D213 - Advanced Data Analytics PA1

July 22, 2022

0.0.1 D213 - Advanced Data Analytics - PA1

0.0.2 Background Info:

As part of the "readmission" project, executives would like to see consider a time series on revenue from the first years of operation. Once they understand any patterns in that data, they feel confident in understanding the impact of readmission in current times. The given time series data records the daily revenue, in million dollars, during the first two years of operation.

A1 Question: Using the previous two years of data, are there any patterns present that can predict the revenue produced by the hospital for the next quarter?

0.0.3 Import Libraries

```
[1]: import pandas as pd
     from pandas.plotting import autocorrelation_plot
     import seaborn as sns
     import numpy as np
     from statsmodels.tsa.seasonal import seasonal_decompose
     from statsmodels.tsa.stattools import adfuller
     from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
     from statsmodels.tsa.arima_model import ARIMA
     from statsmodels.tsa.statespace.sarimax import SARIMAX
     import pmdarima as pm
     import matplotlib.pyplot as plt
     from scipy import signal
     from datetime import datetime
     from sklearn.model_selection import train_test_split
     from tqdm import tqdm
     import warnings
     warnings.filterwarnings('ignore')
     #!pip install joblib
     import joblib
     %matplotlib inline
     %time
     %timeit
```

```
CPU times: user 1 \mus, sys: 0 ns, total: 1 \mus Wall time: 3.1 \mus
```

```
[2]: #%lsmagic
    0.0.4 Load Data From medical time series.csv
[3]: # load data file
     initial_df = pd.read_csv('medical_time_series.csv', index_col='Day',__
      →parse_dates=True)
     # quick test the data is present and see the shape
     print("df shape: ", initial_df.shape)
     initial_df.head()
    df shape: (731, 1)
[3]:
          Revenue
    Day
          0.00000
     1
     2
        -0.292356
     3
        -0.327772
     4
         -0.339987
         -0.124888
[4]: initial_df.info()
    <class 'pandas.core.frame.DataFrame'>
    Int64Index: 731 entries, 1 to 731
    Data columns (total 1 columns):
         Column
                  Non-Null Count Dtype
         Revenue 731 non-null
                                  float64
    dtypes: float64(1)
    memory usage: 11.4 KB
[5]: initial_df.describe()
[5]:
               Revenue
     count 731.000000
    mean
            14.179608
             6.959905
    std
    min
            -4.423299
    25%
             11.121742
    50%
             15.951830
    75%
             19.293506
             24.792249
    max
[6]: # Any Null Values?
     initial_df.isnull().any()
```

[6]: Revenue False dtype: bool

0.0.5 Check for Missing Values

```
[7]: # Mapping to view missing data...none present.
sns.heatmap(initial_df.isnull(), yticklabels=False, cbar=False, cmap='viridis');
```



```
[8]: initial_df.columns
```

[8]: Index(['Revenue'], dtype='object')

```
[9]: Revenue

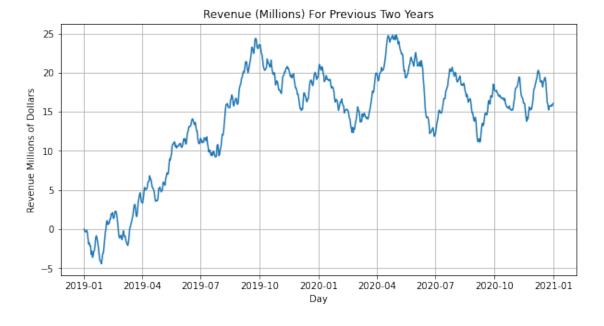
Date
2019-01-01 0.000000
2019-01-02 -0.292356
2019-01-03 -0.327772
2019-01-04 -0.339987
```

```
2019-01-05 -0.124888

... ... ...
2020-12-27 15.722056
2020-12-28 15.865822
2020-12-29 15.708988
2020-12-30 15.822867
2020-12-31 16.069429

[731 rows x 1 columns]
```

0.1 C1 - Provide a line graph visualizing the realization of the time series

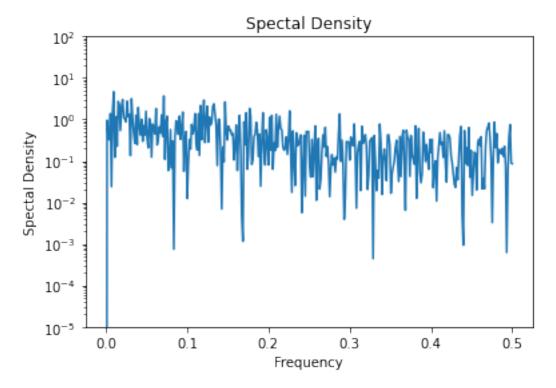


```
[19]: # Drop any null columns
df = initial_df.dropna()
df
```

