# THE DESIGN HIERARCHY

In Lab 2, you build combinational circuits using hierarchical design (a technique that emphasizes modularity). In addition, you use Karnaugh maps to ensure that your circuits are optimized. Before the lab, you prepare by deriving truth tables and logic functions, and by drawing schematics using Logisim Evolution. During the lab, you simulate your designs to demonstrate your understanding of the circuit.

This document describes what you need to prepare and demonstrate for Lab 2. Section 2.3 briefly describes hierarchical design in Logisim Evolution. Section 2.4 describes the tasks you must complete *before* your lab session. Section 2.5 describes the tasks you complete *during* your lab session. The next section describes lab logistics in more detail.

## 2.1 Logistics

Even though you work in pairs during your lab session, you are assessed individually on your Lab Preparation ("pre-lab") and Lab Demonstration ("demo"). All pre-lab exercises are submitted electronically before your lab (see the course website for exact due dates, times, and the submission process). So, **before** each lab, you must read through this document and complete all the pre-lab exercises. During the lab, use your pre-lab designs to help you complete all the required in-lab actions. The more care you put into your pre-lab designs, the faster you will complete your lab.

Before beginning the pre-lab, read Section 2.3. The Lab Preparation must be completed individually and submitted online by the due date. Follow the steps in Section 2.4 for the pre-lab. Remember to download the starter files (if provided).

You must upload every required file for your pre-lab submission to be complete. But you do not need to include images that are not on the list of required files (even if those images are in your lab report). If you have questions about the submission process, please ask ahead of time. The required files for Lab 2's pre-lab (Section 2.4) are:

- Your lab report: lab2\_report.tex, lab2\_report.pdf (as generated from the tex file)
- Your digital designs: lab2\_part1.circ, lab2\_part2.circ

The Lab Demonstration must be completed during the lab session that you are enrolled in. During a lab demonstration, your TA may ask you to: go through parts of your pre-lab, run and simulate your designs in Logisim, and answer questions related to the lab. You may not receive outside help (e.g., from your partner) when asked a question.

## 2.2 Marking Scheme

Each lab is worth 4% of your final grade, where you will be graded out of 4 marks for this lab, as follows.

• Prelab: 1 mark

• Part I (in-lab): 1 mark

• Part II (in-lab): 2 mark

## 2.3 Hierarchical Design in Logisim Evolution

In Lab 1 you designed a 2-to-1 multiplexer. Multiplexers are a common building block in digital circuits. In this section, we first describe how to convert a circuit, like a 2-to-1 multiplexer, into a building block. We then describe how to test your circuits. Testing smaller circuits (e.g., 2-to-1 multiplexer) helps with the testing of your larger circuits (e.g., that use multiplexers).

#### 2.3.1 Subcircuits

In Logisim Evolution, a .circ file can be composed of multiple circuits. There is a top-level circuit, typically called main, which you should be familiar with from Lab 1. But it is possible to add more circuits called *subcircuits* (or *modules*). From your programming experience, this is analgous to creating a function.

Subcircuits are typically building blocks, like a 2-to-1 multiplexer, used in other subcircuits and/or the top-level module. Each time a subcircuit is used in another circuit, it is an *instance* of that module. Note that, if you label an instance, the name should be unique. We can create large circuits by using multiple modules of the same type. From your programming experience, this is analogous to function reuse.

Logisim Evolution includes a tutorial on hierarchical design. You can find it by launching Logisim Evolution and navigating to Help > User's Guide. There, you will find a section (and its subsections) called Subcircuits.

### 2.3.2 Testing Circuits

It is a good idea to verify the correctness of your circuits and subcircuits. Logisim Evolution provides a method to compare what your circuit actually outputs with what you expect it to output. You can accomplish this by navigating to Simulate > Test Vector....

A test vector is essentially a plain text file containing a truth table. The truth table maps a set of inputs to the expected output. The first line of the file specifies the names of the inputs and outputs - these names must match those found in your circuit. In the lines that follow, you include the values to use for the input(s) and the value you expect at the output(s).

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Figure 2.1 shows a circuit that consists of only an AND gate. Listing 2.1 shows the corresponding test vector for the circuit. The test vector must be saved as a text file before it can be loaded into Logisim Evolution. Once loaded, the status of each row is given (Figure 2.2).

Listing 2.1: Test Vector

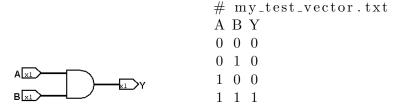


Figure 2.1: Contrived Circuit



Figure 2.2: Test Outcomes

## 2.4 Lab Preparation

Make sure you have read Section 2.3 before beginning your pre-lab.

The pre-lab for Lab 2 consists of two parts. In Part I, you follow a tutorial on Hierarchical Design to implement a 4-to-1 multiplexer. In Part II, you apply hierarchical design to create a decoder that visualizes hexadecimal characters on a 7-segment display.

### 2.4.1 Part I

In this part, you construct a module for the 4-to-1 multiplexer shown in Figure 2.3 with the truth table shown in Table 2.1 using hierarchical design. Note that the truth table in Table 2.1 is given in a short-hand form. A real truth table would consist of rows enumerating all possible combinations of values of inputs u, v, w, x, in addition to  $s_0$  and  $s_1$ , and show the value (0 or 1) of the output m for each row of the truth table.

