current outcome,
                'ai_rec': ai_rec,
                'ev_optimal': ev_optimal_decision,
                'ev_accuracy': ex_ante_correct,
                'rec_accuracy': ex_post_type_correct,
                'outcome accuracy': ex post payoff correct,
                'forced accuracy': forced correct if should include else None,
                'is ev tie': not should include
            })
    # Convert trial sums to averages
    for ai type in config.ai types:
        for metric in ['ex_ante', 'ex_post_type', 'ex_post_payoff']:
            ai_metrics[ai_type][metric] /= config.num_trials
    return ai metrics, detailed data
def run_all_simulations(config: SimulationConfig, num_simulations_to_run:
Optional[int] = None) -> Tuple[Dict[float, Dict[str, Dict[str, float]]],
Dict[float, Dict[str, Dict[str, float]]], pd.DataFrame]:
    Run simulations for all prior probabilities
    Parameters:
```

```
config: Simulation configuration parameters
        num_simulations_to_run: Optional override for number of simulations
    Returns:
       Tuple with:
        - Standard results dictionary
       - Forced choice results dictionary
        - DataFrame with detailed trial data
    if num simulations to run is None:
        num_simulations_to_run = config.num_simulations
    standard results = {}
    forced_results = {}
    all_detailed_data = []
    for p in config.p:
       # Initialize accumulators for this prior
        sums = {ai_type: {
            'ex_ante': 0.0,
            'ex_post_type': 0.0,
            'ex_post_payoff': 0.0,
            'forced correct': 0.0,
            'forced_type_correct': 0.0, # New metric
            'forced_payoff_correct': 0.0, # New metric
            'forced_total': 0.0
       } for ai_type in config.ai_types}
       # Run simulations for this prior probability
        for sim id in range(num simulations to run):
            sim_results, detailed_data = run_simulation(p, sim_id, config)
            # Collect detailed data
            all_detailed_data.extend(detailed_data)
            # Aggregate results
            for ai_type in config.ai_types:
                for metric in sums[ai_type]:
                    sums[ai_type][metric] += sim_results[ai_type][metric]
       # Process standard results
       standard_results[p] = {}
        for ai type in config.ai types:
            standard_results[p][ai_type] = {
                'ex_ante': sums[ai_type]['ex_ante'] / num_simulations_to_run,
                'ex_post_type': sums[ai_type]['ex_post_type'] /
num_simulations_to_run,
                'ex_post_payoff': sums[ai_type]['ex_post_payoff'] /
```

```
num simulations to run
            }
        # Process forced choice results separately
        forced results[p] = {}
        for ai type in config.ai types:
            total_forced = sums[ai_type]['forced_total']
            if total forced > 0:
                ex_ante_accuracy = sums[ai_type]['forced_correct'] /
total forced
                ex_post_type_accuracy = sums[ai_type]['forced_type_correct'] /
total forced # Calculate ex-post type
                ex post payoff accuracy = sums[ai type]
['forced payoff correct'] / total forced # Calculate ex-post payoff
                pct_included = total_forced / (num_simulations_to_run *
config.num trials) * 100
            else:
                ex_ante_accuracy = float('nan')
                ex_post_type_accuracy = float('nan')
                ex_post_payoff_accuracy = float('nan')
                pct included = 0
            # Format exactly like standard_results to work with existing plot
function
            forced_results[p][ai_type] = {
                'ex_ante': ex_ante_accuracy,
                'ex post type': ex post type accuracy,
                'ex_post_payoff': ex_post_payoff_accuracy,
                'pct included': pct included
            }
    # Convert detailed data to DataFrame
    trial_df = pd.DataFrame(all_detailed_data)
    return standard_results, forced_results, trial_df
```

# **Analytical solution**

This section provides the functions for the analytical solution. It comprises the following functions:

- seq\_probability: Calculates the probability of a specific sequence of outcomes given the share type (good or bad) and the prior probability.
- run\_all\_measures: Runs the analytical solution for all measures (ex-ante, ex-post type, and expost payoff) across all prior probabilities and outcomes.

```
######################################
# Probability of a sequence
###############################
def seq_probability(sequence: np.ndarray, share_type: str, config:
SimulationConfig) -> float:
    Probability of seeing 'sequence' if the share is good or bad.
    Parameters:
        sequence: Array of 'high' or 'low' outcomes
        share_type: 'good' or 'bad'
        config: Simulation configuration parameters
    Returns:
       Probability of the sequence occurring
    # Convert sequence to binary array (1 for high, 0 for low)
    if isinstance(sequence, np.ndarray):
        # If already numpy array, use it directly
        seq_arr = sequence
    else:
        # Convert list of strings to binary array
        seq_arr = np.array([1 if o == 'high' else 0 for o in sequence])
    # Count high outcomes
    nH = np.sum(seq_arr)
    # Count low outcomes
    nL = len(seq\_arr) - nH
    if share_type == 'good':
        return (config.q ** nH) * ((1.0 - config.q) ** nL)
    else:
        return ((1.0 - config.q) ** nH) * (config.q ** nL)
###################################
# Main enumeration function
######################################
def run all measures(config: SimulationConfig) -> Tuple[Dict[float, Dict[str,
Dict[str, float]]], Dict[float, Dict[str, Dict[str, float]]]]:
    Enumerates all 2<sup>num</sup> trials sequences, simulates each AI's picks,
    and calculates three measures of accuracy using NumPy for vectorization.
    Parameters:
        config: Simulation configuration parameters
```

```
Returns:
       Tuple with:
        - Standard results dictionary
        - Forced choice results dictionary
    # Pre-generate all possible sequences as binary arrays (θ=low, 1=high)
    # This gives us a 2D array where each row is one possible sequence
    sequences = np.array(list(itertools.product([0, 1],
repeat=config.num_trials)))
    # Results dictionary
    standard_results = {}
    forced_results = {}
    # For each prior probability
    for p in config.p:
        print(f"Calculating analytical solution for p={p}")
       # Pre-calculate probabilities for all sequences
       # Probability of sequence if share is good
        probs good = np.zeros(len(sequences))
        # Probability of sequence if share is bad
        probs_bad = np.zeros(len(sequences))
       # Pre-convert sequences to string representations for processing
        seq_strings = []
        for seq in sequences:
            # Convert binary (0,1) to ('low', 'high')
            seq_str = ['high' if bit == 1 else 'low' for bit in seq]
            seq_strings.append(seq_str)
            # Calculate probabilities for this sequence
            prob_good = seq_probability(seq, 'good', config)
            prob_bad = seq_probability(seq, 'bad', config)
            # Store in arrays
            probs_good[len(seq_strings)-1] = prob_good
            probs_bad[len(seq_strings)-1] = prob_bad
       # Initialize measures for each AI type (standard measures)
       measure_sums = {
            ai_type: {
                'ex ante': 0.0,
                'ex_post_type': 0.0,
                'ex_post_payoff': 0.0
            for ai type in config.ai types
       }
```

