Second Hint for Problem 326

The permutations with four one-cycles and the two-cycle (14), (25), or (36) are in the group of automorphisms. Once you know the cycle structure of D_6 and (14) $D_6 = \{(14)\sigma | \sigma \in D_6\}$, you know the cycle structure of every element of the group.