

FIT3158 Note - W6 MODI

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Example is from [Transportation Problem | Set 6 \(MODI Method - UV Method\) - GeeksforGeeks](#).

▼ More exercises

[transportation problem using modi method \(optimal solution\) Algorithm & Example-1 \(atozmath.com\)](#)

https://s3-us-west-2.amazonaws.com/secure.notion-static.com/b1dc83fb-f33b-4806-86be-811df28d6a56/Degeneracy_Optimisation_techniques_of_Transportation_Problem.pdf

[\(3785\) Transportation problem \[MODI method - U V method with Optimal Solution \] kausewise - YouTube](#)

	V1=	V2=	V3=	V4=
u1 =	200	50		
	3	1	7	4
u2 =		250	100	
	2	6	5	9
u3 =	8	3	250	150
			3	2

$$u_i + v_j = C_{ij}$$

Let $U_1=0$,
 $0 + V_1 = 3$
 $V_1 = 3$

$0 + V_2 = 1$
 $V_2 = 1$

$U_2 + V_2 = 3$
 $U_2 + 1 = 6$
 $U_2 = 5$

$U_2 + V_3 = 5$
 $5 + V_3 = 5$
 $V_3 = 0$

$U_3 + V_3 = 3$
 $U_3 + 0 = 3$
 $U_3 = 3$

$U_3 + V_4 = 2$
 $3 + V_4 = 2$
 $V_4 = -1$

1. Let U_1 ge 情況下，搵allocated cells ge U/V value

	v1=-3	v2=1	v3=0	v4=-1
u1=0	200	250	$0 + 0 - 7 = -7$	$0 + (-1) - 4 = -5$
	3	1	7	4
u2=5	$5 + 3 - 2 = 6$	50	100	$5 + (-1) - 9 = -5$
	2	6	5	9
u3=3	$3 + 3 - 8 = -2$	$3 + 1 - 3 = 1$	250	150
	8	3	3	2

$P_{ij} = u_i + v_j - C_{ij}$

2. Add penalty to unallocated cells. We have two unallocated cells in the first row, two in the second row and two in the third row. Lets compute this one by one.

▼ 幾時可以停？

If we get all the penalties value as zero or negative values that mean the optimality is reached and this answer is the final answer. But if we get any positive value means we need to proceed with the sum in the next step.

	v1=-3	v2=1	v3=0	v4=-1
u1=0	200	250	$0 + 0 - 7 = -7$	$0 + (-1) - 4 = -5$
	3	1	7	4
u2=5	$5 + 3 - 2 = 6$	50	100	$5 + (-1) - 9 = -5$
	2	6	5	9
u3=3	$3 + 3 - 8 = -2$	$3 + 1 - 3 = 1$	250	150
	8	3	3	2

$P_{ij} = u_i + v_j - C_{ij}$

係 penalty 最大值ge cell 到
做個loop

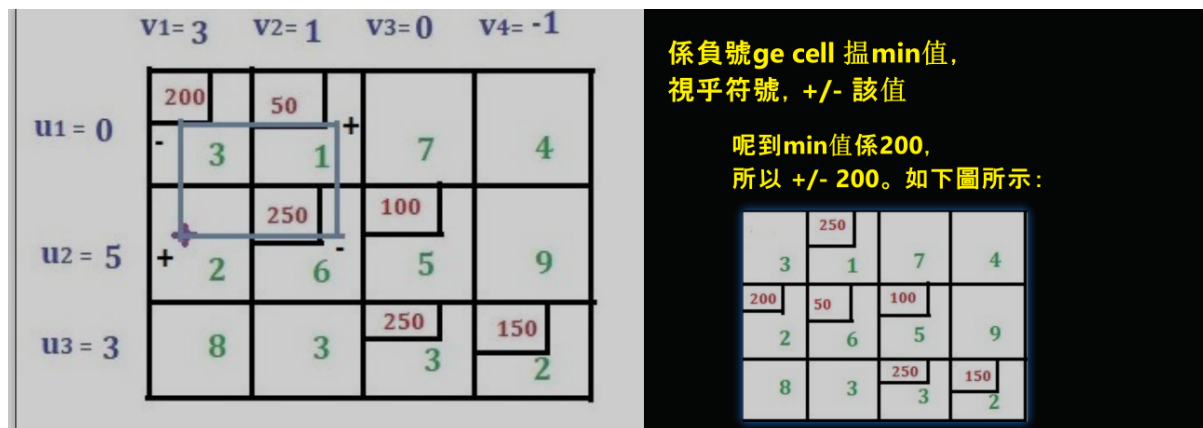
呢到係 C21 (6)

Unallocated cell 唔比轉右
Right angle turn is not permitted in unallocated cell.