```
# Initialize forced choice measures
        forced_sums = {
            ai_type: {
                'ex_ante': 0.0,
                'ex_post_type': 0.0,
                'ex_post_payoff': 0.0,
                'total cases': 0.0,
                'total_weight': 0.0
            for ai_type in config.ai_types
       }
       # For each possible sequence
        for i, (seq, seq_str) in enumerate(zip(sequences, seq_strings)):
            # Probability weights
            prob_good = probs_good[i]
            prob_bad = probs_bad[i]
            seq_weight = p * prob_good + (1.0 - p) * prob_bad
            # Skip sequences with near-zero probability to save computation
            if seq_weight < le-10:</pre>
                continue
            # For each AI type
            for ai_type in config.ai_types:
                # Tracking correctness measures
                correct_ex_ante = 0.0
                correct_ex_post_good = 0.0
                correct ex post bad = 0.0
                correct_ex_post_payoff = 0.0
                # Forced choice measures
                forced_ex_ante = 0.0
                forced_ex_post_type = 0.0
                forced ex post payoff = 0.0
                forced_cases = 0.0
                # Simulate the AI observing outcomes one by one
                observed = []
                for t, outcome in enumerate(seq_str):
                    # Get AI recommendation based on observations so far
                    current trial = len(observed)
                    ai_rec = get_ai_recommendation(ai_type, p, observed,
current_trial, config)
                    # Calculate true Bayesian posterior for EV measure
                    true_posterior_good = calculate_posterior('perfect', p,
```

```
observed, current trial, config)
                    # Calculate expected return for checking EV ties
                    expected return =
calculate_expected_return(true_posterior_good, config)
                    is_ev_tie = abs(expected_return - config.bond_payoff) <</pre>
1e-15
                    # 1) Ex-Ante correctness
                    ex_ante_correct = measure_ex_ante_correctness(ai_rec,
true_posterior_good, config)
                    correct_ex_ante += ex_ante_correct
                    # 2) Ex-Post (share-type) correctness
                    ex_post_good_correct = measure_ex_post_share_type(ai_rec,
'good')
                    ex_post_bad_correct = measure_ex_post_share_type(ai_rec,
'bad')
                    correct_ex_post_good += ex_post_good_correct
                    correct_ex_post_bad += ex_post_bad_correct
                    # 3) Ex-Post (payoff-based) correctness
                    ex_post_payoff_correct = measure_ex_post_payoff(ai_rec,
outcome)
                    correct_ex_post_payoff += ex_post_payoff_correct
                    # Forced choice metrics - only count when not a tie
                    if not is_ev_tie:
                        forced cases += 1
                        forced_ex_ante += ex_ante_correct
                        forced_ex_post_type += (p * prob_good *
ex_post_good_correct +
                                               (1.0 - p) * prob bad *
ex_post_bad_correct) / seq_weight
                        forced_ex_post_payoff += ex_post_payoff_correct
                    # Update observed outcomes for next trial
                    observed.append(outcome)
                # Update measure sums with sequence-weighted correctness
                measure_sums[ai_type]['ex_ante'] += correct_ex_ante *
seq_weight
                measure_sums[ai_type]['ex_post_type'] += (
                    correct_ex_post_good * (p * prob_good) +
                    correct_ex_post_bad * ((1.0 - p) * prob_bad)
                )
```

```
measure sums[ai type]['ex post payoff'] +=
correct_ex_post_payoff * seq_weight
                # Update forced choice measures if we had any non-tie cases
                if forced_cases > 0:
                    # Weight by sequence probability
                    forced_sums[ai_type]['ex_ante'] += forced_ex_ante *
seq weight
                    forced_sums[ai_type]['ex_post_type'] +=
forced ex post type * seq weight
                    forced_sums[ai_type]['ex_post_payoff'] +=
forced_ex_post_payoff * seq_weight
                    forced_sums[ai_type]['total_cases'] += forced_cases *
seq_weight
                    forced_sums[ai_type]['total_weight'] += config.num_trials
* seq weight
        # Process results for this prior probability
        standard_for_p = {}
        forced for p = \{\}
        for ai_type in config.ai_types:
            # Convert sums to fractions by dividing by number of trials
            standard_for_p[ai_type] = {
                'ex_ante': measure_sums[ai_type]['ex_ante'] /
float(config.num_trials),
                'ex_post_type': measure_sums[ai_type]['ex_post_type'] /
float(config.num_trials),
                'ex_post_payoff': measure_sums[ai_type]['ex_post_payoff'] /
float(config.num trials)
           }
            # Calculate forced choice metrics
            total_forced_cases = forced_sums[ai_type]['total_cases']
            if total_forced_cases > 0:
                forced for p[ai type] = {
                    'ex_ante': forced_sums[ai_type]['ex_ante'] /
total_forced_cases,
                    'ex_post_type': forced_sums[ai_type]['ex_post_type'] /
total forced cases,
                    'ex_post_payoff': forced_sums[ai_type]['ex_post_payoff'] /
total_forced_cases,
                    'pct included': (total forced cases / forced sums[ai type]
['total_weight']) * 100
            else:
                forced for p[ai type] = {
                    'ex_ante': float('nan'),
```

# Visualisation and reporting functions

This section defines functions for creating summary visualisations of the results:

- create\_performance\_summary: Creates a bar chart comparing the overall performance of all AI models using both traditional and EV-based accuracy measures.
- plot\_performance\_by\_prior: Creates bar charts showing the performance of AI models across different prior probabilities, using both traditional and EV-based accuracy measures.
- create\_dynamic\_x\_ticks: Helper for dynamic x-ticks in plots.
- plot\_accuracy\_by\_trial: Creates a plot visualizing the accuracy of AI models across trials for different prior probabilities.
- plot\_combined\_accuracy\_by\_trial: Creates a combined plot visualizing the accuracy of AI models across trials for different prior probabilities.
- plot\_analytical\_performance\_by\_prior: Creates a plot visualizing the analytical performance of AI models across different prior probabilities.
- create\_table\_from\_results takes the results dictionaries (containing accuracy data) and a table\_type parameter to create formatted tables summarizing the AI models' performance. It takes three parameters and creates either a summary table (overall AI performance) or a prior probability table (performance for each prior).
  - results: A dictionary containing the traditional accuracy results from the simulations.
  - ev\_results: A dictionary containing the expected value (EV)-based accuracy results from the simulations.
  - ► table\_type: A string indicating the type of table to generate ("summary" or "prior").
- plot\_trial\_by\_trial\_performance: Creates a plot visualizing the traditional accuracy of AI models across trials for different prior probabilities.
- display\_forced\_choice\_results: Displays the forced choice results in a formatted table.

```
# Visualisation Functions
def create_performance_summary(results: Dict[float, Dict[str, Dict[str,
float]]], config: SimulationConfig) -> plt.Figure:
    """
    Create a clear performance summary chart comparing all AI models
    Parameters:
        results: Dictionary with accuracy results in consistent format
```

```
config: Simulation configuration parameters
    Returns:
       matplotlib figure
    # Calculate average accuracy across all priors for all measures
    ex_ante_accuracy = {} # EV-based
    ex_post_type_accuracy = {} # Traditional
    ex_post_payoff_accuracy = {} # Payoff-based
    for ai_type in config.ai_types:
        # Calculate average accuracy across all priors
        ex_ante_sum = sum(results[p][ai_type]['ex_ante'] for p in config.p)
        ex_post_type_sum = sum(results[p][ai_type]['ex_post_type'] for p in
config.p)
        ex_post_payoff_sum = sum(results[p][ai_type]['ex_post_payoff'] for p
in config.p)
        # Average across priors
        ex_ante_accuracy[ai_type] = ex_ante_sum / len(config.p)
        ex_post_type_accuracy[ai_type] = ex_post_type_sum / len(config.p)
        ex_post_payoff_accuracy[ai_type] = ex_post_payoff_sum / len(config.p)
    # Create DataFrame for plotting
    summary_data = []
    for ai_type in config.ai_types:
        summary_data.append({
            'AI Type': ai_type.capitalize(),
            'Accuracy Measure': 'Ex-Ante',
            'Accuracy': ex_ante_accuracy[ai_type]
       })
        summary_data.append({
            'AI Type': ai_type.capitalize(),
            'Accuracy Measure': 'Ex-Post Type',
            'Accuracy': ex_post_type_accuracy[ai_type]
       })
        summary_data.append({
            'AI Type': ai_type.capitalize(),
            'Accuracy Measure': 'Ex-Post Payoff',
            'Accuracy': ex_post_payoff_accuracy[ai_type]
       })
    df = pd.DataFrame(summary data)
    # Create a grouped bar chart
    fig = plt.figure(figsize=(12, 7))
    ax = plt.gca()
```