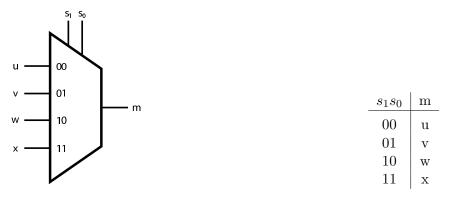


Figure 2.3: Symbol for a 4-to-1 multiplexer

Table 2.1: Truth table for a 4-to-1 multiplexer

- 1. If the truth table in Table 2.1 was given in full, how many rows would it have?
- 2. In a file called lab2\_part1.circ, follow the Subcircuits tutorial in Logisim Evolution to create a 4-to-1 multiplexer out of multiple instances of 2-to-1 multiplexers. However, make sure you meet the following requirements and naming schemes:
  - You must have a subcircuit of a 2-to-1 multiplexer called mux2to1.
  - You must have a subcircuit of a 4-to-1 multiplexer called mux4to1. This module can only contain instances of the mux2to1 subcircuit (as well as wires, inputs, and outputs).

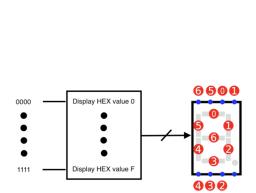
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• You must have a top-level circuit called main. This module should only contain one instance of the mux4to1 subcircuit (as well as wires, inputs, and outputs).

Export the schematic of the mux4to1 subcircuit as an image and include it in your report. Also remember to upload the designs (i.e., the .circ file) as part of your required files.

#### 2.4.2 Part II

In this part, you design a decoder for a 7-segment display (Figure 2.4). As the name implies, the display has seven segments (lines) that can be ON or OFF. The 7-segment display shown in Figure 2.4 has a number associated with each segment. So we can refer to a segment by its number. For example, the top-most horizontal segment is  $S_0$ , which we can turn ON or OFF by driving pin 0 (third dot from the left at the very top of the display).



$D_{3:0}$	Character
0000	0
0001	1
0010	2
0011	3
0100	Ч
0101	S
0110	8
0111	7
1000	8
1001	9
1010	Я
1011	Ь
1100	С
1101	д
1110	٤
1111	۶

Figure 2.4: A decoder driving a 7-segment display Table 2.2: The desired behaviour of the decoder

The segments are arranged in a way such that you can visualize the numbers 1 to F in hexadecimal. See Table 2.2 for a mapping of decoder inputs to the characters that need to be displayed. The decoder you are designing takes, as input, 4 bits and produces a 7-bit output that controls the LEDs in the 7-segment display. To design the decoder, you need to identify when a segment in the display is on or off.

Since there are seven segments, you should first derive seven Boolean functions. Then, use Karnaugh maps to ensure these Boolean functions are minimal. Next, implement each Boolean function as its own subcircuit. And, finally, use hierarchical design to construct the decoder and drive a 7-segment display.

#### CAUTION

Example 2.10 in the textbook is a very useful starting point. But be careful, the textbook example is only concerned with visualizing the characters 0 to 9. This lab is also asking you to visualize the outputs associated with  $\beta$ ,  $\beta$ ,  $\epsilon$ ,  $\beta$ ,  $\xi$ ,  $\xi$ ,  $\xi$  (Table 2.2).

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Perform the following steps:

1. In your lab report, derive seven truth tables, one for each segment of the 7-segment decoder. Another way to ask this question is: which segments should be on (and which should be off) for a given character?

- 2. Use Karnaugh maps to write seven Boolean functions for each segment so that they are optimized. You do not need to include these in your report, but you should save these Karnaugh maps for your Lab Demonstration.
- 3. In a file called lab2\_part2.circ, create seven subcircuits, one for each optimized function. Use the naming scheme HEXO, HEX1, ..., HEX6 for each subcircuit. Each subcircuit should have input pins called D3, D2, D1, D0 and an output pin SX, where X corresponds to which segment is being driven (e.g., S0 for segment 0). Export each subcircuit schematic as an image and include it in your report.
- 4. In the same file, create a subcircuit called HEX\_DECODER using hierarchical design. This module should only contain instances of your HEX# subcircuits (as well as wires, inputs, and outputs).
- 5. In the same file, in your top-level circuit, create a circuit like the one shown in Figure 2.4. The circuit should have four input pins called SW3, SW2, SW1, and SW0. Once again, use hierarchical design to instantiate your HEX\_DECODER subcircuit. In Logisim Evolution, you can find the 7-Segment Display under Input/Output; your top-level circuit should not have an output pin, only the 7-segment display. When you are done, remember to upload your designs (i.e., the .circ file) as part of your required files.

### 2.5 Lab Demonstration

The lab demonstration consists of two parts. Each part corresponds to a part from the pre-lab. When demonstrating a part to your TA, be ready to answer questions **individually**.

### 2.5.1 Part I

Synthesise your design from Section 2.4.1 and download it onto the DE1-SoC board. Refer to Lab 1 if you need to see instructions on how to do this. When you are done, demonstrate your working design to your TA.

#### 2.5.2 Part II

Test your top-level circuit in Logisim Evolution with the Poke tool. Test your subcircuits with test vectors (Section 2.3.2). Make sure you are ready to, if asked, explain your testing methodology and/or how you optimized your Boolean functions with Karnaugh maps. When you are done, demonstrate your working design to your TA.

### Optional

You may wish to synthesise and download your design to the DE1-SoC board. Unfortunately, Logisim Evolution is unable to map its 7-segment display to the one on the board. Instead, you can create a new circuit with standard output pins, then map those pins to the LEDs on the DE1-SoC. While this will not visualize the character itself, it does let you verify your truth tables from the prep.