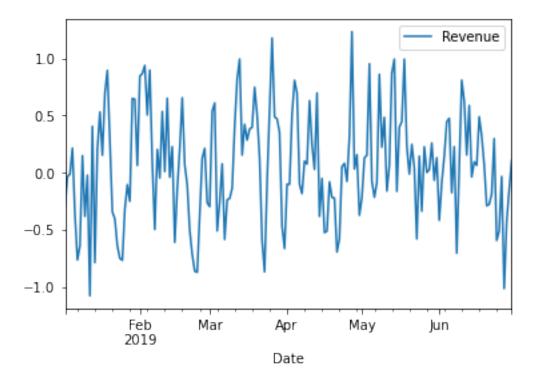
```
[19]:
                   Revenue
     Date
     2019-01-01
                  0.000000
     2019-01-02 -0.292356
     2019-01-03 -0.327772
      2019-01-04 -0.339987
      2019-01-05 -0.124888
      2020-12-27 15.722056
      2020-12-28 15.865822
      2020-12-29 15.708988
      2020-12-30 15.822867
      2020-12-31 16.069429
      [731 rows x 1 columns]
[20]: # Export cleaned data
      pd.DataFrame(df).to_csv("df_cleaned.csv")
     0.2 C3 - Make Time Series Stationary
[21]: # Verify if data is stationary
      result = adfuller(df['Revenue'])
      print("Test Statistics: ", result[0])
      print("p-value: ", result[1])
      print("Critical Values: ",result[4])
     Test Statistics: -2.2183190476089463
     p-value: 0.19966400615064323
     Critical Values: {'1%': -3.4393520240470554, '5%': -2.8655128165959236, '10%':
     -2.5688855736949163}
[22]: # Accept or reject null hypothesis
      if result[1] <= 0.05: #Compare result against threshold</pre>
          print("Reject null hypothesis, this time series data is stationary.")
      else:
          print("Accept null hypothesis, this time series data is non-stationary!")
     Accept null hypothesis, this time series data is non-stationary!
[23]: # Make time series stationary
      df_stationary = df.diff().dropna()
      # View
      df_stationary.head()
```

```
[23]:
                   Revenue
     Date
     2019-01-02 -0.292356
      2019-01-03 -0.035416
     2019-01-04 -0.012215
      2019-01-05 0.215100
      2019-01-06 -0.366702
[24]: # Test if data is stationary again
      result = adfuller(df_stationary['Revenue'])
      print("Test Statistics: ", result[0])
      print("p-value: ", result[1])
      print("Critical Values: ",result[4])
      if result[1] <= 0.05: #Compare result against threshold</pre>
          print("Reject null hypothesis, this time series data is stationary.")
      else:
          print("Accept null hypothesis, this time series data is non-stationary!")
     Test Statistics: -17.37477230355706
     p-value: 5.1132069788403175e-30
     Critical Values: {'1%': -3.4393520240470554, '5%': -2.8655128165959236, '10%':
     -2.5688855736949163}
     Reject null hypothesis, this time series data is stationary.
     0.3 Train, Test, and Split
[25]: # Split for Training and Testing
      X_train = df_stationary.loc[:'2020-09-30']
      X_test = df_stationary['2020-10-01':]
      print('X_train Shape: ', X_train.shape)
      print('X_test Shape: ', X_test.shape)
     X_train Shape: (638, 1)
     X_test Shape: (92, 1)
     0.4 C5 - Prepared Dataset
[26]: # Export stationary data
      pd.DataFrame(df_stationary).to_csv("df_stationary.csv")
[27]: # Spectal Density
```