```
# Use custom colors
    palette = {
        'Ex-Ante': '#2ecc71',
                               # Green
        'Ex-Post Type': '#3498db', # Blue
        'Ex-Post Payoff': '#e67e22' # Orange
    }
    # Create the grouped bar chart
    sns.barplot(
       x='AI Type',
       y='Accuracy',
        hue='Accuracy Measure',
       data=df,
        palette=palette,
        ax=ax
    )
    # Format the plot
    ax.set_title('AI Performance Comparison', fontsize=14)
    ax.set xlabel('AI Model', fontsize=12)
    ax.set_ylabel('Accuracy (%)', fontsize=12)
    ax.set_ylim(0, 1)
    ax.grid(axis='y', linestyle='--', alpha=0.7)
    # Format y-axis as percentages
    ax.set_yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    # Add value labels on the bars
    for container in ax.containers:
        ax.bar_label(container, fmt='{:.1f}%', padding=3, label_type='edge',
                   fontsize=10, fontweight='bold')
    plt.tight_layout()
    return fig
def plot_performance_by_prior(results: Dict[float, Dict[str, Dict[str,
float]]], config: SimulationConfig) -> plt.Figure:
    Create a chart showing performance across different prior probabilities
    Parameters:
       results: Dictionary with all accuracy results in consistent format
        config: Simulation configuration parameters
    Returns:
       matplotlib figure
```

```
# Calculate accuracy for each prior and AI type
    data = []
    for p in config.p:
        for ai_type in config.ai_types:
            # Access metrics directly from results
            ex_ante = results[p][ai_type]['ex_ante']
            ex post type = results[p][ai type]['ex post type']
            ex_post_payoff = results[p][ai_type]['ex_post_payoff']
            # Add to data
            data.append({
                'Prior Probability': p,
                'AI Type': ai_type.capitalize(),
                'Statistical Optimality': ex_ante,
                'Correct Predictions': ex post type,
                'Payoff Accuracy': ex_post_payoff
            })
    df = pd.DataFrame(data)
    # Create figure with three subplots side by side
    fig, (ax1, ax2, ax3) = plt.subplots(1, 3, figsize=(18, 6))
    # 1. Plot Statistical Optimality (Ex-Ante)
    sns.barplot(x='Prior Probability', y='Statistical Optimality', hue='AI
Type',
                data=df, ax=ax1, palette='Greens')
    ax1.set title('AI Statistical Optimality (Ex-Ante)')
    ax1.set ylabel('Statistical Optimality (%)')
    ax1.set ylim(0, 1)
    ax1.grid(axis='y', linestyle='--', alpha=0.7)
    ax1.legend(loc='lower right')
    # Format y-axis as percentages
    ax1.set_yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax1.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    # 2. Plot Correct Predictions (Ex-Post Type)
    sns.barplot(x='Prior Probability', y='Correct Predictions', hue='AI Type',
                data=df, ax=ax2, palette='Blues')
    ax2.set_title('AI Correct Predictions (Ex-Post Type)')
    ax2.set_ylabel('Correct Prediction Rate (%)')
    ax2.set_ylim(0, 1)
    ax2.grid(axis='y', linestyle='--', alpha=0.7)
    ax2.legend(loc='lower right')
```

```
# Format y-axis as percentages
    ax2.set_yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax2.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    # 3. Plot Payoff Accuracy (Ex-Post Payoff)
    sns.barplot(x='Prior Probability', y='Payoff Accuracy', hue='AI Type',
                data=df, ax=ax3, palette='Oranges')
    ax3.set title('AI Payoff Accuracy (Ex-Post Payoff)')
    ax3.set_ylabel('Payoff Accuracy (%)')
    ax3.set_ylim(0, 1)
    ax3.grid(axis='y', linestyle='--', alpha=0.7)
    ax3.legend(loc='lower right')
    # Format y-axis as percentages
    ax3.set_yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax3.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    plt.tight layout()
    return fig
# Dynamic grid function for plotting
def create_dynamic_x_ticks(max_trials: int) -> List[int]:
    Create dynamic x-ticks based on the number of trials:
    - If max_trials <= 11: Show grid lines for all trials</pre>
    - If max_trials > 11: Show grid lines for odd-numbered trials plus the
last trial if even
    Parameters:
       max trials: Maximum number of trials
    Returns:
       List of x-tick positions
    if max_trials <= 11:</pre>
       # If 11 or fewer trials, show all
       x_ticks = list(range(1, max_trials + 1))
       # For more than 11 trials, show odd-numbered trials
       x_ticks = [i for i in range(1, max_trials + 1) if i % 2 == 1]
       # Always include the last trial if it's not already included (if it's
even)
       if max_trials % 2 == 0 and max_trials not in x_ticks:
            x ticks.append(max trials)
```

```
return sorted(x_ticks)
# Plot accuracy by trial function
def plot_accuracy_by_trial(trial_df: pd.DataFrame, accuracy_measure: str =
'ev accuracy',
                          title_prefix: str = 'AI', config: SimulationConfig =
None) -> plt.Figure:
    Plot accuracy across trials for all AI types with dynamic grid
    Parameters:
       trial df: DataFrame with trial-by-trial data
       accuracy measure: Column name for the accuracy measure to plot
       title prefix: Prefix for the plot title
       config: Simulation configuration parameters
    Returns:
       matplotlib figure
    # Group by prior, trial, and AI type to get average performance
    grouped = trial_df.groupby(['prior', 'trial', 'ai_type'])
[accuracy_measure].mean().reset_index()
    # Create a figure with subplots for each prior
    fig, axes = plt.subplots(len(config.p), 1, figsize=(12, 15), sharex=True)
    # Determine the max number of trials
    max_trials = trial_df['trial'].max()
    # Create dynamic x-ticks
    x_ticks = create_dynamic_x_ticks(max_trials)
    # Map accuracy measures to readable labels
    measure_labels = {
        'ev_accuracy': 'Statistical Optimality',
        'rec accuracy': 'Ex-Post Type Accuracy',
        'outcome_accuracy': 'Ex-Post Payoff Accuracy'
    }
    measure label = measure labels.get(accuracy measure,
accuracy_measure.replace('_', ' ').title())
    # Plot for each prior probability
    for i, p in enumerate(config.p):
       ax = axes[i]
       data = grouped[grouped['prior'] == p]
       # Plot each AI type
```