✗ 唔ok

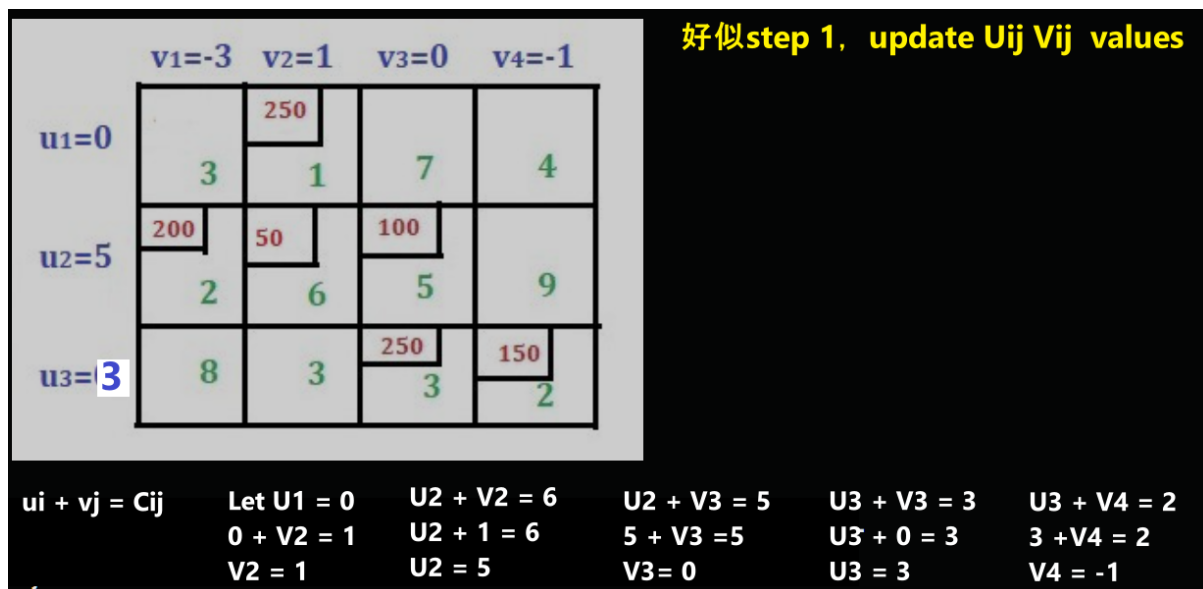
✓ ok

3. 係pen'ality 最大值ge cell 加符號，做個loop。Loop 吾比一開始轉右



Step 4.

Iteration 2



	$v_1=-3$	$v_2=1$	$v_3=0$	$v_4=-1$
$u_1=0$	$0 + (-3) - 3 = -6$ 3	250 1	$0 + 0 - 7 = -7$ 7	$0 + (-1) - 4 = -5$ 4
$u_2=5$	200 2	50 6	100 5	$5 + (-1) - 9 = -5$ 9
$u_3=3$	$3 + (-3) - 8 = -8$ 8	$3 + 1 - 3 = 1$ 3	250 3	150 2

好似step 1, update U_{ij} V_{ij} values

$$P_{ij} = u_i + v_j - C_{ij}$$

Like step 2, Add penalty to unallocated cells. We have two unallocated cells in the first row, two in the second row and two in the third row. Lets compute this one by one.

	$v_1=-3$	$v_2=1$	$v_3=0$	$v_4=-1$
$u_1=0$	$0 + (-3) - 3 = -6$ 3	250 1	$0 + 0 - 7 = -7$ 7	$0 + (-1) - 4 = -5$ 4
$u_2=5$	200 2	50 6	100 5	$5 + (-1) - 9 = -5$ 9
$u_3=3$	$3 + (-3) - 8 = -8$ 8	$3 + 1 - 3 = 1$ 3	250 3	150 2

好似step 1, update U_{ij} V_{ij} values

	$v_1=-3$	$v_2=1$	$v_3=0$	$v_4=-1$
$u_1=0$	3	250 1	7	4
$u_2=5$	200 2	50 6	100 5	9
$u_3=3$	8	3	250 3	150 2

$$P_{ij} = u_i + v_j - C_{ij}$$

	$v_1=-3$	$v_2=1$	$v_3=0$	$v_4=-1$
$u_1=0$	3	250 1	7	4
$u_2=5$	200 2	50 6	100 5	9
$u_3=3$	8	3	250 3	150 2

負號cell Min 值為50, 所以+/- 50

		250		
3	1	7	4	
200		150		9
8	50	3	200	150
		3		2

Iteration 3

	$v_1 = -1$	$v_2 = 1$	$v_3 = 1$	$v_4 = 0$
$u_1 = 0$	250 3	1 7	7 4	4
$u_2 = 4$	200 2	6 5	150 9	9
$u_3 = 2$	50 8	3 3	200 3	150 2

$U_2 + V_3 = 5$
 $U_2 + 1 = 5$
 $U_2 = 4$

$U_2 + V_1 = 3$
 $4 + V_1 = 3$
 $V_1 = -1$

$u_i + v_j = c_{ij}$ Let $u_1 = 0$
 $U_1 + V_2 = 1$ $U_3 + V_2 = 3$ $U_3 + V_3 = 3$ $U_3 + V_4 = 2$
 $V_2 = 1$ $U_3 = 2$ $V_3 = 1$ $2 + V_4 = 2$
 $V_4 = 0$

Like step 1, update U and V value

	$v_1 = -1$	$v_2 = 1$	$v_3 = 1$	$v_4 = 0$
$u_1 = 0$	$0 + (-1) - 3 = -4$ 250 3	$0 + 1 - 7 = -6$ 1 7	$0 + 0 - 4 = -4$ 7 4	4
$u_2 = 4$	$4 + (-1) - 2 = -1$ 200 2	$4 + 1 - 6 = -1$ 6 5	$4 + 0 - 9 = -5$ 150 9	9
$u_3 = 2$	$2 + (-1) - 8 = -7$ 50 8	3 3	200 3	150 2

$U_2 + V_3 = 5$
 $U_2 + 1 = 5$
 $U_2 = 4$

$U_2 + V_1 = 3$
 $4 + V_1 = 3$
 $V_1 = -1$

$u_i + v_j = c_{ij}$ Let $u_1 = 0$
 $U_1 + V_2 = 1$ $U_3 + V_2 = 3$ $U_3 + V_3 = 3$ $U_3 + V_4 = 2$
 $V_2 = 1$ $U_3 = 2$ $V_3 = 1$ $2 + V_4 = 2$
 $V_4 = 0$

由於所有penalty 係負數,
So the optimality is reached.

Now, total cost = $(250 * 1) + (200 * 2) + (150 * 5) + (50 * 3) + (200 * 3) + (150 * 2) = 2450$