## - Module Assumes -

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{\tt EXTENDS}\ Integers,\ Sequences
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You can run this as a model using "No behavior spec" mode Single line comment
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ASSUME

$$\land$$
 TRUE = TRUE

$$\land \neg FALSE = TRUE$$

 $Jason \triangleq$  "jason"

ASSUME

$$Jason = "jason"$$

$$record \triangleq [name \mapsto "jason", age \mapsto 2]$$

ASSUME

$$\land record.name = "jason"$$

$$\land \textit{record.name} \neq \textit{``foo''}$$

ASSUME

$$\forall F \in \{\text{TRUE}\} : F = F$$

ASSUME

$$\forall F \in \{\text{False}\} : F = F$$

ASSUME 
$$\Rightarrow$$
 means "implies", as in  $A \Rightarrow B$  is "(not A) OR B"

 $FALSE \Rightarrow TRUE = TRUE$ 

ASSUME 
$$\Rightarrow$$
 means "implies", as in  $A \Rightarrow B$  is " $(not\ A)$  OR  $B$ "

 $FALSE \Rightarrow FALSE = TRUE$ 

ASSUME 
$$\Rightarrow$$
 means "implies", as in  $A \Rightarrow B$  is "(not A) OR B"

 $\mathtt{TRUE} \Rightarrow \overline{\mathtt{TRUE}} = \overline{\mathtt{TRUE}}$ 

ASSUME 
$$\Rightarrow$$
 means "implies", as in  $A \Rightarrow B$  is " $(not\ A)$  OR  $B$ "

 $\texttt{TRUE} \Rightarrow \texttt{FALSE} = \texttt{FALSE}$ 

ASSUME

 $\mathrm{TRUE} \equiv \mathrm{TRUE}$ 

ASSUME

 $FALSE \equiv FALSE$ 

ASSUME

$$\forall F, G \in \{\text{TRUE}, \text{FALSE}\} : (F \Rightarrow G) \equiv \neg F \vee G$$

Sets

$$\{1, 2, 2, 2, 3\} = \{1, 2, 3\}$$

ASSUME

$$\{1, 2, 3, 3, 4, 4\} \setminus \{4\} = \{1, 2, 3\}$$

ASSUME

$$\{1, 2, 3\} \cup \{4, 5, 6\} = \{1, 2, 3, 4, 5, 6\}$$

ASSUME

$$\exists x \in \{3, 4, 5\} : x = 5$$

ASSUME

$$\{1, 3\} \subseteq \{3, 2, 1\}$$

$$IsPrime(x) \stackrel{\triangle}{=} x > 1 \land \neg \exists d \in 2 ... (x-1) : x\%d = 0$$

For all y in S such that y is not prime or y is less than or equal to x

$$LargestPrime(S) \stackrel{\triangle}{=} CHOOSE \ x \in S:$$

$$\land IsPrime(x)$$

$$\land \, \forall \, y \in S :$$

$$IsPrime(y) \Rightarrow y \leq x$$

or 
$$y > x \Rightarrow \neg IsPrime(y)$$

ASSUME

$$LargestPrime(\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}) = 7$$

$$IsEven(x) \triangleq x\%2 = 0$$

$$LargetEven(S) \stackrel{\triangle}{=} CHOOSE \ x \in S:$$

$$\land \mathit{IsEven}(x)$$

$$\land \forall y \in S$$
:

$$IsEven(y) \Rightarrow y \leq x$$

ASSUME

$$LargetEven({1, 2, 3, 4, 5, 5, 5}) = 4$$

ASSUME

$$\forall x \in \{\} : \text{False}$$

ASSUME

$$\forall x \in \{\} : \text{TRUE}$$

ASSUME

```
\forall x \in \{\}: 7
ASSUME
  \forall x \in \{\text{FALSE}\} : \text{TRUE}
ASSUME
  \forall x \in \{\text{TRUE}\}: \text{TRUE}
ASSUME
  (\forall x \in \{\text{FALSE}\} : \text{FALSE}) = \text{FALSE}
IsCommutative(Op(\_, \_), S) \stackrel{\triangle}{=} \forall x \in S:
                                        \forall y \in S : Op(x, y) = Op(y, x)
Add(x, y) \stackrel{\Delta}{=} x + y
Divide(x, y) \triangleq x \div y
ASSUME
  IsCommutative(Add, \{1, 2, 3\})
  IsCommutative(Divide, \{1, 2, 3\}) = FALSE
ASSUME
  IsCommutative(Divide, \{1, 2, 3\}) \Rightarrow FALSE
  IsCommutative(Divide, \{1, 2, 3\}) \Rightarrow TRUE
ASSUME
  \neg IsCommutative(Divide, \{1, 2, 3\})
  \neg \exists x \in \{1, 3, 5\} : IsEven(x)
Pick(S) \stackrel{\triangle}{=} CHOOSE \ s \in S : TRUE
RECURSIVE SetReduce(_, _, _)
SetReduce(Op(\_,\_), S, value) \stackrel{\triangle}{=} IF S = \{\} THEN value ELSE LET s \stackrel{\triangle}{=} Pick(S)
                                          IN SetReduce(Op, S \setminus \{s\}, Op(s, value))
Sum(S) \stackrel{\Delta}{=} LET \_op(a, b) \stackrel{\Delta}{=} a + b
                 IN SetReduce(\_op, S, 0)
ASSUME
  Sum(\{1, 2, 3\}) = 6
Min(S) \stackrel{\triangle}{=} CHOOSE \ x \in S : \forall y \in S : x \leq y
```

 $\land \land$  "one", "two" $\ \ \in digits$  $\land \land$  "three", "four" $\ \ \ \in digits$ 

 $\begin{array}{ccc} A & \stackrel{\triangle}{=} & \{1\} \\ B & \stackrel{\triangle}{=} & \{2\} \\ C & \stackrel{\triangle}{=} & \{3\} \end{array}$ 

### ASSUME

#### Structures.

Structures are hashes. They have keys and values. You specify them as  $[\ker \mapsto value]$  and query them with either ["key"] or .key. Both are legal and valid.

$$SomeHash \stackrel{\triangle}{=} [x \mapsto 1, y \mapsto \{2, 3\}]$$

#### ASSUME

- $\land SomeHash.x = 1$  $\land SomeHash["x"] = 1$

Aside from that, there's one extra trick structures have. Instead of key  $\mapsto value$ , you can do key : set. In that case, instead of a structure you get the set of all structures which have, for each given key, a value in the set.

$$SetOfStructures \triangleq [x:\{1\}, y:\{2, 3, 4\}]$$

If you use: syntax and any of the values are not sets, then the entire construct is invalid. In other words, while  $[a: \{1\}, b: \{2, 3\}]$  is the above set,  $[a: 1, b: \{2, 3\}]$  will throw an error if you try to use it.

#### ASSUME

## Type Composition

Any type can be squeezed inside any other type.

$$\mathit{crazy} \ \stackrel{\triangle}{=} \ [a \mapsto \{\langle \rangle, \ \langle 1, \ 2, \ 3 \rangle, \ \langle 3, \ 2, \ 1 \rangle \}, \ b \mapsto \langle [a \mapsto 0] \rangle]$$

A function of keys mapping to sets of tuples or of keys mapping to tuples of functions.

# ASSUME

crazy.b[1].a = 0 Remember that tuples are 1 indexed.

$$blah \ \stackrel{\triangle}{=} \ [name \mapsto \text{"jason"}, \ hobbies \mapsto [outdoor \mapsto \langle \text{"cycling"}, \text{ "hiking"} \rangle, \ indoor \mapsto \langle \text{"reading"}, \text{ "watching tv"} \rangle]]$$
 ASSUME

$$\land blah.name = "jason"$$

 $\land \mathit{blah.hobbies.outdoor}[1] = \mathsf{``cycling''}$ 

$$sing \triangleq \langle \langle 4, 5, 6 \rangle, \langle \rangle, \langle \rangle \rangle$$

ASSUME

Domain  $sing = \{1, 2, 3\}$ 

- \ \* Last modified Sun Apr 21 20:00:41 PDT 2019 by jasondebolt \ \* Created Sat Apr 20 20:01:34 PDT 2019 by jasondebolt