```
for ai type in config.ai types:
            ai_data = data[data['ai_type'] == ai_type]
            ax.plot(ai_data['trial'], ai_data[accuracy_measure],
                   marker='o', label=ai_type.capitalize(), linewidth=2)
        ax.set title(f'{title prefix} {measure label} Across Trials (Prior
p={p})')
        ax.set ylim(0, 1.05)
        ax.set_ylabel(measure_label)
        ax.legend(loc='lower right')
       # Set dynamic x-axis ticks and grid
       ax.set xticks(x ticks)
        ax.set_xlim(0.5, max_trials + 0.5)
        ax.grid(True, which='both', axis='both', linestyle='--', alpha=0.7)
    # Label the bottom plot with x-axis title
    axes[-1].set_xlabel('Trial Number')
    plt.tight layout()
    return fig
def plot_combined_accuracy_by_trial(trial_df: pd.DataFrame, config:
SimulationConfig) -> plt.Figure:
    Plot all three accuracy measures side by side for each prior probability
    with dynamic grid that adjusts to trial count
    Parameters:
        trial df: DataFrame with trial-by-trial data
        config: Simulation configuration parameters
    Returns:
       matplotlib figure
    # Calculate mean values for each measure by prior, trial, and AI type
    ex_ante_grouped = trial_df.groupby(['prior', 'trial', 'ai_type'])
['ev_accuracy'].mean().reset_index()
    ex_post_type_grouped = trial_df.groupby(['prior', 'trial', 'ai_type'])
['rec accuracy'].mean().reset index()
    ex_post_payoff_grouped = trial_df.groupby(['prior', 'trial', 'ai_type'])
['outcome_accuracy'].mean().reset_index()
   # Create figure with 3 columns (one for each measure) and len(config.p)
rows
    fig, axes = plt.subplots(len(config.p), 3, figsize=(18, 15), sharex=True)
    # Custom colors for AI types
```

```
ai colors = {
        'perfect': '#1f77b4',
                              # Blue
        'shortsighted': '#ff7f0e', # Orange
        'earlycommitment': '#2ca02c', # Green
        'conservative': '#9467bd', # Purple
        'naiveprior': '#d62728'
   }
   # Determine the max number of trials
   max_trials = trial_df['trial'].max()
   # Create dynamic x-ticks based on the number of trials
   x ticks = create_dynamic_x_ticks(max_trials)
   # Plot for each prior probability
   for i, p in enumerate(config.p):
       # 1. Ex-Ante (Statistical Optimality)
       ax_ex_ante = axes[i, 0]
       data = ex_ante_grouped[ex_ante_grouped['prior'] == p]
        for ai type in config.ai types:
            ai_data = data[data['ai_type'] == ai_type]
            ax_ex_ante.plot(ai_data['trial'], ai_data['ev_accuracy'],
                          marker='o', label=ai_type.capitalize(),
                          color=ai_colors[ai_type], linewidth=2)
       ax ex ante.set title(f'Ex-Ante (p={p})', fontsize=12)
       if i == 0:
            ax ex ante.set title(f'Ex-Ante\nStatistical Optimality (p={p})',
fontsize=12)
        ax_ex_ante.set_ylim(0, 1.05)
       if i == len(config.p) - 1:
           ax_ex_ante.set_xlabel('Trial Number')
       if i == 0:
            ax_ex_ante.legend(loc='lower right')
       # Set dynamic x-axis ticks and grid
       ax_ex_ante.set_xticks(x_ticks)
        ax_ex_ante.set_xlim(0.5, max_trials + 0.5)
        ax ex ante.grid(True, which='both', axis='both', linestyle='--',
alpha=0.7)
       # 2. Ex-Post Type (Correct Predictions)
        ax_ex_post_type = axes[i, 1]
       data = ex_post_type_grouped[ex_post_type_grouped['prior'] == p]
        for ai type in config.ai types:
            ai_data = data[data['ai_type'] == ai_type]
```

```
ax ex post type.plot(ai data['trial'], ai data['rec accuracy'],
                               marker='o', label=ai_type.capitalize(),
                               color=ai colors[ai type], linewidth=2)
        ax ex post type.set title(f'Ex-Post Type (p={p})', fontsize=12)
       if i == 0:
            ax_ex_post_type.set_title(f'Ex-Post Type\nCorrect Predictions
(p=\{p\})', fontsize=12)
        ax_ex_post_type.set_ylim(0, 1.05)
       if i == len(config.p) - 1:
            ax_ex_post_type.set_xlabel('Trial Number')
       # Set dynamic x-axis ticks and grid
        ax_ex_post_type.set_xticks(x_ticks)
        ax_ex_post_type.set_xlim(0.5, max_trials + 0.5)
        ax ex post type.grid(True, which='both', axis='both', linestyle='--',
alpha=0.7)
       # 3. Ex-Post Payoff (Outcome Accuracy)
        ax ex post payoff = axes[i, 2]
        data = ex_post_payoff_grouped[ex_post_payoff_grouped['prior'] == p]
        for ai type in config.ai types:
            ai data = data[data['ai_type'] == ai_type]
            ax_ex_post_payoff.plot(ai_data['trial'],
ai_data['outcome_accuracy'],
                                 marker='o', label=ai_type.capitalize(),
                                 color=ai_colors[ai_type], linewidth=2)
        ax ex post payoff.set title(f'Ex-Post Payoff (p={p})', fontsize=12)
       if i == 0:
            ax ex post payoff.set title(f'Ex-Post Payoff\nPayoff-Based
Accuracy (p={p})', fontsize=12)
        ax_ex_post_payoff.set_ylim(0, 1.05)
       if i == len(config.p) - 1:
            ax ex post payoff.set xlabel('Trial Number')
       # Set dynamic x-axis ticks and grid
        ax_ex_post_payoff.set_xticks(x_ticks)
        ax ex post payoff.set xlim(0.5, max trials + 0.5)
        ax_ex_post_payoff.grid(True, which='both', axis='both',
linestyle='--', alpha=0.7)
    # Set common y-label on the left
    for i, p in enumerate(config.p):
        axes[i, 0].set_ylabel(f'Accuracy (p={p})', fontsize=12)
    plt.tight layout()
```

```
return fig
def plot analytical performance by prior(analytical results: Dict[float,
Dict[str, Dict[str, float]]], config: SimulationConfig) -> plt.Figure:
    Create a chart showing analytical performance across different prior
probabilities.
    Parameters:
        analytical results: Dictionary with analytical accuracy results
        config: Simulation configuration parameters
    Returns:
       matplotlib figure
    # Prepare data for plotting
    data = []
    for p in config.p:
        for ai type in config.ai types:
            # Extract values from the analytical_results dictionary
            ex_ante = analytical_results[p][ai_type]['ex_ante']
            ex post type = analytical results[p][ai type]['ex post type']
            ex_post_payoff = analytical_results[p][ai_type]['ex_post_payoff']
            # Add to data
            data.append({
                'Prior Probability': p,
                'AI Type': ai_type.capitalize(),
                'Ex-Ante': ex ante,
                'Ex-Post Type': ex_post_type,
                'Ex-Post Payoff': ex_post_payoff
            })
    df = pd.DataFrame(data)
    # Create figure with three subplots in a row
    fig, (ax1, ax2, ax3) = plt.subplots(1, 3, figsize=(18, 6))
    # Plot ex-ante accuracy
    sns.barplot(x='Prior Probability', y='Ex-Ante', hue='AI Type',
                data=df, ax=ax1, palette='Greens')
    ax1.legend(loc='lower right')
    ax1.set_title('Analytical Ex-Ante Optimality')
    ax1.set_ylabel('Correct Prediction Rate (%)')
    ax1.set ylim(0, 1)
    ax1.grid(axis='y', linestyle='--', alpha=0.7)
```