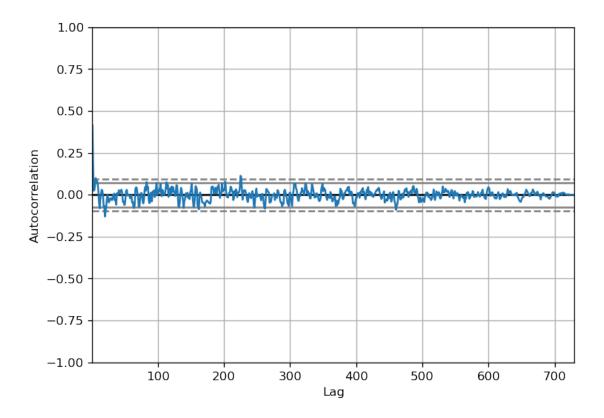
```
f, Pxx_den=signal.periodogram(df_stationary['Revenue'])
plt.semilogy(f,Pxx_den)
plt.ylim([1e-5,1e2])
plt.title('Spectal Density')
plt.xlabel('Frequency')
plt.ylabel('Spectal Density')
plt.show()
```



```
[28]: # Look for seasonality in data df_stationary.loc[:'2019-06-30'].plot();
```

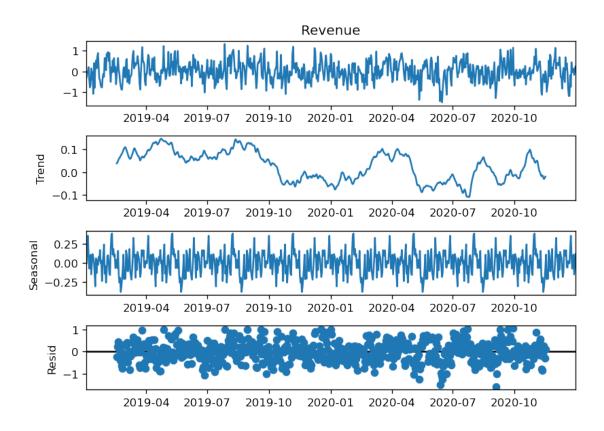


```
[29]: # Continue looking for seasonality
plt.rcParams.update({'figure.figsize':(7,5), 'figure.dpi':120})
autocorrelation_plot(df_stationary.Revenue.tolist());
```



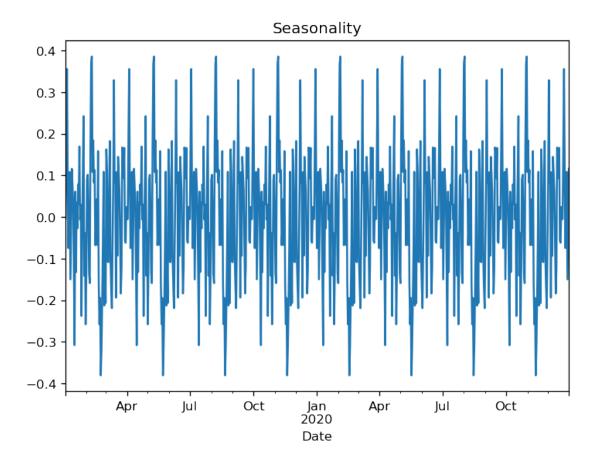
```
[30]: # Decomposition
decomp = seasonal_decompose(df_stationary['Revenue'], period=90)

# Plot decomposition
decomp.plot()
plt.show()
```

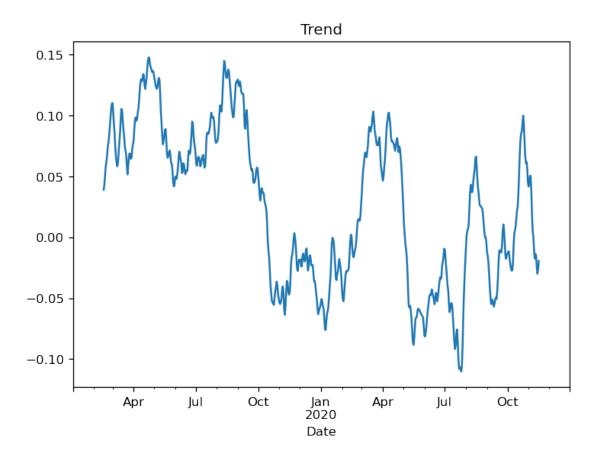


```
[31]: # Plot Seasonality

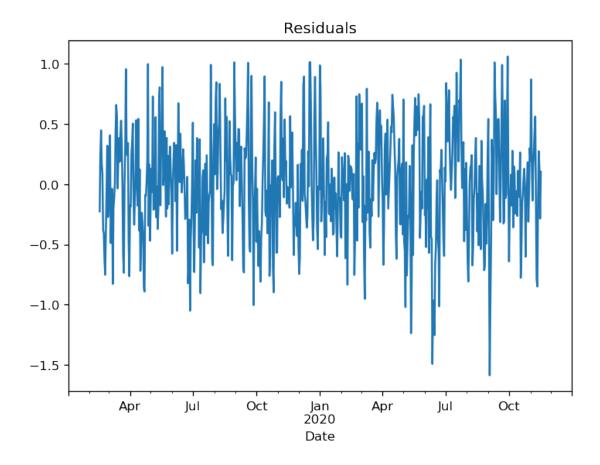
plt.title('Seasonality')
decomp.seasonal.plot();
```



```
[32]: # View Trend
plt.title('Trend')
decomp.trend.plot();
```



```
[33]: # Plot Residual
plt.title('Residuals')
decomp.resid.plot();
```

