

EXTENDS *Integers*  
 VARIABLES *small, big*

In the movie *Die Hard 3*, our heroes, *John McClain* (Bruce Willis) and Zeus (Samuel L. Jackson), are at the bidding of the evil *Peter Krieg* (Jeremy Irons). First they are sent to the pay phone, then to the subway, and finally to the park. It is here that they must make exactly four gallons from five and three gallon jugs. They did it just in time.

$$\begin{aligned}
 \textit{TypeOK} &\triangleq \wedge \textit{small} \in 0 \dots 3 \\
 &\quad \wedge \textit{big} \in 0 \dots 5 \\
 \\
 \textit{Init} &\triangleq \wedge \textit{big} = 0 \\
 &\quad \wedge \textit{small} = 0 \\
 \\
 \textit{FillSmall} &\triangleq \wedge \textit{small}' = 3 \\
 &\quad \wedge \textit{big}' = \textit{big} \\
 \\
 \textit{FillBig} &\triangleq \wedge \textit{big}' = 5 \\
 &\quad \wedge \textit{small}' = \textit{small} \\
 \\
 \textit{EmptySmall} &\triangleq \wedge \textit{small}' = 0 \\
 &\quad \wedge \textit{big}' = \textit{big} \\
 \\
 \textit{EmptyBig} &\triangleq \wedge \textit{big}' = 0 \\
 &\quad \wedge \textit{small}' = \textit{small} \\
 \\
 \textit{SmallToBig} &\triangleq \vee \wedge \textit{big} + \textit{small} \leq 5 \\
 &\quad \wedge \textit{big}' = \textit{big} + \textit{small} \\
 &\quad \wedge \textit{small}' = 0 \\
 &\quad \vee \wedge \textit{big}' = 5 \\
 &\quad \wedge \textit{small}' = \textit{small} - (5 - \textit{big}) \\
 \\
 \textit{BigToSmall} &\triangleq \vee \wedge \textit{big} + \textit{small} \leq 3 \\
 &\quad \wedge \textit{small}' = \textit{big} + \textit{small} \\
 &\quad \wedge \textit{big}' = 0 \\
 &\quad \vee \wedge \textit{small}' = 3 \\
 &\quad \wedge \textit{big}' = \textit{small} - (3 - \textit{big}) \\
 \\
 \textit{Invariant} &\triangleq \textit{big} \neq 4 \\
 \\
 \textit{Next} &\triangleq \vee \textit{FillSmall} \\
 &\quad \vee \textit{FillBig} \\
 &\quad \vee \textit{EmptySmall} \\
 &\quad \vee \textit{EmptyBig} \\
 &\quad \vee \textit{SmallToBig} \\
 &\quad \vee \textit{BigToSmall}
 \end{aligned}$$

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