```
# Format y-axis as percentages
    ax1.set yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax1.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    # Plot ex-post type accuracy
    sns.barplot(x='Prior Probability', y='Ex-Post Type', hue='AI Type',
                data=df, ax=ax2, palette='Oranges')
    ax2.legend(loc='lower right')
    ax2.set_title('Analytical Ex-Post Type Correctness')
    ax2.set_ylabel('Correct Prediction Rate (%)')
    ax2.set ylim(0, 1)
    ax2.grid(axis='y', linestyle='--', alpha=0.7)
    # Format y-axis as percentages
    ax2.set_yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax2.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    # Plot ex-post payoff accuracy
    sns.barplot(x='Prior Probability', y='Ex-Post Payoff', hue='AI Type',
                data=df, ax=ax3, palette='Blues')
    ax3.legend(loc='lower right')
    ax3.set_title('Analytical Ex-Post Payoff')
    ax3.set_ylabel('Statistical Optimality (%)')
    ax3.set_ylim(0, 1)
    ax3.grid(axis='y', linestyle='--', alpha=0.7)
    # Format y-axis as percentages
    ax3.set_yticks([0, 0.2, 0.4, 0.6, 0.8, 1.0])
    ax3.set_yticklabels(['0%', '20%', '40%', '60%', '80%', '100%'])
    plt.tight_layout()
    return fig
# Plot trial performance
def plot_trial_by_trial_performance(trial_df: pd.DataFrame, config:
SimulationConfig) -> plt.Figure:
    Plot performance across trials for all AI types
    Parameters:
        trial df: DataFrame with trial-by-trial data
       config: Simulation configuration parameters
    Returns:
       matplotlib figure
```

```
0.00
    # Group by prior, trial, and AI type to get average performance
    grouped = trial_df.groupby(['prior', 'trial', 'ai_type'])
['rec_accuracy'].mean().reset_index()
    # Create a figure with subplots for each prior
    fig, axes = plt.subplots(len(config.p), 1, figsize=(12, 15), sharex=True)
    # Plot for each prior probability
    for i, p in enumerate(config.p):
        ax = axes[i]
       data = grouped[grouped['prior'] == p]
       # Plot each AI type
        for ai_type in config.ai_types:
            ai data = data[data['ai type'] == ai type]
            ax.plot(ai_data['trial'], ai_data['rec_accuracy'],
                   marker='o', label=ai_type, linewidth=2)
        ax.set title(f'AI Correct Predictions Across Trials (Prior p={p})')
        ax.set ylim(0, 1.05)
       ax.set_ylabel('Correct Prediction Rate')
        ax.grid(True, linestyle='--', alpha=0.7)
        ax.legend(loc='lower right')
    # Label the bottom plot with x-axis title
    axes[-1].set_xlabel('Trial Number')
    plt.tight layout()
    return fig
# create analytical table function
def create_analytical_table(ex_ante_results: Dict, ex_post_results: Dict,
                           config: SimulationConfig) -> pd.DataFrame:
    Create a Pandas DataFrame for analytical results.
    Parameters:
       ex_ante_results: Dictionary with ex-ante accuracy results
       ex post results: Dictionary with ex-post accuracy results
       config: Simulation configuration parameters
    Returns:
       Pandas DataFrame with analytical results
    data = []
    for p in config.p:
        for ai_type in config.ai_types:
```

```
data.append({
                'Prior Probability': p,
                'AI Type': ai type.capitalize(),
                'Ex-Ante Accuracy': ex_ante_results[p][ai_type],
                'Ex-Post Accuracy': ex_post_results[p][ai_type]
            })
    df = pd.DataFrame(data)
    return df
# create_table_from_results function
def create table from results(results: Dict, ev results: Dict,
                             config: SimulationConfig,
                             table_type: str = "summary") -> pd.DataFrame:
    Create a Pandas DataFrame to display the data in a tabular format.
    Parameters:
       results: Dictionary with traditional accuracy results.
       ev results: Dictionary with EV-based accuracy results.
       config: Simulation configuration parameters.
       table_type: "summary" or "prior" to indicate the type of table to
generate.
    Returns:
       A Pandas DataFrame containing the table data.
    if table_type == "summary":
        # Overall performance summary table
       trad accuracy = {}
        ev_accuracy = {}
        payoff_accuracy = {}
        for ai_type in config.ai_types:
            correct = sum(results[p][ai_type]['correct'] for p in config.p)
            total = sum(results[p][ai type]['total'] for p in config.p)
            trad_accuracy[ai_type] = correct / total
            ev_correct = sum(ev_results[p][ai_type]['ev_correct'] for p in
config.p)
            ev_total = sum(ev_results[p][ai_type]['total'] for p in config.p)
            ev_accuracy[ai_type] = ev_correct / ev_total
            payoff_correct = sum(results[p][ai_type]['outcome_correct'] for p
in config.p)
            payoff_total = sum(results[p][ai_type]['total'] for p in config.p)
            payoff accuracy[ai type] = payoff correct / payoff total
```

```
summary data = []
        for ai_type in config.ai_types:
            summary data.append({
                'AI Type': ai_type.capitalize(),
                'Ex-Ante (Statistical Optimality)': ev_accuracy[ai_type],
                'Ex-Post Type (Correct Predictions)': trad_accuracy[ai_type],
                'Ex-Post Payoff (Payoff Accuracy)': payoff_accuracy[ai_type]
           })
        df = pd.DataFrame(summary data)
        return df
    elif table type == "prior":
       # Performance by prior probability table
        data = []
        for p in config.p:
            for ai_type in config.ai_types:
                trad_acc = results[p][ai_type]['correct'] / results[p]
[ai_type]['total']
                ev_acc = ev_results[p][ai_type]['ev_correct'] / ev_results[p]
[ai_type]['total']
                payoff_acc = results[p][ai_type]['outcome_correct'] /
results[p][ai_type]['total']
                data.append({
                    'Prior Probability': p,
                    'AI Type': ai_type.capitalize(),
                    'Ex-Ante (Statistical Optimality)': ev_acc,
                    'Ex-Post Type (Correct Predictions)': trad acc,
                    'Ex-Post Payoff (Payoff Accuracy)': payoff acc
                })
        df = pd.DataFrame(data)
        return df
    else:
        return None
def display results table(results: Dict[float, Dict[str, Dict[str, float]]],
config: SimulationConfig) -> None:
    Display results in a tabular format
    Parameters:
        results: Dictionary with accuracy results in consistent format
        config: Simulation configuration parameters
```

```
print(f"Number of trials num trials={config.num trials}\n")
    for p in config.p:
        print(f"===== p = {p} =====")
        for ai type in config.ai types:
            # Access metrics directly from results
            ex_ante = results[p][ai_type]['ex_ante']
            ex post type = results[p][ai type]['ex post type']
            ex_post_payoff = results[p][ai_type]['ex_post_payoff']
            print(f" {ai_type:15s} => ex-ante={ex_ante:.4f}, ex-post-
type={ex_post_type:.4f}, ex-post-payoff={ex post payoff:.4f}")
       print()
def display forced choice results(forced results: Dict[float, Dict[str,
Dict[str, float]]], config: SimulationConfig) -> None:
    Display forced choice results in a tabular format
    Parameters:
        forced results: Dictionary with forced choice accuracy results
        config: Simulation configuration parameters
    print("\n===== FORCED CHOICE ACCURACY (EXCLUDING EV TIES) =====")
    for p in config.p:
        print(f"Prior p = {p}")
        for ai type in config.ai types:
            ex ante = forced results[p][ai type]['ex ante']
            ex post type = forced results[p][ai type]['ex post type']
            ex_post_payoff = forced_results[p][ai_type]['ex_post_payoff']
            pct_included = forced_results[p][ai_type]['pct_included']
            if np.isnan(ex_ante):
               print(f" {ai type:15s} => N/A (no non-tie cases)")
            else:
                print(f" {ai_type:15s} => ex-ante={ex_ante:.4f}, ex-post-
type={ex_post_type:.4f}, ex-post-payoff={ex_post_payoff:.4f} (using
{pct included:.1f}% of trials)")
       print()
```

#### **Main Execution Function**

This section defines the run\_analysis function, which orchestrates the entire analysis process:

- It sets the number of simulations to run.
- It runs the normal simulations and the EV-based simulations.
- It performs detailed trial-by-trial analysis if enabled.

• It returns all results in a dictionary.