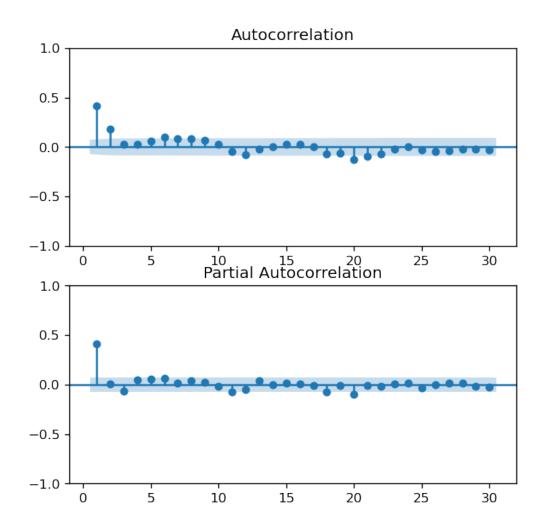


```
# ACF and PACF Autocorrelation Plots

# fig
fig, (ax1, ax2) = plt.subplots(2,1, figsize=(6,6))

# Plot ACF of df
plot_acf(df_stationary, lags=30, zero=False, ax=ax1)

# Plot PACF of df
plot_pacf(df_stationary, lags=30, zero=False, ax=ax2)
plt.show();
```



```
[35]: # Pick best order by aic

best_aic = np.inf
best_order = None
best_mdl = None
rng = range(3)
for p in rng: # loop over p-values
    for q in rng: #loop over q values
    try:

    #create and fit ARIMA(p,q) model
    model = SARIMAX(df_stationary, order=(p,1,q), trend = 'c')
    results = model.fit()
    tmp_aic = results.aic
    print(p, q, results.aic, results.bic)
    if tmp_aic < best_aic:</pre>
```

```
best_aic = tmp_aic
                best_order = (p, q)
                best_mdl = tmp_mdl
            # Print order and results
        except:
            print(p,q, None, None)
print('\nBest AIC: {:6.5f} | order: {}'.format(best_aic, best_order))
RUNNING THE L-BFGS-B CODE
           * * *
Machine precision = 2.220D-16
N =
               2
                                   10
             \ensuremath{\text{0}} variables are exactly at the bounds
At XO
At iterate
           0 f= 7.72420D-01 |proj g|= 3.63370D-05
Tit = total number of iterations
Tnf = total number of function evaluations
Tnint = total number of segments explored during Cauchy searches
Skip = number of BFGS updates skipped
Nact = number of active bounds at final generalized Cauchy point
Projg = norm of the final projected gradient
     = final function value
                Tnf Tnint Skip Nact
                                                       F
   N
       Tit
                                          Projg
                             0 0 3.634D-05 7.724D-01
                21
                        1
 F = 0.77242001314190578
ABNORMAL_TERMINATION_IN_LNSRCH
0 0 1131.7332191871824 1140.9165666511997
0 0 None None
RUNNING THE L-BFGS-B CODE
           * * *
Machine precision = 2.220D-16
 N =
               3
                                   10
```

At XO 0 variables are exactly at the bounds

At iterate 0 f= 6.96400D-01 |proj g|= 8.69365D-02

At iterate 5 f = 6.73133D - 01 |proj g| = 2.18277D - 01

At iterate 10 f= 6.72711D-01 |proj g|= 4.35275D-05

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 3 11 13 1 0 0 7.492D-08 6.727D-01 F = 0.67271143814447110

CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL

0 1 988.1586996909278 1001.9337208869538

0 1 None None

RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16

 $N = 4 \qquad M = 10$

At XO 0 variables are exactly at the bounds

At iterate 0 f= 6.48526D-01 |proj g|= 6.45857D-02

This problem is unconstrained.

Line search cannot locate an adequate point after MAXLS function and gradient evaluations.

Previous x, f and g restored.

Possible causes: 1 error in function or gradient evaluation; 2 rounding error dominate computation.

This problem is unconstrained.

