

1. (a) Write a specification of an hour-clock that sends the time to the environment over a channel *chan*. The specification should make use of the definitions from the *Channel* and *HourClock* modules by incorporating them with an *EXTENDS* statement. Write two versions of the specification.

Version 1: The clock can tick at any time.

Version 2: The clock cannot tick between sending a value on *chan* and the receipt of that value by the environment.

Include type invariants and use *TLC* to check them.

(b) Use *TLC* to check that the Version 1 specification implements the *Channel* specification with *Data* replaced by $1 \dots 12$. That is, every behavior allowed by your specification satisfies the specification *Spec* of module *Channel*, with *Data* replaced by the set $1 \dots 12$. Use *TLC* to check that Version 2 implements the specification *HourClockChannel* that you wrote in Exercise 1 of folder *AsynchronousInterface*.

(c) Write specifications that hides the clock in the specifications of part (a). Explain informally why the resulting specification is equivalent to:

- The *Channel* specification with *Data* replaced by $1 \dots 12$, for Version 1.
- The *HourClockChannel* specification, for Version 2.

EXTENDS *Naturals*, *HourClock*, *Channel*, *TLC*

$$PrintVal(id, exp) \triangleq Print(\langle id, exp \rangle, TRUE)$$

$$IsSending \triangleq chan.rdy \neq chan.ack$$

$$\begin{aligned} HCChannelInit &\triangleq \wedge TypeInvariant \\ &\wedge chan.ack = chan.rdy \\ &\wedge HCini \end{aligned}$$

$$\begin{aligned} HCChannelSend(d) &\triangleq \wedge chan.rdy = chan.ack \\ &\wedge chan' = [chan \text{ EXCEPT } !.val = d, !.rdy = 1 - @] \\ &\wedge UNCHANGED \langle hr \rangle \end{aligned}$$

$$\begin{aligned} HCChannelRcv &\triangleq \wedge chan.rdy \neq chan.ack \\ &\wedge chan' = [chan \text{ EXCEPT } !.ack = 1 - @] \\ &\wedge UNCHANGED \langle hr \rangle \end{aligned}$$

$$\begin{aligned} HCnxtChannel &\triangleq \wedge HCnxt \\ &\wedge \neg IsSending \\ &\wedge UNCHANGED \langle chan \rangle \\ &\wedge PrintVal("HCnxtChannel", \langle hr, chan \rangle) \end{aligned}$$

$$HCChannelNext \triangleq (\exists d \in Data : HCChannelSend(d)) \vee HCChannelRcv \vee HCnxtChannel$$

$$HCChannelSpec \triangleq HCChannelInit \wedge \Box [HCChannelNext]_{\langle chan, hr \rangle}$$

THEOREM $HCChannelSpec \Rightarrow \Box TypeInvariant$

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