```
# Main Execution Function
def display_trial_accuracy_charts(trial_df: pd.DataFrame, config:
SimulationConfig) -> plt.Figure:
    Display the combined 3×3 chart of all accuracy metrics across trials
    Parameters:
       trial df: DataFrame with trial-by-trial data
        config: Simulation configuration parameters
    Returns:
       Combined chart figure
    print("\nACCURACY ACROSS TRIALS")
    # Only create the combined chart
    combined chart = plot combined accuracy by trial(trial df, config)
    # Show the chart
    plt.figure(combined_chart.number)
    plt.show()
    return combined_chart
def run_analysis(config: SimulationConfig,
                num simulations to run: Optional[int] = None,
                run_analytical: bool = True) -> Dict[str, Any]:
    Run the complete analysis with simulations
    Parameters:
        config: Simulation configuration parameters
        num_simulations_to_run: Optional override for number of simulations
        run analytical: Whether to run the analytical solution
    Returns:
       Dictionary with results and figures
    if num_simulations_to_run is None:
        num_simulations_to_run = config.num_simulations
    # Run tests first
    test_ai_recommendations(config)
    # Run simulations with unified format
    print(f"\nRunning simulations ({num_simulations_to_run} iterations per
```

```
prior)...")
    standard_results, forced_results, trial_df = run_all_simulations(config,
num_simulations_to_run)
    # Run analytical solution with unified format if requested
    analytical results = None
    analytical_forced_results = None
    if run analytical:
        print("\nCalculating analytical solution...")
        analytical results, analytical forced results =
run_all_measures(config)
    # Return all results
    return {
        'standard': standard_results,
        'forced': forced results,
        'analytical': analytical_results,
        'analytical_forced': analytical_forced_results,
        'trial_df': trial_df
   }
```

# **Diagnostic and Testing Functions**

This section includes functions for testing and validating the AI recommendations:

• **test\_ai\_recommendations**: Runs controlled scenarios to verify that the AI models are making expected recommendations in specific cases. This helps ensure the correctness of the simulation logic.

```
# Diagnostic and Testing Functions
def test_ai_recommendations(config: SimulationConfig) -> None:
    """
    Function to test AI recommendations in controlled scenarios

Parameters:
        config: Simulation configuration parameters
    """
    print("Testing AI recommendations in controlled scenarios...")

# Test case 1: Good share, perfect knowledge
    print("\nCase 1: Good share with perfect knowledge")
    true_share_type = 'good'
    correct_decision = get_correct_decision(true_share_type, config)
    ai_rec = get_ai_recommendation('perfect', 0.5, ['high', 'high', 'high'],
3, config)
    print(f"True share type: {true_share_type}")
    print(f"Correct decision: {correct_decision}")
    print(f"Perfect AI recommendation: {ai_rec}")
```

```
print(f"Match: {ai rec == correct decision}")
   # Test case 2: Bad share, perfect knowledge
   print("\nCase 2: Bad share with perfect knowledge")
   true share type = 'bad'
   correct decision = get correct decision(true share type, config)
   ai_rec = get_ai_recommendation('perfect', 0.5, ['low', 'low', 'low'], 3,
config)
   print(f"True share type: {true_share_type}")
   print(f"Correct decision: {correct decision}")
   print(f"Perfect AI recommendation: {ai_rec}")
   print(f"Match: {ai rec == correct decision}")
   # Test Naive Prior AI progression
   print("\nTesting Naive Prior AI progression over trials...")
   outcomes = ['high', 'high', 'low', 'high', 'high', 'low', 'high']
   for trial in range(1, len(outcomes) + 1):
        current_outcomes = outcomes[:trial-1] # Exclude current trial
        nH = sum(1 for o in current_outcomes if o == 'high')
        nL = sum(1 for o in current outcomes if o == 'low')
        posterior = calculate posterior('naiveprior', 0.5, current outcomes,
trial-1, config)
        expected return = calculate expected return(posterior, config)
        recommendation = get ai recommendation('naiveprior', 0.5,
current outcomes, trial-1, config)
        print(f"Trial {trial}: High={nH}, Low={nL}, Posterior={posterior:.4f},
E[Return]={expected_return:.4f}, Recommendation={recommendation}")
```

#### **Execution Code**

This section contains the code to execute the analysis:

- It calls the run analysis function with desired parameters.
- It displays the performance summary, performance by prior probability, and performance across trials using the visualization functions defined earlier.

```
run analytical: Whether to run analytical solution
   Returns:
      Tuple of (config, results)
   # Create a copy of the config if we need to override num simulations
   if num_simulations_override is not None:
       # Since SimulationConfig is frozen, we need to create a new instance
        config = SimulationConfig(
            p=config.p,
            q=config.q,
            high payoff=config.high payoff,
            low payoff=config.low payoff,
            bond payoff=config.bond payoff,
            num_trials=config.num_trials,
            num simulations=num simulations override,
            ai_types=config.ai_types,
            beta=config.beta
        )
   # Run the analysis with the provided config
    results = run_analysis(config, num_simulations_to_run=None,
run_analytical=run_analytical)
   # Only display results if requested
   if display results:
       # ===== STANDARD RESULTS SECTION =====
       print("\n======= STANDARD RESULTS =======")
        print(f"Based on Monte Carlo simulation with {config.num simulations}
iterations")
        print("\nStandard Results Table:")
       display results table(results['standard'], config)
       # Show simulation performance visualizations
        print("\nSTANDARD PERFORMANCE BY PRIOR PROBABILITY")
        prior comparison = plot performance by prior(results['standard'],
config)
       plt.show()
       # Show performance across trials
       trial_charts = display_trial_accuracy_charts(results['trial_df'],
config)
        # ===== FORCED CHOICE SECTION =====
       print("\n======== FORCED CHOICE RESULTS =======")
        print(f"Based on Monte Carlo simulation with {config.num_simulations}
iterations")
        print("(Excluding cases where EV(share) = bond payoff exactly)")
```