This problem is unconstrained.

At iterate 5 f = 6.37907D - 01 |proj g| = 1.07031D - 01|proj g|= 2.62385D-01 At iterate 10 f= 6.25222D-01 At iterate f= 6.23246D-01 |proj g|= 7.96411D-01 15 At iterate 20 f= 6.20389D-01 |proj g|= 1.99214D+00 At iterate f= 6.19495D-01 |proj g|= 2.21354D-01 25 At iterate |proj g|= 6.77096D-02 30 f= 6.19398D-01

Bad direction in the line search; refresh the lbfgs memory and restart the iteration.

Warning: more than 10 function and gradient evaluations in the last line search. Termination may possibly be caused by a bad search direction. This problem is unconstrained.

This problem is unconstrained.

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 4 31 74 2 0 0 6.771D-02 6.194D-01 F = 0.61939751825460820

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH
0 2 912.320376651728 930.6870715797627
0 2 None None
RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16N = 3 M = 10 At XO 0 variables are exactly at the bounds

At iterate 0 f= 7.25538D-01 |proj g|= 2.12223D-03

At iterate 5 f= 7.25538D-01 |proj g|= 2.49879D-05

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 3 6 8 1 0 0 1.433D-05 7.255D-01 F = 0.72553774292633710

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH
1 0 1065.2851046724522 1079.0601258684783
RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16N = 4 M =

At XO 0 variables are exactly at the bounds

At iterate 0 f= 6.50193D-01 |proj g|= 1.64012D-01

10

At iterate 5 f = 6.36116D-01 |proj g| = 1.76948D-01

At iterate 10 f = 6.33139D-01 |proj g| = 1.06543D-01

At iterate 15 f= 6.14880D-01 |proj g|= 2.92431D+00

At iterate 20 f= 6.10487D-01 |proj g|= 6.16222D-01

At iterate 25 f = 6.03877D-01 |proj g|= 4.98576D+00

At iterate 30 f = 6.02712D-01 |proj g|= 5.53957D-01

At iterate 35 f= 6.02587D-01 |proj g|= 4.27588D-02

At iterate 40 f= 6.02509D-01 |proj g|= 4.43931D-01

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 4 43 66 1 0 0 2.585D-01 6.025D-01 F = 0.60250925503394537

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH

- 1 1 887.6635123495602 906.0302072775949
- 1 1 None None

RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16

 $N = 5 \qquad M = 10$

At XO 0 variables are exactly at the bounds

At iterate 0 f= 6.28707D-01 |proj g|= 5.90938D-01

At iterate 5 f= 6.26311D-01 |proj g|= 1.66440D-01

At iterate 10 f= 6.20894D-01 |proj g|= 4.35677D-01

At iterate 15 f = 6.18420D-01 |proj g| = 3.31768D-02

Warning: more than 10 function and gradient evaluations in the last line search. Termination may possibly be caused by a bad search direction. This problem is unconstrained.

At iterate 20 f= 6.18327D-01 |proj g|= 1.43175D-01

At iterate 25 f= 6.13978D-01 |proj g|= 5.64560D-01

At iterate 30 f= 6.11709D-01 |proj g|= 7.09927D-01 At iterate f= 6.07473D-01 |proj g|= 3.60963D-01 35 At iterate f= 6.03987D-01 |proj g|= 3.25555D+00 40 At iterate 45 f= 6.02676D-01 |proj g|= 1.41252D+00 |proj g|= 8.22343D-01 At iterate 50 f= 6.02511D-01

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 5 50 56 1 0 0 8.223D-01 6.025D-01 F = 0.60251149149345451

STOP: TOTAL NO. of ITERATIONS REACHED LIMIT 1 2 889.6667775804435 912.6251462404869 RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16

 $N = 4 \qquad M = 10$

At XO 0 variables are exactly at the bounds

At iterate 0 f= 7.10268D-01 |proj g|= 4.82104D-03

At iterate 5 f= 7.10266D-01 |proj g|= 4.30004D-06

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point
Projg = norm of the final projected gradient
F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 4 5 8 1 0 0 4.300D-06 7.103D-01 F = 0.71026607797511199

CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL 2 0 1044.9884738436635 1063.3551687716981 RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16

 $N = 5 \qquad M = 10$

At XO 0 variables are exactly at the bounds

At iterate 0 f= 7.81060D-01 |proj g|= 4.12026D-01

At iterate 5 f= 7.00036D-01 |proj g|= 5.77628D-02

This problem is unconstrained.

This problem is unconstrained.

At iterate 10 f= 6.80209D-01 |proj g|= 1.58045D-01

At iterate 15 f = 6.26507D-01 |proj g| = 4.53023D-02

At iterate 20 f= 6.10201D-01 |proj g|= 3.80628D-01

At iterate 25 f= 6.03752D-01 |proj g|= 8.88891D+00

At iterate 30 f= 6.02826D-01 |proj g|= 9.65316D-01

At iterate 35 f = 6.02496D-01 |proj g|= 7.85718D-02

* * *

Tit = total number of iterations

Inf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 5 38 68 1 0 0 6.071D-02 6.025D-01 F = 0.60248035125047006

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH 2 1 889.6213128256863 912.5796814857297 RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16N = 6 M = 10

At XO 0 variables are exactly at the bounds

At iterate 0 f= 9.07847D-01 |proj g|= 1.15640D+00

Warning: more than 10 function and gradient evaluations in the last line search. Termination may possibly be caused by a bad search direction. This problem is unconstrained.

f= 6.61875D-01 |proj g|= 1.11694D-01 At iterate 5 At iterate 10 f= 6.36518D-01 |proj g|= 4.38022D-01 At iterate 15 f= 6.19589D-01 |proj g|= 3.50045D-01 At iterate f= 6.03511D-01 |proj g|= 7.63593D-01 20 25 At iterate f= 6.02224D-01 |proj g|= 3.36742D-01

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

```
N
       Tit
               Tnf Tnint Skip Nact
                                          Projg
                              0
                                        2.696D-03
                                                     6.022D-01
   6
                48
 F = 0.60220556374000445
CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH
2 2 891.2201230604064 918.7701654524584
Best AIC: 887.66351 | order: (1, 1)
Warning: more than 10 function and gradient
   evaluations in the last line search. Termination
  may possibly be caused by a bad search direction.
```

1 Uncomment Code to run Auto ARIMA; Takes > 120 min

```
[36]: # Use Auto ARIMA to Find best model
      # https://www.machinelearningplus.com/time-series/
       \rightarrow arima-model-time-series-forecasting-python/
      #%time
      #tqdm.pandas()
      #model = pm.auto_arima(df_stationary,
                              seasonal=True, m=90,
      #
                              d=1, D=1,
      #
                              start_p=1, start_q=1,
      #
                              max_p=2, maxq=2,
      #
                              maxP=2, maxQ=2,
      #
                              trace=True,
      #
                              error_action='ignore',
      #
                              suppress_warnings=True)
```

```
[37]: #print(model.summary())
```

2 Terminal: nbconvert -to pdf D213_PA1.ipynb

```
[38]: # Create Time Series Model

model = SARIMAX(df_stationary, order=(1,1,0),seasonal_order=(1,1,0,90))
results = model.fit()
results.summary()
```

RUNNING THE L-BFGS-B CODE

* * *

Machine precision = 2.220D-16

 $N = 3 \qquad M = 10$

At XO 0 variables are exactly at the bounds

At iterate 0 f= 8.65762D-01 |proj g|= 2.80477D-01

This problem is unconstrained.

At iterate 5 f= 8.52032D-01 |proj g|= 2.52986D-03

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 3 9 12 1 0 0 2.269D-06 8.520D-01

F = 0.85202993770228830

CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL

[38]: <class 'statsmodels.iolib.summary.Summary'>

SARIMAX Results

Dep. Variable: Revenue No. Observations:

730

Model: SARIMAX(1, 1, 0)x(1, 1, 0, 90) Log Likelihood

-621.982

Date: Fri, 22 Jul 2022 AIC

1249.964

Time: 19:05:20 BIC

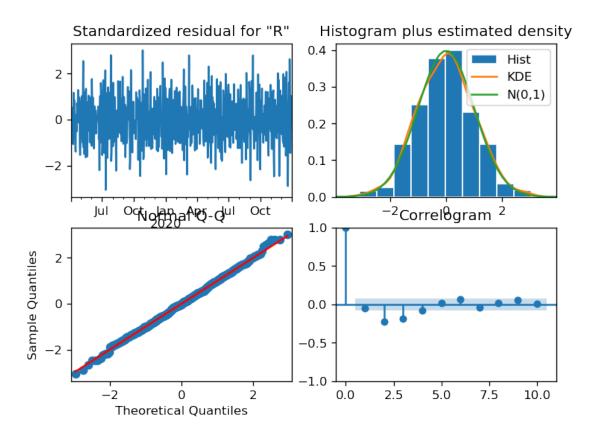
1263.343

Sample: 01-02-2019 HQIC

1255.157

- 12-31-2020

			opg			
	coef	std err	z	P> z	[0.025	0.975]
ar.L1	-0.3084	0.037	-8.398	0.000	-0.380	-0.236
ar.S.L90	-0.4726	0.039	-12.259	0.000	-0.548	-0.397
sigma2	0.3958	0.022	17.749		0.352	0.439
===						
Ljung-Box (1 0.19	L1) (Q):		2.01	Jarque-Bera	(JB):	
Prob(Q): 0.91			0.16	Prob(JB):		
	sticity (H):		1.10	Skew:		
Prob(H) (two	o-sided):		0.48	Kurtosis:		
	nce matrix c	alculated u	sing the o	uter product	of gradients	(complex
Warnings:	nce matrix c	alculated u	sing the o	uter product	of gradients	(complex
Warnings: [1] Covariantstep). """ # Warnings: #[1] Covari	ance matrix			uter product		
Warnings: [1] Covariantstep). """ # Warnings: #[1] Covari	ance matrix	calculated	using the	outer product		
Warnings: [1] Covariants step). """ # Warnings: #[1] Covari	ance matrix -step) value indica value indic	calculated tes residua	using the ls are not	_	of gradient	
Warnings: [1] Covariant step). """ : # Warnings: #[1] Covariant complex- # Prob(Q):	ance matrix -step) value indica value indic	calculated tes residua	using the ls are not	outer product correlated.	of gradient	
Warnings: [1] Covariants step). """ : # Warnings: #[1] Covariants (complex- # Prob(Q): # Prob(JB): # Model eva	ance matrix -step) value indica value indic	calculated tes residua ates residu	using the ls are not	outer product correlated.	of gradient	
Warnings: [1] Covariantstep). """ # Warnings: #[1] Covari	ance matrix -step) value indica value indic luation	calculated tes residua ates residu rror sults.resid	using the ls are not als are no	outer product correlated.	of gradient	
Warnings: [1] Covariantstep). """ # Warnings: #[1] Covari Gomplex- # Prob(JB): # Prob(JB): # Model eva # Print mea mae = np.mea	ance matrix -step) value indica value indic luation n absolute e an(np.abs(re	calculated tes residua ates residu rror sults.resid	using the ls are not als are no	outer product correlated.	of gradient	
Warnings: [1] Covariantstep). """ : # Warnings: #[1] Covariantstep). # [1] Covariantstep). # Prob(Q): # Prob(JB): # Model eva : # Print meantstep mae = np.mentstep print("Meantstep) Mean Absolute: # Create the	ance matrix -step) value indica value indic luation n absolute e an(np.abs(re Absolute Er	calculated tes residua ates residu rror sults.resid ror: ", mae 49873094599 ics plots	using the ls are not als are no	outer product correlated.	of gradient	



```
# Validate w/Test Set

# Predictions
prediction = results.get_prediction(start=-90)

# Prediction Mean
mean_prediction = prediction.predicted_mean

# Confidence Intervals of Predictions
confidence_intervals = prediction.conf_int()

# Upper & lower conf limits
lower_limits = confidence_intervals.loc[:,'lower Revenue']
upper_limits = confidence_intervals.loc[:,'upper Revenue']

# Print predictions (best estimate)
# print(mean_forcast)

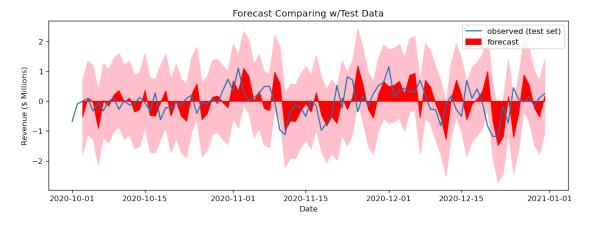
[43]: # Plot Data
plt.figure(figsize=(12,4))
```

```