```
display forced choice results(results['forced'], config)
       # Use the existing plotting function for forced choice
        print("\nFORCED CHOICE ACCURACY BY PRIOR PROBABILITY")
        forced_chart = plot_performance_by_prior(results['forced'], config)
        plt.show()
       # ==== ANALYTICAL RESULTS SECTION =====
       if results['analytical']:
            print("\n======= ANALYTICAL RESULTS =======")
            print("Exact mathematical solution for all possible sequences")
            print("\nAnalytical Results Table:")
            display_results_table(results['analytical'], config)
            # Display analytical performance by prior probability
            print("\nANALYTICAL PERFORMANCE BY PRIOR PROBABILITY")
            analytical_prior =
plot_analytical_performance_by_prior(results['analytical'], config)
            plt.show()
            # ==== ANALYTICAL FORCED CHOICE SECTION =====
            if results['analytical_forced']:
               print("\n======= ANALYTICAL FORCED CHOICE RESULTS
=======")
               print("Exact mathematical solution excluding cases where
EV(share) = bond payoff exactly")
               print("\nAnalytical Forced Choice Results Table:")
               display_forced_choice_results(results['analytical_forced'],
config)
               # Display analytical forced choice performance by prior
probability
                print("\nANALYTICAL FORCED CHOICE PERFORMANCE BY PRIOR
PROBABILITY")
               analytical_forced_prior =
plot performance by prior(results['analytical forced'], config)
                plt.show()
   return config, results
```

# Run the Analysis

This section initiates the analysis by calling the run\_analysis function.

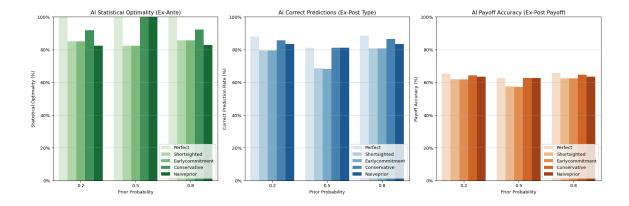
- It sets the num\_simulations\_to\_run parameter, which controls the number of simulations to perform for each prior probability.
- The run\_analysis function encapsulates the entire simulation process, including generating outcomes, calculating AI recommendations, and aggregating results.

• The results of the analysis are stored in the analysis\_results dictionary, which will be used for further processing and visualization.

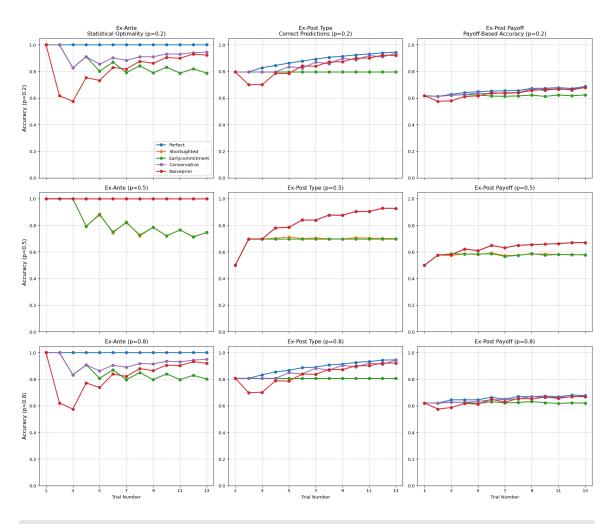
```
# Run the analysis
if __name__ == "__main__":
   # Run with default configuration
    config = DEFAULT CONFIG
    config, results = main(config, run_analytical=True)
   # Alternatively, you can override configurations:
   # custom_config = SimulationConfig(
   p=[0.3, 0.5, 0.7], \# Different priors
   \# q=0.6, \# Different q \# high_payoff=10, \# Different payoffs
   # low_payoff=0,
# bond_payoff=5,
# num_trials=10,
                          # Fewer trials
   # num simulations=1000, # Fewer simulations
        ai_types=['perfect', 'shortsighted', 'conservative'], # Subset of
AIs
   #
        beta=0.3
                            # Different beta
   # )
   # results = main(custom config)
   # Or just override the number of simulations:
    # results = main(num_simulations_override=500)
```

```
Testing AI recommendations in controlled scenarios...
Case 1: Good share with perfect knowledge
True share type: good
Correct decision: share
Perfect AI recommendation: share
Match: True
Case 2: Bad share with perfect knowledge
True share type: bad
Correct decision: bond
Perfect AI recommendation: bond
Match: True
Testing Naive Prior AI progression over trials...
Trial 1: High=0, Low=0, Posterior=0.5000, E[Return]=3.0000,
Recommendation=indifferent
Trial 2: High=1, Low=0, Posterior=0.7000, E[Return]=3.3200,
Recommendation=share
Trial 3: High=2, Low=0, Posterior=0.8448, E[Return]=3.5517,
```

```
Recommendation=share
Trial 4: High=2, Low=1, Posterior=0.7000, E[Return]=3.3200,
Recommendation=share
Trial 5: High=3, Low=1, Posterior=0.8448, E[Return]=3.5517,
Recommendation=share
Trial 6: High=4, Low=1, Posterior=0.9270, E[Return]=3.6832,
Recommendation=share
Trial 7: High=4, Low=2, Posterior=0.8448, E[Return]=3.5517,
Recommendation=share
Trial 8: High=5, Low=2, Posterior=0.9270, E[Return]=3.6832,
Recommendation=share
Running simulations (10000 iterations per prior)...
Calculating analytical solution...
Calculating analytical solution for p=0.2
Calculating analytical solution for p=0.5
Calculating analytical solution for p=0.8
====== STANDARD RESULTS ======
Based on Monte Carlo simulation with 10000 iterations
Standard Results Table:
Number of trials num_trials=13
===== p = 0.2 =====
               => ex-ante=1.0000, ex-post-type=0.8812, ex-post-
 perfect
payoff=0.6531
 shortsighted
                 => ex-ante=0.8505, ex-post-type=0.7958, ex-post-
payoff=0.6184
 earlycommitment => ex-ante=0.8505, ex-post-type=0.7958, ex-post-
payoff=0.6184
 conservative
                 => ex-ante=0.9188, ex-post-type=0.8556, ex-post-
payoff=0.6431
 naiveprior
                 => ex-ante=0.8244, ex-post-type=0.8332, ex-post-
payoff=0.6341
===== p = 0.5 =====
 perfect
                 => ex-ante=1.0000, ex-post-type=0.8118, ex-post-
payoff=0.6254
                 => ex-ante=0.8229, ex-post-type=0.6862, ex-post-
 shortsighted
payoff=0.5739
 earlycommitment => ex-ante=0.8230, ex-post-type=0.6811, ex-post-
payoff=0.5737
 conservative
                 => ex-ante=1.0000, ex-post-type=0.8118, ex-post-
payoff=0.6254
                 => ex-ante=1.0000, ex-post-type=0.8118, ex-post-
 naiveprior
payoff=0.6254
```

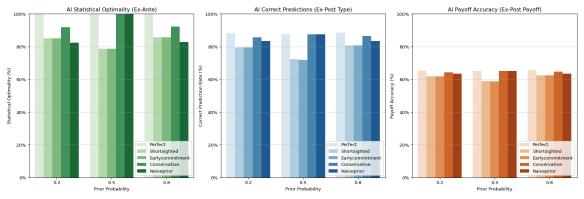


#### ACCURACY ACROSS TRIALS

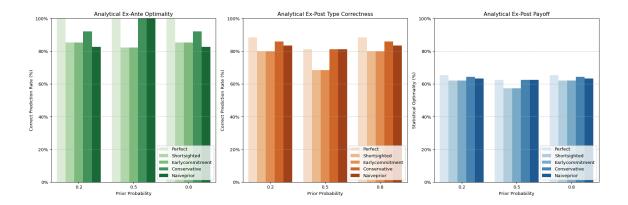


```
====== FORCED CHOICE RESULTS =======
Based on Monte Carlo simulation with 10000 iterations
(Excluding cases where EV(share) = bond payoff exactly)
==== FORCED CHOICE ACCURACY (EXCLUDING EV TIES) =====
Prior p = 0.2
 perfect
                 => ex-ante=1.0000, ex-post-type=0.8812, ex-post-
payoff=0.6531 (using 100.0% of trials)
                 => ex-ante=0.8505, ex-post-type=0.7958, ex-post-
 shortsighted
payoff=0.6184 (using 100.0% of trials)
 earlycommitment => ex-ante=0.8505, ex-post-type=0.7958, ex-post-
payoff=0.6184 (using 100.0% of trials)
               => ex-ante=0.9188, ex-post-type=0.8556, ex-post-
 conservative
payoff=0.6431 (using 100.0% of trials)
                 => ex-ante=0.8244, ex-post-type=0.8332, ex-post-
 naiveprior
payoff=0.6341 (using 100.0% of trials)
```