plt.plot(np.array(X_test.index), np.array(X_test[['Revenue']]), label='observed_\( \) \( \text{\test set} \)'\)

# shade upper conf. limit area
plt.fill_between(upper_limits.index, upper_limits, lower_limits, color='pink')

# plot mean predictions
plt.fill_between(mean_prediction.index, mean_prediction, color='red',\( \) \( \text{\test} \) label='forecast')

# Labels and Legends
plt.title('Forecast Comparing w/Test Data')
plt.xlabel('Date')
plt.ylabel('Revenue ($ Millions)')
plt.legend()
plt.show()
```



```
# Validate w/Test Set

# Predictions
prediction = results.get_prediction(start=0)

# Prediction Mean
mean_prediction = prediction.predicted_mean

# Confidence Intervals of Predictions
confidence_intervals = prediction.conf_int()

# Upper & lower conf limits
lower_limits = confidence_intervals.loc[:,'lower Revenue']
upper_limits = confidence_intervals.loc[:,'upper Revenue']
```

```
# Print predictions (best estimate)
      # print(mean_forcast)
[45]: # Perform forecast
      diff_forecast = results.get_forecast(steps=180)
      mean_forecast = diff_forecast.predicted_mean
      # Conf intervals of predictions
      confidence_intervals = diff_forecast.conf_int()
      # Upper & Lower conf limits
      lower_limits = confidence_intervals.loc[:,'lower Revenue']
      upper_limits = confidence_intervals.loc[:,'upper Revenue']
[46]: df_stationary[['Revenue']].reset_index(drop=True)
[46]:
           Revenue
      0
          -0.292356
      1 -0.035416
        -0.012215
      2
      3 0.215100
      4
         -0.366702
     725 -0.032693
      726 0.143766
     727 -0.156834
      728 0.113880
      729 0.246562
      [730 rows x 1 columns]
[47]: lower_limits.index
[47]: DatetimeIndex(['2021-01-01', '2021-01-02', '2021-01-03', '2021-01-04',
                     '2021-01-05', '2021-01-06', '2021-01-07', '2021-01-08',
                     '2021-01-09', '2021-01-10',
                     '2021-06-20', '2021-06-21', '2021-06-22', '2021-06-23',
                     '2021-06-24', '2021-06-25', '2021-06-26', '2021-06-27',
                     '2021-06-28', '2021-06-29'],
                    dtype='datetime64[ns]', length=180, freq='D')
[48]: # Plot forecast
      plt.plot(np.array(df_stationary.index), np.array(df_stationary[['Revenue']].

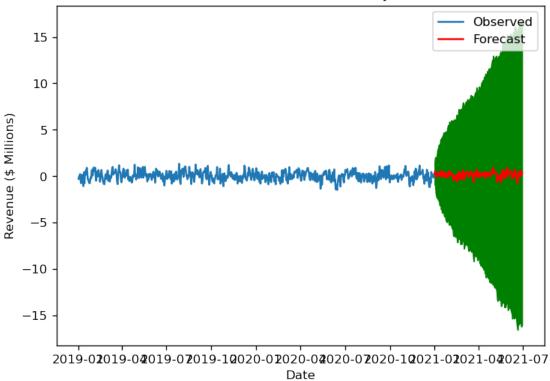
¬reset_index(drop=True)), label='Observed')
```

```
# shade conf. limit area
plt.fill_between(lower_limits.index, lower_limits, upper_limits, color='green')

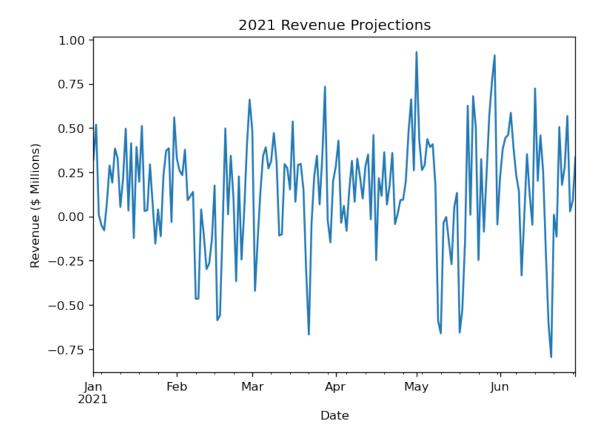
# Plot mean predictions
plt.plot(mean_forecast.index, mean_forecast, color='red', label='Forecast')

# Labels and Legends
plt.title('Forecasted 2021 Revenue Projections')
plt.xlabel('Date')
plt.ylabel('Revenue ($ Millions)')
plt.legend()
plt.show()
```

Forecasted 2021 Revenue Projections



```
[49]: # Mean Forecast Plot
plt.title('2021 Revenue Projections')
plt.xlabel('Date')
plt.ylabel('Revenue ($ Millions)')
mean_forecast.plot();
```



```
[50]: # Save model
joblib.dump(model, "time_series_model.pkl")
```

[50]: ['time_series_model.pkl']

3 Terminal: nbconvert -to pdf D213_PA1.ipynb

3.1 End