```
Prior p = 0.5
 perfect
                 => ex-ante=1.0000, ex-post-type=0.8748, ex-post-
payoff=0.6507 (using 83.2% of trials)
 shortsighted => ex-ante=0.7871, ex-post-type=0.7235, ex-post-
payoff=0.5897 (using 83.2% of trials)
 earlycommitment => ex-ante=0.7872, ex-post-type=0.7187, ex-post-
payoff=0.5879 (using 83.2% of trials)
                 => ex-ante=1.0000, ex-post-type=0.8748, ex-post-
 conservative
payoff=0.6507 (using 83.2% of trials)
                 => ex-ante=1.0000, ex-post-type=0.8748, ex-post-
payoff=0.6507 (using 83.2% of trials)
Prior p = 0.8
                 => ex-ante=1.0000, ex-post-type=0.8858, ex-post-
 perfect
payoff=0.6562 (using 100.0% of trials)
 shortsighted
                => ex-ante=0.8560, ex-post-type=0.8066, ex-post-
payoff=0.6236 (using 100.0% of trials)
 earlycommitment => ex-ante=0.8560, ex-post-type=0.8066, ex-post-
payoff=0.6236 (using 100.0% of trials)
                 => ex-ante=0.9223, ex-post-type=0.8645, ex-post-
 conservative
payoff=0.6468 (using 100.0% of trials)
 naiveprior
                 => ex-ante=0.8284, ex-post-type=0.8343, ex-post-
payoff=0.6352 (using 100.0% of trials)
FORCED CHOICE ACCURACY BY PRIOR PROBABILITY
```

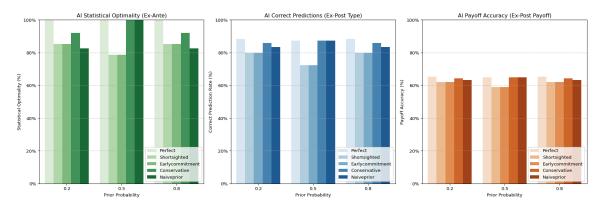


```
perfect
                 => ex-ante=1.0000, ex-post-type=0.8827, ex-post-
payoff=0.6531
  shortsighted
                 => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200
 earlycommitment => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200
                 => ex-ante=0.9204, ex-post-type=0.8593, ex-post-
 conservative
payoff=0.6437
                 => ex-ante=0.8259, ex-post-type=0.8335, ex-post-
 naiveprior
payoff=0.6334
===== p = 0.5 =====
 perfect
                 => ex-ante=1.0000, ex-post-type=0.8104, ex-post-
payoff=0.6242
  shortsighted
                 => ex-ante=0.8222, ex-post-type=0.6846, ex-post-
payoff=0.5738
 earlycommitment => ex-ante=0.8222, ex-post-type=0.6846, ex-post-
payoff=0.5738
                 => ex-ante=1.0000, ex-post-type=0.8104, ex-post-
 conservative
payoff=0.6242
 naiveprior
                 => ex-ante=1.0000, ex-post-type=0.8104, ex-post-
payoff=0.6242
===== p = 0.8 =====
                 => ex-ante=1.0000, ex-post-type=0.8827, ex-post-
 perfect
payoff=0.6531
  shortsighted
                 => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200
 earlycommitment => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200
 conservative
                 => ex-ante=0.9204, ex-post-type=0.8593, ex-post-
payoff=0.6437
 naiveprior
                 => ex-ante=0.8259, ex-post-type=0.8335, ex-post-
payoff=0.6334
ANALYTICAL PERFORMANCE BY PRIOR PROBABILITY
```



```
====== ANALYTICAL FORCED CHOICE RESULTS =======
Exact mathematical solution excluding cases where EV(share) = bond payoff
exactly
Analytical Forced Choice Results Table:
==== FORCED CHOICE ACCURACY (EXCLUDING EV TIES) =====
Prior p = 0.2
 perfect
                 => ex-ante=1.0000, ex-post-type=0.8827, ex-post-
payoff=0.6531 (using 100.0% of trials)
                 => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
 shortsighted
payoff=0.6200 (using 100.0% of trials)
 earlycommitment => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200 (using 100.0% of trials)
 conservative
                 => ex-ante=0.9204, ex-post-type=0.8593, ex-post-
payoff=0.6437 (using 100.0% of trials)
 naiveprior
                 => ex-ante=0.8259, ex-post-type=0.8335, ex-post-
payoff=0.6334 (using 100.0% of trials)
Prior p = 0.5
                 => ex-ante=1.0000, ex-post-type=0.8733, ex-post-
 perfect
payoff=0.6493 (using 83.2% of trials)
                 => ex-ante=0.7862, ex-post-type=0.7220, ex-post-
 shortsighted
payoff=0.5888 (using 83.2% of trials)
 earlycommitment => ex-ante=0.7862, ex-post-type=0.7220, ex-post-
payoff=0.5888 (using 83.2% of trials)
 conservative
                => ex-ante=1.0000, ex-post-type=0.8733, ex-post-
payoff=0.6493 (using 83.2% of trials)
                 => ex-ante=1.0000, ex-post-type=0.8733, ex-post-
 naiveprior
payoff=0.6493 (using 83.2% of trials)
Prior p = 0.8
 perfect
                 => ex-ante=1.0000, ex-post-type=0.8827, ex-post-
payoff=0.6531 (using 100.0% of trials)
```

```
shortsighted => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200 (using 100.0% of trials)
  earlycommitment => ex-ante=0.8531, ex-post-type=0.8000, ex-post-
payoff=0.6200 (using 100.0% of trials)
  conservative => ex-ante=0.9204, ex-post-type=0.8593, ex-post-
payoff=0.6437 (using 100.0% of trials)
  naiveprior => ex-ante=0.8259, ex-post-type=0.8335, ex-post-
payoff=0.6334 (using 100.0% of trials)
ANALYTICAL FORCED CHOICE PERFORMANCE BY PRIOR PROBABILITY
```



# Analysis of Germann and Merkle data using framework

```
# load the data from data/germann-and-merkle-2023.dta
import os

from dataclasses import dataclass, field
from typing import Optional
from typing import Dict, Any, List, Tuple

# Load the data

data_path = os.path.join(os.getcwd(), 'data', 'germann-and-merkle-2023.dta')
df = pd.read_stata(data_path)
df.head()
```

	ac-										skill ing									
troi	ınd																			
0	11	NaN3	0	3	1	0	1.0	1	1		4.0	3.0	2.0	4.0	2.0	3.0	4.0	2.0	0.0	1.0
1	12	NaN3	0	3	5	1	1.0	1	1		4.0	3.0	2.0	4.0	2.0	3.0	4.0	2.0	0.0	2.0

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2	13	NaN1	1	1	1	1	1.0	1 1		4.0	3.0	2.0	4.0	2.0	3.0	4.0	2.0	1.0	3.0
3	14	NaN1	1	3	1	1	1.0	1 1		4.0	3.0	2.0	4.0	2.0	3.0	4.0	2.0	0.0	4.0
4	15	NaN3	0	3	1	0	1.0	1 1		4.0	3.0	2.0	4.0	2.0	3.0	4.0	2.0	0.0	5.0